$$\begin{split} s(x,y,z) &= \int s(x,y,z,\omega) d\omega \\ &= \int (\int \int s(x',y',z=0,\omega) e^{-j\frac{2\omega}{c}||x'-x,y'-y,z||} dx' dy') d\omega \\ \\ S(k_x,k_y,z) &= \int S(k_x,k_y,z=0,\omega) e^{-jk_zz} d\omega \\ \\ &= \int S(k_x,k_y,z=0,k_z) e^{-jk_zz} dk_z \\ \\ &= \mathrm{IFT}_{k_z} \{ S(k_x,k_y,z=0,k_z) e^{-jk_zz_0} \} \\ \\ s(x,y,z) &= \mathrm{IFT}_{k_x,k_y} \{ \mathrm{IFT}_{k_z} \{ \mathrm{Stolt} \{ \mathrm{FT}_{x,y} \{ s(x',y',z=0,\omega) \} \} e^{-jk_zz_0} \} \}. \end{split}$$