**贝格迈思科技（深圳）股份公司**

聚焦数据智能技术创新 • 助力企业智能技术进步升级

 **Bigmath SIMD Libary**

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**Bigmath SIMD Libary**

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# Introduction

The BIGMATH SIMD vector class library is a tool that allows C++ programmers to make their code much faster by handling multiple data in parallel. Modern CPU’s have *“Single Instruction Multiple Data”* (SIMD) instructions for handling vectors of multiple data elements in parallel. The compiler may be able to use SIMD instructions automatically in simple cases, but a human programmer is often able to do it better by organizing data into vectors that fit the SIMD instructions. The BIGMATH SIMD library is a tool that makes it easier for the programmer to write vector code without having to use assembly language or intrinsic functions. Let us explain this with an example:

// Example 1a. Calculations on arrays

float a[8], b[8], c[8]; // declare arrays

... // put values into arrays for (int i = 0; i < 8; i++) { // loop for 8 elements

c[i] = a[i] + b[i]\*1.5f; // operations on each element

}

The vector class library allows you to write this code as vectors:

// Example 1b. Same code using vectors

#include "vectorsimd.h" // use vector class library float a[8], b[8], c[8]; // declare arrays

... // put values into arrays Vec8f avec, bvec, cvec; // define vectors avec.load(a); // load array a into vector

bvec.load(b); // load array b into vector cvec = avec + bvec \* 1.5f; // do operations on vectors

cvec.store(c); // save result in array c

Example 1b does the same as example 1a, but more efficiently because it utilizes SIMD instructions that do eight additions and/or eight multiplications in a single instruction. Modern microprocessors have these instructions which may give you a throughput of eight floating point additions and eight multiplications per clock cycle. A good optimizing compiler may actually convert example 1a automatically to use the SIMD instructions, but in more complicated cases you cannot be sure that the compiler is able to vectorize your code in an optimal way.

## *How it works*

The type Vec8f in example 1b is a class that encapsulates the intrinsic type m256 which represents a 256-bit vector register holding 8 floating point numbers of 32 bits each. The overloaded operators + and \* represent the SIMD instructions for adding and multiplying vectors. These operators are inlined so that no extra code is generated other than the SIMD instructions. All you have to do to get access to these vector operations is to include "vectorsimd.h" in your C++ code and specify the desired instruction set (e.g. SSE2 or AVX512) in your compiler options.

The code in example 1b can be reduced to just 4 machine instructions if the instruction set AVX or higher is enabled. The SSE2 instruction set will give 8 machine instructions because the maximum vector register size is half as big for instruction sets prior to AVX. The code in example 1a will generate approximately 44 instructions if the compiler does not automatically vectorize the code.

## *Features*

* vectors of 8-, 16-, 32- and 64-bit integers, signed and unsigned
* vectors of single and double precision floating point numbers
* total vector size 128, 256 or 512 bits
* defines almost all common operators
* boolean operations and branches on vector elements
* many arithmetic functions
* standard mathematical functions
* permute, blend, gather, scatter and table look-up functions
* fast integer division
* can build code for different instruction sets from the same source code
* CPU dispatching to utilize higher instruction sets when available
* uses metaprogramming to find the best implementation for the selected instruction set and parameter values of a given operator or function
* includes several extra header files for special purposes and applications

## *Instruction sets supported*

Since 1997, each new CPU model has extended the x86 instruction set with more SIMD instructions. The BIGMATH SIMD library requires the SSE2 instruction set as a minimum, and supports SSE2, SSE3, SSSE3, SSE4.1, SSE4.2, AVX, AVX2, XOP, FMA3, FMA4, and AVX512F/VL/BW/DQ/ER.

## *Platforms supported*

Windows, Linux and Mac, 32-bit and 64-bit, with Intel, AMD or VIA x86 or x86-64 instruction set processor. The AVX and later instruction sets require one of the following operating system versions or later: Windows 7 SP1, Windows Server 2008 R2 SP1, Linux kernel version 2.6.30, Apple OS X Snow Leopard 10.6.8.

A special version of the vector class library for the Intel Knights Corner coprocessor has been developed at CERN. It is available from <https://bitbucket.org/veclibknc/vlcknc.git>

## *Compilers supported*

The vector class library works with Microsoft, Intel, Gnu and Clang C++ compilers. It is recommended to use the newest version of the compiler if the newest instruction sets are used.

The AVX512 instruction set requires at least Gnu compiler version 5.1, with binutils version 2.24 or later, Clang version 3.7, or Intel compiler version 14.0. Microsoft compilers do not yet have support for AVX512 (November 2016). Gnu compilers for Windows may have a problem with alignment of vectors bigger than 128 bits.

The vector class library uses standard C++, but it is planned that a future version will use C++14 in order to use the improved metaprogramming features.

## *Intended use*

This vector class library is intended for experienced C++ programmers. It is useful for improving code performance where speed is critical and where the compiler is unable to vectorize the code automatically in an optimal way.

Combining explicit vectorization by the programmer with other kinds of optimization done by the compiler, it has the potential for generating highly efficient code. This can be useful for optimizing library functions and critical innermost loops (hotspots) in CPU-intensive programs. There is no reason to use it in less critical parts of a program.

## *How BIGMATH SIMD uses metaprogramming*

The vector class library uses metaprogramming extensively to resolve as much work as possible at compile time rather than at run time. Especially, it uses metaprogramming to find the optimal instructions and algorithms, depending on constants in the code and the selected instruction set.

The C++ language does not have very good metaprogramming features, but the SIMD makes the best use of the available features. Three methods are used for metaprogramming:

1. preprocessing directives.
2. templates.
3. if and switch statements with constant conditions to be optimized away.
4. future versions may use C++14 metaprogramming features.

The if and switch statements are actually seen when debugging the code, but the compiler will optimize them away in the optimized version of the code.

All three metaprogramming methods rely on expressions that can be computed at compile time. The C++ syntax requires that expressions such as template parameters can be recognized as *compile-time constants*. A compile-time constant is typically just a number, such as 5, but it may also contain operators, preprocessing macros and template parameters. It may not contain function calls, loops, etc. It may contain ?: branches, but not if-else branches. Later versions of C++ allow constexpr for generating compile-time constants.

An optimizing compiler may be able to resolve more calculations than these at compile time, but the syntax requires that the above rules be obeyed where a compile-time constant is required. Several of the functions in BIGMATH SIMD require compile-time constants for certain parameters, especially where templates are used.

The following cases illustrate the use of metaprogramming in BIGMATH SIMD:

* Compiling for different instruction sets. If you are using a bigger vector size than supported by the instruction set then the BIGMATH SIMD code will split the big vector into multiple smaller vectors. If you are multiplying vectors of 32-bit integers with an instruction set that supports only 16-bit multiplication then the BIGMATH SIMD code will calculate the 32-bit product using multiple 16-bit multiplications. If you compile the same code again for a higher instruction set then you will get a more efficient program.
* Permute, blend and gather functions. There are many different machine instructions that move data between different vector elements. Some of these instructions can only do very specific data permutations. The BIGMATH SIMD uses quite a lot of metaprogramming to find the instruction or sequence of instructions that best fits the specific permutation pattern specified. Often, the higher instruction sets give more efficient results.
* Integer division. Integer division can be done faster by a combination of multiplication and bit-shifting. The BIGMATH SIMD can use metaprogramming to find

the optimal division method and calculate the multiplication factor and shift count at compile time if the divisor is a known constant. See page [22](#_bookmark21) for details.

* Raising to a power. Calculating x8 can be done faster by squaring x three times rather than by a loop that multiplies seven times. The BIGMATH SIMD can determine the optimal way of raising floating point vectors to an integer or rational power in the functions pow\_const and pow\_rational.

# The basics

## *How to compile*

Copy the header files (\*.h) from simd.zip to the same folder as your C++ source files. The header files in the sub-archive named special.zip should only be included if needed.

Include the header file vectorsimd.h in your C++ source file:

#include "vectorsimd.h"

Several other header files will be included automatically.

Set your compiler options to the desired instruction set. The instruction set must be at least SSE2. See page [93](#_bookmark50) for a list of compiler options. You may compile multiple versions for different instruction sets as explained in the chapter starting at page [92](#_bookmark49).

If you are using the Gnu compiler version 3.x or 4.x then you must set the ABI version to 4 or more, or 0 for a reasonable default. For example:

**g++ -mavx -fabi-version=0 -O3 myfile.cpp**

The following simple C++ example may help you get started:

// Simple vector class example C++ file #include <stdio.h>

#include "vectorsimd.h"

int main() {

// define and initialize integer vectors a and b Vec4i a(10,11,12,13);

Vec4i b(20,21,22,23);

// add the two vectors Vec4i c = a + b;

// Print the results

for (int i = 0; i < c.size(); i++) {

printf(" %5i", c[i]);

}

printf("\n");

return 0;

}

## *Overview of vector classes*

The vector class library supports vectors of 8-bit, 16-bit, 32-bit and 64-bit signed and unsigned integers, 32-bit single precision floating point numbers, and 64-bit double precision floating point numbers. A vector contains multiple elements of the same type to a total size of 128, 256 or 512 bits. The vector elements are indexed, starting at 0 for the first element.

The constant MAX\_VECTOR\_SIZE indicates the maximum vector size. The default maximum vector size is 256 in the current version and possibly larger in future versions. You can get access to 512-bit vectors by defining

#define MAX\_VECTOR\_SIZE 512

before including the vector class header files.

The vector class also defines boolean vectors. These are mainly used for conditionally selecting elements from vectors.

The following vector classes are defined:

### Integer vector classes

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| **vector class** | **integer size, bits** | **signed** | **elements per vector** | **total bits** | **recommen- ded instruction set** |
| Vec16c | 8 | signed | 16 | 128 | SSE2 |
| Vec16uc | 8 | unsigned | 16 | 128 | SSE2 |
| Vec8s | 16 | signed | 8 | 128 | SSE2 |
| Vec8us | 16 | unsigned | 8 | 128 | SSE2 |
| Vec4i | 32 | signed | 4 | 128 | SSE2 |
| Vec4ui | 32 | unsigned | 4 | 128 | SSE2 |
| Vec2q | 64 | signed | 2 | 128 | SSE2 |
| Vec2uq | 64 | unsigned | 2 | 128 | SSE2 |
| Vec32c | 8 | signed | 32 | 256 | AVX2 |
| Vec32uc | 8 | unsigned | 32 | 256 | AVX2 |
| Vec16s | 16 | signed | 16 | 256 | AVX2 |
| Vec16us | 16 | unsigned | 16 | 256 | AVX2 |
| Vec8i | 32 | signed | 8 | 256 | AVX2 |
| Vec8ui | 32 | unsigned | 8 | 256 | AVX2 |
| Vec4q | 64 | signed | 4 | 256 | AVX2 |
| Vec4uq | 64 | unsigned | 4 | 256 | AVX2 |
| Vec16i | 32 | signed | 16 | 512 | AVX512 |
| Vec16ui | 32 | unsigned | 16 | 512 | AVX512 |
| Vec8q | 64 | signed | 8 | 512 | AVX512 |
| Vec8uq | 64 | unsigned | 8 | 512 | AVX512 |

Note that vectors of 8-bit and 16-bit integers are not available as 512 bit vectors in the AVX512 instruction set, but they may be available in a future AVX512BW instruction set.

### Floating point vector classes

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| **vector class** | **precision** | **elements per vector** | **total bits** | **recommen- ded instruc- tion set** |
| Vec4f | single | 4 | 128 | SSE2 |
| Vec2d | double | 2 | 128 | SSE2 |
| Vec8f | single | 8 | 256 | AVX |
| Vec4d | double | 4 | 256 | AVX |
| Vec16f | single | 16 | 512 | AVX512 |
| Vec8d | double | 8 | 512 | AVX512 |

### Boolean vector classes

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| **Boolean vector** | **for use with** | **elements per vector** | **total bits** | **recommen- ded instruc- tion set** |
| Vec128b |  | 128 | 128 | SSE2 |
| Vec16cb | Vec16c, Vec16uc | 16 | 128 | SSE2 |
| Vec8sb | Vec8s, Vec8us | 8 | 128 | SSE2 |
| Vec4ib | Vec4i, Vec4ui | 4 | 128 | SSE2 |
| Vec2qb | Vec2q, Vec2uq | 2 | 128 | SSE2 |
| Vec256b |  | 256 | 256 | AVX2 |
| Vec32cb | Vec32c, Vec32uc | 32 | 256 | AVX2 |
| Vec16sb | Vec16s, Vec16us | 16 | 256 | AVX2 |
| Vec8ib | Vec8i, Vec8ui | 8 | 256 | AVX2 |
| Vec4qb | Vec4q, Vec4uq | 4 | 256 | AVX2 |
| Vec512b |  | 512 | 512 | AVX512 |
| Vec16ib | Vec16i, Vec16ui | 16 | 16 or 512 | AVX512 |
| Vec8qb | Vec8q, Vec8uq | 8 | 8 or 512 | AVX512 |
| Vec4fb | Vec4f | 4 | 128 | SSE2 |
| Vec2db | Vec2d | 2 | 128 | SSE2 |
| Vec8fb | Vec8f | 8 | 256 | AVX |
| Vec4db | Vec4d | 4 | 256 | AVX |
| Vec16fb | Vec16f | 16 | 16 or 512 | AVX512 |
| Vec8db | Vec8d | 8 | 8 or 512 | AVX512 |

## *Constructing vectors and loading data into vectors*

There are many ways to create vectors and put data into vectors. These methods are listed here.

|  |  |
| --- | --- |
| **method** | default constructor |
| **defined for** | all vector classes |
| **description** | the vector is created but not initialized. The value is unpredictable |
| **efficiency** | good |

Example:

Vec4i a; // creates a vector of 4 signed integers

|  |  |
| --- | --- |
| **method** | constructor with one parameter |
| **defined for** | all vector classes except bit vectors Vec128b, Vec256b, Vec512b |
| **description** | all elements get the same value |
| **efficiency** | good |

Examples:

Vec4i a(5); // all four elements = 5

|  |  |
| --- | --- |
| **method** | assignment to scalar |
| **defined for** | all vector classes except bit vectors Vec128b, Vec256b, Vec512b |
| **description** | all elements get the same value |
| **efficiency** | good |

Examples:

Vec4i a = 5; // all four elements = 5

|  |  |
| --- | --- |
| **method** | constructor with one parameter for each vector element |
| **defined for** | all vector classes except bit vectors Vec128b, Vec256b, Vec512b |
| **description** | each element gets a specified value. The parameter for element number 0 comes first |
| **efficiency** | good for constant. Medium for variables as parameters |

Examples:

Vec4i a(10,11,12,13); // a = (10,11,12,13) Vec4i b = Vec4i(20,21,22,23); // b = (20,21,22,23)

|  |  |
| --- | --- |
| **method** | constructor with one parameter for each half vector |
| **defined for** | all vector classes bigger than 128 bits. |
| **description** | Concatenates two 128-bit vectors into one 256-bit vector. Concatenates two 256-bit vectors into one 512-bit vector. |
| **efficiency** | good |

Example:

Vec4i a(10,11,12,13); Vec4i b(20,21,22,23);

Vec8i c(a, b); // c = (10,11,12,13,20,21,22,23)

|  |  |
| --- | --- |
| **method** | insert(index, value) |
| **defined for** | all vector classes except bit vectors Vec128b, Vec256b, Vec512b |
| **description** | changes the value of element number (index) to (value). The index starts at 0. |
| **efficiency** | medium, depending on instruction set |

Example:

Vec4i a(0);

a.insert(2, 9); // a = (0,0,9,0)

|  |  |
| --- | --- |
| **method** | load(const pointer) |
| **defined for** | all integer and floating point vector classes |
| **description** | loads all elements from an array |
| **efficiency** | good, except immediately after inserting elements separately into the array. |

This is the preferred way of putting values into a vector, except immediately after values have been put into the array one by one (see §10.4).

