

**Friction drag coefficient for steady, constant property, 2-D, uniform flow over a flat plate:**

Laminar:  $C_{Df} = 1.328 Re_\ell^{-1/2}$   $Re_\ell < 5 \times 10^5$

Mixed or Transitional:  $C_{Df} = 0.0743 Re_\ell^{-1/5} - \frac{1740}{Re_\ell}$   $5 \times 10^5 < Re_\ell < 10^7$

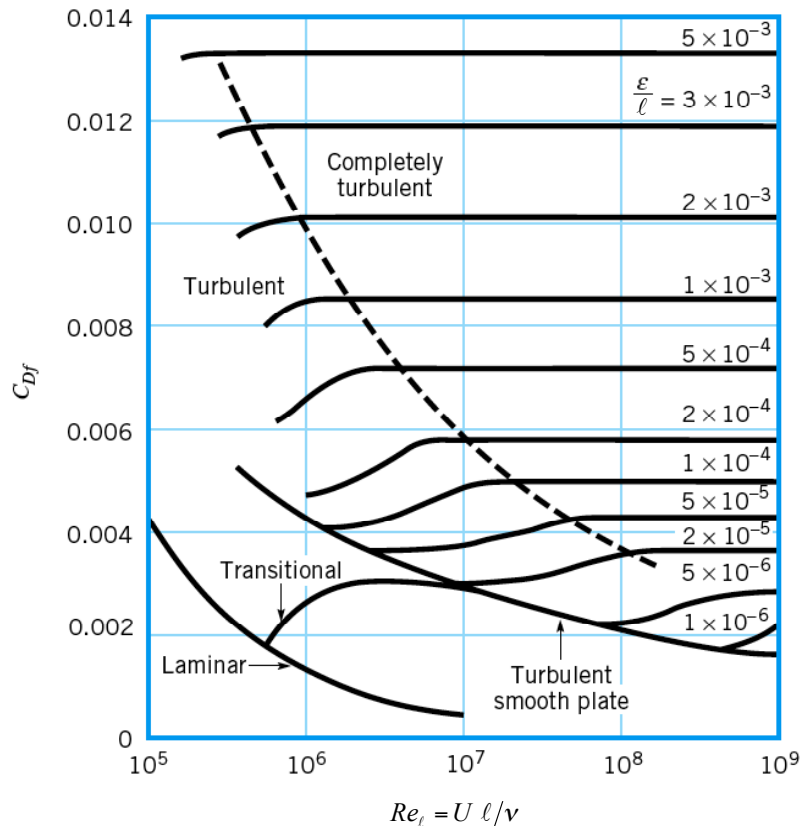
$C_{Df} = \frac{0.455}{(\log Re_\ell)^{2.58}} - \frac{1700}{Re_\ell}$   $5 \times 10^5 < Re_\ell < 10^9$

Turbulent (smooth plate):  $C_{Df} = 0.0743 Re_\ell^{-1/5}$   $5 \times 10^5 < Re_\ell < 10^7$

