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import numpy as np
import random
import matplotlib.pyplot as plt

def rastrigin(x):
    return 10 * len(x) + sum([(xi ** 2 - 10 * np.cos(2 * np.pi * xi)) for xi in x])

class Particle:
    def __init__(self, dim, bounds):
        self.position = np.random.uniform(bounds[0], bounds[1], dim)
        self.velocity = np.random.uniform(-1, 1, dim)
        self.best_position = np.copy(self.position)
        self.best_value = rastrigin(self.position)

    def evaluate(self):
        current_value = rastrigin(self.position)
        if current_value < self.best_value:
            self.best_value = current_value
            self.best_position = np.copy(self.position)

def pso(dim, bounds, num_particles=30, max_iter=100, w=0.5, c1=1.5, c2=1.5):
    particles = [Particle(dim, bounds) for _ in range(num_particles)]

    global_best_position = None
    global_best_value = float('inf')

    best_values_over_iterations = []

    for iter in range(max_iter):
        for particle in particles:
            particle.evaluate()
            if particle.best_value < global_best_value:
                global_best_value = particle.best_value
                global_best_position = np.copy(particle.best_position)

        best_values_over_iterations.append(global_best_value)

        for particle in particles:
            inertia = w * particle.velocity
            cognitive = c1 * np.random.random() * (particle.best_position - particle.position)
            social = c2 * np.random.random() * (global_best_position - particle.position)

            particle.velocity = inertia + cognitive + social
            particle.position = particle.position + particle.velocity

            particle.position = np.clip(particle.position, bounds[0], bounds[1])

        if (iter+1) % 10 == 0:
            print(f"Iteration {iter+1}/{max_iter}, Global Best Value: {global_best_value}")

    return global_best_position, global_best_value, particles, best_values_over_iterations

if __name__ == "__main__":
    dim = 2
    bounds = [-5.12, 5.12]

    best_position, best_value, particles, best_values_over_iterations = pso(dim, bounds, num_particles=30, max_iter=100)

    print("\nFinal Best Position:", best_position)
    print("Final Best Value:", best_value)

    fig, ax = plt.subplots(figsize=(8, 6))

    final_best_positions = np.array([particle.best_position for particle in particles])

    ax.scatter(final_best_positions[:, 0], final_best_positions[:, 1], color='blue', label="Particle Best Positions", alpha=0.7)

```

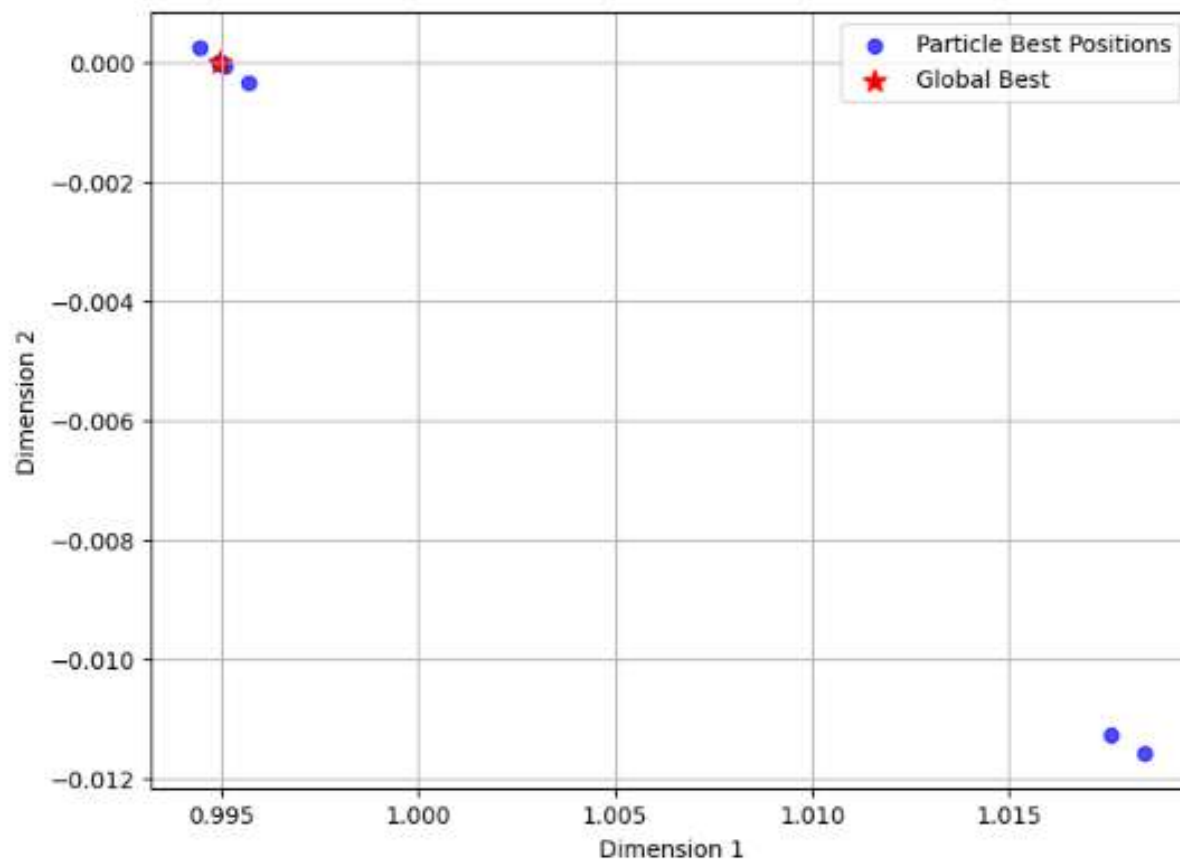
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ax.set_title("Final Particle Positions in PSO")
ax.set_xlabel("Dimension 1")
ax.set_ylabel("Dimension 2")
ax.legend()
plt.grid(True)
plt.show()

plt.figure(figsize=(8, 6))
plt.plot(range(1, len(best_values_over_iterations) + 1), best_values_over_iterations, color='green')
plt.title("Global Best Value vs. Iterations")
plt.xlabel("Iterations")
plt.ylabel("Global Best Value (Fitness)")
plt.grid(True)
plt.show()
```

Iteration 10/100, Global Best Value: 2.003250667292207  
 Iteration 20/100, Global Best Value: 1.0371970536607833  
 Iteration 30/100, Global Best Value: 0.9965161455248861  
 Iteration 40/100, Global Best Value: 0.9949848667711656  
 Iteration 50/100, Global Best Value: 0.9949610887864182  
 Iteration 60/100, Global Best Value: 0.994959059938175  
 Iteration 70/100, Global Best Value: 0.9949590571109823  
 Iteration 80/100, Global Best Value: 0.9949590570934674  
 Iteration 90/100, Global Best Value: 0.9949590570932898  
 Iteration 100/100, Global Best Value: 0.9949590570932898

Final Best Position: [ 9.94958638e-01 -8.70961770e-10]  
 Final Best Value: 0.9949590570932898

Final Particle Positions in PSO



Global Best Value vs. Iterations

