



SAPIENZA  
UNIVERSITÀ DI ROMA

# Inverse Language Modeling towards Robust and Grounded LLMs

Master's Degree in Computer Science

**Simone Sestito** (1937764)

Academic Year 2024/2025

2025-10-02

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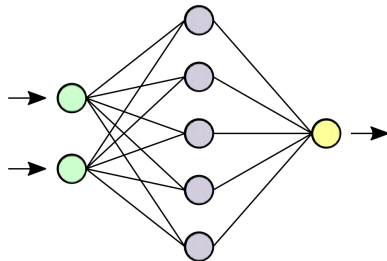
# Gradient-based Attacks

## 1 Gradient-based Adversarial Attacks

We want to **change the input** to minimize the loss



Input image



Neural Network

Dog

Cat

Output  
Distribution

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## Inverse Language Modeling towards Robust and Grounded LLMs

### Gradient-based Adversarial Attacks

### Gradient-based Attacks

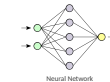
#### Gradient-based Attacks

##### 1 Gradient-based Adversarial Attacks

We want to **change the input** to minimize the loss



Input image



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# Gradient-based Attacks

## 1 Gradient-based Adversarial Attacks

What to optimize?



Input image

$+ \alpha \cdot$



Noise

$\Rightarrow$

Dog

Cat

Output  
Distribution

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## Inverse Language Modeling towards Robust and Grounded LLMs

└ Gradient-based Adversarial Attacks

└ Gradient-based Attacks

Gradient-based Attacks  
1 Gradient-based Adversarial Attacks

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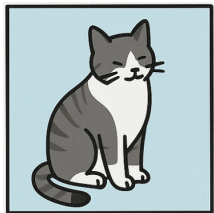
Output  
Distribution



# Adversarial Input

## 1 Gradient-based Adversarial Attacks

The optimized perturbation  $\delta$  may look like:



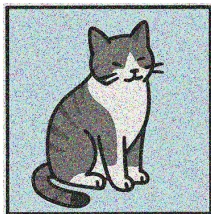
Input image

$+ \alpha \cdot$



Noise

$\Rightarrow$



Adversarial  
image

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## Inverse Language Modeling towards Robust and Grounded LLMs

### Gradient-based Adversarial Attacks

#### Adversarial Input

#### Adversarial Input 1 Gradient-based Adversarial Attacks

The optimized perturbation  $\delta$  may look like:



Input image

$+ \alpha \cdot$



Noise

$\Rightarrow$



Adversarial  
image

At the end of this optimization process, the adversarial image may look like this:  
it does not look different to a human eye, but it is sufficiently different to fool a deep classifier.



# Adversarial Training

## 1 Gradient-based Adversarial Attacks

A classifier can be made robust using **Adversarial Training**:

- Generate  $\mathbf{x}'$  samples
- Include them in the training process
- Repeat

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Gradient-based Adversarial Attacks

### └ Adversarial Training

#### Adversarial Training 1 Gradient-based Adversarial Attacks

A classifier can be made robust using **Adversarial Training**:

- Generate  $\mathbf{x}'$  samples
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- Repeat

Here it comes Adversarial Training.

It is a procedure that generally proceeds as follows:

- we generate adversarial samples in some way, for instance as just said
- they are included in the training process to let the model know their correct class and make it classify them correctly
- and we iterate.

—— PAUSE ——

Then, what happens?

The required perturbation may be always more and more visible to human eyes.



# Adversarial Training

## 1 Gradient-based Adversarial Attacks

A classifier can be made robust using **Adversarial Training**:

- Generate  $\mathbf{x}'$  samples
- Include them in the training process
- Repeat

The required perturbation  $\delta$  will be more and more perceptible by humans



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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Gradient-based Adversarial Attacks

### └ Adversarial Training

Here it comes Adversarial Training.