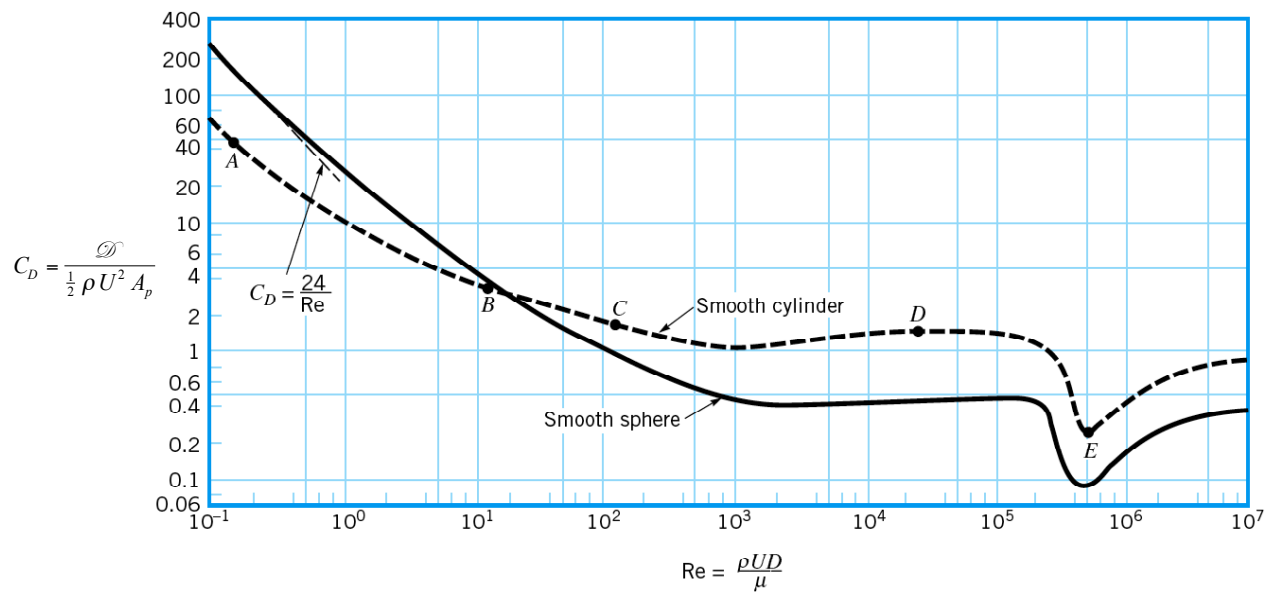
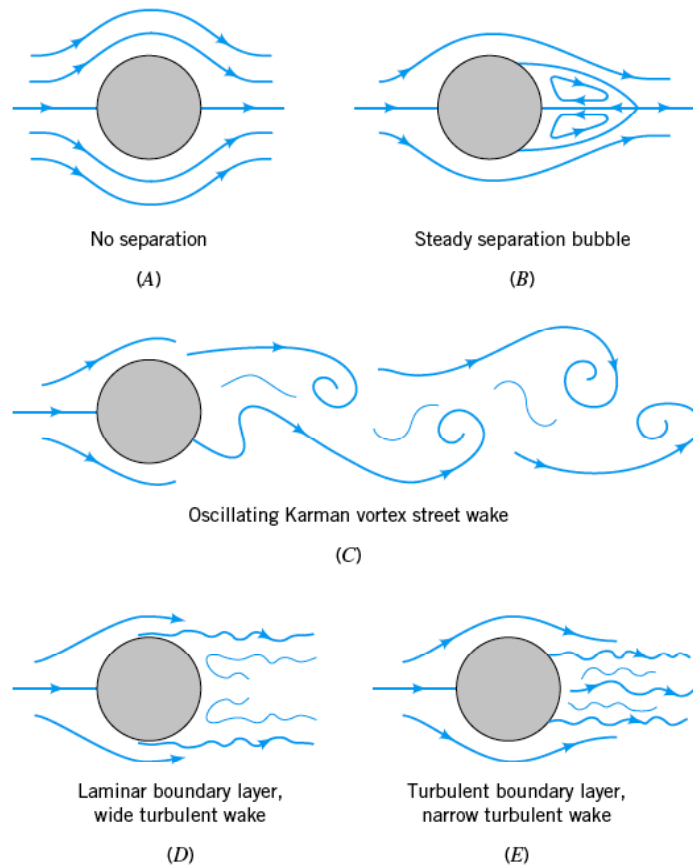
$C_{Df} = \frac{0.455}{(\log Re_\ell)^{2.58}}$   $5 \times 10^5 < Re_\ell < 10^9$

Turbulent (completely turbulent):  $C_{Df} = \left[ 1.89 - 1.62 \log \left( \frac{\varepsilon}{\ell} \right) \right]^{-2.5}$  see Table 8.1 for  $\varepsilon$

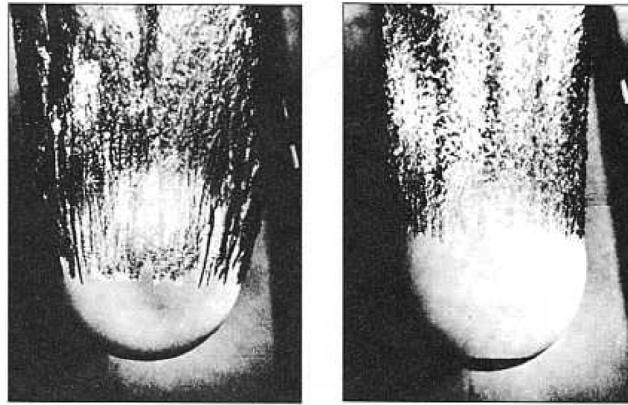
where  $Re_\ell = U \ell / \nu$  is Reynolds number,  $U$  is free stream velocity,  $\nu$  is kinematic viscosity,  $\ell$  is plate length,  $b$  is plate width,  $\varepsilon$  is plate roughness, and  $\mathcal{D}_f$  is drag force due to friction.



