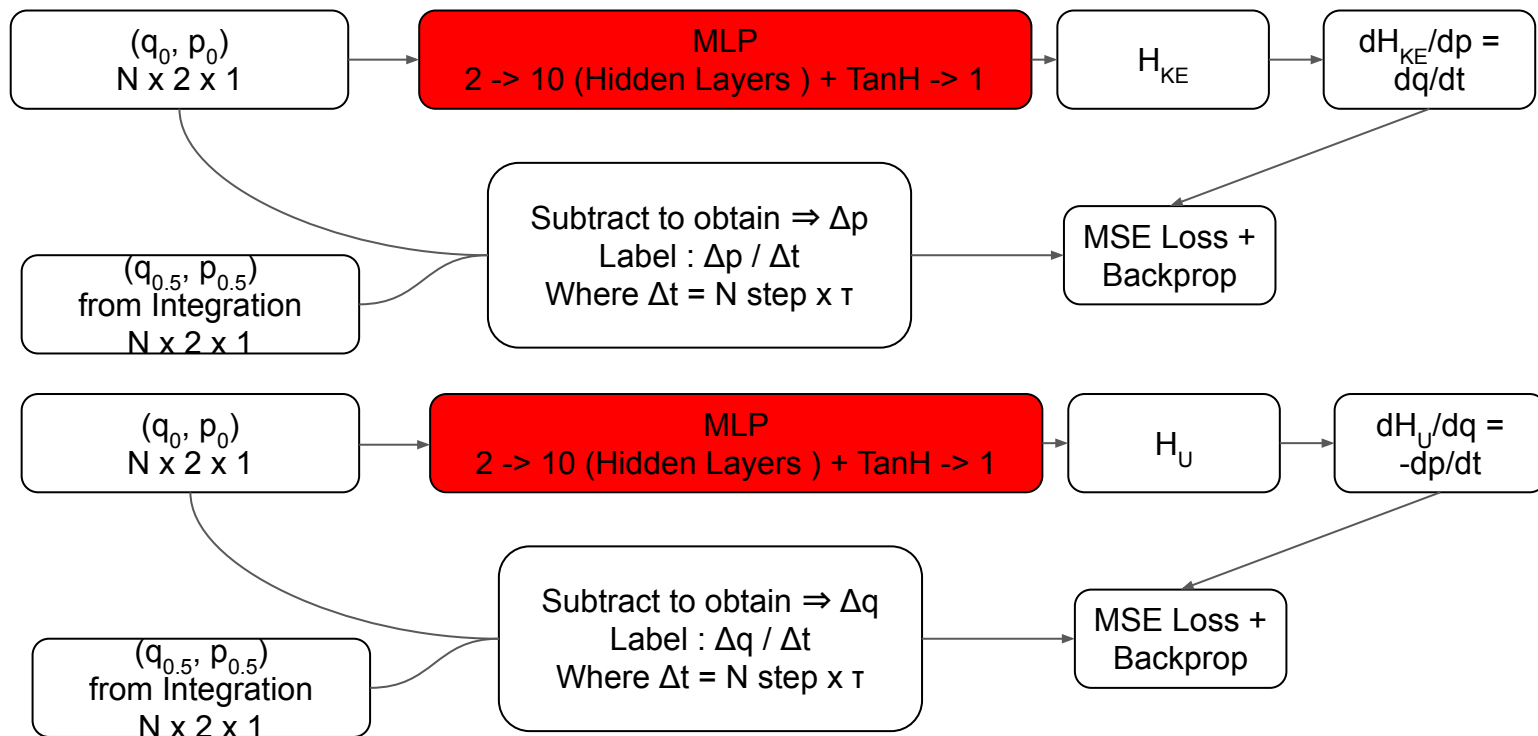


MD ML 7

2 Models

Proposed Hamiltonian Architecture



Training Setting

Optimizer : Adam

Learning Rate (LR) : 1e-3

Scheduler : None

Seed : 937162211 (9-digit Prime Number)