Example:

int list[8] = {10,11,12,13,14,15,16,17};

Vec4i a, b;

a.load(list); // a = (10,11,12,13)

b.load(list+4); // b = (14,15,16,17)

|  |  |
| --- | --- |
| **method** | load\_a(const pointer) |
| **defined for** | all integer and floating point vector classes |
| **description** | loads all elements from an aligned array |
| **efficiency** | good, except immediately after inserting elements separately into the array. |

This method does the same as the load method (see above), but requires that the pointer points to an address divisible by 16 for 128-bit vectors, by 32 for 256- bit vectors, or by 64 for 512 bit vectors. If you are not certain that the array is properly aligned then use load instead of load\_a. There is hardly any difference in efficiency between load and load\_a on newer microprocessors.

|  |  |
| --- | --- |
| **method** | load\_partial(int n, const pointer) |
| **defined for** | all integer and floating point vector classes |
| **description** | loads n elements from an array into a vector. Sets remaining elements to 0. 0 ≤ n ≤ (vector size). |
| **efficiency** | medium |

Example:

float list[3] = {1.0f, 1.1f, 1.2f}; Vec4f a;

a.load\_partial(2, list); // a = (1.0, 1.1, 0.0, 0.0)

|  |  |
| --- | --- |
| **method** | cutoff(int n) |
| **defined for** | all integer and floating point vector classes |
| **description** | leaves the first n elements unchanged and sets the remaining elements to zero. 0 ≤ n ≤ (vector size). |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

a.cutoff(2); // a = (10, 11, 0, 0)

|  |  |
| --- | --- |
| **method** | set\_bit(index, value) |
| **defined for** | all integer vector classes smaller than 512 bits |
| **description** | element 0 and ends with the last bit of the last element. value = 0 or 1. |
| **efficiency** | medium |

Example:

Vec4i a(10);

a.set\_bit(34, 1); // a = (10,14,10,10)

|  |  |
| --- | --- |
| **method** | gather<indexes>(array) |
| **defined for** | floating point vector classes and integer vector classes with 32-bit and 64-bit elements |
| **description** | gather non-contiguous data from an array. |
| **efficiency** | medium |

Example:

int list[8] = {10,11,12,13,14,15,16,17};

Vec4i a = gather4i<0,2,1,6>(list);

// a = (10,12,11,16)

## *Reading data from vectors*

There are many ways to extract elements or parts of a vector. These methods are listed here.

|  |  |
| --- | --- |
| **method** | store(pointer) |
| **defined for** | all integer and floating point vector classes |
| **description** | stores all elements into an array |
| **efficiency** | good |

This is the preferred way of getting the individual elements of a vector. Example:

Vec4i a(10,11,12,13); Vec4i b(20,21,22,23);

int list[8]; a.store(list);

b.store(list+4); // list contains (10,11,12,13,20,21,22,23)

|  |  |
| --- | --- |
| **method** | store\_a(pointer) |
| **defined for** | all integer and floating point vector classes |
| **description** | stores all elements into an aligned array |
| **efficiency** | good |

This method does the same as the store method (see above), but requires that the pointer points to an address divisible by 16 for 128-bit vectors, by 32 for 256- bit vectors, or by 64 for 512-bit vectors. If you are not certain that the array is properly aligned then use store instead of store\_a.

|  |  |
| --- | --- |
| **method** | store\_partial(int n, pointer) |
| **defined for** | all integer and floating point vector classes |
| **description** | stores the first n elements into an array. 0 ≤ n ≤ (vector size). |
| **efficiency** | medium |

Example:

float list[3] = {9.0f, 9.0f, 9.0f};

Vec4f a(1.0f, 1.1f, 1.2f, 1.3f);

a.store\_partial(2, list); // list contains (1.0, 1.1, 9.0)

|  |  |
| --- | --- |
| **method** | extract(index) |
| **defined for** | all integer, floating point and boolean vector classes |
| **description** | gets a single element from a vector |
| **efficiency** | medium |

Example:

Vec4i a(10,11,12,13);

int b = a.extract(2); // b = 12

|  |  |
| --- | --- |
| **method** | operator [] |
| **defined for** | all integer, floating point and boolean vector classes |
| **description** | gets a single element from a vector |
| **efficiency** | medium |

The operator [] does exactly the same as the extract method. Note that you can read a vector element with the [] operator, *but not write an element*.

Example:

Vec4i a(10,11,12,13);

int b = a[2]; // b = 12

a[3] = 5; // not allowed!

|  |  |
| --- | --- |
| **method** | get\_bit(index) |
| **defined for** | all integer vector classes smaller than 512 bits |
| **description** | reads a single bit. index starts at bit 0 of element 0 and ends with the last bit of the last element. |
| **efficiency** | medium |

Example:

Vec4i a(10);

int b = a.get\_bit(34); // b = 0

|  |  |
| --- | --- |
| **method** | get\_low() |
| **defined for** | all vector classes of 256 bits or more |
| **description** | gets the lower half of a 256-bit vector as a 128-bit vector. gets the lower half of a 512-bit vector as a 256-bit vector. |
| **efficiency** | good |

Example:

Vec8i a(10,11,12,13,14,15,16,17);

Vec4i b = a.get\_low(); // b = (10,11,12,13)

|  |  |
| --- | --- |
| **method** | get\_high() |
| **defined for** | all vector classes of 256 bits or more |
| **description** | gets the upper half of a 256-bit vector as a 128-bit vector. gets the upper half of a 512-bit vector as a 256-bit vector. |
| **efficiency** | good |

Example:

Vec8i a(10,11,12,13,14,15,16,17);

Vec4i b = a.get\_high(); // b = (14,15,16,17)

|  |  |
| --- | --- |
| **method** | size() |
| **defined for** | all vector classes |
| **description** | static member function indicating the number of elements that the vector can contain |
| **efficiency** | good |

Example:

Vec8f a;

int s = a.size(); // a = 8

## *Arrays of vectors*

If you make an array of vectors, this should preferably have fixed size. For example:

const int datasize = 1024; // size of data set Vec8f mydata[datasize/8]; // array of fixed size

...

for (int i = 0; i < datasize/8; i++) {

mydata[i] = mydata[i] \* 0.1f + 2.0f;

}

If you need an array of a size that is determined at runtime, then you will have a problem with alignment. Each vector needs to be stored at an address divisible by 16, 32 or 64 bytes, according to its size. The compiler can do this when defining a fixed-size array, as in the above example, but not necessarily with dynamic memory allocation. If you create an array of dynamic size by using new, malloc or an STL container, or any other method, then you may not get the proper alignment for vectors and the program will very likely crash when accessing a misaligned vector. The C++ [standard says](http://en.cppreference.com/w/cpp/language/object) "It is implementation- defined if new-expression, [...] support over-aligned types". Possible solutions are to use posix\_memalign, \_aligned\_malloc, std::aligned\_storage, std::align, etc. depending on what is supported by your compiler, but the method may not be portable to all platforms.

I would recommend to make an array of scalars instead of an array of vectors in order to avoid these complications. If datasize in the above example is variable, then the code could be implemented in this way:

int datasize = 1024; // size of dataset, variable float \*mydata = new float[datasize]; // dynamic array

...

Vec8f x;

for (int i = 0; i < datasize; i += 8) {

x.load(mydata+i);

x = x \* 0.1f + 2.0f; x.store(mydata+i);

}

...

delete[] mydata;

See page [101](#_bookmark57) for discussion of the case where the data size is not a multiple of the vector size.

## *Using a namespace*

In general, there is no need to put the vector class library into a separate namespace. Therefore, the use of a namespace is optional. You can give the vector class library a namespace with a name of your choosing by defining BIGMATH SIMD\_NAMESPACE, for example:

#define BIGMATH SIMD\_NAMESPACE bigmath simd #include "vectorsimd.h"

using namespace bigmath simd;

// your vector code here...

# Operators

## *Arithmetic operators*

|  |  |
| --- | --- |
| **operator** | +, ++, += |
| **defined for** | all integer and floating point vector classes |
| **description** | addition |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(20, 21, 22, 23);

Vec4i c = a + b; // c = (30, 32, 34, 36)

|  |  |
| --- | --- |
| **operator** | -, --, -=, unary - |
| **defined for** | all integer and floating point vector classes |
| **description** | subtraction |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(20, 21, 22, 23);

Vec4i c = a - b; // c = (-10, -10, -10, -10)

|  |  |
| --- | --- |
| **operator** | \*, \*= |
| **defined for** | all integer and floating point vector classes |

|  |  |
| --- | --- |
| **description** | multiplication |
| **efficiency** | 8 bit integers: poor 16 bit integers: good  32 bit integers: good for SSE4.1 instruction set, poor otherwise  64 bit integers: good for AVX512DQ instruction set, poor otherwise  float: good double: good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(20, 21, 22, 23);

Vec4i c = a \* b; // c = (200, 231, 264, 299)

|  |  |
| --- | --- |
| **operator** | /, /= (floating point) |
| **defined for** | all floating point vector classes |
| **description** | division |
| **efficiency** | medium or poor |

Example:

Vec4f a(1.0f, 1.1f, 1.2f, 1.3f);

Vec4f b(2.0f, 2.1f, 2.2f, 2.3f);

Vec4f c = a / b; // c = (0.500f, 0.524f, 0.545f, 0.565f)

|  |  |
| --- | --- |
| **operator** | /, /= (integer vector divided by scalar) |
| **defined for** | all classes of 8-bit, 16-bit and 32-bit integers, signed and unsigned. Not available for 64-bit integers. |
| **description** | division by scalar. Results are truncated to integer. All elements are divided by the same divisor. See page [22](#_bookmark21) for explanation |
| **efficiency** | poor |

Example:

Vec4i a(10, 11, 12, 13);

int b = 3;

Vec4i c = a / b; // c = (3, 3, 4, 4)

|  |  |
| --- | --- |
| **operator** | /, /= (integer vector divided by constant) |
| **defined for** | all classes of 8-bit, 16-bit and 32-bit integers, signed and unsigned. Not available for 64-bit integers. |
| **description** | division by compile-time constant. All elements are divided by the same divisor. See page [22](#_bookmark21) for explanation |
| **efficiency** | poor, but better than division by scalar variable. Good if divisor is a power of 2 |

Example:

// signed

Vec4i a(10, 11, 12, 13);

Vec4i b = a / const\_int(3); // b = (3, 3, 4, 4)

// unsigned

Vec4ui c(10, 11, 12, 13);

Vec4ui d = c / const\_uint(3); // d = (3, 3, 4, 4)

## *Logic operators*

|  |  |
| --- | --- |
| **operator** | <<, <<= |
| **defined for** | all integer vector classes |
| **description** | logical shift left. All vector elements are shifted by the same amount.  Shifting left by n is a fast way of multiplying by 2n |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b = a << 2; // b = (40, 44, 48, 52)

|  |  |
| --- | --- |
| **operator** | >>, >>= |
| **defined for** | all integer vector classes |
| **description** | shift right. All vector elements are shifted by the same amount.  Unsigned integers use logical shift, signed integers use arithmetic shift (i. e. sign bit is copied) |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b = a >> 2; // b = (2, 2, 3, 3)

|  |  |
| --- | --- |
| **operator** | == |
| **defined for** | all integer and floating point vector classes |
| **description** | test if equal. Result is a boolean vector |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(14, 13, 12, 11);

Vec4ib c = a == b; // c = (false, false, true, false)

|  |  |
| --- | --- |
| **operator** | != |
| **defined for** | all integer and floating point vector classes |
| **description** | test if not equal. Result is a boolean vector |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(14, 13, 12, 11);

Vec4ib c = a != b; // c = (true, true, false, true)

|  |  |
| --- | --- |
| **operator** | > |
| **defined for** | all integer and floating point vector classes |
| **description** | test if bigger. Result is a boolean vector |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(14, 13, 12, 11);

Vec4ib c = a > b; // c = (false, false, false, true)

|  |  |
| --- | --- |
| **operator** | >= |
| **defined for** | all integer and floating point vector classes |
| **description** | test if bigger or equal. Result is a boolean vector |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(14, 13, 12, 11);

Vec4ib c = a >= b; // c = (false, false, true, true)

|  |  |
| --- | --- |
| **operator** | < |
| **defined for** | all integer and floating point vector classes |
| **description** | test if smaller. Result is a boolean vector |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(14, 13, 12, 11);