It is a procedure that generally proceeds as follows:

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### Adversarial Training

#### 1 Gradient-based Adversarial Attacks

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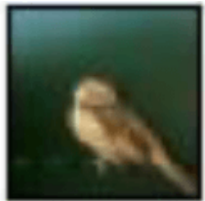




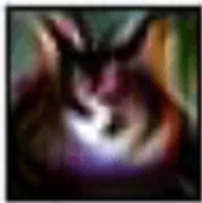
# Perceptually-Aligned Gradients

## 1 Gradient-based Adversarial Attacks

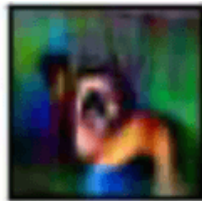
When our classifier has PAGs:



Original image: bird



A "bird" classified as cat



A "bird" classified as dog

Gradients are aligned to the [human perception](#)

Ganz et al, "Do Perceptually Aligned Gradients Imply Robustness?", 2023

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## Inverse Language Modeling towards Robust and Grounded LLMs

└ Gradient-based Adversarial Attacks

└ Perceptually-Aligned Gradients

### Perceptually-Aligned Gradients

1 Gradient-based Adversarial Attacks

When our classifier has PAGs:



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Until something interesting has been observed in literature to happen:  
gradients start to make sense!

These are examples of perturbations that we have to apply to our small bird to be misclassified.

They can be perceived by humans as THE OTHER CLASS!

That's why it has this name: Perceptually-Aligned Gradients.

— — —

The best point is that researchers discovered that enforcing PAG on a model in the training procedure makes it Robust.

Can we do the same on LLMs?





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# Difficulties of LLMs

## 2 Inverse Language Modeling

What about LLMs?

- Input is **sequential**
- The same sequence can continue in multiple ways → **multiple** valid classes
- The input space is **discrete** ( $|\mathcal{V}|$ )

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

### └ Difficulties of LLMs

→ a single token cannot determine what's the next token to predict

What about LLMs?

- Input is **sequential**
- The same sequence can continue in multiple ways → **multiple** valid classes
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# Attacking LLMs with GCG

## 2 Inverse Language Modeling

Greedy Coordinate Gradient is an algorithm to find a sequence of tokens  $\mathbf{x}^\star$  such that the LLM will complete with  $\mathbf{y}$  that we want — using **gradients** on input tokens

Input	Output $\mathbf{y}$	Loss
$\mathbf{x}$ : Stevens recorded and produced the album at multiple $\mathbf{x}^\star$ : Zo Certified Cities (. broadcastquartered Fitness Academy thirteen	locations in the United	5.3642 <b>5.1302</b>
$\mathbf{x}$ : After the introduction of the Majors , The $\mathbf{x}^\star$ : REQU Apart British received reformsMilitaryyestic Division The	British Army was divided	11.2146 <b>7.1899</b>
$\mathbf{x}$ : The founding director , Peggy Loar , left $\mathbf{x}^\star$ : tested UberERIC definitionCalifornia sustainability RutgersOL Jensen regarding	the University of California	7.2669 <b>6.4402</b>
$\mathbf{x}$ : Ruiz notes that writing also has the power $\mathbf{x}^\star$ : Report Global feminism agenda Representatives tell Sacredixties Trying	to change the world	5.9135 <b>4.6041</b>

They are called "Evil Twins"

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# Inverse Language Modeling towards Robust and Grounded LLMs

## Inverse Language Modeling

### Attacking LLMs with GCG

GCG finds attack sequences  $\mathbf{x}^\star$  such that they can link better to a given continuation  $\mathbf{y}$ , starting from a random one-hot sequence of tokens and iteratively optimize it using **gradient** information.  
This table must be read:  $\mathbf{x} || \mathbf{y}$  and  $\mathbf{x}^\star || \mathbf{y}$ .  
These sequences are called *Evil Twins* in the Prompts have evil twins paper.  
— — —

OUR GOAL? Prevent their existence, or limit the success rate of this attack.