Epochs : 100

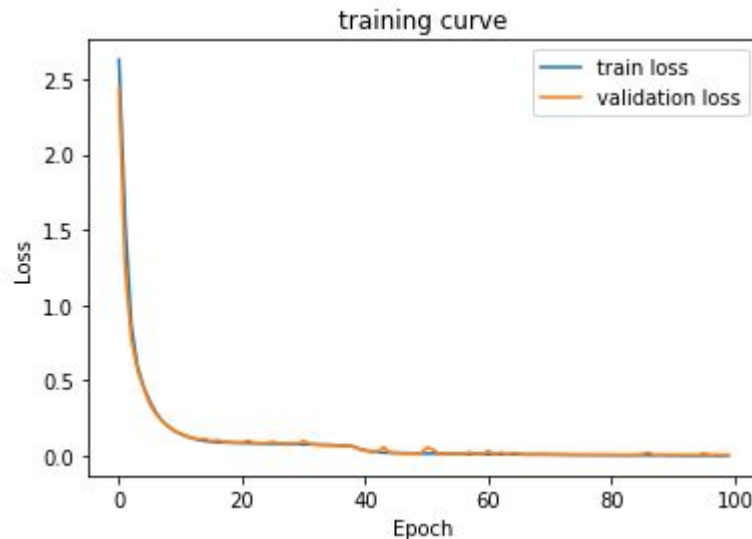
Batch Size : 32 / Shuffle

Large Time Step : 0.01 (1 Step) = 0.01

Ground Truth : 0.01

Final Statistic : $\Delta q = 0.00034$ (5 d.p)

$\Delta p = 0.00099$ (5 d.p)



Remarks :

1. Tried using scheduler of reduce on plateau, patience = 10 , factor = 0.99, loss stuck at ~1.2
2. Temperature used : 1 - 10, interval 1
3. Tried 50 epochs, loss seems to be fluctuating
4. Seed to consider :
 - a. Random.seed
 - b. Numpy.seed
 - c. Torch.seed
 - d. Torch.cuda.seed

Distribution Sampling

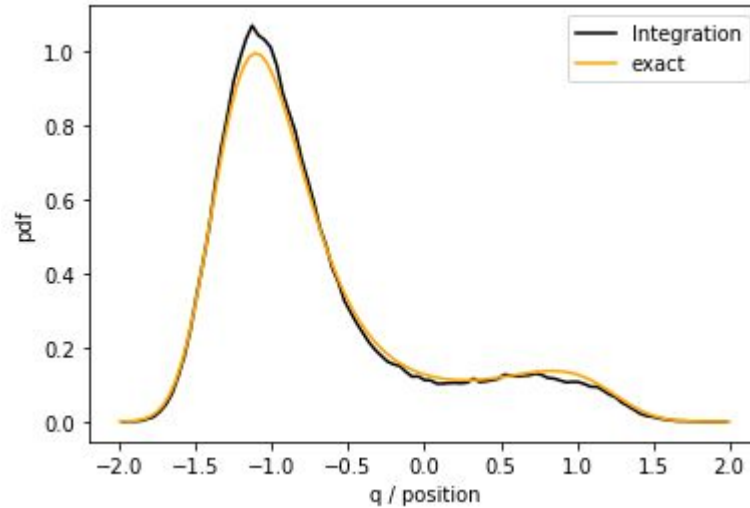
To update the distribution, we use the following splitting :

$$P(t = t + \Delta t) = [L_Y (L_{p(\Delta t/n)} L_{q(\Delta t/n)} L_{p(\Delta t/n)})^n L_Y] P(t = t)$$

Where $\Delta t/n = 0.01$ for the ground truth reference to calculate the **mean absolute error**