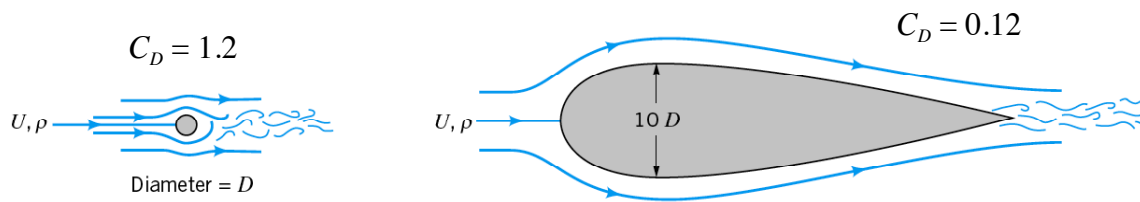
## Streamlines for cylinder in uniform cross flow for a range of Reynolds numbers.



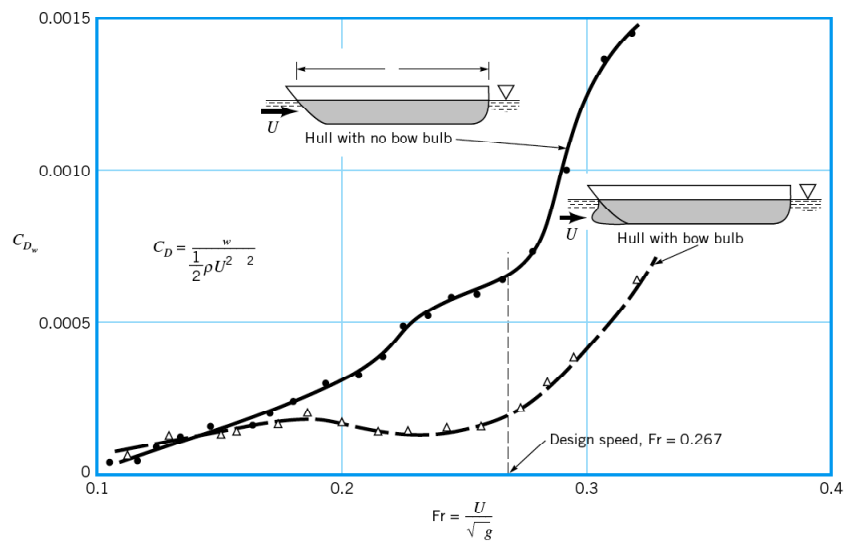
Drag coefficient,  $C_D$ , versus Reynolds number,  $Re$ , where  $\mathcal{D}$  is total drag,  $U$  is uniform velocity,  $D$  is diameter,  $A_p$  is projected frontal area,  $\rho$  is density, and  $\mu$  is viscosity.



Strong differences in laminar and turbulent separation on an 8.5-in. bowling ball entering water at 25 ft/s: (a) smooth ball, laminar boundary layer; (b) same entry, turbulent flow induced by patch of nose-sand roughness (NAVAIR Weapons Division Historical Archives.)

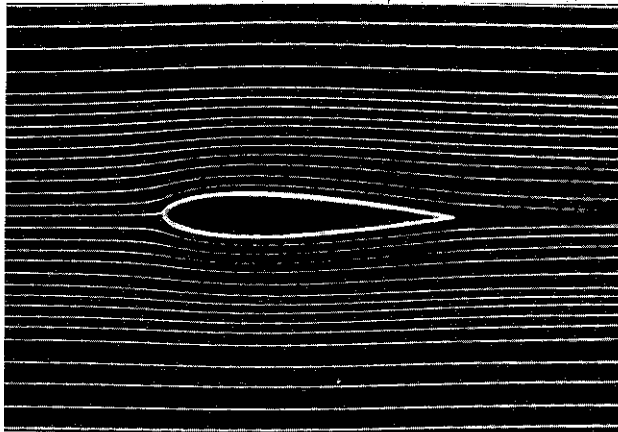


Two objects of considerably different size that have the same drag force.