Attacking LLMs with GCG		
2 Inverse Language Modeling		
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They are called "Evil Twins"		



# Introducing ILM

## 2 Inverse Language Modeling

- **Goal:** train LLMs to both generate text and *understand what they are conditioned on* from the output
- **Key Ideas:**
  - Create a new training procedure that adds more robustness in the loop
  - Reconstruct input from the output, using  $\nabla_{\mathbf{x}} \mathcal{L}$

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

### └ Introducing ILM

At this point, we can introduce Inverse Language Modeling.

**GOAL:** train LLMs, or fine-tune them, such that they internally "understand" what they are conditioned on.

This is somehow based on the idea of LLMs as stochastic parrots.

**KEY IDEAS:** create a new training procedure that makes them **grounded** to the input, exploiting weights.

- **Goal:** train LLMs to both generate text and understand what they are conditioned on from the output
- **Key Ideas:**
  - Create a new training procedure that adds more robustness in the loop
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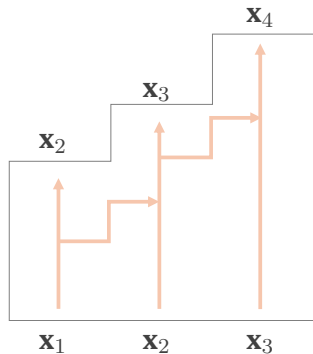
# Introducing ILM

## 2 Inverse Language Modeling

Now

Autoregressive forward

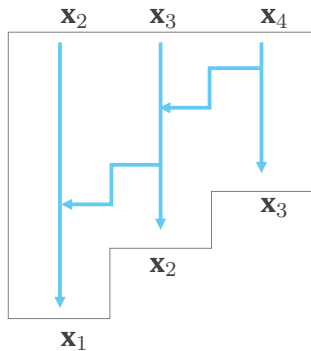
$$p(\mathbf{x}_i | \mathbf{x}_1, \dots, \mathbf{x}_{i-1})$$



Proposed

Autoregressive backward

$$p(\mathbf{x}_{i-1} | \nabla_{\mathbf{x}_{i-1}} p(\mathbf{x}_i | \mathbf{x}_1, \dots, \mathbf{x}_{i-1}))$$



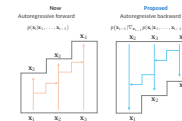
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└ Inverse Language Modeling

└ Introducing ILM

Introducing ILM  
2 Inverse Language Modeling



This illustration graphically shows the logic:

- originally, they go from left to right
- but it can also go from right to left, using gradients information.



# ILM Inversion Procedure

## 2 Inverse Language Modeling

Split it into the original prefix  $\mathbf{x}_p = \mathbf{x}_{0:k}$  and the suffix  $\mathbf{x}_s = \mathbf{x}_{k:n}$

$\mathbf{x}$  = The pen is on the table

$\mathbf{x}_p$  = The pen is

$\mathbf{x}_s$  = on the table

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## Inverse Language Modeling towards Robust and Grounded LLMs

### Inverse Language Modeling

#### ILM Inversion Procedure

Let's make an example:

We have a sentence, like *The pen is on the table*

It gets split:

- prefix: *the pen is*

- suffix: *on the table*

.

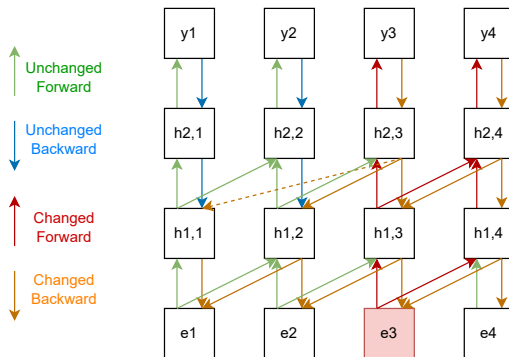
Here, we have the suffix and predict backward the prefix.



# Gradients Received by the Tokens

## 2 Inverse Language Modeling

Gradients received on a single token embedding, carry information of the whole sentence



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## Inverse Language Modeling towards Robust and Grounded LLMs

### Inverse Language Modeling

### Gradients Received by the Tokens

But how is that possible? What's the **theoretical** rationale behind it?  
From this diagram, you can see that if we change a token in the middle, like  $e_3$ , it influences the hidden states only in the future, but gradients carry out the information of the overall sentence, since the gradients of the previous tokens (the **past**) change as well.