Vec4ib c = a < b; // c = (true, true, false, false)

|  |  |
| --- | --- |
| **operator** | <= |
| **defined for** | all integer and floating point vector classes |
| **description** | test if smaller or equal. Result is a boolean vector |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(14, 13, 12, 11);

Vec4ib c = a <= b; // c = (true, true, true, false)

|  |  |
| --- | --- |
| **operator** | &, &= |
| **defined for** | all vector classes |
| **description** | bitwise and |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(20, 21, 22, 23);

Vec4i c = a & b; // c = (0, 1, 4, 5)

|  |  |
| --- | --- |
| **operator** | |, |= |
| **defined for** | all vector classes |
| **description** | bitwise or |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(20, 21, 22, 23);

Vec4i c = a | b; // c = (30, 31, 30, 31)

|  |  |
| --- | --- |
| **operator** | ^, ^= |
| **defined for** | all vector classes |
| **description** | bitwise exclusive or |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(20, 21, 22, 23);

Vec4i c = a ^ b; // c = (30, 30, 26, 26)

|  |  |
| --- | --- |
| **operator** | ~ |
| **defined for** | all integer and boolean vector classes |
| **description** | bitwise not |
| **efficiency** | good |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b = ~a; // b = (-11, -12, -13, -14)

|  |  |
| --- | --- |
| **operator** | ! |
| **defined for** | all integer and floating point vector classes |
| **description** | logical not. Result is a boolean vector |
| **efficiency** | good |

Example:

Vec4i a(-1, 0, 1, 2);

Vec4ib b = !a; // b = (false,true,false,false)

## *Integer division*

There are no instructions in the x86 instruction set extensions that are useful for integer vector division, and such instructions would be quite slow if they existed. Therefore, the vector class library is using an algorithm for fast integer division. The basic principle of this algorithm can be expressed in this formula:

*a* / *b* ≈ *a* \* (2*n* / *b*) >> *n*

This calculation goes through the following steps:

1. find a suitable value for *n*
2. calculate 2*n* / *b*
3. calculate necessary corrections for rounding errors
4. do the multiplication and shift-right and apply corrections for rounding errors

This formula is advantageous if multiple numbers are divided by the same divisor

1. Steps 1, 2 and 3 need only be done once while step 4 is repeated for each value of the dividend *a*. The mathematical details are described in the file vectori128.h. (See also T. Granlund and P. L. Montgomery: Division by Invariant Integers Using Multiplication)

The implementation in the vector class library uses various variants of this method with appropriate corrections for rounding errors to get the exact result truncated towards zero.

The way to use this in your code depends on whether the divisor *b* is a variable or constant, and whether the same divisor is applied to multiple vectors. This is illustrated in the following examples:

// Division example A:

// A variable divisor is applied to one vector

Vec4i a(10, 11, 12, 13);// dividend is an integer vector int b = 3; // divisor is an integer variable Vec4i c = a / b; // result c = (3, 3, 4, 4)

// Division example B:

// The same divisor is applied to multiple vectors int b = 3; // divisor

Divisor\_i divb(b); // this object contains the results

// of calculation steps 1, 2, and 3

for (...) { // loop through multiple vectors Vec4i a = ... // get dividend

a = a / divb; // do step 4 of the division

... // store results

}

// Division example C:

// The divisor is a constant, known at compile time

Vec4i a(10, 11, 12, 13); // dividend is integer vector Vec4i c = a / const\_int(3); // result c = (3, 3, 4, 4)

Explanation:

The class Divisor\_i in example B takes care of the calculation steps 1, 2 and 3 in the algorithm described above. The overloaded / operator takes a vector on the left hand side and an object of class Divisor\_i on the right hand side. This object is created before the loop with the divisor as parameter to the constructor. We are saving time by doing this time-consuming calculation only once while step 4 in the calculation is done multiple times inside the loop by a = a / divb;.

In example A, we are also creating an object of class Divisor\_i, but this is done implicitly. The compiler sees an integer on the right hand side of the / operator where it needs an object of class Divisor\_i, and therefore converts the integer b to such an object by calling the constructor Divisor\_i(int).

The following divisor classes are available:

|  |  |
| --- | --- |
| **Dividend vector type** | **Divisor class required** |
| Vec16c, Vec32c | Divisor\_s |
| Vec16uc, Vec32uc | Divisor\_us |
| Vec8s, Vec16s | Divisor\_s |
| Vec8us, Vec16us | Divisor\_us |
| Vec4i, Vec8i, Vec16i | Divisor\_i |
| Vec4ui, Vec8ui, Vec16ui | Divisor\_ui |

If the divisor is a constant and the value is known at compile time, then we can use the method in example C. The implementation here uses macros and templates to do the calculation steps 1, 2 and 3 at compile time rather than at execution time. This makes the code even faster. The expression to put on the right-hand side of the / operator looks as follows:

|  |  |
| --- | --- |
| **Dividend vector type** | **Divisor expression** |
| Vec16c, Vec32c | const\_int |
| Vec16uc, Vec32uc | const\_uint |
| Vec8s, Vec16s | const\_int |
| Vec8us, Vec16us | const\_uint |
| Vec4i, Vec8i, Vec16i | const\_int |
| Vec4ui, Vec8ui, Vec16ui | const\_uint |

The compiler will generate an error message if the parameter to const\_int or const\_uint is not a valid compile-time constant. (A valid compile time constant can contain integer literals and operators, as well as macros that are expanded to compile time constants, but not function calls).

A further advantage of the method in example C is that the code is able to use different methods for different values of the divisor. The division is particularly fast if the divisor is a power of 2. Make sure to use const\_int or const\_uint on the right hand side of the / operator if you are dividing by 2, 4, 8, 16, etc.

Division is faster for vectors of 16-bit integers than for vectors of 8-bit or 32-bit integers. There is no support for division of vectors of 64-bit integers. Unsigned division is faster than signed division.

# Functions

## *Integer functions*

|  |  |
| --- | --- |
| **function** | horizontal\_add |
| **defined for** | all integer and floating point vector classes |
| **description** | calculates the sum of all vector elements |
| **efficiency** | medium |

Example:

Vec4i a(10, 11, 12, 13);

int b = horizontal\_add(a); // b = 46

|  |  |
| --- | --- |
| **function** | horizontal\_add\_x |
| **defined for** | all 8-bit, 16-bit and 32-bit integer vector classes |
| **description** | calculates the sum of all vector elements. The sum is calculated with a higher number of bits to avoid overflow |
| **efficiency** | medium (slower than horizontal\_add) |

Example:

Vec4i a(10, 11, 12, 13);

int64\_t b = horizontal\_add\_x(a); // b = 46

|  |  |
| --- | --- |
| **function** | add\_saturated |
| **defined for** | all 8-bit, 16-bit and 32-bit integer vector classes |
| **description** | same as operator +. Overflow is handled by saturation rather than wrap-around |
| **efficiency** | fast for 8-bit and 16-bit integers. Medium for 32-bit integers |

Example:

|  |  |  |  |
| --- | --- | --- | --- |
| Vec4i a(0x10000000, | 0x20000000, | 0x30000000, | 0x40000000); |
| Vec4i b(0x30000000, | 0x40000000, | 0x50000000, | 0x60000000); |
| Vec4i c = add\_saturated(a, b);  //c = (0x40000000,0x60000000, 0x7FFFFFFF,0x7FFFFFFF)  Vec4i d = a + b;  //d = (0x40000000,0x60000000,-0x80000000,-0x60000000) | | | |

|  |  |
| --- | --- |
| **function** | sub\_saturated |
| **defined for** | all 8-bit, 16-bit and 32-bit integer vector classes |
| **description** | same as operator -. Overflow is handled by saturation rather than wrap-around |
| **efficiency** | fast for 8-bit and 16-bit integers. Medium for 32-bit integers |

Example:

Vec4i a(-0x10000000,-0x20000000,-0x30000000,-0x40000000); Vec4i b( 0x30000000, 0x40000000, 0x50000000, 0x60000000);

Vec4i c = sub\_saturated(a, b);

// c = (-0x40000000,-0x60000000,-0x80000000,-0x80000000)

Vec4i d = a - b;

// d = (-0x40000000,-0x60000000,-0x80000000, 0x60000000)

|  |  |
| --- | --- |
| **function** | max |
| **defined for** | all integer vector classes |
| **description** | returns the biggest of two values |
| **efficiency** | fast for Vec16uc, Vec32uc, Vec8s, Vec16s, medium for other integer vector classes |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(14, 13, 12, 11);

Vec4i c = max(a, b); // c = (14, 13, 12, 13)

|  |  |
| --- | --- |
| **function** | min |
| **defined for** | all integer vector classes |
| **description** | returns the smallest of two values |
| **efficiency** | fast for Vec16uc, Vec32uc, Vec8s, Vec16s, medium for other integer vector classes |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(14, 13, 12, 11);

Vec4i c = min(a, b); // c = (10, 11, 12, 11)

|  |  |
| --- | --- |
| **function** | abs |
| **defined for** | all signed integer vector classes |
| **description** | calculates the absolute value |
| **efficiency** | medium |

Example:

Vec4i a(-1, 0, 1, 2);

Vec4i b = abs(a); // b = (1, 0, 1, 2)

|  |  |
| --- | --- |
| **function** | abs\_saturated |
| **defined for** | all signed integer vector classes |
| **description** | calculates the absolute value. Overflow saturates to make sure the result is never negative when the input is INT\_MIN |
| **efficiency** | medium (slower than abs) |

Example:

Vec4i a(-0x80000000, -1, 0, 1);

Vec4i b = abs\_saturated(a); // b=( 0x7FFFFFFF,1,0,1) Vec4i c = abs(a); // c=(-0x80000000,1,0,1)

|  |  |
| --- | --- |
| **function** | vector = rotate\_left(vector, int) |
| **defined for** | all integer vector classes |
| **description** | rotates the bits of each element. Use a negative count to rotate right |
| **efficiency** | 8 bit: poor  16 bit: medium  32 and 64 bit: good for AVX512DQ instruction set, medium otherwise. |

Example:

Vec4i a(0x12345678, 0x0000FFFF, 0xA000B000, 0x00000001);

Vec4i b = rotate\_left(a, 8);

// b = (0x34567812, 0x00FFFF00, 0x00B000A0, 0x00000100)

|  |  |
| --- | --- |
| **function** | vector shift\_bytes\_up(vector, int) vector shift\_bytes\_down(vector, int) |
| **defined for** | Vec16c, Vec32c |
| **description** | shifts the bytes of a vector up or down and inserts zeroes at the vacant places |
| **efficiency** | medium. (you may use permute functions instead if the shift count is a compile-time constant) |

Example:

Vec16c a(10,11,12,13,14,15,16,17,18,19,20,21,22,23,24,25);

Vec16c b = shift\_bytes\_up(a,5);

// b = (0,0,0,0,0,10,11,12,13,14,15,16,17,18,19,20)

## *Floating point simple mathematical functions*

|  |  |
| --- | --- |
| **function** | horizontal\_add |
| **defined for** | all floating point vector classes |
| **description** | calculates the sum of all vector elements |
| **efficiency** | medium |

Example:

Vec4f a(1.0, 1.1, 1.2, 1.3);

float b = horizontal\_add(a); // b = 4.6

|  |  |
| --- | --- |
| **function** | max |
| **defined for** | all floating point vector classes |
| **description** | returns the biggest of two values |
| **efficiency** | good |

Example:

Vec4f a(1.0, 1.1, 1.2, 1.3);

Vec4f b(1.4, 1.3, 1.2, 1.1);

Vec4f c = max(a, b); // c = (1.4, 1.3, 1.2, 1.3)

|  |  |
| --- | --- |
| **function** | min |
| **defined for** | all floating point vector classes |
| **description** | returns the smallest of two values |
| **efficiency** | good |

Example:

Vec4f a(1.0, 1.1, 1.2, 1.3);

Vec4f b(1.4, 1.3, 1.2, 1.1);

Vec4f c = min(a, b); // c = (1.0, 1.1, 1.2, 1.1)

|  |  |
| --- | --- |
| **function** | abs |
| **defined for** | all floating point vector classes |
| **description** | gets the absolute value |
| **efficiency** | good |

Example:

Vec4f a(-1.0, 0.0, 1.0, 2.0);

Vec4f b = abs(a); // b = (1.0, 0.0, 1.0, 2.0)

|  |  |
| --- | --- |
| **function** | change\_sign<i0, i1, ...>(vector) |
| **defined for** | all floating point vector classes |
| **description** | changes sign of vector elements |
| **efficiency** | good |

Each template parameter is 1 for changing sign of the corresponding element, and 0 for no change. Example:

Vec4f a(10.0f, 11.0f, 12.0f, 13.0f);

Vec4f b = change\_sign<0,1,1,0>(a); // b = (10,-11,-12,13)

|  |  |
| --- | --- |
| **function** | sqrt |
| **defined for** | all floating point vector classes |
| **description** | calculates the square root |
| **efficiency** | poor |

Example:

Vec4f a(0.0, 1.0, 2.0, 3.0);

Vec4f b = sqrt(a); // b = (0.000, 1.000, 1.414, 1.732)

|  |  |
| --- | --- |
| **function** | square |
| **defined for** | all floating point vector classes |
| **description** | calculates the square |
| **efficiency** | good |

Example:

Vec4f a(0.0, 1.0, 2.0, 3.0);

Vec4f b = square(a); // b = (0.0, 1.0, 4.0, 9.0)

|  |  |
| --- | --- |
| **function** | pow(vector x, int n) |
| **defined for** | all floating point vector classes |
| **description** | raises all vector elements to the same integer power.  Will generate a compiler error if n is floating point and vectormath\_exp is not included, or in general if n is not of type int.  See page [41](#_bookmark32) for pow with floating point exponent. |
| **precision** | slightly imprecise for extreme values of n due to accumulation of rounding errors |
| **efficiency** | medium |

Example:

Vec4f a(0.0, 1.0, 2.0, 3.0);

int b = 3;