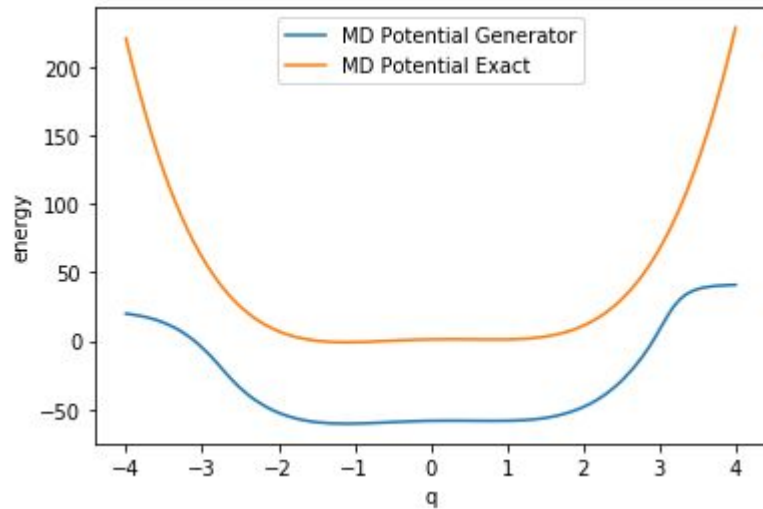
1. $(L_{p(\Delta t/n)} L_{q(\Delta t/n)} L_{p(\Delta t/n)})^n$ can be replaced by the model separately where $n = 1$
2. The constant random term is kept constant for Model and exact integration and the distribution is sampled after each update

Distribution Performance (10^4 Sampling)

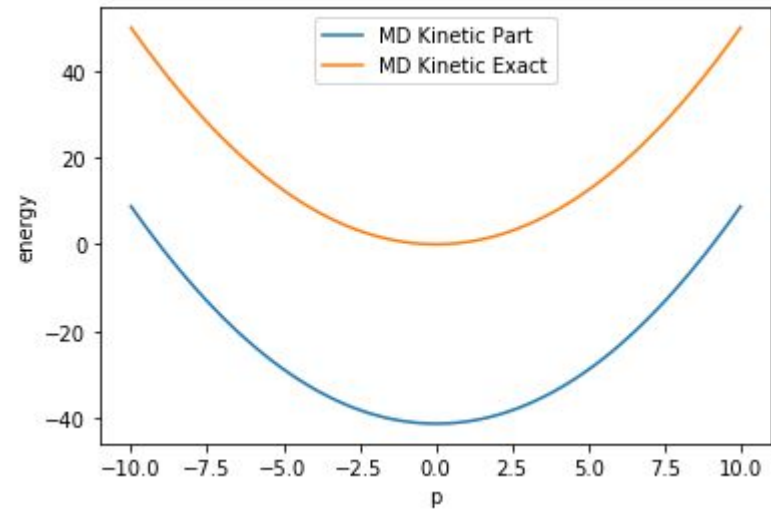


Hamiltonian Checking (time step : 0.01)