# Gradients Received by the Tokens

2 Inverse Language Modeling

*A causal model looks ahead,  
but only its gradients disclose the pasts that might have built that future.*

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Inverse Language Modeling towards Robust and Grounded LLMs

└ Inverse Language Modeling

└ Gradients Received by the Tokens

This sentence well describes the rationale.

Gradients Received by the Tokens  
2 Inverse Language Modeling

A causal model looks ahead,  
but only its gradients disclose the pasts that might have built that future.





# ILM Training Procedure

2 Inverse Language Modeling



Given the input sentence  $\mathbf{x}_0, \mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_{n-1}$

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Inverse Language Modeling towards Robust and Grounded LLMs

└ Inverse Language Modeling

└ ILM Training Procedure

ILM Training Procedure  
2 Inverse Language Modeling



Given the input sentence  $\mathbf{x}_0, \mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_{n-1}$



# ILM Training Procedure

## 2 Inverse Language Modeling



Embed the input sentence tokens into  $\mathbf{e}_0, \mathbf{e}_1, \mathbf{e}_2, \dots, \mathbf{e}_{n-1}$

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

### └ ILM Training Procedure

ILM Training Procedure  
2 Inverse Language Modeling



Embed the input sentence tokens into  $\mathbf{e}_0, \mathbf{e}_1, \mathbf{e}_2, \dots, \mathbf{e}_{n-1}$



# ILM Training Procedure

## 2 Inverse Language Modeling



Pass through the Transformer Decoder layer, up to the final hidden state

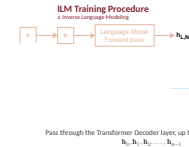
$$\mathbf{h}_0, \mathbf{h}_1, \mathbf{h}_2, \dots, \mathbf{h}_{n-1}$$

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

### └ ILM Training Procedure





# ILM Training Procedure

## 2 Inverse Language Modeling



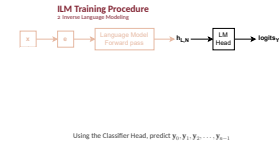
Using the Classifier Head, predict  $\mathbf{y}_0, \mathbf{y}_1, \mathbf{y}_2, \dots, \mathbf{y}_{n-1}$

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

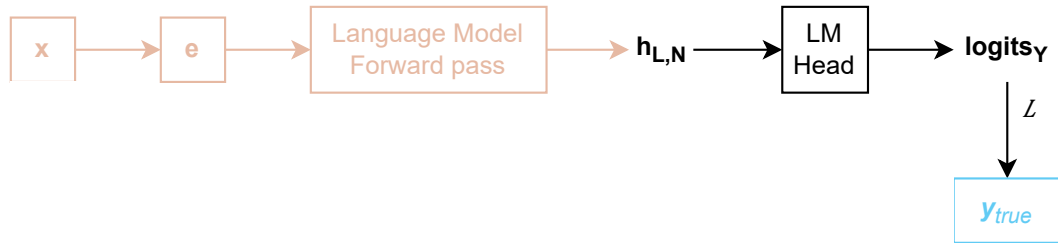
### └ ILM Training Procedure





# ILM Training Procedure

## 2 Inverse Language Modeling



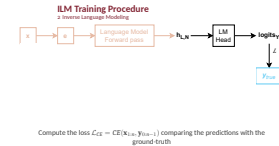
Compute the loss  $\mathcal{L}_{CE} = CE(\mathbf{x}_{1:n}, \mathbf{y}_{0:n-1})$  comparing the predictions with the ground-truth