Vec4f c = pow(a, b); // c = (0.0, 1.0, 8.0, 27.0)

|  |  |
| --- | --- |
| **function** | pow\_const(vector x, const int n) |
| **defined for** | all floating point vector classes |
| **description** | raises all vector elements to the same integer power n, where n is a compile-time constant |
| **precision** | slightly imprecise for extreme values of n due to accumulation of rounding errors |
| **efficiency** | medium, often better than pow(vector, int) |

Example:

Vec4f a(0.0, 1.0, 2.0, 3.0);

Vec4f b = pow\_const(a, 3);

// b = (0.0, 1.0, 8.0, 27.0)

|  |  |
| --- | --- |
| **function** | round |
| **defined for** | all floating point vector classes |
| **description** | round to nearest integer (even value if two values are equally near). The value is returned as a floating point vector. See also round\_to\_int and round\_to\_int64 on page [70](#_bookmark41). |
| **efficiency** | good if SSE4.1 instruction set |

Example:

Vec4f a(1.0, 1.4, 1.5, 1.6)

Vec4f b = round(a); // b = (1.0, 1.0, 2.0, 2.0)

|  |  |
| --- | --- |
| **function** | truncate |
| **defined for** | all floating point vector classes |
| **description** | truncates number towards zero. The value is returned as a floating point vector. See also truncate\_to\_int and truncate\_to\_int64 on page [71](#_bookmark42). |
| **efficiency** | good if SSE4.1 instruction set |

Example:

Vec4f a(1.0, 1.5, 1.9, 2.0)

Vec4f b = truncate(a); // b = (1.0, 1.0, 1.0, 2.0)

|  |  |
| --- | --- |
| **function** | floor |
| **defined for** | all floating point vector classes |
| **description** | rounds number towards -∞. The value is returned as a floating point vector |
| **efficiency** | good if SSE4.1 instruction set |

Example:

Vec4f a(-0.5, 1.5, 1.9, 2.0)

Vec4f b = floor(a); // b = (-1.0, 1.0, 1.0, 2.0)

|  |  |
| --- | --- |
| **function** | ceil |
| **defined for** | all floating point vector classes |
| **description** | rounds number towards +∞. The value is returned as a floating point vector |
| **efficiency** | good if SSE4.1 instruction set |

Example:

Vec4f a(-0.5, 1.1, 1.9, 2.0)

Vec4f b = ceil(a); // b = (0.0, 2.0, 2.0, 2.0)

|  |  |
| --- | --- |
| **function** | approx\_recipr |
| **defined for** | Vec4f, Vec8f, Vec16f |
| **description** | Fast approximate calculation of reciprocal. The relative accuracy depends on the instruction set:  Default: 2-11  AVX512F: 2-14  AVX512ER: full precision |
| **efficiency** | good |

Example:

Vec4f a(1.5, 2.0, 3.0, 4.0)

Vec4f b(0.5, 1.0, 0.5, 1.0)

Vec4f c = a \* approx\_recipr(b); // c ≈ a/b

In some cases it is faster to calculate a division in this way.

|  |  |
| --- | --- |
| **function** | approx\_rsqrt |
| **defined for** | Vec4f, Vec8f, Vec16f |
| **description** | Reciprocal square root. Fast approximate calculation of value to the power of -0.5.  The relative accuracy depends on the instruction set: Default: 2-11  AVX512F: 2-14  AVX512ER: full precision |
| **efficiency** | good |

Example:

Vec4f a(1.0, 2.0, 3.0, 4.0)

Vec4f b = a \* approx\_rsqrt(a); // b ≈ sqrt(a)

In some cases it is faster to calculate a square root in this way.

|  |  |
| --- | --- |
| **function** | exponent |
| **defined for** | all floating point vector classes |
| **description** | extracts the exponent part of a floating point number. Result is an integer vector.  exponent(a) = floor(log2(abs(a))), except for a = 0 |
| **efficiency** | medium |

Example:

// single precision:

Vec4f a(1.0, 2.0, 3.0, 4.0);

Vec4i b = exponent(a); // b = (0, 1, 1, 2)

// double precision: Vec2d a(1.0, 2.0);

Vec2q b = exponent(a); // b = (0, 1)

|  |  |
| --- | --- |
| **function** | fraction |
| **defined for** | all floating point vector classes |
| **description** | extracts the fraction part of a floating point number.  a = pow(2, exponent(a)) \* fraction(a), except for a = 0 |
| **efficiency** | medium |

Example:

Vec4f a(2.0, 3.0, 4.0, 5.0);

Vec4f b = fraction(a); // b = (1.00, 1.50, 1.00, 1.25)

|  |  |
| --- | --- |
| **function** | exp2 |
| **defined for** | all floating point vector classes |
| **description** | calculates integer powers of 2. The input is an integer vector, the output is a floating point vector. Overflow gives  +INF, underflow gives zero. This function will never produce subnormals, and never raise exceptions |
| **efficiency** | medium |

Example:

// single precision: Vec4i a(-1, 0, 1, 2);

Vec4f b = exp2(a); // b = (0.5, 1.0, 2.0, 4.0)

// double precision: Vec2q a(-1, 0);

Vec2d b = exp2(a); // b = (0.5, 1.0)

|  |  |
| --- | --- |
| **function** | mul\_add nmul\_add mul\_sub mul\_sub\_x |
| **defined for** | all floating-point vector classes |
| **description** | mul\_add(a,b,c) = a\*b+c nmul\_add(a,b,c) = -a\*b+c mul\_sub(a,b,c) = a\*b-c mul\_sub\_x(a,b,c) = a\*b-c  These functions use fused multiply-and-add (FMA) instructions if available. Some compilers use FMA automatically for expressions like a\*b+c. Use these functions for optimal performance on all compilers or to specify calculation order, etc. |
| **precision** | The intermediate product a\*b is calculated with infinite precision if the FMA or FMA4 instruction set is enabled. mul\_sub\_x has extra precision even if FMA or FMA4 is not available, just slightly less precise. |
| **efficiency** | mul\_add, nmul\_add, mul\_sub: better than a\*b+c, etc. mul\_sub\_x: good if FMA or FMA4 enabled, medium otherwise |

## *Floating point categorization functions*

|  |  |
| --- | --- |
| **function** | sign\_bit |
| **defined for** | all floating point vector classes |
| **description** | returns a boolean vector with true for elements that have the sign bit set, including -0.0, -INF and -NAN. |
| **efficiency** | good |

Example:

// single precision:

Vec4f a(-1.0, 0.0, 1.0, 2.0);

Vec4fb b = sign\_bit(a); // b = (true, false, false, false)

// double precision: Vec2d a(-1.0, 0.0);

Vec2db b = sign\_bit(a); // b = (true, false)

|  |  |
| --- | --- |
| **function** | sign\_combine(vector a, vector b) |
| **defined for** | all floating point vector classes |
| **description** | Returns the value of a, with the sign inverted if b has its sign bit set.  Corresponds to select(sign\_bit(b), -a, a) |
| **efficiency** | good |

|  |  |
| --- | --- |
| **function** | is\_finite |
| **defined for** | all floating point vector classes |
| **description** | returns a boolean vector with true for elements that are normal, subnormal or zero, false for INF and NAN |
| **efficiency** | medium |

Example:

Vec4f a( 0.0, 1.0, 2.0, 3.0);

Vec4f b(-1.0, 0.0, 1.0, 2.0);

Vec4f c = a / b;

Vec4fb d = is\_finite(c); // d = (true, false, true, true)

|  |  |
| --- | --- |
| **function** | is\_inf |
| **defined for** | all floating point vector classes |
| **description** | returns a boolean vector with true for elements that are  +INF or -INF, false for all other values, including NAN |
| **efficiency** | good |

Example:

Vec4f a( 0.0, 1.0, 2.0, 3.0);

Vec4f b(-1.0, 0.0, 1.0, 2.0);

Vec4f c = a / b;

Vec4fb d = is\_inf(c); // d = (false, true, false, false)

|  |  |
| --- | --- |
| **function** | is\_nan |
| **defined for** | all floating point vector classes |
| **description** | returns a boolean vector with true for all types of NAN, false for all other values, including INF |
| **efficiency** | medium |

Example:

Vec4f a(-1.0, 0.0, 1.0, 2.0);

Vec4f b = sqrt(a);

Vec4fb c = is\_nan(b); // c = (true, false, false, false)

|  |  |
| --- | --- |
| **function** | is\_subnormal is\_zero\_or\_subnormal |
| **defined for** | all floating point vector classes |
| **description** | returns a boolean vector with true for subnormal (denormal) vector elements, false for normal numbers, INF and NAN.  is\_zero\_or\_subnormal also returns true for elements that are zero. |
| **efficiency** | is\_subnormal: medium is\_zero\_or\_subnormal: good |

Example:

Vec4f a(1.0, 1.0E-10, 1.0E-20, 1.0E-30);

Vec4f b = a \* a; // b = (1., 1.E-20, 1.E-40, 0.)

Vec4fb c = is\_subnormal(b); // c = (false,false,true,false)

|  |  |
| --- | --- |
| **function** | infinite4f, infinite8f, infinite16f, infinite2d, infinite4d, infinite8d |
| **defined for** | all floating point vector classes |
| **description** | returns positive infinity |
| **efficiency** | good |

Example:

Vec4f a = infinite4f(); // a = (INF, INF, INF, INF)

|  |  |
| --- | --- |
| **function** | nan4f(unsigned int n) nan8f(unsigned int n) nan16f(unsigned int n) nan2d(unsigned int n) nan4d(unsigned int n) nan8d(unsigned int n) |
| **defined for** | all floating point vector classes |
| **description** | returns not-a-number (NAN).  The optional parameter n may be used for error tracing. The maximum value of n is 0x003FFFFF for single precision, unlimited for double precision. This parameter can be retrieved later by the function nan\_code (page [52](#_bookmark33)). |
| **efficiency** | good |

Example:

Vec4f a = nan4f(); // a = (NAN, NAN, NAN, NAN)

## *Floating point control word manipulation functions*

MXCSR is a control word that controls floating point exceptions, rounding mode and subnormal numbers. There is one MXCSR for each thread.

The MXCSR has the following bits:

|  |  |
| --- | --- |
| **bit index** | **meaning** |
| 0 | Invalid Operation Flag |
| 1 | Denormal (subnormal) Flag |
| 2 | Divide-by-Zero Flag |
| 3 | Overflow Flag |
| 4 | Underflow Flag |
| 5 | Precision Flag |
| 6 | Denormals (subnormals) Are Zeros |

|  |  |
| --- | --- |
| 7 | Invalid Operation Mask |
| 8 | Denormal (subnormal) Operation Mask |
| 9 | Divide-by-Zero Mask |
| 10 | Overflow Mask |
| 11 | Underflow Mask |
| 12 | Precision Mask |
| 13-14 | Rounding control:  00: round to nearest or even 01: round down towards -infinity 10: round up towards +infinity  11: round towards zero (truncate)  If the rounding mode is temporarily changed then it must be set back to 00 for the vector class library to work correctly. |
| 15 | Flush to Zero |

Please see programming manuals from Intel or AMD for further explanation.

|  |  |
| --- | --- |
| **function** | get\_control\_word |
| **description** | reads the MXCSR control word |
| **efficiency** | medium |

Example:

int m = get\_control\_word(); // default value m = 0x1F80

|  |  |
| --- | --- |
| **function** | set\_control\_word |
| **description** | writes the MXCSR control word |
| **efficiency** | medium |

Example:

set\_control\_word(0x1980); // overflow and divide by zero

// exceptions

|  |  |
| --- | --- |
| **function** | reset\_control\_word |
| **description** | sets the MXCSR control word to the default value |
| **efficiency** | medium |

Example:

reset\_control\_word();

|  |  |
| --- | --- |
| **function** | no\_subnormals |
| **description** | Disables the use of subnormal (denormal) values. Floating point numbers with an absolute value below 1.18∙10-38 for single precision or 2.22∙10-308 for double precision are represented by subnormal numbers. The handling of subnormal numbers is extremely time- consuming on many CPUs. The no\_subnormals function  sets the "denormals are zeros" and "flush to zero" mode to avoid the use of subnormal numbers. It is recommended to call this function at the beginning of each thread in order to improve the speed of mathematical calculations if very low numbers are likely to occur. |
| **efficiency** | medium |

Example:

no\_subnormals();

## *Floating point mathematical functions*

Mathematical functions such as logarithms, exponential functions, power, trigonometric functions, etc. are available either as inline code or through external function libraries. These functions all take vectors as input and produce vectors as output.

The use of vector math functions is straightforward. Example:

#include <stdio.h> #include "vectorsimd.h"

#include "vectormath\_trig.h" // trigonometric functions

int main() {

Vec4f a(0.0, 0.5, 1.0, 1.5);// define vector Vec4f b = sin(a); // sine function

// b = (0.0000, 0.4794, 0.8415, 0.9975)

// output results:

for (int i = 0; i < b.size(); i++) {

printf("%6.4f ", b[i]);

}

printf("\n"); return 0;

}

Inline mathematical functions

The inline mathematical functions are made available by including the appropriate header file, e. g. math/exp.h for powers, logarithms and exponential functions, and vectormath\_trig.h for trigonometric functions. An advantage of the inline version is that the compiler can optimize the code across function calls, eliminate common sub-expressions, etc. The disadvantage is that you may get multiple instances of the same function taking up space in the code cache.

The speed of the inline functions is similar to or better than external vector function libraries in most cases and many times faster than standard (scalar) math function libraries.

The precision is good. The calculation error is typically below 1 ULP (Unit in the Last Place = least significant bit) on the output. (The relative value of one ULP is 2-52 for double precision and 2-23 for single precision). Cases where the error can exceed 2 ULP are mentioned under the specific function.

The functions do not generate exceptions or set errno when an input is out of range. This would be inefficient and it would be problematic for the error handler to detect which vector element caused the error. Instead, the functions just return INF (infinity) or NAN (not a number) in case of error. Generally, an overflow will produce INF. A negative overflow produces -INF. An underflow towards zero returns 0. Other errors produce NAN. An efficient way of detecting errors is to let the INF and NAN codes propagate through the calculations and detect the error at the end of a series of calculations. It is possible to include an error code in a NAN and detect it with the function nan\_code on page [52](#_bookmark33).

