

## Excitation-induced non-thermal melting effects in silicon

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### Introduction

- We developed electron temperature-dependent interaction potentials for silicon to study the dynamics of silicon under laser irradiation.
- Electron temperature-dependent potentials give rise to electron temperature-dependent lattice expansion, elastic constants, and melting temperature.
- Novel material dynamics under laser irradiation can be observed with the new potential and electron-phonon coupling.
- Experimental ablation depth is reproduced with surprising accuracy.

### Interatomic potential

#### Functional form:

- Modified Tersoff potential (MOD):

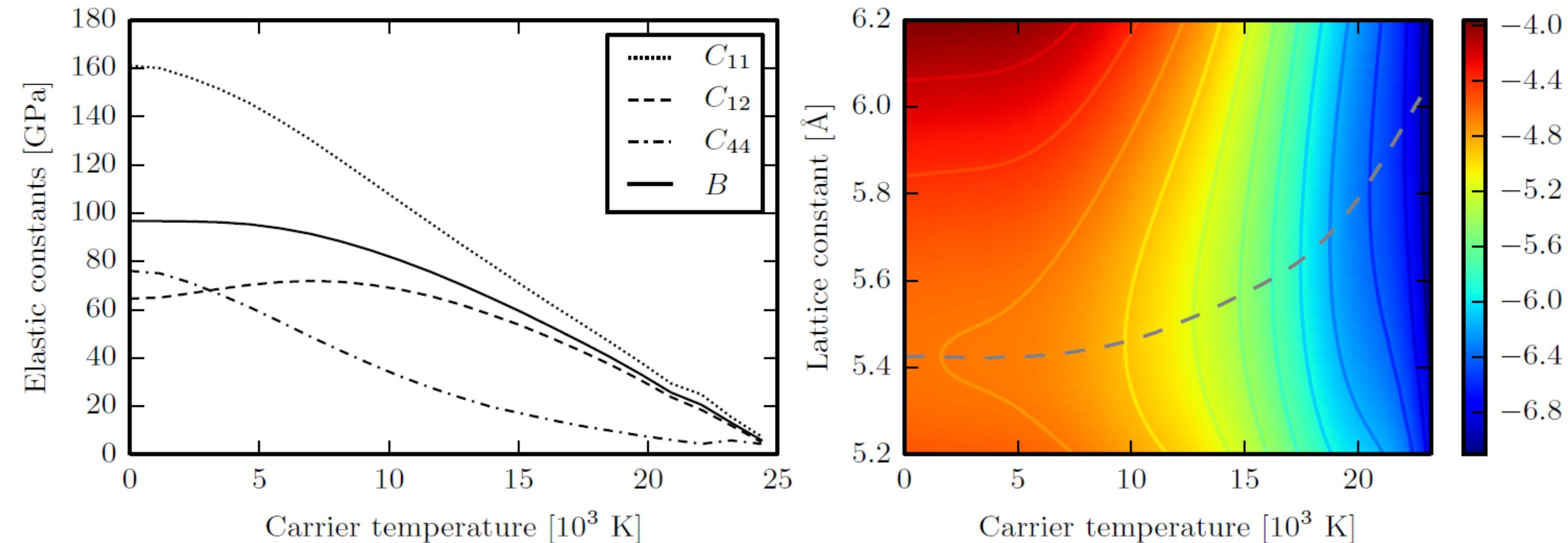
$$V = \frac{1}{2} \sum_i \sum_{j \neq i} f_c(r_{ij}) [a_{ij} f_R(r_{ij}) + b_{ij} f_A(r_{ij})]$$

$$f_A(r_{ij}) = -B \exp(-\lambda_2 r_{ij}) \quad \text{and} \quad f_R(r_{ij}) = A \exp(-\lambda_1 r_{ij})$$

- Electron temperature-dependent parameters (MOD\*) [1]:

$$P_t(T_c) = \sum_{n=0}^m a_n (k_B T_c)^n$$

#### $T_c$ -dependent properties:



### $T_c$ -dependent phase diagram

#### Thermodynamic integration:

- Hamiltonian of two systems coupled by  $\lambda$ :

$$H = H_1 + \lambda(H_2 - H_1).$$

- Work from switching  $\lambda$  over time:

$$W_{1 \rightarrow 2}^S = \int_{t_1}^{t_2} \left[ \frac{\partial H(\lambda)}{\partial \lambda} + p \frac{\partial V(\lambda)}{\partial \lambda} \right] \frac{\partial \lambda}{\partial t} dt$$