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

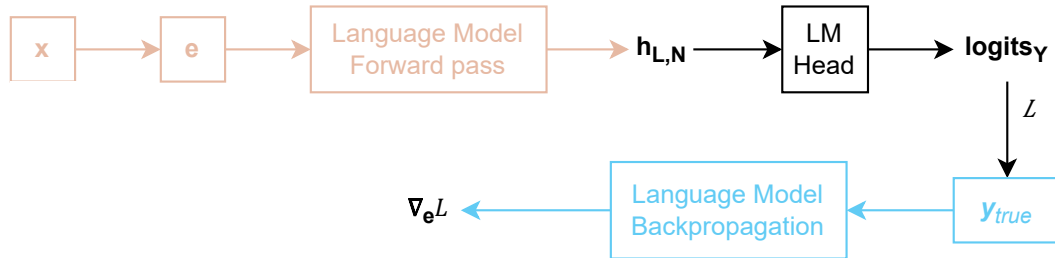
### └ ILM Training Procedure





# ILM Training Procedure

## 2 Inverse Language Modeling



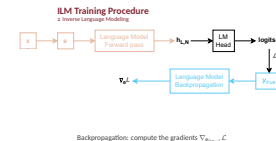
Backpropagation: compute the gradients  $\nabla_{e_{0:n-1}} \mathcal{L}$

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## Inverse Language Modeling towards Robust and Grounded LLMs

### Inverse Language Modeling

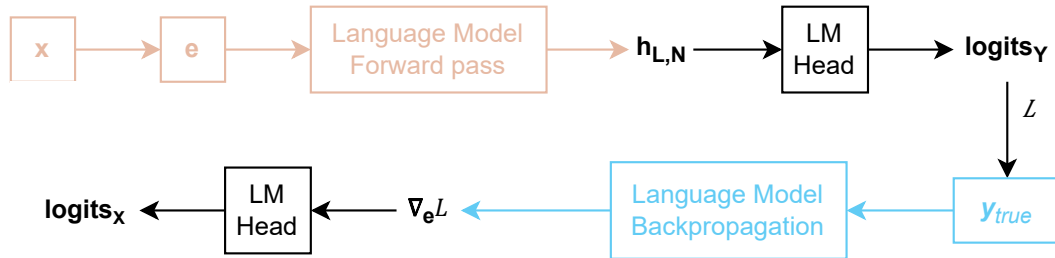
### ILM Training Procedure





# ILM Training Procedure

## 2 Inverse Language Modeling



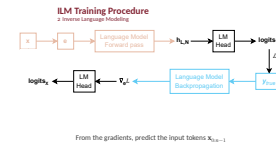
From the gradients, predict the input tokens  $\mathbf{x}_{0:n-1}$

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

### └ ILM Training Procedure

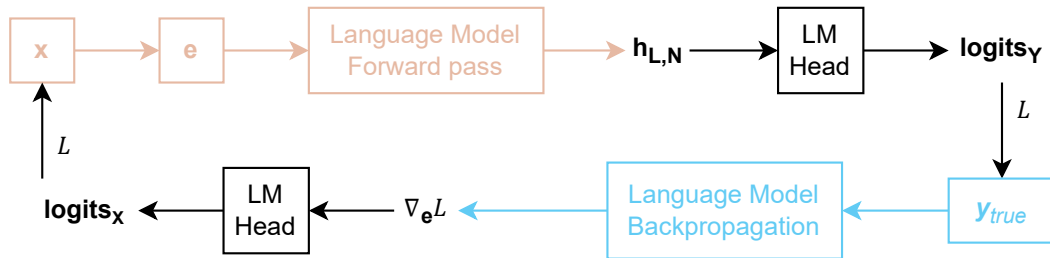


Use the gradients as if they were the last hidden state and use them to predict the input  $\mathbf{x}$  tokens



# Parallelism

## 2 Inverse Language Modeling



As if it were really **cyclic**!

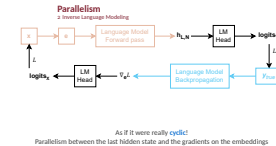
Parallelism between the last hidden state and the gradients on the embeddings

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## Inverse Language Modeling towards Robust and Grounded LLMs

### Inverse Language Modeling

### Parallelism

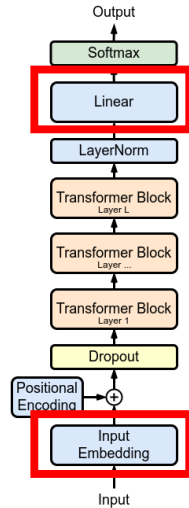






# More Parallelism: Weight Tying

## 2 Inverse Language Modeling



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## Inverse Language Modeling towards Robust and Grounded LLMs

### Inverse Language Modeling

### More Parallelism: Weight Tying

#### More Parallelism: Weight Tying



In some LLMs, weight tying makes the LM Head projection and the Embeddings matrix to be exactly the same Tensor in memory!