There are a few cases, though, where INF and NAN codes do not propagate. For example, dividing a nonzero number by INF produces zero. Error codes cannot propagate through integer and boolean vectors. For example:

Vec4d a, b;

...

b = select(a > 1.0, a, 0.5);

Now, if an element of a is NAN then the boolean vector element in a > 1.0 will be either true or false because a boolean can have no other values. Whether it is true of false is implementation-dependent. If it happens to be false then the corresponding element in b will be 0.5, and the error is not propagated to b.

Therefore, you have to check for errors before making a boolean expression. This can be done like this:

Vec4d a, b;

…

if ( ! horizontal\_and (is\_finite (a))) {

// handle error

…

}

b = select(a > 1.0, a, 0.5);

It is not recommended to unmask floating point exceptions. It is not guaranteed that this will generate exceptions in case of errors in these functions.

Note that many of the inline math functions do not support subnormal numbers. Subnormal numbers may be treated as zero by the logarithm, exponential, power and root functions. It is recommended to set the “denormals are zero” and “flush to zero” flags by calling the function no\_subnormals() first (see above). This will speed up some calculations and give more consistent results.

A description of each mathematical function is given below.

Using an external library for mathematical functions

As an alternative to the inline mathematical functions, you can use an external function library. Include the header file vectormath\_lib.h for this. Set the define VECTORMATH to one of the following values to specify which external library you are using:

|  |  |
| --- | --- |
| **VECTORMATH**  **value** | **Function library** |
| 0 | Uses the standard math library that is included with the compiler. You do not have to include any extra libraries. The library function is called once for each vector element. This is slow (especially for the Gnu library).  Use this option for testing purposes or where performance is not critical. |
| 1 | AMD LIBM library. The [LIBM](http://developer.amd.com/libraries/LibM/Pages/default.aspx) library is available for 64-bit Linux and 64-bit Windows, but not for 32-bit systems. File name: amdlibm.lib or libamdlibm.a.  Performance is good for AMD processors with FMA4, but inferior for processors without FMA4. Currently, the FMA4 instruction set is supported only in AMD processors. |
| 2 | Use Intel SVML library (Short Vector Math Library) with any compiler. The SVML library is available for all platforms relevant to the vector class library. It is included with [Intel C++](http://software.intel.com/en-us/articles/intel-compilers/) [compilers](http://software.intel.com/en-us/articles/intel-compilers/) but can be used with other compilers as well. File name: svml\_dispmt.lib or libsvml.a. Be sure to choose the 32- bit version or 64-bit version according to the platform you are compiling for.  Performance is good on Intel processors. Performance may be inferior on other brands of processors unless you replace Intel's own CPU dispatch function. Link in the library libircmt.lib to use Intel's own CPU dispatch function for Intel processors, or use an object file from the [asmlib library](http://www.agner.org/optimize/#asmlib) under "inteldispatchpatch" for best performance on all brands of processors. See [my blog](http://www.agner.org/optimize/blog/read.php?i=49) and [my C++ manual](http://www.agner.org/optimize/#manual_cpp) for details. |
| 3 | Use Intel SVML library with an Intel compiler. You do not have to link in any extra libraries. The Intel compiler gives access to different versions with different precision. Performance is good on Intel processors, but inferior on other brands of processors unless you link in the dispatch patch from the [asmlib library](http://www.agner.org/optimize/#asmlib) as described above. |

The value of VECTORMATH can be defined on the compiler command line or by a define statement:

#define VECTORMATH 2 #include "vectormath\_lib.h"

The chosen function library must be linked into your project if the value of

VECTORMATH is 1 or 2.

Details about range, error handling and precision must be sought in the documentation for the specific library.

If you want to use both inline and library math functions then you have to include the header files for the inline functions *before* vectormath\_lib.h. This will give you the library version for functions that are not available as inline versions.

List of mathematical functions

The available vector math functions are listed below. The efficiency is listed as poor because mathematical functions take more time to execute than most other functions, but they are still faster than most alternatives. The details listed apply to the inline version. Details for the library versions may be sought in the documentation for the specific library.

### Powers, exponential functions and logarithms

|  |  |
| --- | --- |
| **function** | pow(vector, vector)  pow(vector, scalar) |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | all values of VECTORMATH have pow(vector, vector) |
| **description** | pow(a,b) = ab  See also faster alternatives below for integer and rational powers. |
| **range** | Subnormal numbers are treated as zero. The result is NAN if a is negative and b is not an integer. pow(0,0) = 1. pow(NAN,0) is NAN or 1, depending on the implemen- tation. pow(1,NAN) is NAN or 1, depending on the implementation. |
| **precision** | better than (0.1\*abs(b)+1) ULP |
| **efficiency** | poor |

Example:

Vec4f a( 1.0, 2.0, 3.0, 4.0);

Vec4f b( 0.0, -1.0, 0.5, 2.0);

Vec4f c = pow(a, b);

// c = (1.0000, 0.5000, 1.7321, 16.0000)

Vec4f d = pow(a, 2.4f);

// d = (1.0000, 5.2780, 13.9666, 27.8576)

|  |  |
| --- | --- |
| **function** | pow(vector, int) |
| **defined for** | all floating point vector classes |
| **inline version** | no extra header file required |
| **library versions** | not available |
| **description** | see page [30](#_bookmark25). |
| **efficiency** | medium |

|  |  |
| --- | --- |
| **function** | pow\_const(vector x, const int n) |
| **defined for** | all floating point vector classes |
| **inline version** | no extra header file required |
| **library versions** | not available |
| **description** | see page [30](#_bookmark26). |
| **efficiency** | medium, often better than pow(vector, int) |

|  |  |
| --- | --- |
| **function** | pow\_ratio(vector x, const int a, const int b) |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | not available |
| **description** | Raises all elements of x to the rational power a/b. a and b must be compile-time constant integers.  For example pow\_ratio(x, -1, 2) gives the reciprocal square root of x.  x may be zero only if a and b are positive. x may be negative only if b is odd. The result when x is infinite is implementation dependent. |
| **range** | subnormal numbers are treated as zero in some cases |
| **precision** | slightly imprecise for extreme values of a due to accumulation of rounding errors. the precision is similar to the pow function when b is not 1, 2, 3, 4, 6 or 8. |
| **efficiency** | Quite good for b = 1, 2, 4, or 8. Reasonable for b = 3 or 6. No better than pow for other values of b. |

|  |  |
| --- | --- |
| **function** | exp |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | all values of VECTORMATH |
| **description** | exponential function ex |
| **range** | double: abs(x) < 708.39. float: abs(x) < 87.3 |
| **efficiency** | Poor. The performance of the inline version for single precision vectors (Vec16f etc.) is better when the instruction set AVX512ER is enabled. The performance can be improved further, at a slight loss of precision, when BIGMATH SIMD\_FASTEXP is defined in addition to AVX512ER. |

Example:

#define BIGMATH SIMD\_FASTEXP #include "math/exp.h" Vec16f a, b;

b = exp(a); // fast if AVX512ER enabled

|  |  |
| --- | --- |
| **function** | expm1 |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | all values of VECTORMATH, except 0 for some libraries |
| **description** | ex-1. Useful to avoid loss of precision if x is close to 0 |
| **range** | double: abs(x) < 708.39. float: abs(x) < 87.3 |
| **efficiency** | Poor. (not improved with AVX512ER) |

|  |  |
| --- | --- |
| **function** | exp2 |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | all values of VECTORMATH, except 0 for some libraries |
| **description** | 2x |
| **range** | double: abs(x) < 1022. float: abs(x) < 126. |
| **efficiency** | Poor without AVX512ER.  The performance of the inline version is good for single precision vectors with instruction set AVX512ER. (BIGMATH SIMD\_FASTEXP not needed) |

|  |  |
| --- | --- |
| **function** | exp10 |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | all values of VECTORMATH |
| **description** | 10x |
| **range** | double: abs(x) < 307.65. float: abs(x) < 37.9. |
| **efficiency** | Poor. The performance of the inline version for single precision vectors (Vec16f etc.) is better when the instruction set AVX512ER is enabled. The performance can be improved further, at a slight loss of precision, when BIGMATH SIMD\_FASTEXP is defined in addition to AVX512ER. |

Example:

#define BIGMATH SIMD\_FASTEXP #include "math/exp.h" Vec16f a, b;

b = exp10(a); // very fast if AVX512ER enabled

// Use pow or pow\_const instead if a is an integer.

|  |  |
| --- | --- |
| **function** | log |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | all values of VECTORMATH |
| **description** | natural logarithm |
| **range** | The input must be a normal number. Subnormal numbers are treated as zero. |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | log1p |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | all values of VECTORMATH, except 0 for some libraries |
| **description** | log(1+x)  Useful to avoid loss of precision if x is close to 0 |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | log2 |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | all values of VECTORMATH |
| **description** | logarithm base 2 |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | log10 |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | all values of VECTORMATH |
| **description** | logarithm base 10 |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | cbrt |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | VECTORMATH = 1, 2, 3 |
| **description** | cube root |
| **range** | input must be a normal number. Subnormal numbers are treated as zero |
| **efficiency** | faster than pow |

|  |  |
| --- | --- |
| **function** | cexp |
| **defined for** | all floating point vector classes |
| **inline version** | not available |
| **library versions** | VECTORMATH = 0, 2, 3 |
| **description** | complex exponential function. Even-numbered vector elements are real part, odd-numbered vector elements are imaginary part. |
| **efficiency** | poor |

### Trigonometric functions (angles in radians)

|  |  |
| --- | --- |
| **function** | sin(x) |
| **defined for** | all floating point vector classes |
| **inline version** | vectormath\_trig.h |
| **library versions** | all values of VECTORMATH |
| **description** | sine function. |
| **range** | Defined for abs(x) < 1.7∙109. 0 otherwise |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | cos(x) |
| **defined for** | all floating point vector classes |
| **inline version** | vectormath\_trig.h |
| **library versions** | all values of VECTORMATH |
| **description** | cosine function. |
| **range** | Defined for abs(x) < 1.7∙109. 1 otherwise |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | sincos(x) |
| **defined for** | all floating point vector classes |
| **inline version** | vectormath\_trig.h |
| **library versions** | all values of VECTORMATH, may not be available for Vec16f and Vec8d |
| **description** | sine and cosine computed simultaneously. |
| **range** | Defined for abs(x) < 1.7∙109. 0 and 1 otherwise |
| **efficiency** | poor |

Example:

Vec4f a(0.0, 0.5, 1.0, 1.5);

Vec4f s, c;

s = sincos(&c, a);

// s = (0.0000, 0.4794, 0.8415, 0.9975)

// c = (1.0000, 0.8776, 0.5403, 0.0707)

|  |  |
| --- | --- |
| **function** | tan(x) |
| **defined for** | all floating point vector classes |
| **inline version** | vectormath\_trig.h |
| **library versions** | all values of VECTORMATH |
| **description** | tangent function.  tan(π/2) will not produce infinity because the value of π/2 cannot be represented exactly as a floating point number. The output will be big, though, when the input is as close to π/2 as possible. |
| **range** | Defined for abs(x) < 1.7∙109. 0 otherwise |
| **efficiency** | poor |

### Inverse trigonometric functions (angles in radians)

|  |  |
| --- | --- |
| **function** | asin |
| **defined for** | all floating point vector classes |
| **inline version** | vectormath\_trig.h |
| **library versions** | VECTORMATH = 0, 2, 3 |
| **description** | inverse sine function |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | acos |
| **defined for** | all floating point vector classes |
| **inline version** | vectormath\_trig.h |
| **library versions** | VECTORMATH = 0, 2, 3 |
| **description** | inverse cosine function |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | atan |
| **defined for** | all floating point vector classes |
| **inline version** | vectormath\_trig.h |
| **library versions** | VECTORMATH = 0, 2, 3 |
| **description** | Inverse tangent.  Results between -π/2 and π/2. |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | atan2 |
| **defined for** | all floating point vector classes |
| **inline version** | vectormath\_trig.h |
| **library versions** | VECTORMATH = 0, 2, 3 |
| **description** | Inverse tangent with two parameters, x and y, gives the angle to a point in the (x,y) plane.  Results between -π and π.  The result of atan2(0,0) is 0 by convention. |
| **efficiency** | poor |

### Hyperbolic functions and inverse hyperbolic functions

|  |  |
| --- | --- |
| **function** | sinh |
| **defined for** | all floating point vector classes |
| **inline version** | math/hyp.h |
| **library versions** | VECTORMATH = 0, 2, 3 |
| **description** | hyperbolic sine |
| **range** | double: abs(x) < 709.7. float: abs(x) < 89. |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | cosh |
| **defined for** | all floating point vector classes |
| **inline version** | math/hyp.h |
| **library versions** | VECTORMATH = 0, 2, 3 |
| **description** | hyperbolic cosine |
| **range** | double: abs(x) < 709.7. float: abs(x) < 89. |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | tanh |
| **defined for** | all floating point vector classes |
| **inline version** | math/hyp.h |
| **library versions** | VECTORMATH = 0, 2, 3 |
| **description** | hyperbolic tangent |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | asinh |
| **defined for** | all floating point vector classes |
| **inline version** | math/hyp.h |
| **library versions** | VECTORMATH = 2, 3 |
| **description** | inverse hyperbolic sine |
| **precision** | The error is less than 3 ULP for double and 4 ULP for float |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | acosh |
| **defined for** | all floating point vector classes |
| **inline version** | math/hyp.h |
| **library versions** | VECTORMATH = 2, 3 |
| **description** | inverse hyperbolic cosine |
| **precision** | The error is less than 5 ULP for double and 4 ULP for float |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | atanh |
| **defined for** | all floating point vector classes |
| **inline version** | math/hyp.h |
| **library versions** | VECTORMATH = 2, 3 |
| **description** | inverse hyperbolic tangent |
| **efficiency** | poor |

### Error function

|  |  |
| --- | --- |
| **function** | erf |
| **defined for** | all floating point vector classes |
| **inline version** | not available |
| **library versions** | VECTORMATH = 2, 3, and some libraries VECTORMATH  = 0 |
| **description** | error function |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | erfc |
| **defined for** | all floating point vector classes |
| **inline version** | not available |
| **library versions** | VECTORMATH = 2, 3, and some libraries VECTORMATH  = 0 |
| **description** | error function complement |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | erfinv |
| **defined for** | all floating point vector classes |
| **inline version** | not available |
| **library versions** | VECTORMATH = 2, 3 |
| **description** | inverse error function |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | cdfnorm |
| **defined for** | all floating point vector classes |
| **inline version** | not available |
| **library versions** | VECTORMATH = 2, 3 |
| **description** | cumulative normal distribution function |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | cdfnorminv |
| **defined for** | all floating point vector classes |
| **inline version** | not available |
| **library versions** | VECTORMATH = 2, 3 |
| **description** | inverse cumulative normal distribution function |
| **efficiency** | poor |

### Miscellaneous

|  |  |
| --- | --- |
| **function** | Vec4i nan\_code(Vec4f) Vec8i nan\_code(Vec8f) Vec16i nan\_code(Vec16f) Vec2q nan\_code(Vec2d) Vec4q nan\_code(Vec4d) Vec8q nan\_code(Vec8d) |
| **defined for** | all floating point vector classes |
| **inline version** | math/exp.h |
| **library versions** | not available |
| **description** | Extracts an error code hidden in a NAN. This code can be generated with the functions nan4f etc. (page [36](#_bookmark28)) and propagated through a series of calculations. When two NANs are combined (e. g. NAN+NAN), current processors propagate the first one. It has been suggested that future processors should OR the two values. NANs produced by CPU instructions, such as 0./0. or sqrt(-1.) do not have a code. NANs cannot propagate through integer and boolean vectors.  The return value is (0x00400000 + code) for single precision and (0x0008000000000000 + code) for double. The sign bit is ignored.  The return value is 0 for inputs that are not NAN. |
| **efficiency** | medium |

## *Permute, blend, lookup, gather and scatter functions*

### Permute function

|  |  |
| --- | --- |
| **function** | permute..<i0, i1, ...>(vector) |
| **defined for** | all integer and floating point vector classes |
| **description** | permutes vector elements |
| **efficiency** | depends on parameters and instruction set |

The permute functions can move any element of a vector into any position, copy the same element to multiple positions, and set any element to zero.