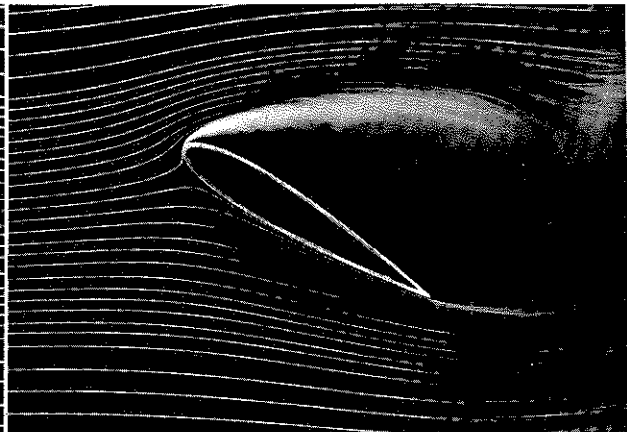


Drag coefficient as a function of Froude number and hull characteristics for that portion of the drag due to the generation of waves (Inui, *Wave Making Resistance of Ships*, 1962).

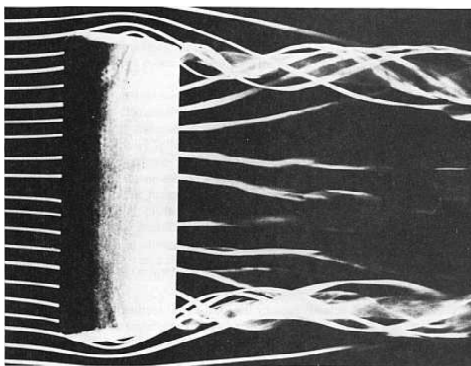
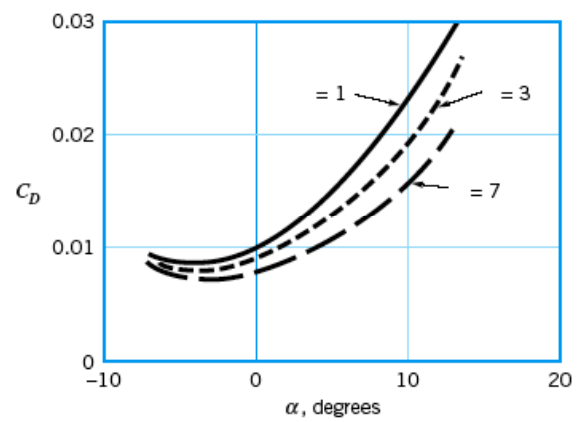
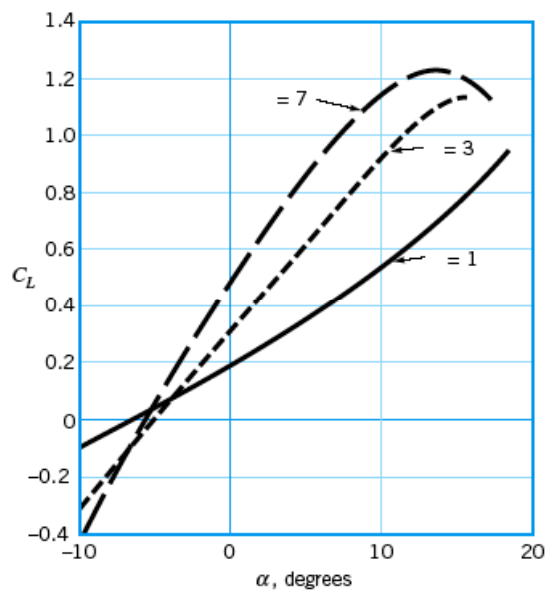
Effect of angle of attack,  $\alpha$ , and aspect ratio,  $\mathcal{H} = b/c$  where  $b$  is span and  $c$  is chord length, on lift coefficient,  $C_L$ , and drag coefficient,  $C_D$ , for typical airfoils.