# ILM Variants

## 2 Inverse Language Modeling

$$\mathcal{L} = \underbrace{\mathcal{L}_{CE}(\mathbf{y}_{\text{true}}, \mathbf{y}_{\text{pred}})}_{\text{Forward: from the input } \mathbf{x}, \text{ encode } \mathbf{y}} + \underbrace{\lambda \mathcal{L}_{CE}(\mathbf{x}, f(\mathbf{x}, \nabla \mathbf{x}))}_{\text{Backward: from gradients, decode back } \mathbf{x}}$$

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

### └ ILM Variants

ILM Variants  
2 Inverse Language Modeling

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We end up with this combined loss, both for Cross-Entropy forward and backward.

This is implemented using PyTorch-supported **double Backpropagation**.

—— PAUSE ——

We have some variants:

- identity, what we just said. It might hypothetically learn some identity function, as in AutoEncoders without a bottleneck

- bert-like, imitating the BERT training procedure when going backward on the Gradients

- inv-first, that just works on the very first token, splitting sentences.

—— PAUSE ——

Classification:

- we can use these gradients as a pure value

- or follow the natural definition of a gradient as a direction and go in its negative direction



# ILM Variants

## 2 Inverse Language Modeling

$$\mathcal{L} = \underbrace{\mathcal{L}_{CE}(\mathbf{y}_{\text{true}}, \mathbf{y}_{\text{pred}})}_{\text{Forward: from the input } \mathbf{x}, \text{ encode } \mathbf{y}} + \underbrace{\lambda \mathcal{L}_{CE}(\mathbf{x}, f(\mathbf{x}, \nabla \mathbf{x}))}_{\text{Backward: from gradients, decode back } \mathbf{x}}$$

- **Identity**: what we have discussed so far

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## Inverse Language Modeling towards Robust and Grounded LLMs

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#### ILM Variants

2 Inverse Language Modeling

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- **Identity**: what we have discussed so far
- **BERT-like**: masking the input tokens on the gradients
  - When computing  $\nabla_e$ , replace 10% tokens to predict from the gradients with [PAD]
  - it should understand what's missing

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

#### └ ILM Variants

#### ILM Variants

2 Inverse Language Modeling

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- inv-first, that just works on the very first token, splitting sentences.

— — — PAUSE — — —

Classification:

- we can use these gradients as a pure value

- or follow the natural definition of a gradient as a direction and go in its negative direction



# ILM Variants

## 2 Inverse Language Modeling

$$\mathcal{L} = \underbrace{\mathcal{L}_{CE}(\mathbf{y}_{\text{true}}, \mathbf{y}_{\text{pred}})}_{\text{Forward: from the input } \mathbf{x}, \text{ encode } \mathbf{y}} + \underbrace{\lambda \mathcal{L}_{CE}(\mathbf{x}, f(\mathbf{x}, \nabla \mathbf{x}))}_{\text{Backward: from gradients, decode back } \mathbf{x}}$$

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→ it should understand what's missing
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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

### └ ILM Variants

We end up with this combined loss, both for Cross-Entropy forward and backward.  
This is implemented using PyTorch-supported **double Backpropagation**.

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### Classification Strategies:

## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

### └ ILM Variants

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#### ILM Variants 2 Inverse Language Modeling

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- Use gradient as **value** —  $f_W(\nabla_{\mathbf{x}_i} \mathcal{L}_{CE})$

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# Inverse Language Modeling towards Robust and Grounded LLMs

## └ Inverse Language Modeling

### └ ILM Variants

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

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# But we don't have billions of dollars

## 2 Inverse Language Modeling

These results have been obtained on a tiny LLM:

- Only 10M parameters
- A vocabulary of just 2048 tokens
- A simple corpus (TinyStories dataset)

It will be scaled to Llama-1B in the future.