The name of the permute function is "permute" + the vector type suffix, for example permute4i for Vec4i. The permute function for a vector of *n* elements has *n* indexes, which are entered as template parameters in angle brackets. Each index indicates the desired contents of the corresponding element in the result vector. An index *i* in the interval 0 ≤ *i* ≤ *n*-1 indicates that element number *i* from the input vector should be placed in the corresponding position in the result vector. An index *i* = -1 gives a zero in the corresponding position. An index *i* =

-256 means don't care (i. e. use whatever implementation is fastest, regardless of what value it puts in this position). The value you get with "don't care" may be different for different implementations or different instruction sets.

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b = permute4i<2,2,3,0>(a); // b = (12, 12, 13, 10)

Vec4i c = permute4i<-1,-1,1,1>(a); // c = ( 0, 0, 11, 11)

The indexes in angle brackets must be compile-time constants, they cannot contain variables or function calls. If you need variable indexes then use the lookup functions instead (see §4.6.3).

The permute functions contain a lot of metaprogramming code which is used for finding the best implementation for the given set of indexes and the specified instruction set. This metaprogramming produces a lot of extra code when compiling in debug mode, but it is reduced out when compiling for release mode with optimization on. The call to a permute function is reduced to just one or a few machine instructions in favorable cases. But in unfavorable cases where the selected instruction set has no machine instruction that matches the desired permutation pattern, it may produce many machine instructions.

The performance is generally good when the instruction set SSSE3 or higher is enabled. The performance for permuting vectors of 16-bit integers is medium, and the performance for permuting vectors of 8-bit integers is poor for instruction sets lower than SSSE3.

### Blend functions

|  |  |
| --- | --- |
| **function** | blend..<i0, i1, ...>(vector, vector) |
| **defined for** | all integer and floating point vector classes |
| **description** | permutes and blends elements from two vectors |
| **efficiency** | depends on parameters and instruction set |

The blend functions are similar to the permute functions, but with two input vectors. An index *i* in the interval 0 ≤ *i* ≤ *n*-1 indicates that element number *i* from the first input vector should be placed in the corresponding position in the result vector. An index *i* in the interval n ≤ *i* ≤ 2\**n*-1 indicates that element number *i-n* from the second input vector should be placed in the corresponding position in the result vector. An index *i* = -1 gives a zero in the corresponding position. An index *i* = -256 means don't care.

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(20, 21, 22, 23);

Vec4i c = blend4i<4,0,4,3>(a, b); // c = (20, 10, 20, 13)

If you want to blend input from more than two vectors, there are three different methods you can use:

* 1. A binary tree of blend calls, where unused values are set to don't care (-256). Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(20, 21, 22, 23);

Vec4i c(30, 31, 32, 33);

Vec4i d(40, 41, 42, 43);

Vec4i r = blend4i<0,5,-256,-256>(a, b);// r = (10,21,?,?)

Vec4i s = blend4i<-256,-256,2,7>(c, d);// s = (?,?,32,43) Vec4i t = blend4i<0,1,6,7>(r, s); // t = (10,21,32,43)

* 1. Set unused values to zero, and OR the results. Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(20, 21, 22, 23);

Vec4i c(30, 31, 32, 33);

Vec4i d(40, 41, 42, 43);

Vec4i r = blend4i<0,5,-1,-1>(a, b);// r = (10,21,0,0)

Vec4i s = blend4i<-1,-1,2,7>(c, d);// s = (0,0,32,43) Vec4i t = r | s; // t = (10,21,32,43)

* 1. If the input vectors are stored sequentially in memory then use the lookup functions shown below.

### Lookup functions

|  |  |
| --- | --- |
| **function** | Vec16c lookup16(Vec16c, Vec16c) Vec32c lookup32(Vec32c, Vec32c) Vec8s lookup8(Vec8s, Vec8s) Vec16s lookup16(Vec16s, Vec16s) Vec4i lookup4(Vec4i, Vec4i)  Vec8i lookup8(Vec8i, Vec8i) Vec16i lookup16(Vec16i, Vec16i) Vec4q lookup4(Vec4q, Vec4q) Vec8q lookup8(Vec8q, Vec8q) |
| **defined for** | Vec16c, Vec32c, Vec8s, Vec16s, Vec4i, Vec8i, Vec16i, Vec4q, Vec8q |
| **description** | permutation with variable indexes. The first input vector contains the indexes, the second input vector is the data source. Each index must be in the range 0 ≤ *i* ≤ *n*-1 where n is the number of elements in a vector. |
| **efficiency** | good for AVX2, medium for lower instruction sets |
| **function** | Vec16c lookup32(Vec16c, Vec16c, Vec16c) Vec8s lookup16(Vec8s, Vec8s, Vec8s) Vec4i lookup8(Vec4i, Vec4i, Vec4i)  Vec4i lookup16(Vec4i, Vec4i, Vec4i, Vec4i, Vec4i) |

|  |  |
| --- | --- |
| **defined for** | Vec16c, Vec8s, Vec4i |
| **description** | blend with variable indexes. The first input vector contains the indexes, the following two or four input vectors contain the data source. Each index must be in the range 0 ≤ *i* ≤ *n*- 1 where n is the number indicated by the name. |
| **efficiency** | good for AVX2, medium for lower instruction sets |

|  |  |
| --- | --- |
| **function** | Vec4f lookup4(Vec4i, Vec4f) Vec8f lookup8(Vec8i, Vec8f) Vec16f lookup16(Vec16i, Vec16f) Vec2d lookup2(Vec2q, Vec2d) Vec4d lookup4(Vec4q, Vec4d) Vec8d lookup8(Vec8q, Vec8d) |
| **defined for** | all floating point vector classes |
| **description** | permutation of floating point vectors with integer indexes. Each index must be in the range 0 ≤ *i* ≤ *n*-1 where n is the number of elements in a vector. |
| **efficiency** | good for AVX2, medium for lower instruction sets |

|  |  |
| --- | --- |
| **function** | Vec4f lookup8(Vec4i, Vec4f, Vec4f) Vec2d lookup4(Vec2q, Vec2d, Vec2d) |
| **defined for** | Vec4f, Vec2d |
| **description** | blend of floating point vectors with integer indexes. Each index must be in the range 0 ≤ *i* ≤ 2\**n*-1 where n is the number of elements in a vector. |
| **efficiency** | medium |
| **function** | Vec16c lookup<n>(Vec16c index, void const \* table) Vec32c lookup<n>(Vec32c index, void const \* table) Vec8s lookup<n>(Vec8s index, void const \* table) Vec16s lookup<n>(Vec16s index, void const \* table) Vec4i lookup<n>(Vec4i index, void const \* table) Vec8i lookup<n>(Vec8i index, void const \* table) Vec16i lookup<n>(Vec16i index, void const \* table) Vec4q lookup<n>(Vec4q index, void const \* table) Vec8q lookup<n>(Vec8q index, void const \* table) Vec4f lookup<n>(Vec4i index, float const \* table)  Vec8f lookup<n>(Vec8i const & index, float const \* table) Vec16f lookup<n>(Vec16i const & index, float const \* table) Vec2d lookup<n>(Vec2q index, double const \* table) Vec4d lookup<n>(Vec4q const & i, double const \* table) Vec8d lookup<n>(Vec8q const & i, double const \* table) |

|  |  |
| --- | --- |
| **defined for** | all floating point and signed integer vector classes |
| **description** | permute, blend, table lookup or gather data from array with an integer vector of indexes.  Each index must be in the range 0 ≤ *i* ≤ *n*-1, where n is indicated as a template parameter (n must be a positive compile-time constant). |
| **efficiency** | good for AVX2, medium for lower instruction sets |

The lookup functions are similar to the permute and blend functions, but with variable indexes. They cannot be used for setting an element to zero, and there is no "don't care" option. The lookup functions can be used for several purposes:

* + 1. permute with variable indexes
    2. blend with variable indexes
    3. blend from more than two sources
    4. table lookup
    5. gather non-contiguous data from an array

The index is always an integer vector. The input can be one or more vectors or an array. The result is a vector of the same type as the input. All elements in the index vector must be in the specified range. The behavior for an index out of range is implementation-dependent and may give any value for the corresponding element. The function may in some cases read up to one vector size past the end of the table for the sake of efficient permutation.

The lookup functions are not defined for unsigned integer vector types, but the corresponding signed versions can be used. You don't have to worry about overflow when converting unsigned integers to signed here, as long as the result vector is converted back to unsigned.

Example of permutation with variable indexes:

Vec4f a(1.0, 1.1, 1.2, 1.3);

Vec4i b(2, 3, 3, 0);

Vec4f c = lookup4(b, a); // c = (1.2, 1.3, 1.3, 1.0)

Example of blending with variable indexes:

Vec4f a(1.0, 1.1, 1.2, 1.3);

Vec4f b(2.0, 2.1, 2.2, 2.3);

Vec4i c(4, 3, 2, 7);

Vec4f d = lookup4(c,a,b); // d = (2.0, 1.3, 1.2, 2.3)

Example of blending from more than two sources:

float sources[12] = { 1.0,1.1,1.2,1.3,2.0,2.1,2.2,2.3,3.0,3.1,3.2,3.3};

Vec4i i(11, 0, 5, 5);

Vec4f c = lookup<12>(i, sources); // c = (3.3,1.0,2.1,2.1)

A function with a limited number of possible input values can be replaced by a lookup table. This is useful if table lookup is faster than calculating the function. This example has a table of the function *y* = *x*2 - 1

// table of the function x\*x-1 int table[6] = {-1,0,3,8,15,24}; Vec4i x(4,2,0,5);

Vec4i y = lookup<6>(table); // y = (15, 3, -1, 24)

Example of gathering non-contiguous data from an array:

float x[16] = { ... };

Vec4i i(0,4,8,12);

Vec4f y = lookup<16>(i, x); // y = (x[0],x[4],x[8],x[12])

### Gather functions

|  |  |
| --- | --- |
| **function** | Vec4i gather4i<indexes>(void const \* table) Vec8i gather8i<indexes>(void const \* table) Vec16i gather16i<indexes>(void const \* table) Vec2q gather2q<indexes>(void const \* table) Vec4q gather4q<indexes>(void const \* table) Vec8q gather8q<indexes>(void const \* table) Vec4f gather4f<indexes>(void const \* table) Vec8f gather8f<indexes>(void const \* table) Vec16f gather16f<indexes>(void const \* table) Vec2d gather2d<indexes>(void const \* table) Vec4d gather4d<indexes>(void const \* table) Vec8d gather8d<indexes>(void const \* table) |
| **defined for** | Vec4i, Vec8i, Vec16i, Vec2q, Vec4q, Vec8q, Vec4f, Vec8f, Vec16f, Vec2d, Vec4d, Vec8d |
| **description** | Load non-contiguous data from table. Indexes cannot be negative. There is no option for zeroing or don't care. If you need variable indexes, use the lookup functions instead.  (If all indexes are smaller than the vector size, the function may read a full vector and permute it) |
| **efficiency** | medium |

Example:

int tab[8] = {10,11,12,13,14,15,16,17};

Vec4i a = gather4i<6,4,4,0>(tab);

// a = (16, 14, 14, 10);

### Scatter functions

|  |  |
| --- | --- |
| **function** | scatter<indexes>(Vec4i data, void \* array) scatter<indexes>(Vec8i data, void \* array) scatter<indexes>(Vec16i data, void \* array) scatter<indexes>(Vec2q data, void \* array) scatter<indexes>(Vec4q data, void \* array)  scatter<indexes>(Vec8q data, void \* array) scatter<indexes>(Vec4f data, float \* array) scatter<indexes>(Vec8f data, float \* array) scatter<indexes>(Vec16f data, float \* array) scatter<indexes>(Vec2d data, double \* array) scatter<indexes>(Vec4d data, double \* array) scatter<indexes>(Vec8d data, double \* array) |
| **defined for** | Vec4i, Vec8i, Vec16i, Vec2q, Vec4q, Vec8q, Vec4f, Vec8f, Vec16f, Vec2d, Vec4d, Vec8d |
| **description** | Store vector elements into non-contiguous positions in an array. Each vector element is stored in the array position indicated by the corresponding index. An element is not stored if the corresponding index is negative. |
| **efficiency** | Medium for 512 bit vectors if AVX512F instruction set supported.  Medium for 256 bit vectors if AVX512F, or better AVX512VL, supported.  Medium for 128 bit vectors if AVX512VL supported. Poor otherwise.  The scatter function is used for sparse arrays. For dense arrays, it may be more efficient to permute the vector and then store the whole vector into the array. |