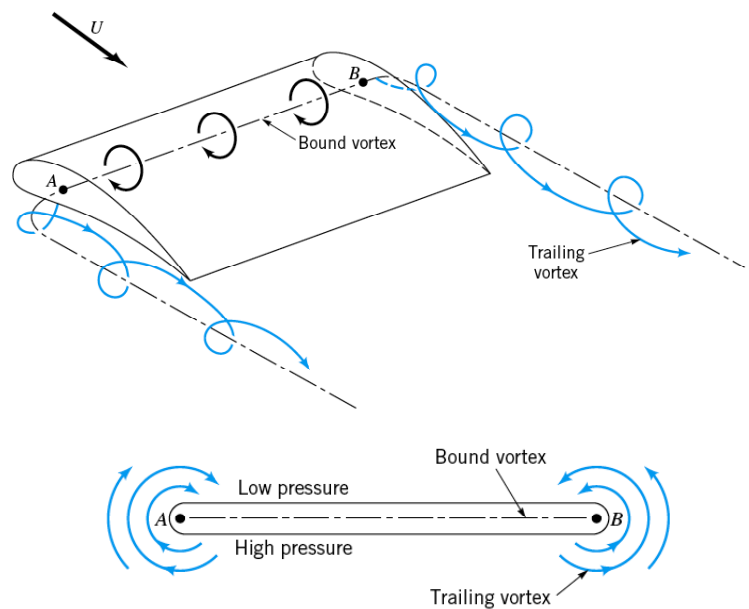
$\alpha = 0^\circ$

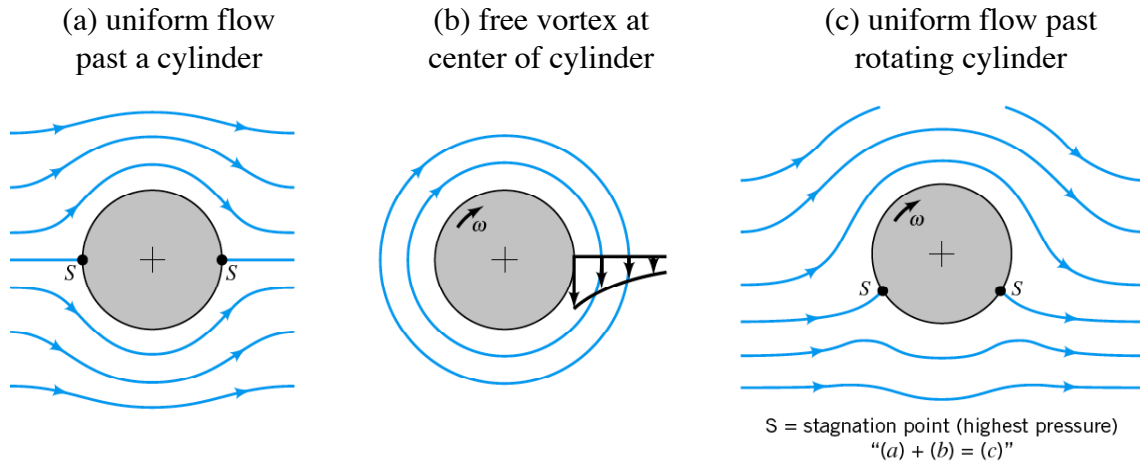


stall at high  $\alpha$

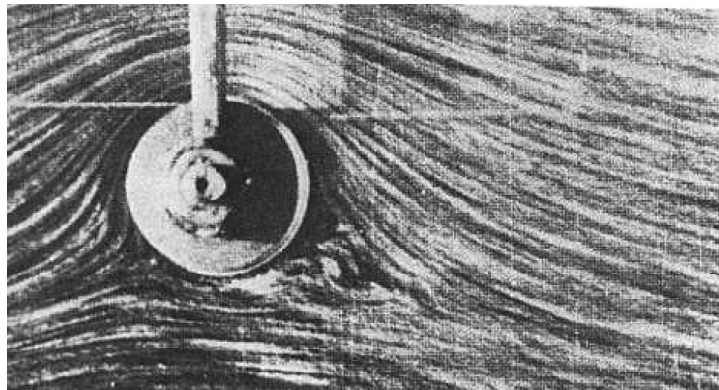


Wing with trailing vortices.





Rotating cylinder  
with separation



Lift coefficient,  $C_L$ , and drag coefficient,  $C_D$ , versus spin ratio,  $SR = (\omega D)/(2U)$ , for a spinning smooth sphere where:

$\omega$	rate of rotation
$D$	diameter
$U$	uniform velocity
$Re$	Reynolds number
$\rho$	density
$\nu$	kinematic viscosity
$\mathcal{D}$	drag
$\mathcal{L}$	lift