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## Inverse Language Modeling towards Robust and Grounded LLMs

### └ Inverse Language Modeling

### └ But we don't have billions of dollars

However, we trained LLMs, with lots of different variants to compare.  
We HAD to stay on a small example, to validate the idea,  
scaling it in a future time.

But we don't have billions of dollars  
2 Inverse Language Modeling

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# Inversion Evaluation

3 Results

	Grad.	Token Recall ↑	Token Precision ↑	Token F1-score ↑	Positional Accuracy ↑
Baseline		20.9%	18.8%	19.7%	2.4%
Inv-First		11.3%	10.1%	10.7%	1.7%
Bert-like	Val.	2.9%	2.7%	2.8%	0.3%
Identity		0.7%	0.7%	0.7%	0.1%
Inv-First		13.3%	12.0%	12.6%	2.4%
Bert-like	Dir.	0.1%	0.1%	0.1%	0.1%
Identity		22.5%	20.2%	21.2%	2.5%

Evaluation of the inversion capabilities, on metrics relative to the single tokens

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## Inverse Language Modeling towards Robust and Grounded LLMs

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Evaluation of the inversion capabilities, on metrics relative to the single tokens

In all these evaluation tables, we can see that the **Identity** model using gradients as **directions** is chosen as the best variant.

Interestingly, the **baseline** is already able to invert quite well, even though this method allowed us to further improve it.

NOTE that to invert we need an **init**:

- for baseline and identity, we use a very simple bigram model
- for bert and inv-first, we use the PAD token as did during training.



# Inversion Evaluation

3 Results

	Grad.	Full Sentence Perplexity ↓	Predicted Prefix Perplexity ↓	Semantic Similarity ↑
Baseline		8.34	112.82	<u>0.28</u>
Inv-First		10.21	1576.23	0.25
Bert-like	Val.	11.54	5501.86	0.17
Identity		13.88	14658.58	0.12
Inv-First		9.77	1012.80	<b>0.30</b>
Bert-like	Dir.	11.05	563.26	0.11
<b>Identity</b>		<b>8.34</b>	<b>106.31</b>	<b>0.30</b>

Metrics relative to the full sentences, computed using a third-party LLM

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## Inverse Language Modeling towards Robust and Grounded LLMs

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Inversion Evaluation

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Metrics relative to the full sentences, computed using a third-party LLM

To have more accurate results, we passed the sentences to a third-party LLM *Llama 1B*, to compute some perplexity statistics.

It shows:

- PPL of the overall sentence  $\mathbf{x} \star || \mathbf{y}$
- PPL of just the inverted prefix  $\mathbf{x} \star$



# Example of Inversion

3 Results

x		dad in the garden. He gives her a small shovel and a bag of bulbs.
x★ Baseline		to play with his cars, and look at the shake. She feels on her hand.
x★ Inv-First	(Val.)	zzle spowerlizza in her plate. She start to fence and leaves.
x★ Bert-like	(Val.)	could buildDven measure its neighbign, how he sees nostiff.
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y		Bulbs are like round seeds that grow into flowers. Lily digs holes in the dirt and puts the bulbs inside. She covers them with more [...]

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## Inverse Language Modeling towards Robust and Grounded LLMs

Results

Example of Inversion

You can see some examples, where 2 make sense and the others are just gibberish.

