

# Performance Modeling of Computer Systems and Networks

Prof. Vittoria de Nitto Personè

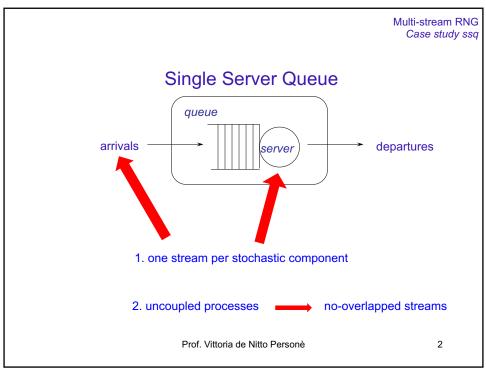
Multi-stream application examples

Università degli studi di Roma Tor Vergata

Department of Civil Engineering and Computer Science Engineering

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```
P. 110 discrete
                                                                            Multi-stream RNG
                                                                              Case study ssq
                            ssq2 revisited
                Use rngs functions for arrivals and services
                         double GetArrival(void) {
                         static double arrival = START;
                         SelectStream(0); posso method do & a 255
                         arrival += Exponential(2.0);
                         return (arrival);
                         double GetService(void) {
                         SelectStream(2);
                         return (Uniform(1.0, 2.0));
                                                  inizializza tulti
7 i 256 flussi
                • include "rngs.h" and use PlantSeeds(12345)
                                        (in place of PutSeed(12345))
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```

```
arrival and service processes are uncoupled
  stream 0 for arrivals, stream 1 for services
    for 10025 jobs
      average interarrival time = 1.99
      average wait ..... = 3.92
      average delay ..... = 2.41
      average service time .... = 1.50
      average # in the node ... = 1.96
      average # in the queue .. = 1.21
      utilization ..... = 0.75
stream 0 for arrivals, stream 2 for services (or e.g. stream 128 to get more separation)
   for 10025 jobs
    average interarrival time = 1.99
    average wait ..... = 3.86
    average delay ..... = 2.36
    average service time .... = 1.50
                                                      Theoretical values
                                                              \overline{d}
                                                      \overline{w}
                                                                     \overline{S}
                                                                                           \bar{x}
    average # in the node ... = 1.93
    average # in the queue .. = 1.18
                                              2.00 3.83 2.33 1.50 1.92 1.17
                                                                                         0.75
    utilization ..... = 0.75
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                                                                                     4
```

P63 Mide, PIII discrete

Multi-stream RNG
Case study ssq

#### **Uncoupling Stochastic Processes**

Consider changing the service process to Stessa media Uniform(0.0, 1.5) + Uniform(0.0, 1.5) + Uniform(0.0, 1.5)

- Without uncoupling, arrival process sequence would change!
- With uncoupling, the service process "sees" exactly the same arrival sequence
- · Important variance reduction technique

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```
Theoretical values
                                         2.00 3.83 2.33 1.50 1.92 1.17 0.75
stream 0 for arrivals, stream 1 for services
       for 10025 jobs
         average interarrival time = 1.99
                                              diversió como della variabilità!
         average wait ..... = 4.29
         average delay ..... = 2.78
         average service time .... = 1.51
         average # in the node ... = 2.15
         average # in the queue .. = 1.40
         utilization ..... = 0.76
                                           for 10025 jobs
                                             average interarrival time = 1.99
                                             average wait ..... = 3.92
                                             average delay ..... = 2.41
                                             average service time .... = 1.50
                                             average # in the node ... = 1.96
                                             average # in the queue .. = 1.21
                                             utilization ..... = 0.75
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```

Multi-stream RNG Case study ssq

# ssq with Multiple Job Types

- · Consider multiple job types, each with its own arrival and service process
- Two job types:
   Class 0: Exponential(4.0) interarrivals, Uniform(1.0, 3.0) service
   Classe 1: Exponential(6.0) interarrivals, Uniform(0.0, 4.0) service
- Use rngs to allocate a different stream to each stochastic process

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Multi-stream RNG Case study ssq

