1 Imports

```
[5]: import numpy as np
import os
import matplotlib.pyplot as plt
import matplotlib.cm as cm
from scipy.stats import multivariate_normal
```

2 Berechnen des Mittelwertsvektors und der Kovarianzmatrix

```
[6]: x1 = np.array([[1], [2]])
     x2 = np.array([[-1], [-1]])
     x3 = np.array([[-5], [1]])
     x4 = np.array([[1], [2]])
     # Stichprobenmatrix erstellen
     X = np.hstack((x1, x2, x3, x4))
     X_mean = np.mean(X, axis=1, keepdims=True)
     print(f'Mittelwertsvektor:\n {X_mean}')
    Mittelwertsvektor:
     [[-1.]
     [ 1.]]
[7]: C = (1 / X.shape[1]) * np.dot((X - X_mean), (X - X_mean).T)
     print(f'Auto Kovarianzmatrix:\n {C}')
    Auto Kovarianzmatrix:
     [[6. 1.]
     [1. 1.5]]
```

3 Subplot Funktion für 3D-, Contour- & 2D-Sample-Plot

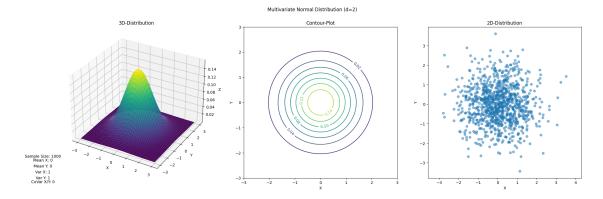
```
[8]: def generate_plts(mean, cov, sample_size):
    # Gitter erstellen und anhand der Mean/Cov automatisch scalen
    cov_max = max(cov[0][0], cov[1][1])
    mean_max = max(mean[0], mean[1])
    x_min = y_min = mean_max - 3 * np.sqrt(cov_max)
    x_max = y_max = mean_max + 3 * np.sqrt(cov_max)

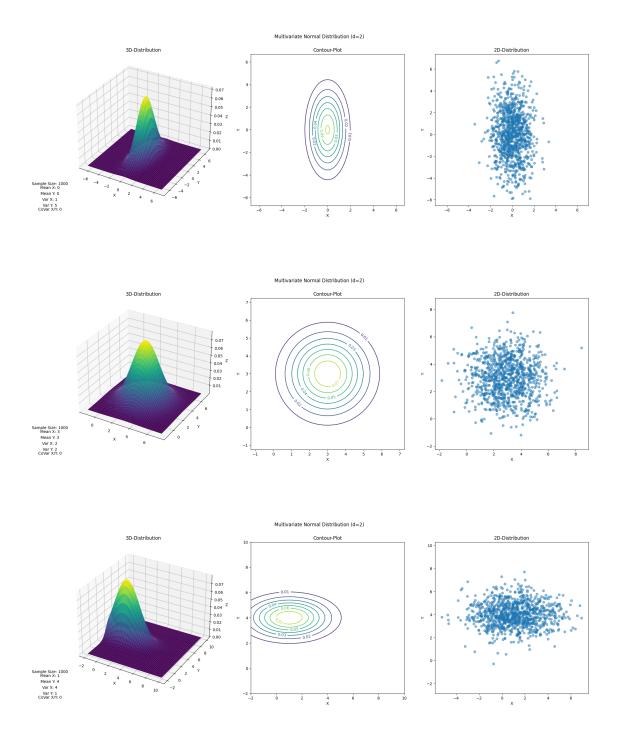
    x, y = np.meshgrid(np.linspace(x_min, x_max, 100), np.linspace(y_min, y_max, 100))
    pos = np.dstack((x, y))
```