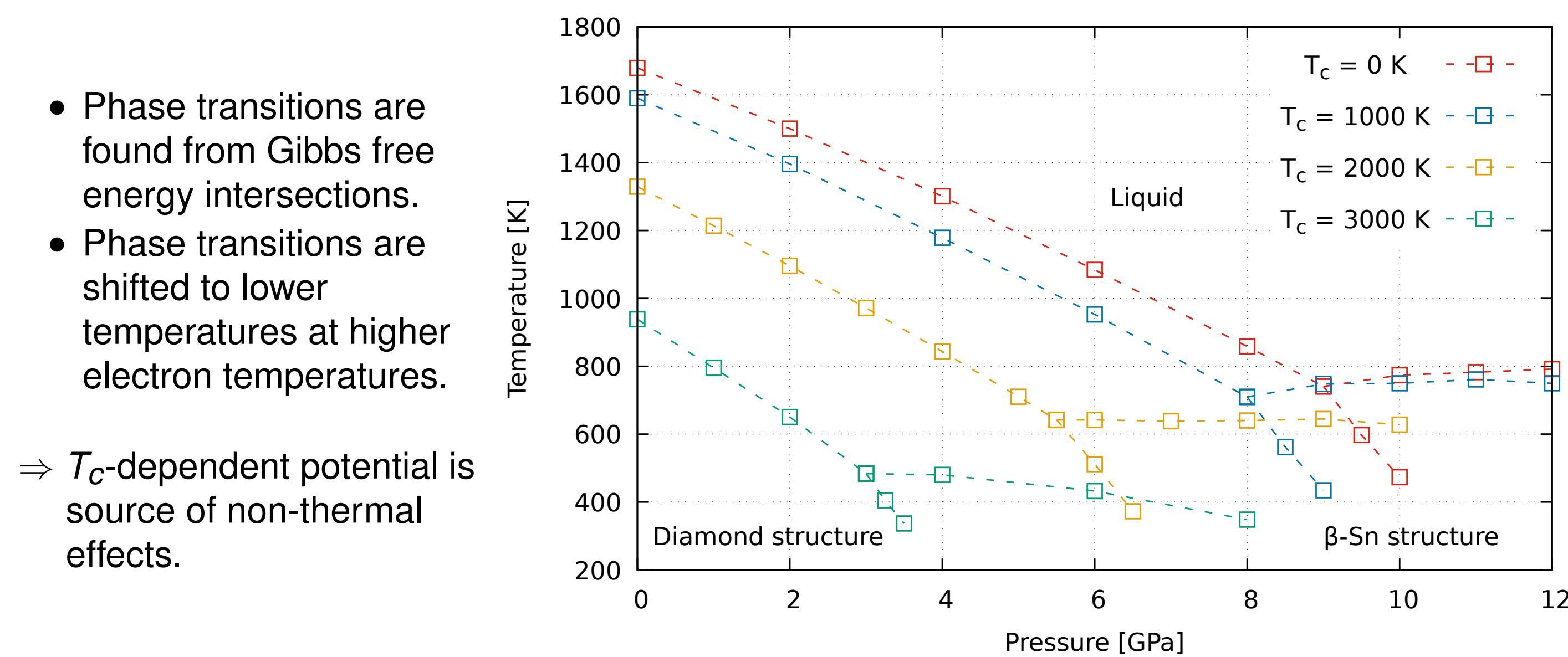
⇒ Increase or decrease temperature over time at different constant pressures.  
⇒ Dissipated energy  $E_d$  vanishes if temperature is changed slowly.

- Calculation of Gibbs free energy:

$$\Delta G = \frac{1}{2} (W_{1 \rightarrow 2}^S - W_{2 \rightarrow 1}^S)$$

$$\Rightarrow G(N, p, T_2) = G(N, p, T_1) - \frac{3}{2} k_B T_2 N \ln \left( \frac{T_2}{T_1} \right) + \frac{T_2}{T_1} \Delta G$$