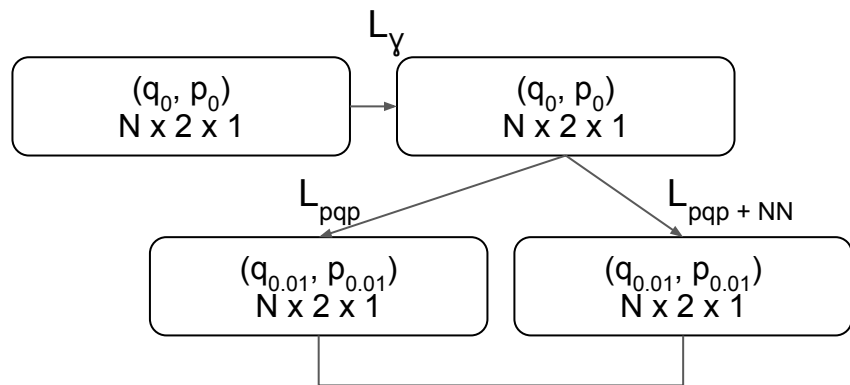
Potential



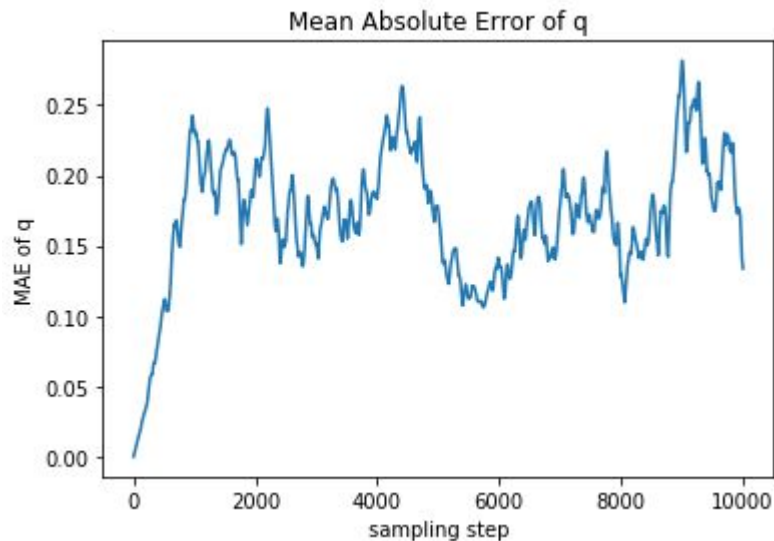
Kinetic Energy



Mean Absolute Error (time step : 0.01)



***Subtract to obtain
Mean Absolute Error***



Training Setting

Optimizer : Adam

Learning Rate (LR) : 1e-3

Scheduler : None

Seed : 937162211 (9-digit Prime Number)

Epochs : 100

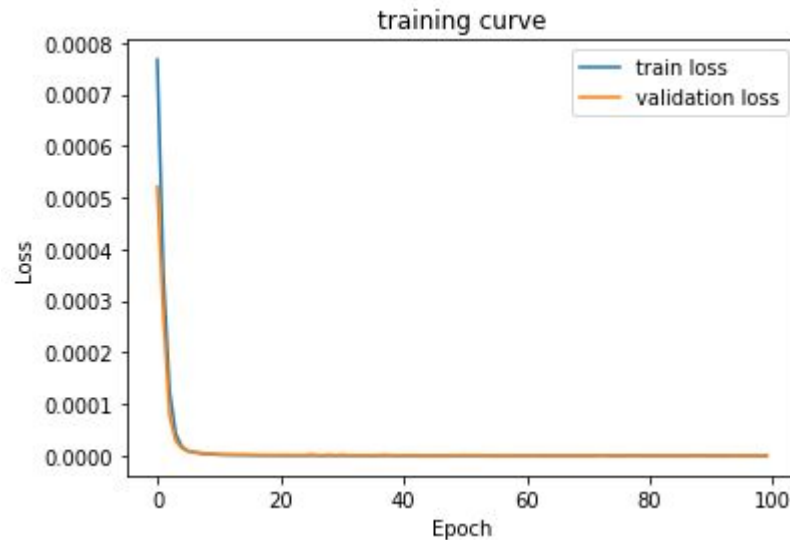
Batch Size : 32 / Shuffle

Large Time Step : 0.01 (50 Step) = 0.5

Ground Truth : 0.01

Final Statistic : $\Delta q = 0.00018$ (5 d.p)

