

# Integrály

## 0.1 Základní typy

$$1. \int x^2(x+3) dx$$

$$5. \int \frac{1}{\sqrt{x}} dx$$

$$8. \int \sqrt[3]{x} dx$$

$$2. \int \sqrt{x} dx$$

$$6. \int \frac{1}{x^4} dx$$

$$9. \int \frac{x+1}{x^3} dx$$

$$3. \int x^2\sqrt{x} dx$$

$$7. \int \frac{2}{x^3} dx$$

$$10. \int \frac{x^2+x+3}{x^2} dx$$

## 0.2 Jednoduché substituce řešitelné “z hlavy”

$$1. \int e^{-3x} dx$$

$$6. \int \cos \frac{x}{2} dx$$

$$11. \int \frac{x}{x^2+2} dx$$

$$2. \int \cos 3x dx$$

$$7. \int \sin \frac{x}{3} dx$$

$$12. \int \operatorname{tg} x dx$$

$$3. \int e^{-x} dx$$

$$8. \int (3x-5)^5 dx$$

$$13. \int \operatorname{cotg} x dx$$

$$4. \int \sin 5x dx$$

$$9. \int \frac{1}{2x-3} dx$$

$$14. \int \frac{3x}{x^2+5} dx$$

$$5. \int e^{4x} dx$$

$$10. \int \frac{1}{(2x+5)^3} dx$$

## 0.3 Substituce

$$1. \int x \sin x^2 dx$$

$$6. \int \sin^3 x \cos x dx$$

$$11. \int \frac{\cos x}{\cos^2 x + 7} \sin x dx$$

$$2. \int x \sin(x^2+3) dx$$

$$7. \int \frac{\cos x}{\sin^2 x} dx$$

$$12. \int \frac{x}{\sqrt{x+3}} dx$$

$$3. \int x e^{x^2} dx$$

$$8. \int \frac{\sin x}{\cos^4 x} dx$$

$$13. \int \frac{3}{x\sqrt{x-1}} dx$$

$$4. \int x \cos x^2 dx$$

$$9. \int \frac{\sin x}{\sin^2 x + 5} \cos x dx$$

$$14. \int \frac{1}{x+\sqrt{x}} dx$$

$$5. \int x^2 e^{x^3+2} dx$$

$$10. \int \frac{x}{\sqrt{x-2}} dx$$

## 0.4 Per partes

$$1. \int x \cos x \, dx$$

$$5. \int x \ln x \, dx$$

$$9. \int \operatorname{arctg} x \, dx$$

$$2. \int x^2 e^x \, dx$$

$$6. \int x^2 \sin x \, dx$$

$$10. \int x \operatorname{arctg} x \, dx$$

$$3. \int \ln x \, dx$$

$$7. \int x^2 \ln x \, dx$$

$$11. \int x e^{-x} \, dx$$

$$4. \int x e^x \, dx$$

$$8. \int x \cos 3x \, dx$$

$$12. \int x \sin 2x \, dx$$

## 0.5 Určitý integrál

$$1. \int_0^1 (x^2 + x + 2) \, dx$$

$$3. \int_1^2 (2x + 1) \, dx$$

$$5. \int_0^1 (x^3 - 3x^2 + 1) \, dx$$

$$2. \int_0^2 (x^2 + 1) \, dx$$

$$4. \int_1^2 (x^3 - 2x + 1) \, dx$$

$$6. \int_1^2 \frac{x^3 + 2x + 3}{x^2} \, dx$$