#### Pressure-temperature phase diagram:



### Simulation model

The Boltzmann equation of the electron distribution in the drift-diffusion limit yields the continuity equation of the charge carrier density and the energy

$$\frac{\partial n_c}{\partial t} = -\vec{\nabla} \cdot \vec{J} + \frac{dn_c}{dt} \quad \text{and} \quad \frac{\partial U}{\partial t} = -\vec{\nabla} \cdot \vec{W} + \frac{dU}{dt}$$

with the total carrier flux density

$$\vec{J} = -D_0 \left( \vec{\nabla} n_c + \frac{2n_c}{k_B T_c} \vec{\nabla} E_g + \frac{n_c}{2T_c} \vec{\nabla} T_c \right)$$

and total energy flux

$$\vec{W} = (E_g + 3n_c k_B T_c) \vec{J} - \kappa_c \vec{\nabla} T_c.$$

Optical properties of the material are included via

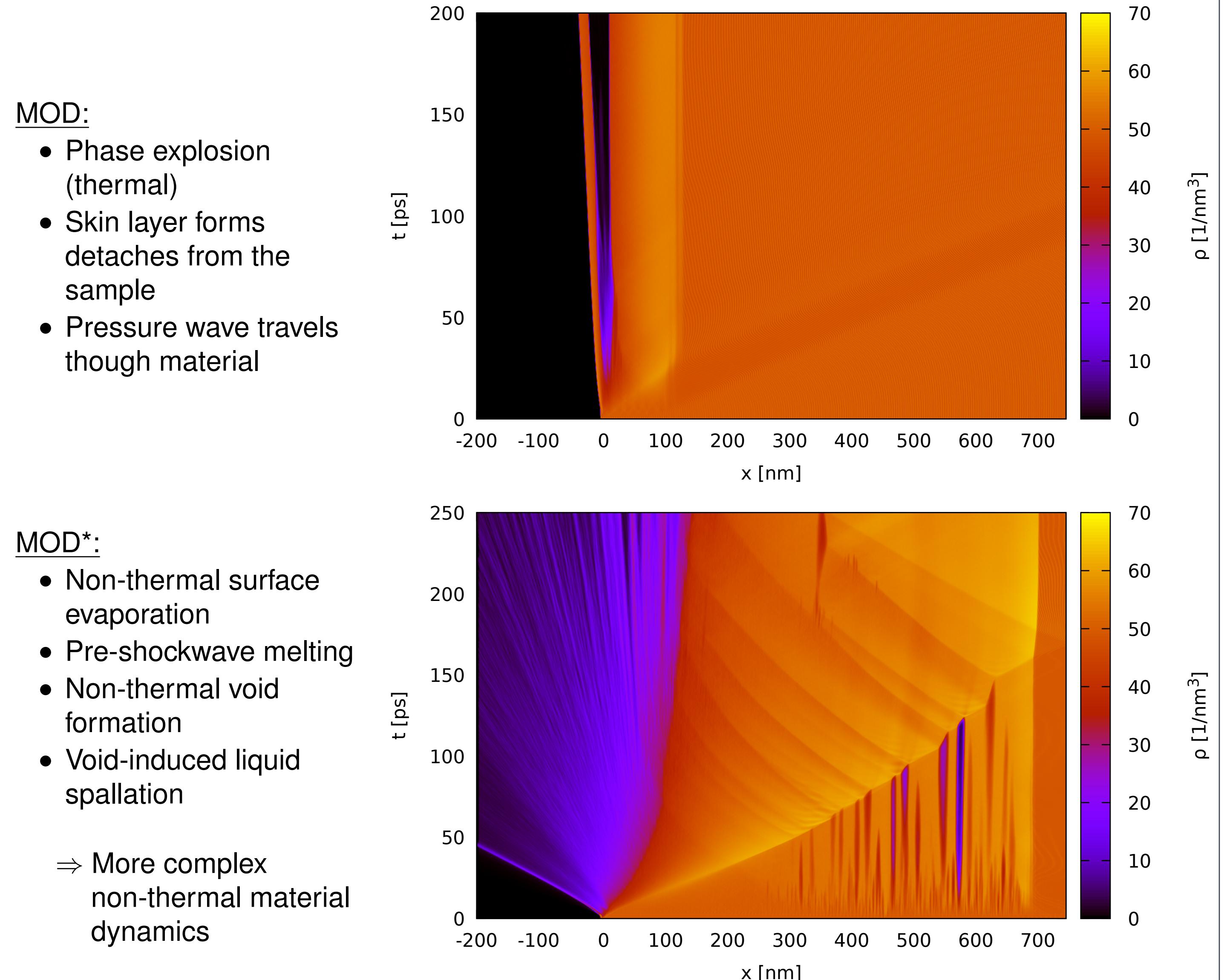
$$\frac{dI}{dx} = -(\alpha_{SPA} + \alpha_{FCA}) I - \beta_{TPA} I^2$$

and

$$\frac{dn_c}{dt} = \sum_k I^k \frac{\alpha_k}{k \hbar \nu} + \delta_{imp} n_c - \gamma_{Aug} n_c^3.$$