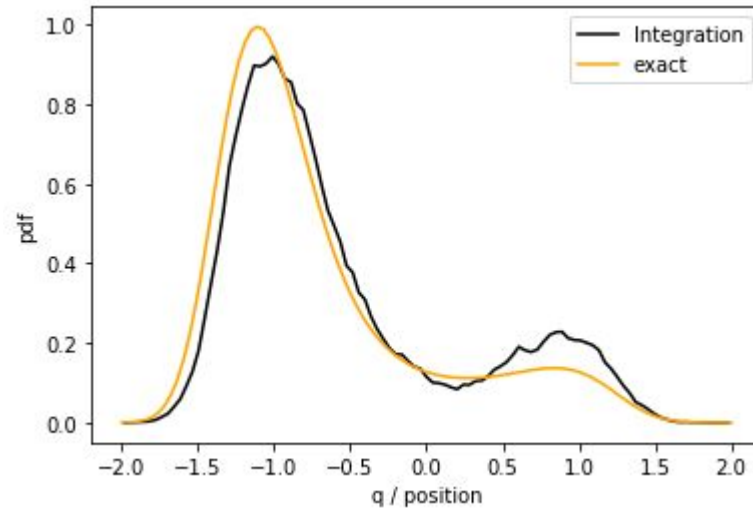
$\Delta p = 0.00023$ (5 d.p)



Remarks :

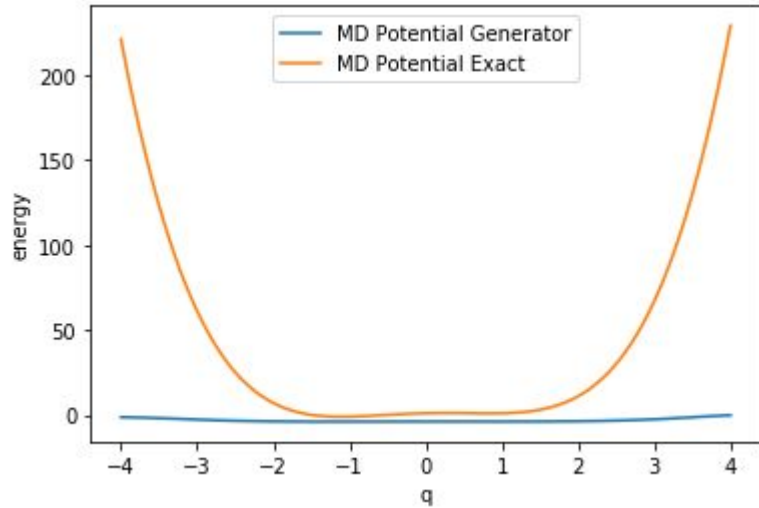
1. Tried using scheduler of reduce on plateau, patience = 10 , factor = 0.99, loss seems to be stuck again
2. Temperature used : 1 - 10, interval 1
3. Seed to consider :
 - a. Random.seed
 - b. Numpy.seed
 - c. Torch.seed
 - d. Torch.cuda.seed

Distribution Performance (10^4 Sampling)

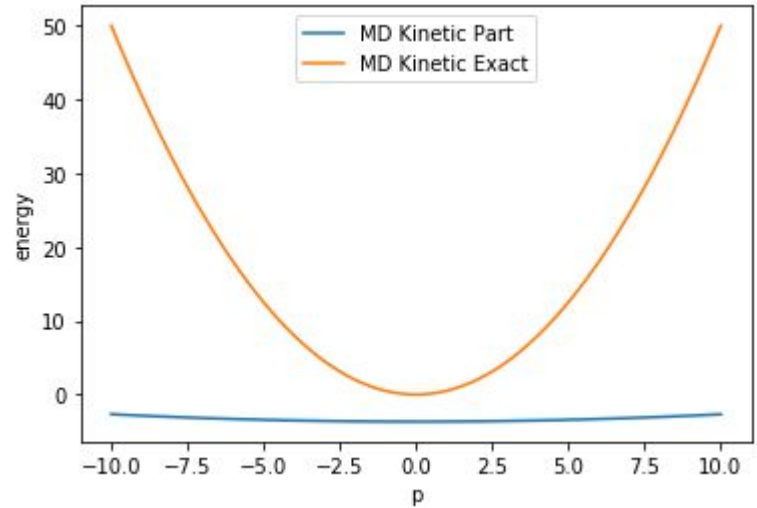


Hamiltonian Checking (time step : 0.5)

