# Homework assignment #1

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## **Definitions**

#### Problem 1. (5 points)

Write down the definition of independence of two events.

## Problem 2. (5 points)

Write down the definition of the *cumulative distribution function* of a random variable.

## **Problems**

### Problem 3. (9 points)

Let  $\Omega = \{a_1, a_2, a_3, a_4, a_5\}$  be an outcome space, and let  $\mathbb{P}$  be a probability on  $\Omega$ . Assume that  $\mathbb{P}[A] = 0.5$ ,  $\mathbb{P}[B] = 0.4$ ,  $\mathbb{P}[C] = 0.4$ , and  $\mathbb{P}[D] = 0.2$ , where

$$A = \{a_1, a_2, a_3\}, B = \{a_2, a_3, a_4\},\$$
  
 $C = \{a_3, a_5\} \text{ and } D = \{a_4\}.$ 

Are the events A and B independent? Why?

# Textbook problems

#### Problem 4. (4 points)

Solve **Problem 3.4** from the textbook.

# Problem 5. (4 points)

Solve **Problem 3.6** from the textbook.

Problem 6. (a-e are 2 points each; f is 5 points=15 points total)

Solve **Problem 3.8** from the textbook.

Problem 7. (4 points)

Solve Problem 3.20 from the textbook.

Problem 8. (4 points)

Solve **Problem 3.22** from the textbook.