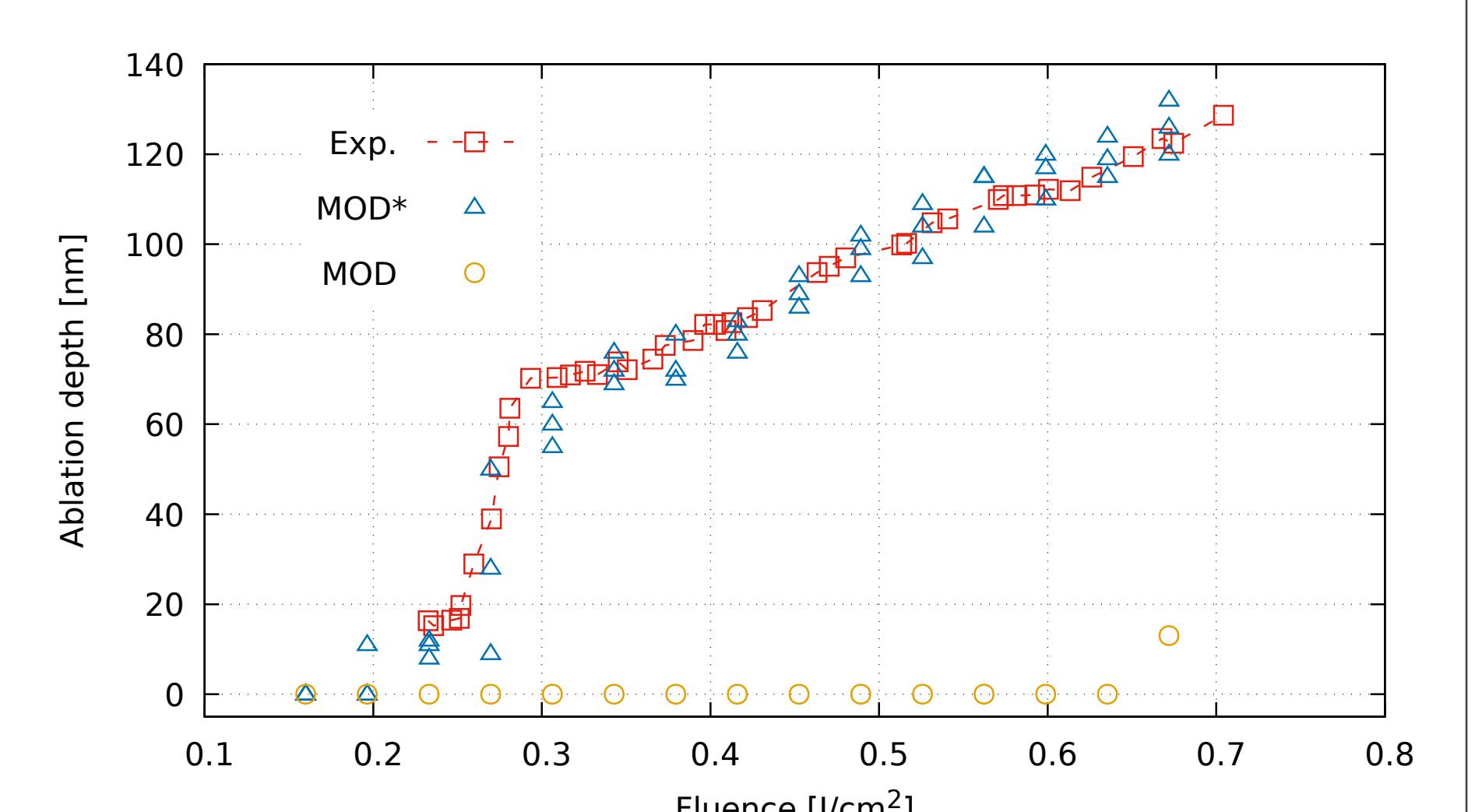
The atoms are moved via MD.

### Material dynamics during laser treatment



### Ablation depth from MOD and MOD\*

- MOD doesn't reproduce correct ablation behaviour.
- MOD\* reproduces experimental ablation depth accurately.
- Experimental data taken from [2].



### References:

- [1] Alexander Kiselev. "Molecular dynamics simulations of laser ablation in covalent materials". PhD thesis. 2017.
- [2] Hao Zhang. "Single-shot femtosecond laser ablation on the nanoscale". PhD thesis. 2013.