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# Arrival process

```
double GetArrival(int *j)
                                      /* j corrisponds to job type */
const double mean[2] = \{4.0, 6.0\};
static double arrival[2] = {START, START};
static int init = 1;
double temp;
                                                       if (arrival[0] <= arrival[1])
if (init) {
                                                                  *j = 0; ___
                                                                                → The first arrival
           SelectStream(0);
                                                                                  is of class 0!
           arrival[0] += Exponential(mean[0]);
                                                                  *j = 1;
           SelectStream(1);
                                                       temp = arrival[*j];
           arrival[1] += Exponential(mean[1]);
                                                       SelectStream(*j);
           init = 0;
                                                       arrival[*j] += Exponential(mean[*j]);
                                                       return (temp);
                                                                       ritorna prossimo arrivol
time e sob type con
indice & o I.
                                                      }
   • streams 0 and 1 are used for interarrival times of
     class 0 and class 1 jobs respectively
```

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Multi-stream RNG Case study ssq

example 3.2.9 Service process

```
double GetService(int j) pclasse \emptyset \circ 1 {

const double min[2] = {1.0, 0.0};

const double max[2] = {3.0, 4.0};

SelectStream(j + 2); s^{\text{tream } 2} \circ s^{\text{tream } 2}

return (Uniform(min[j], max[j]));
}
```

- *j* corrisponds to the job type (0 or 1)
- streams 2 and 3 are used for service times of class 0 and 1 respectively
- All four simulated stochastic processes are uncoupled!
- Any process could be changed without altering the random sequence of others!

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Consistency checks

(Ar complie un modelle, t' importante variationne le consistence!)

• The "teorethical" steady-state statistics are  $\overline{r}$   $\overline{w}$   $\overline{d}$   $\overline{s}$   $\overline{l}$   $\overline{q}$   $\overline{x}$ 2.40 7.92 5.92 2.00 3.30 2.47 0.83 exact analytical results, No simulation!

• obvious consistency checks:

• both job types have avg service time of  $2.0 \rightarrow \overline{s} = 2.00$ • arrival rate should be

1/4 + 1/6 = 5/12  $\rightarrow \overline{r} = 12/5 = 2.40$ •  $\overline{x}$  should be ratio of arrival to service rates  $\frac{5/12}{1/2} = 5/6 \cong 0.83$ Prof. Vittoria de Nitto Personè 10

Multi-stream RNG
Case study ssq

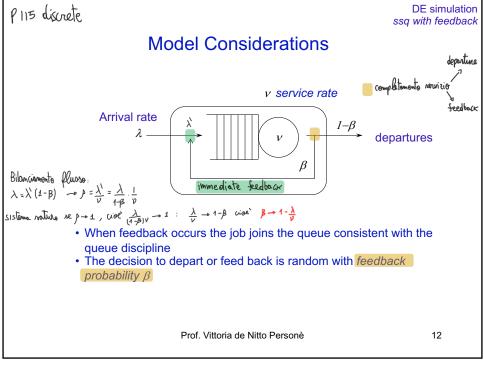
# **Exercises**

• Exercises: 3.2.3, 3.2.4, 3.2.7

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```
PE simulation ssq with feedback

• Feedback is independent of past history
• In theory, a job may feed back arbitrarily many times