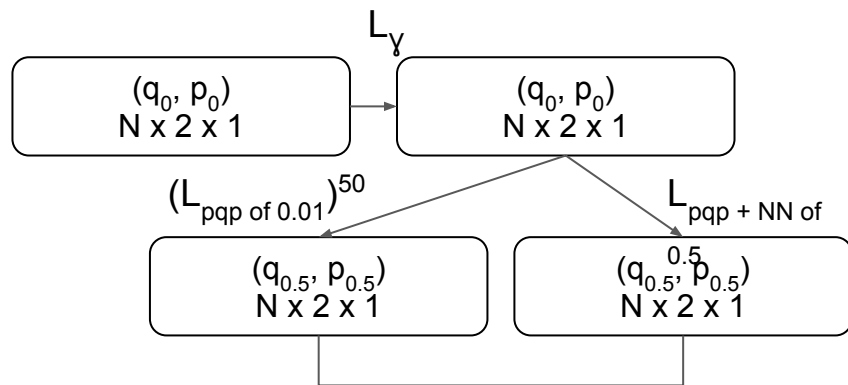
Potential



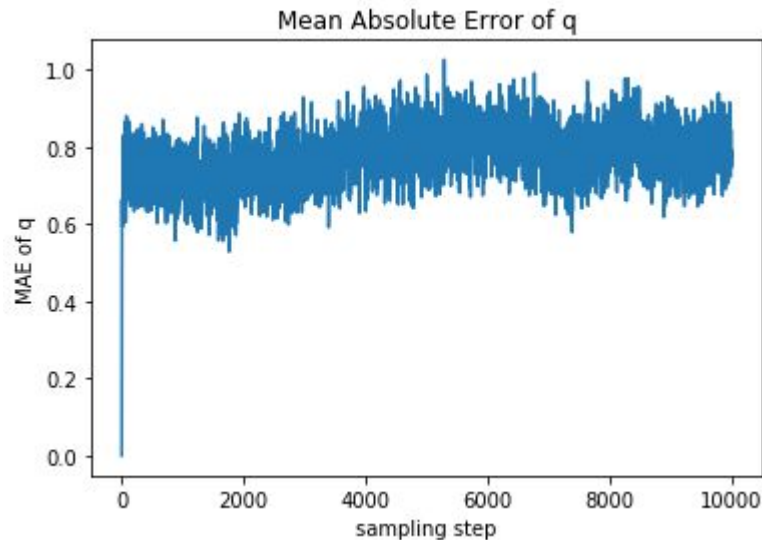
Kinetic Energy



Mean Absolute Error (time step : 0.5)



**Subtract to obtain
Mean Absolute Error**



Analysis

Literature Review

1) Langevin Process :

1. Introduction to the theory of stochastic processes and Brownian motion problems by J. L. Garcia-Palacios (<https://arxiv.org/abs/cond-mat/0701242v1>) \Rightarrow Reference that I used
2. Overleaf Document by Liu Wei

2) Hamiltonian Neural Network :

1. Hamiltonian Neural Networks by Sam Greydanus, Misko Dzamba, Jason Yosinski (<https://arxiv.org/abs/1906.01563>)
2. Symplectic Recurrent Neural Networks by Zhengdao Chen, Jianyu Zhang, Martin Arjovsky, Léon Bottou (<https://arxiv.org/abs/1909.13334>)

3) Langevin Sampling :

1. Robust and efficient configurational molecular sampling via Langevin Dynamics by Benedict Leimkuhler, Charles Matthews (<https://arxiv.org/abs/1304.3269>)