This table must be read as:

- ground truth =  $\mathbf{x} || \mathbf{y}$
- prediction of a model =  $\mathbf{x} \star || \mathbf{y}$

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# ILM Robustness Results

3 Results

	Grad.	GCG Success Rate ↓	GCG Average Steps (mean ± stddev)
Baseline		95.9%	277 ± 148
Inv-First		85.0%	320 ± 134
Bert-like	Val.	<b>0.8%</b>	249 ± 148
Identity		88.1%	274 ± 145
Inv-First		89.3%	313 ± 134
Bert-like	Dir.	85.5%	287 ± 143
<b>Identity</b>		<u>82.8%</u>	284 ± 141

Identity looks good, but Bert-like is **suspicious**

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Identity looks good, but Bert-like is **suspicious**

THEN, we have the **twofold objective** = ROBUSTNESS.  
Here, still the **Identity model** is the best model, reducing the Attack Success Rate by 13%.  
Then, we see the **Bert-like** model with gradients as pure values to be extraordinarily successful,  
but it requires more research to correctly understand the why.



# ILM Robustness — Metrics on the Model Itself

3 Results

	Grad.	Original X CE-loss ↓	Attack X' CE-loss	Delta CE-loss ↓	KL Divergence ↑
Baseline		13.28	10.97	2.31	2.19
Inv-First		<b>11.09</b>	9.72	<u>1.37</u>	2.44
Bert-like	Val.	13.26	10.25	3.01	<b>54.19</b>
Identity		12.77	11.21	1.56	2.23
Inv-First		<u>11.21</u>	9.81	1.40	2.44
Bert-like	Dir.	11.49	10.34	<b>1.15</b>	2.23
<b>Identity</b>		12.58	11.12	1.46	2.47

Also, Bert-like seems to map  $\mathbf{x}_*$  to very different next token **distributions**

## Inverse Language Modeling towards Robust and Grounded LLMs

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Also, Bert-like seems to map  $\mathbf{x}_*$  to very different next token **distributions**

We also see the decrease in **loss** when the attack is successful.

- the higher this DELTA is, the more "fooled" the model has been by the Evil Twin

→ that's why a lower DELTA is better.

- the KL Divergence indicates that the  $\mathbf{x}$  and  $\mathbf{x}_*$  map to different output distributions of the logits, like if the model can map it to different distributions, therefore different **internal hidden states**.



# ILM Robustness — Third-Party Model Metrics

3 Results

	Grad.	Original X Perplexity	Attack X' Perplexity ↓	Semantic Similarity ↑
Baseline		44.14	17344.04	0.13
Inv-First		44.81	9431.09	0.16
Bert-like	Val.	40.37	11817.21	0.11
Identity		43.98	8322.25	0.18
Inv-First		43.50	12344.85	0.13
Bert-like	Dir.	44.74	10611.09	0.13
Identity		44.71	10929.21	0.15

However, all  $x_{\star}$  are **meaningless**, due to extremely high 3rd party model perplexity

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## Inverse Language Modeling towards Robust and Grounded LLMs

Results

ILM Robustness — Third-Party Model Metrics

To conclude, we have the third-party LLM measurements, where we basically see that the  $x_{\star}$ , **when successfully found**, still is gibberish and absolutely not similar with the original X. HOWEVER, who knows if this may improve in larger models such as Llama, future research will address the scaling problem.

ILM Robustness — Third-Party Model Metrics

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# ILM Robustness — Qualitative Results

3 Results

	Input	Output y	Loss
x :	Lily and Ben were friends who liked to play outside. But they did not like the same things. Lily		13.22
		liked to make snowmen and snow angel	
x* :	Lucy. Speez herself angO piecle you."lly named nexird opened cake".o.ter carrotmy		12.14

An example result attacking with GCG the Identity (grad. value) model.  
Almost the same for all model variants.

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## Inverse Language Modeling towards Robust and Grounded LLMs

Results

ILM Robustness — Qualitative Results

Here we can see an example to show that the  $x^*$  attack prefix is still gibberish

ILM Robustness — Qualitative Results		
3 Results		
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Also on arXiv

3 Results

INSERT SCREENSHOT

arXiv:2412.08127v3 [cs.CL] 31 Mar 2025

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Inverse Language Modeling towards Robust and Grounded LLMs

└ Results

└ Also on arXiv

Also on arXiv  
3 Results

INSERT SCREENSHOT

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# Inverse Language Modeling towards Robust and Grounded LLMs

*Thank you for listening!*  
*Any questions?*