int GetFeedback(double beta) /* 0.0 <= β < 1.0 */

{
    SelectStream(2);
    if (Random() < beta)
        return (1); /* feedback*/
    else
        return (0); /* no feedback */
}
```

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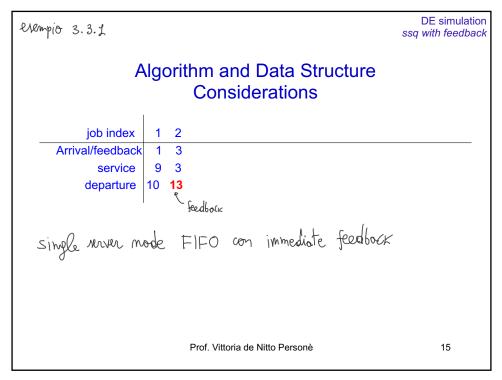
DE simulation ssq with feedback

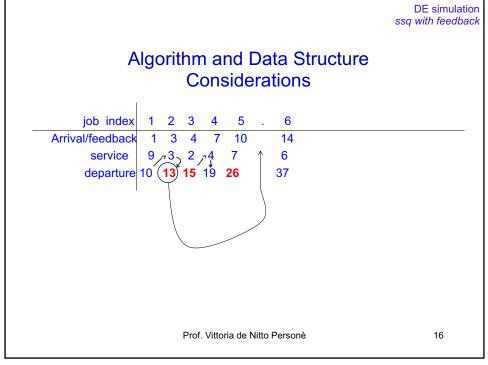
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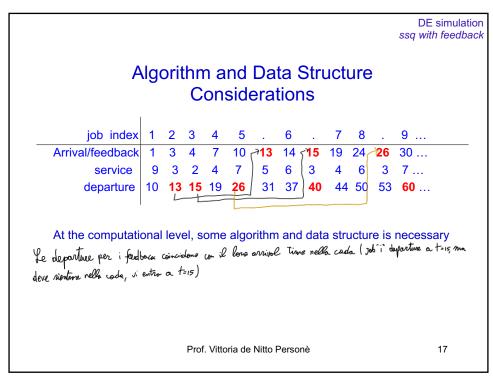
#### Statistical considerations

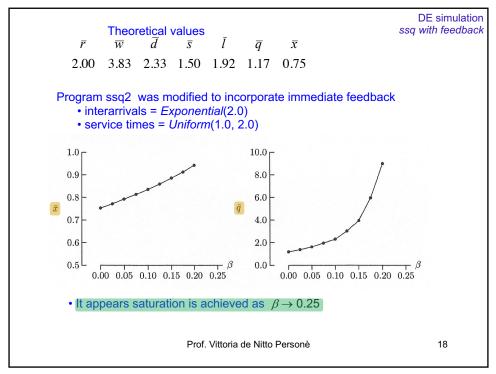
- Index i=1, 2, 3, ... counts jobs that enter the service node
   fed-back jobs are not recounted
- Using this indexing, all job-averaged statistics remain valid
- We must update delay times, wait times and service times for each feedback
- Jobs from outside the system are merged with jobs from the feedback process
- The steady-state request-for-service rate is larger than  $\lambda$  by the positive additive factor  $\beta \bar{x}v$  ( Rub. forthack . job in sorvice rate service)
- Note that  $\bar{s}$  increases with feedback but  $1/\nu$  is the average service time per request

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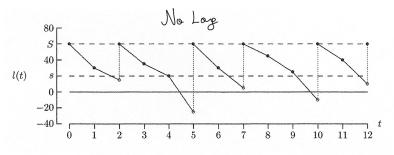




DE simulation InvSys with delivery lag

### Inventory system with delivery lag

- delivery lag (dl) occurs when orders are not delivered immediately
- Lag is assumed to be random and independent of order size
- Without lag, inventory jumps occur only at inventory review times



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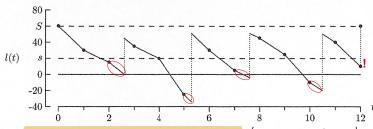
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DE simulation InvSys with delivery lag

## Inventory system with delivery lag

· With delivery lag, inventory jumps occur at arbitrary times

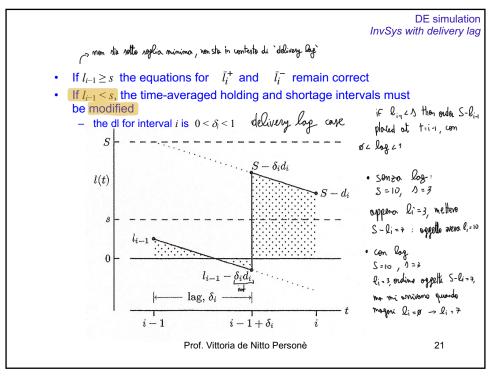


- . The last order is assumed to have no lag (per bilanciomento flund)
- We assume that orders are delivered before the next inventory review

· With this assumption, there is no change to the specification model

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#### Discrete-Event Simulation

## **Consistency Checks**

- It is fundamentally important to verify extended models with the parent model (before the extension)
  - Set system parameters to special values
- Set  $\beta = 0$  for the ssq with feedback
  - Verify that all statistics agree with parent
- Using the library rngs facilitates this kind of comparison
- It is a good practice to check for intuitive "small-perturbation" consistency
  - Use a small, but non-zero  $\pmb{\beta}$  and check that appropriate statistics are slightly larger

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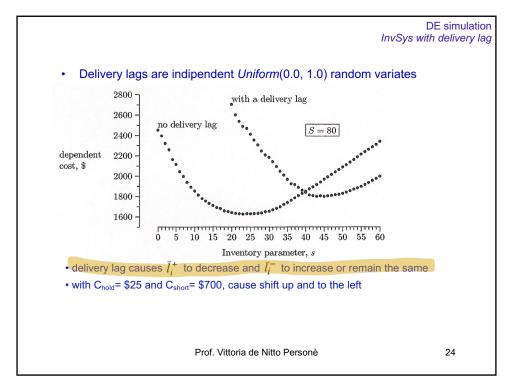
DE simulation InvSys with delivery lag

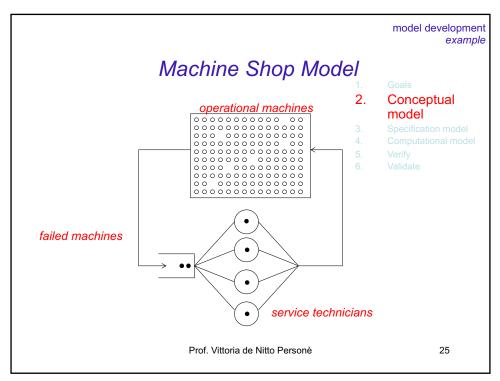
- For the InvSys with delivery lag,  $\delta_i = 0.0$  iff no order during  $i^{\text{th}}$  interval,  $0 < \delta_i < 1.0$  otherwise
- The InvSys is *lag-free* iff  $\delta_i = 0.0$  for all i
- If (S, s) are fixed then, even with small dl:
