



Parallel Computing

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Parallel Algorithms	Linear Array and Ring
Parallel sorting Merge sort Bitonic Merging Bitonic Sorting Prefix Computation Binary Adder forse? FFT for Powers of Two Benes Permutation	Linear Array Ring Binary Hypercube Binary Hypercube Multidimensional Meshes and Tori Embeddings and simulations
Network Definitions	Altri blocchi di embedding specifiche

Degree
In an undirected graph $G = (V, E)$, the **degree of a node** $a \in V$ is the number of its immediate neighbours, that is:

$$\text{degree}(a) = |\{b \in V : (a, b) \in E\}|$$

The **degree of a graph** is the maximum degree of any of its nodes, that is:

$$\text{degree}(G) = \max_{a \in V}(\text{degree}(a))$$

A graph is said to be **regular of degree** Δ if all its nodes have degree Δ

Diameter

In an undirected graph $G = (V, E)$, the distance $\text{dist}_G(a, b)$ between two nodes a and b is defined as the length of a shortest path in G from a to b . The **diameter of G** is defined as the maximum distance between any pair of nodes, that is:

$$\text{diam}(G) = \max_{a, b \in V}(\text{dist}_G(a, b))$$

Diameter and Degree Lower bound for any connected graph G with P nodes and $\text{degree}(G) = \delta \geq 3$:

$$\text{diam}(G) > \log_{\delta-1}(P - 1) + \log_{\delta-1}((\delta - 2)/\delta)$$

Bandwidth

Let $G = (V, E)$ be an undirected graph. Let $S \subseteq V$ be a subset of nodes. $\delta_G(S)$ is the number of edges between set S and its complement $V - S$

$$\delta_G(S) = |(S \times (V - S)) \cap E|$$

Dichotomy width Given m integer $0 \leq m \leq |V|$:

$$\delta_G(m) = \min_{S \subseteq V, |S|=m} \delta_G(S)$$

Bisection width Bisection width with $m = \lfloor |V|/2 \rfloor$:

$$b_G = \delta_G(\lfloor |V|/2 \rfloor)$$

Tipo LA e H, H e M, M e LA presi anche da esami e soluzioni del prof oltre che dalle slide viste a lezione