Example:

Vec8i a(10,11,12,13,14,15,16,17);

int array[10] = {0};

scatter<5,4,3,2,-1,-1,7,0>(a, array);

// array = (17,0,13,12,11,10,0,16,0,0)

|  |  |
| --- | --- |
| **function** | scatter(Vec4i index, uint32\_t limit, Vec4i data, void \* array) scatter(Vec8i index, uint32\_t limit, Vec8i data, void \* array) scatter(Vec16i index, uint32\_t limit, Vec16i data, void \* array) scatter(Vec4i index, uint32\_t limit, Vec2q data, void \* array) scatter(Vec2q index, uint32\_t limit, Vec2q data, void \* array) scatter(Vec4i index, uint32\_t limit, Vec4q data, void \* array) scatter(Vec4q index, uint32\_t limit, Vec4q data, void \* array) scatter(Vec8i index, uint32\_t limit, Vec8q data, void \* array) scatter(Vec8q index, uint32\_t limit, Vec8q data, void \* array) scatter(Vec4i index, uint32\_t limit, Vec4f data, float \* array) scatter(Vec8i index, uint32\_t limit, Vec8f data, float \* array) scatter(Vec16i index, uint32\_t limit, Vec16f data, float \* array) scatter(Vec4i index, uint32\_t limit, Vec2d data, double \* array) scatter(Vec2q index, uint32\_t limit, Vec2d data, double \* array) scatter(Vec4i index, uint32\_t limit, Vec4d data, double \* array) scatter(Vec4q index, uint32\_t limit, Vec4d data, double \* array) scatter(Vec8i index, uint32\_t limit, Vec8d data, double \* array) scatter(Vec8q index, uint32\_t limit, Vec8d data, double \* array) |
| **defined for** | Vec4i, Vec8i, Vec16i, Vec2q, Vec4q, Vec8q, Vec4f, Vec8f, Vec16f, Vec2d, Vec4d, Vec8d |
| **description** | Store vector elements into non-contiguous positions in an array. Each vector element is stored in the array position indicated by the corresponding element of the index vector. An element is not stored if the corresponding index is negative or bigger than or equal to the limit. The limit will typically be the size of the array. |
| **efficiency** | Medium for 512 bit vectors if AVX512F instruction set supported.  Medium for 256 bit vectors if AVX512F, or better AVX512VL, supported.  Medium for 128 bit vectors if AVX512VL supported. Poor otherwise.  The scatter function is used for sparse arrays. For dense arrays, it may be more efficient to permute the vector and then store the whole vector into the array. |

Example:

Vec8i a(10,11,12,13,14,15,16,17);

Vec8i x(5,4,3,2,-1,99,7,0);

int array[10] = {0}; scatter(x, 5, a, array);

// array = (17,0,13,12,11,0,0,0,0,0)

## *Number - string conversion functions*

These functions require the header file "decimal.h" from the sub-archive named "special.zip".

### Binary to binary-coded-decimal (BCD) conversion

|  |  |
| --- | --- |
| **function** | vector bin2bcd(vector) |
| **defined for** | All unsigned integer vector types |
| **description** | Each vector element is converted to BCD code. The behavior in case of overflow is implementation dependent. |
| **efficiency** | medium. |

Example:

#include "decimal.h"

...

Vec4ui a(100,101,102,103);

Vec4ui b = bin2bcd(a); // b = (0x100, 0x101, 0x102, 0x103)

// (maximum value without overflow = 99999999)

### Binary to decimal ASCII string conversion

|  |  |  |
| --- | --- | --- |
| **function** | int bin2ascii (vector a, char \* string, int fieldlen, int numdat, bool signd, char ovfl, char separator, bool term) | |
| **defined for** | Vec16c, Vec32c, Vec8s, Vec16s, Vec4i, Vec8i | |
| **description** | Makes an ASCII string of numbers, where each vector element is converted to a human-readable decimal ASCII representation, right-justified in a field of specified length. | |
| **parameters** | a | Vector of signed or unsigned integers to convert |
| string | Character array that will receive the string. Must be big enough to contains the worst-case string length, including separators and terminating zero. |
| fieldlen | Desired length of each field in the output string. (default = 2, 4, or 8 depending on vector type) |
| numdat | Number of vector elements to convert. (default = number of elements in a) |
| signd | Each number will be interpreted as signed if signd = true, unsigned if false.  (default = true) |
| ovfl | Specifies how to handle cases where a number is too big to fit into a field of length fieldlen.  ovfl = 0: the size of the field will be made big enough to hold the number (max 11 characters). ovfl = ASCII character: the field will be filled with this character if the number is too big to fit into the field. (default = '\*') |
| separator | Specifies an ASCII character to insert between fields (but not after the last field).  0 for no separator. (default = ',') |
| term | Writes a zero-terminated ASCII string if term is true. The string has no terminator if term is false. (default = true) |
| return value | The returned value is the length of the string written. The terminating zero is not included in the count. |
| **efficiency** | poor, but better than alternatives. Improved by instruction sets SSSE3, SSE4.1, AVX2. | |

Example:

#include "decimal.h"

...

Vec4ui a(123, 123456, 0, -78);

char text[50];

bin2ascii(a, text, 5, 4, true, '\*', ',', true);

// text = " 123,\*\*\*\*\*, 0, -78"

### Binary to hexadecimal ASCII string conversion

|  |  |  |
| --- | --- | --- |
| **function** | int bin2hex\_ascii (vector a, char \* string, int numdat, char separator, bool term) | |
| **defined for** | All signed integer vector types | |
| **description** | Makes an ASCII string of hexadecimal numbers, where each vector element is converted to an unsigned hexadecimal ASCII representation in a field of 8, 4 or 2 characters, depending on the vector type. | |
| **parameters** | a | Vector of integers to convert |
| string | Character array that will receive the string. Must be big enough to contains the string length, including separators and terminating zero. |
| numdat | Number of vector elements to convert. (default = number of elements in a) |
| separator | Specifies an ASCII character to insert between fields (but not after the last field).  0 for no separator. (default = ',') |
| term | Writes a zero-terminated ASCII string if term is true. The string has no terminator if term is false. (default = true) |
| return value | The returned value is the length of the string written. The terminating zero is not included in the count. |
| **efficiency** | Medium. Improved by instruction sets SSSE3, AVX2. | |

Example:

#include "decimal.h"

...

Vec4ui a(256, 0x1234abcd, 0, -1); char text[50];

bin2hex\_ascii(a, text, 4, ',', true);

// text = "00000100,1234ABCD,00000000,FFFFFFFF"

### Decimal ASCII string to binary number conversion

|  |  |
| --- | --- |
| **function** | Vec4i ascii2bin(Vec32c string) |
| **defined for** | Vec32c |
| **description** | The input vector contains an ASCII string, organized as four fields of 8 characters each. Each field contains a decimal number. There are no separator or terminator characters. Each number must be right-justified in its field. Spaces and a minus sign are allowed to the left of each number. No other characters are allowed.  The function returns a vector of four signed integers. A syntax error is indicated by the value 0x80000000, which cannot occur otherwise. |
| **efficiency** | medium. |

Each field must be exactly 8 characters wide. The number must have one or more digits '0' - '9'. Spaces and one minus sign are allowed to the left of the number. Nothing is allowed to the right of the number. No other characters than digits, spaces and minus sign are allowed. The syntax of the input string can be defined with the following EBNF description:

<string> ::= <field> <field> <field> <field>

<field> ::= { <space> } [ <minus> ] { <space> } <digit> { <digit> }

<space> ::= ' '

<minus> ::= '-'

<digit> ::= '0' | '1' | '2' | '3' | '4' | '5' | '6' | '7' | '8' | '9'

A syntax error in a field will set the corresponding number to INT\_MIN = 0x80000000. This will not affect the other numbers. It is OK to input a string where only part of the string contains valid numbers and ignore the rest because there is no performance penalty for syntax errors.

The error-value 0x80000000 = -2147483648 cannot occur with a correct input because it requires more than eight digits to represent. The numbers cannot be bigger than 99999999 or smaller than -9999999 because they have to fit into eight characters.

The following example has a syntax error in the last field because there are spaces to the right of the number:

#include "decimal.h"

...

char str[] = " 123 -45678 - 0004 5 ";

Vec32c string = Vec32c().load(str); Vec4i a = ascii2bin(string);

// a = (123, -45678, -4, 0x80000000)

# Boolean operations and per-element branches

Consider this piece of C++ code:

int a[4], b[4], c[4], d[4];

...

for (int i = 0; i < 4; i++) {

d[i] = (a[i] > 0 && a[i] < 10) ? b[i] : c[i];

}

We can do this with vectors in the following way:

Vec4i a, b, c, d;

...

d = select(a > 0 & a < 10, b, c);

The select function is similar to the ? : operator. It has three vector parameters: the first parameter is a boolean vector that chooses between the elements of the second and third vector parameter. The relational operators >,

>=, <, <=, ==, != produce boolean vectors, which accept the boolean operations &, |, ^, ~ (and, or, exclusive or, not). In the above example, the expressions a > 0 and a < 10 are boolean vectors of type Vec4ib. The boolean vectors must have the same number of elements as the vectors they are used with. There is a table on page [9](#_bookmark13) showing which boolean vector class to use for each vector type.

The vector elements that are not selected are calculated anyway because normally all parts of a vector are calculated. For example:

Vec4f a(-1.0f, 0.0f, 1.0f, 2.0f);

Vec4f b = select(a >= 0.0f, sqrt(a), 0.0f);

Here, we will be calculating the squareroot of -1 even though we are not using it. This could possibly generate an exception if floating point exceptions are not masked. A better solution would therefore be:

Vec4f a(-1.0f, 0.0f, 1.0f, 2.0f);

Vec4f b = sqrt(max(a, 0.0f));

Likewise, the & and | operators are calculating both input operands, even if the second operand is not used. The following examples illustrates this:

// array version:

float a[4] = {0.0f, 1.0f, 2.0f, 3.0f}; float b[4];

for (int i = 0; i < 4; i++) {

if (a[i] > 0.0f && 1.0f/a[i] != 4.0f) b[i] = a[i];

else

b[i] = 1.0f;

}

and the vector version of the same:

// vector version:

Vec4f a(0.0f, 1.0f, 2.0f, 3.0f);

Vec4f b = select(a > 0.0f & 1.0f/a != 4.0f, a, 1.0f);

In the array version, we will never divide by zero because the && operator does not evaluate the second operand when the first operand is false. But in the vector version we are indeed dividing by zero because the & operator always evaluates both operands. The vector class library defines the operators && and || as synonyms to & and | for convenience, but they are still doing a bitwise AND or OR operation, so & and | are actually more representative of what these operators really do. This example should, of course, be changed to:

Vec4f a(0.0f, 1.0f, 2.0f, 3.0f);

Vec4f b = select(a > 0.0f & a != 0.25f, a, 1.0f);

## *Internal representation of boolean vectors*

The way boolean vectors are stored depends on the instruction set, and it may change in a future version of BIGMATH SIMD. For all data vectors of 128 bit and 256 bit size, the boolean vectors are stored as integer vectors with the same element size as the integer or floating point vectors they are used for. For example, the boolean vector class Vec4fb is stored as a vector of four 32-bit integers because it is used with vectors Vec4f of four single precision floating point numbers, using 32 bits each. The boolean vector class Vec4db is stored as a vector of four 64-bit integers because it is used with vectors Vec4d of four double precision floating point numbers, using 64 bits each. Note that the integer representation of true in a boolean vector element is not 1, but -1. The representation of false is 0. Any other values than 0 and -1 will most likely produce wrong and inconsistent results that depend on the instruction set.

The AVX512 instruction set allows boolean vectors to be stored internally as compact bitfields with a single bit for each vector element. This method is used in boolean vectors for use with 512 bit data vectors when compiling for AVX512 or higher instruction sets. The old method is used when compiling for AVX2 and lower instruction sets, even for 512 bit vectors. Future versions of BIGMATH SIMD may use the bitfield method for all vector sizes when compiling for the AVX512VL instruction set.

If you want your code to be compatible with multiple instruction sets, then you should make no assumption about how a boolean vector is stored. For example, the boolean vector Vec16ib uses 16 bits of storage when compiling for AVX512, but 512 bits of storage when compiling for AVX2.

Boolean vectors for use with floating point and integer vectors are in principle identical when they have the same number of bits per element. For example, the boolean vector types Vec8fb and Vec8ib are both vectors of 8 boolean elements, using 32 bits each. These types can easily be converted to each other, but it is still recommended to choose Vec8fb for use with Vec8f and Vec8ib for use with Vec8i because this helps the compiler select the fastest implementation in each case. See page [75](#_bookmark43) for conversion of boolean vectors.