  - $\bar{o}, \bar{d}, \bar{u}$  are the same regardless of delivery lag
  - Compared to the lag-free system,  $\bar{l}_i^+$  will decrease
- Compared to the lag-free system,  $\bar{l}_i^- \text{will}$  increase or remain unchanged

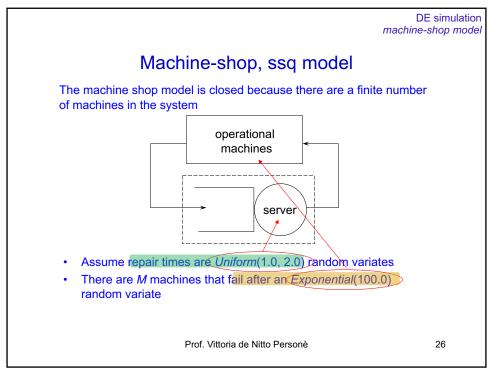
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DE simulation machine-shop model

#### Program ssms

- program ssms simulates a Single Server Machine-Shop
- the library rngs is used to uncouple the random process
- · the failure process is defined by the array failures
  - a O(M) search is used to find the next failure
  - alternate data structures can be used to increase computational efficiency

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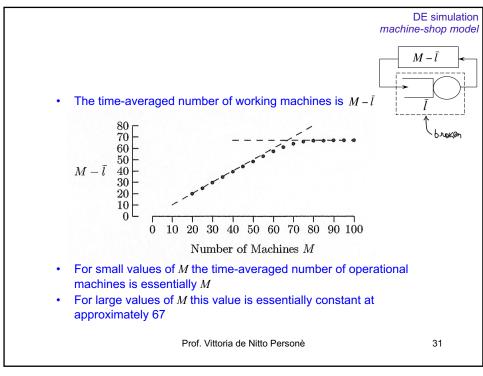
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```
double GetFailure(void)
{ SelectStream(0);
   return (Exponential(100.0));}
double NextFailure(double failure[], int *m)
{ int i = 0;
   double t = failure[0];
   *m = i;
   for (i = 1; i < M; i++)</pre>
       if (failure[i] < t) {</pre>
          t = failure[i];
         *m = i;
       }
   return (t);
}
double GetService(void)
  SelectStream(1);
   return (Uniform(1.0, 2.0));
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                                                            28
```

```
int main(void)
            = 0; /* job (machine failure) index */
long
    index
double arrival = START; /* time of arrival (failure) */
*/
                                           */
double departure = START; /* time of service completion
                                           */
                   /* machine index 0,1,...(M-1)
                                           */
int m;
                   /* list of next failure times */
double failure[M];
struct {
                   /* sum of ...
 double wait;
                   /* wait times
 double delay;
                   /* delay times
                                     */
 double service;
 \} sum = {0.0, 0.0, 0.0};
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                                        29
```

```
PlantSeeds(123456789);
                               /* initial failures */
for (m = 0; m < M; m++)
failure[m] = START + GetFailure();
while (index < LAST) {</pre>
  index++;
              = NextFailure(failure, &m);
  arrival
  if (arrival < departure)</pre>
      delay
                = departure - arrival;
  else
                 = 0.0;
    delay
  service
               = GetService();
  wait
               = delay + service;
                                    /* completion of service */
  departure
               = arrival + wait;
  failure[m] = departure + GetFailure(); /* next failure, machine m */
              += wait;
  sum.wait
             += delay;
  sum.delay
  sum.service += service;
sum.interarrival = arrival - START;
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                                                                30
```



Exercises

• Exercises: 3.3.2, 3.3.3, 3.3.4, 3.3.7