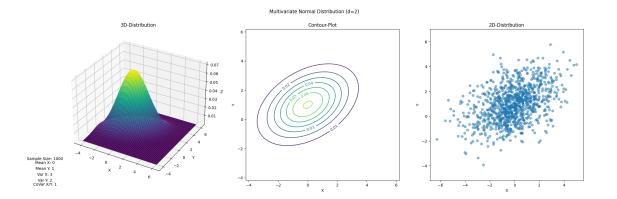
```
# Normalverteilungswerte berechnen
  rv = multivariate_normal(mean, cov)
  z = rv.pdf(pos)
  # Zufällige Samples generieren
  samples = rv.rvs(sample_size)
  fig = plt.figure(figsize=(24,7))
  # 3D Plot
  ax1 = fig.add_subplot(1, 3, 1, projection='3d')
  ax1.set_title('3D-Distribution')
  ax1.plot_surface(x, y, z, cmap='viridis', linewidth=0)
  ax1.set_xlabel('X')
  ax1.set_ylabel('Y')
  ax1.set_zlabel('Z')
  # Contour Plot
  ax2 = fig.add_subplot(1, 3, 2)
  ax2.set_title('Contour-Plot')
  ax2.set_xlabel('X')
  ax2.set_ylabel('Y')
  cp = ax2.contour(x, y, z)
  ax2.clabel(cp, inline=True, fontsize=10)
  # 2D-Distribution of random sample
  ax3 = fig.add_subplot(1, 3, 3)
  ax3.set_title('2D-Distribution')
  ax3.set_xlabel('X')
  ax3.set_ylabel('Y')
  ax3.scatter(samples[:, 0], samples[:, 1], alpha=0.5)
  plt.axis('equal')
  fig.suptitle('Multivariate Normal Distribution (d=2)')
  fig.text(0.1, 0.22, f'Sample Size: {sample_size}',__
⇔horizontalalignment='center', verticalalignment='center')
  fig.text(0.1, 0.2, f'Mean X: {mean[0]}', horizontalalignment='center', u
⇔verticalalignment='center')
  fig.text(0.1, 0.17, f'Mean Y: {mean[1]}', horizontalalignment='center', u
⇔verticalalignment='center')
  fig.text(0.1, 0.14, f'Var X: {cov[0][0]}', horizontalalignment='center',
⇔verticalalignment='center')
  fig.text(0.1, 0.11, f'Var Y: {cov[1][1]}', horizontalalignment='center',
⇔verticalalignment='center')
```

```
fig.text(0.1, 0.09, f'CoVar X/Y: {cov[0][1]}', horizontalalignment='center', verticalalignment='center')
plt.show()
```

```
[11]: sample_size = 1000
      # Mittelwert, Kovarianzmatrix und Sample Size definieren
      mean = [0, 0]
      cov = [[1, 0], [0, 1]]
      generate_plts(mean, cov, sample_size)
      mean = [0, 0]
      cov = [[1, 0], [0, 5]]
      generate_plts(mean, cov, sample_size)
      mean = [3, 3]
      cov = [[2, 0], [0, 2]]
      generate_plts(mean, cov, sample_size)
      mean = [1, 4]
      cov = [[4, 0], [0, 1]]
      generate_plts(mean, cov, sample_size)
      mean = [0, 1]
      cov = [[3, 1], [1, 2]]
      generate_plts(mean, cov, sample_size)
```





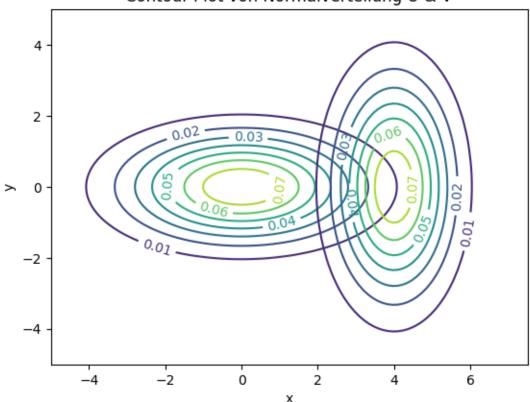


4 Lage von U & V

```
[105]: # Parameter für die erste Normalverteilung
       mean_u = [0, 0]
       cov_u = [[4, 0], [0, 1]]
       # Parameter für die zweite Normalverteilung
       mean_v = [4, 0]
       cov_v = [[1, 0], [0, 4]]
       # Gitter erstellen
       x, y = np.meshgrid(np.linspace(-5, 7.5, 100), np.linspace(-5, 5, 100))
       pos = np.dstack((x, y))
       # PDFs der Normalverteilungen berechnen
       rv_u = multivariate_normal(mean_u, cov_u)
       z_u = rv_u.pdf(pos)
       rv_v = multivariate_normal(mean_v, cov_v)
       z_v = rv_v.pdf(pos)
       # Contour-Plots erstellen
       fig, ax = plt.subplots()
       cp_u = ax.contour(x, y, z_u)
       ax.clabel(cp_u, inline=True, fontsize=10)
       cp_v = ax.contour(x, y, z_v)
       ax.clabel(cp_v, inline=True, fontsize=10)
       # Titel und Achsenbeschriftungen hinzufügen
       ax.set_title('Contour-Plot von Normalverteilung U & V')
       ax.set_xlabel('x')
       ax.set_ylabel('y')
```

```
# Schaubild anzeigen
plt.show()
```





5 Trennfunktion für U & V

```
[106]: # Trennfunktion berechnen
z_trenn = np.log(rv_u.pdf(pos) / rv_v.pdf(pos))

# Contour-Plots erstellen
fig, ax = plt.subplots()
cp_u = ax.contour(x, y, z_u)
ax.clabel(cp_u, inline=True, fontsize=10)
cp_v = ax.contour(x, y, z_v)
ax.clabel(cp_v, inline=True, fontsize=10)
cp_trenn = ax.contour(x, y, z_trenn, levels=0, linewidths=1)

# Titel und Achsenbeschriftungen hinzufügen
```

```
ax.set_title('Contour-Plot von Normalverteilung U & V mit Trennfunktion')
ax.set_xlabel('x')
ax.set_ylabel('y')

# Schaubild anzeigen
plt.show()
```

Contour-Plot von Normalverteilung U & V mit Trennfunktion