## *Functions for use with booleans*

|  |  |
| --- | --- |
| **function** | vector select(boolean vector s, vector a, vector b) |
| **defined for** | all integer and floating point vector classes |
| **description** | branch per element. result[i] = s[i] ? a[i] : b[i] |
| **efficiency** | good |

Example:

Vec4i a(-1, 0, 1, 2);

Vec4i b = select(a>0, a+10, a-10); // b = (-11,-10,11,12)

|  |  |
| --- | --- |
| **function** | vector if\_add(boolean vector f, vector a, vector b) |
| **defined for** | all integer and floating point vector classes |
| **description** | conditional addition.  result[i] = f[i] ? a[i] + b[i] : a[i] |
| **efficiency** | good |

Example:

Vec4i a(-1, 0, 1, 2);

Vec4i b = if\_add(a < 0, a, 100); // b = (99,0,1,2)

|  |  |
| --- | --- |
| **function** | vector if\_mul(boolean vector f, vector a, vector b) |
| **defined for** | all floating point vector classes |
| **description** | conditional multiplication. result[i] = f[i] ? a[i] \* b[i] : a[i] |
| **efficiency** | good |

|  |  |
| --- | --- |
| **function** | vector andnot(vector, vector) |
| **defined for** | all boolean vector classes |
| **description** | andnot(a,b) = a & ~ b |
| **efficiency** | good (better than a & ~ b) |

|  |  |
| --- | --- |
| **function** | bool horizontal\_and(boolean vector) |
| **defined for** | all boolean vector classes |
| **description** | The output is the AND combination of all elements |
| **efficiency** | medium. Better if SSE4.1 enabled |

Example:

Vec4i a(-1, 0, 1, 2);

bool b = horizontal\_and(a > 0); // b = false

|  |  |
| --- | --- |
| **function** | bool horizontal\_or(boolean vector) |
| **defined for** | all boolean vector classes |
| **description** | The output is the OR combination of all elements |
| **efficiency** | medium. Better if SSE4.1 enabled |

Example:

Vec4i a(-1, 0, 1, 2);

bool b = horizontal\_or(a > 0); // b = true

|  |  |
| --- | --- |
| **function** | int horizontal\_find\_first(boolean vector) |
| **defined for** | all boolean vector classes, except Vec128b, Vec256b, Vec512b |
| **description** | Returns an index to the first element that is true. Returns -1 if all elements are false |
| **efficiency** | medium |

Example:

Vec4i a(1, 2, 3, 4);

Vec4i b(0, 2, 3, 0);

Vec4ib c = a == b;

int d = horizontal\_find\_first(c); // d = 1

|  |  |
| --- | --- |
| **function** | unsigned int horizontal\_count(boolean vector) |
| **defined for** | all boolean vector classes, except Vec128b, Vec256b, Vec512b |
| **description** | counts the number of elements that are true |
| **efficiency** | medium if SSE4.2 enabled |

Example:

Vec4i a(1, 2, 3, 4);

Vec4i b(0, 2, 3, 0);

Vec4ib c = a == b;

int d = horizontal\_count(c); // d = 2

# Conversion between vector types

Below is a list of methods and functions for conversion between different vector types, vector sizes or precisions.

|  |  |
| --- | --- |
| **method** | conversion between vector class and intrinsic vector type |
| **defined for** | all vector classes |
| **description** | conversion between a vector class and the corresponding intrinsic vector type m128, m128d, m128i, m256,  m256d, m256i, m512, m512d, m512i can be done implicitly or explicitly.  Boolean vectors can be converted to their internal representation, which is either an integer vector or a single integer, depending on the size and instruction set. |
| **efficiency** | good |

Example:

Vec4i a(0,1,2,3);

m128i b = a; // b = 0x00000003000000020000000100000000

Vec4i c = b; // c = (0,1,2,3)

|  |  |
| --- | --- |
| **method** | conversion from scalar to vector |
| **defined for** | all integer and floating point vector classes |
| **description** | conversion from a scalar (single value) to a vector can be done explicitly by calling a constructor, or implicitly by putting a scalar where a vector is expected. All vector elements get the same value. |
| **efficiency** | good for constant. Medium for variable as parameter |

Example:

Vec4i a, b;

a = Vec4i(5); // explicit conversion. a = (5,5,5,5) b = a + 3; // implicit conversion to Vec4i.

// b = (8,8,8,8)

Implicit conversion is convenient in the example b = a + 3, which adds 3 to all elements of the vector. Use explicit conversion where there is ambiguity about the desired vector type.

|  |  |
| --- | --- |
| **method** | conversion between signed and unsigned integer vectors |
| **defined for** | all integer vector classes |
| **description** | signed ↔ unsigned conversion can be done implicitly or explicitly. Overflow and underflow wraps around |
| **efficiency** | good |

Example:

Vec4i a(-1,0,1,2); // signed vector

Vec4ui b = a; // implicit conversion to unsigned.

// b = (0xFFFFFFFF,0,1,2)

Vec4ui c = Vec4ui(a); // same, with explicit conversion Vec4i d = c; // convert back to signed

|  |  |
| --- | --- |
| **method** | conversion between different integer vector types |
| **defined for** | all integer vector classes |
| **description** | conversion can be done implicitly or explicitly between all integer vector classes with the same total number of bits. This conversion does not change any bits, just the grouping of bits into elements is changed |
| **efficiency** | good |

Example:

Vec8s a(0,1,2,3,4,5,6,7);

Vec4i b = Vec4i(a); // b = (0x1000, 0x3002, 0x5004, 0x7006)

|  |  |
| --- | --- |
| **method** | reinterpret\_d, reinterpret\_f, reinterpret\_i |
| **defined for** | all integer and floating point vector classes |
| **description** | reinterprets a vector as a different type without changing any bits (bit casting).  reinterpret\_d is used for converting to Vec2d or Vec4d, reinterpret\_f is used for converting to Vec4f or Vec8f, reinterpret\_i is used for converting to any integer vector type |
| **efficiency** | good |

Example

Vec4f a(1.0f, 1.5f, 2.0f, 2.5f);

Vec4i b = reinterpret\_i(a);

// b = (0x3F800000, 0x3FC00000, 0x40000000, 0x40200000)

|  |  |
| --- | --- |
| **method** | Vec4i round\_to\_int(Vec4f) Vec4i round\_to\_int(Vec2d)  Vec4i round\_to\_int(Vec2d, Vec2d) Vec8i round\_to\_int(Vec8f)  Vec16i round\_to\_int(Vec16f) Vec4i round\_to\_int(Vec4d) Vec8i round\_to\_int(Vec8d) |
| **defined for** | all floating point vector classes |
| **description** | rounds floating point numbers to nearest integer and returns integer vector. (where two integers are equally near, the even integer is returned) |
| **efficiency** | medium |

Example:

Vec4f a(1.0f, 1.5f, 2.0f, 2.5f);

Vec4i b = round\_to\_int(a); // b = (1,2,2,2)

|  |  |
| --- | --- |
| **method** | Vec2q round\_to\_int64(Vec2d x) Vec4q round\_to\_int64(Vec4d x) Vec8q round\_to\_int64(Vec8d x)  Vec2q round\_to\_int64\_limited(Vec2d x) Deprecated! Vec4q round\_to\_int64\_limited(Vec4d x) Deprecated! Vec8q round\_to\_int64\_limited(Vec8d x) Deprecated! |
| **defined for** | Vec2d, Vec4d, Vec8d |
| **description** | rounds floating point numbers to nearest integer and returns integer vector. (where two integers are equally near, the even integer is returned).  The \_limited versions are limited to abs(x) < 231. Outside of this range, the result is implementation dependent. |
| **efficiency** | good if AVX512DQ instruction set, otherwise: round\_to\_int64: poor round\_to\_int64\_limited: medium |

Example:

Vec4d a(1.0, 1.5, 2.0, 2.5);

Vec4q b = round\_to\_int64(a); // b = (1,2,2,2)

|  |  |
| --- | --- |
| **method** | Vec4i truncate\_to\_int(Vec4f)  Vec4i truncate\_to\_int(Vec2d, Vec2d) Vec8i truncate\_to\_int(Vec8f)  Vec16i truncate\_to\_int(Vec16f) Vec4i truncate\_to\_int(Vec4d) Vec8i truncate\_to\_int(Vec8d) |
| **defined for** | all floating point vector classes |
| **description** | truncates floating point numbers towards zero and returns signed integer vector. |
| **efficiency** | medium |

Example:

Vec4f a(1.0f, 1.5f, 2.0f, 2.5f);

Vec4i b = truncate\_to\_int(a); // b = (1,1,2,2)

|  |  |
| --- | --- |
| **method** | Vec2q truncate\_to\_int64(Vec2d x) Vec4q truncate\_to\_int64(Vec4d x) Vec8q truncate\_to\_int64(Vec8d x)  Vec2q truncate\_to\_int64\_limited(Vec2d x) Deprecated! Vec4q truncate\_to\_int64\_limited(Vec4d x) Deprecated! Vec8q truncate\_to\_int64\_limited(Vec8d x) Deprecated! |
| **defined for** | Vec2d, Vec4d, Vec8d |
| **description** | truncates floating point numbers towards zero and returns signed integer vector.  The \_limited versions are limited to abs(x) < 231. Outside of this range, the result is implementation dependent. |
| **efficiency** | good if AVX512DQ instruction set, otherwise: truncate\_to\_int64: poor truncate\_to\_int64\_limited: medium |

Example:

Vec4d a(1.0, 1.5, 2.0, 2.5);

Vec4q b = truncate\_to\_int64(a); // b = (1,2,2,2)

|  |  |
| --- | --- |
| **method** | Vec4f to\_float(Vec4i) Vec8f to\_float(Vec8i) Vec16f to\_float(Vec16i) |
| **defined for** | Vec4i, Vec8i, Vec16i |
| **description** | converts signed integers to single precision float |
| **efficiency** | good |

Example:

Vec4i a(0, 1, 2, 3);

Vec4f b = to\_float(a); // b = (0.0f, 1.0f, 2.0f, 3.0f)

|  |  |
| --- | --- |
| **method** | Vec4f to\_float(Vec4ui) Vec8f to\_float(Vec8ui) Vec16f to\_float(Vec16ui) |
| **defined for** | Vec4ui, Vec8ui, Vec16ui |
| **description** | converts unsigned integers to single precision float |
| **efficiency** | good if AVX512VL instruction set. Poor otherwise |

|  |  |
| --- | --- |
| **method** | Vec4d to\_double(Vec4i) Vec8d to\_double(Vec8i) |
| **defined for** | Vec4i, Vec8i |
| **description** | converts signed 32-bit integers to double precision float |
| **efficiency** | medium |

Example:

Vec4i a(0, 1, 2, 3);

Vec4d b = to\_double(a); // b = (0.0, 1.0, 2.0, 3.0)

|  |  |
| --- | --- |
| **method** | Vec2d to\_double(Vec2q x) Vec4d to\_double(Vec4q x) Vec8d to\_double(Vec8q x)  Vec2d to\_double\_limited(Vec2q x) Deprecated! Vec4d to\_double\_limited(Vec4q x) Deprecated! Vec8d to\_double\_limited(Vec8q x) Deprecated! |
| **defined for** | Vec2q, Vec4q, Vec8q |
| **description** | converts signed 64-bit integers to double precision float. The \_limited versions are limited to abs(x) < 231. Outside of this range, the result is implementation dependent. |
| **efficiency** | to\_double: good if AVX512DQ and AVX512VL instruction sets, otherwise poor.  to\_double\_limited: medium |

Example:

Vec2q a(0, 1);

Vec2d b = to\_double(a); // b = (0.0, 1.0)

|  |  |
| --- | --- |
| **method** | Vec2d to\_double\_low(Vec4i) Vec2d to\_double\_high(Vec4i) |
| **defined for** | Vec4i |
| **description** | converts signed 32-bit integers to double precision float |
| **efficiency** | medium |

Example:

Vec4i a(0, 1, 2, 3);

Vec2d b = to\_double\_low(a); // b = (0.0, 1.0) Vec2d c = to\_double\_high(a); // c = (2.0, 3.0)

|  |  |
| --- | --- |
| **method** | concatenating vectors |
| **defined for** | all 128-bit and 256-bit vector classes and corresponding boolean vector classes |
| **description** | two 128-bit vectors can be concatenated into one 256-bit vector of the corresponding type by calling a constructor. two 256-bit vectors can be concatenated into one 512-bit vector of the corresponding type by calling a constructor. |
| **efficiency** | good |

Example:

Vec4i a(10,11,12,13); Vec4i b(20,21,22,23);

Vec8i c(a, b); // c = (10,11,12,13,20,21,22,23)

|  |  |
| --- | --- |
| **method** | get\_low, get\_high |
| **defined for** | all 256-bit and 512-bit vector classes |
| **description** | one big vector can be split into two vectors of half the size by calling the methods get\_low and get\_high |
| **efficiency** | good |

Example:

Vec8i a(10,11,12,13,14,15,16,17);

Vec4i b = a.get\_low(); // b = (10,11,12,13) Vec4i c = a.get\_high(); // c = (14,15,16,17)

|  |  |
| --- | --- |
| **method** | extend\_low, extend\_high |
| **defined for** | Vec16c, Vec16uc, Vec8s, Vec8us, Vec4i, Vec4ui,  Vec32c, Vec32uc, Vec16s, Vec16us, Vec8i, Vec8ui, Vec16i, Vec16ui |
| **description** | extends integers to a larger number of bits per element. Unsigned integers are zero-extended, signed integers are sign-extended. |
| **efficiency** | good |

Example:

Vec8s a(-2, -1, 0, 1, 2, 3, 4, 5);

Vec4i b = extend\_low(a); // b = (-2, -1, 0, 1)

Vec4i c = extend\_high(a); // c = (2, 3, 4, 5)

|  |  |
| --- | --- |
| **method** | extend\_low, extend\_high |
| **defined for** | Vec4f, Vec8f, Vec16f |
| **description** | extends single precision floating point numbers to double precision |
| **efficiency** | good |

Example:

Vec4f a(1.0f, 1.1f, 1.2f, 1.3f);

Vec2d b = extend\_low(a); // b = (1.0, 1.1) Vec2d c = extend\_high(a); // c = (1.2, 1.3)

|  |  |
| --- | --- |
| **method** | compress |
| **defined for** | Vec8s, Vec8us, Vec4i, Vec4ui, Vec2q, Vec2uq  Vec16s, Vec16us, Vec8i, Vec8ui, Vec4q, Vec4uq, Vec16i, Vec16ui, Vec8q, Vec8uq |
| **description** | reduces integers to a lower number of bits per element. Overflow and underflow wraps around |
| **efficiency** | medium |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(20, 21, 22, 23);

Vec8s c = compress(a, b); // c = (10,11,12,13,20,21,22,23)

|  |  |
| --- | --- |
| **method** | compress |
| **defined for** | Vec2d, Vec4d, Vec8d |
| **description** | reduces double precision floating point numbers to single precision |
| **efficiency** | medium |

Example:

Vec2d a(1.0, 1.1);

Vec2d b(2.0, 2.1);

Vec4f c = compress(a, b); // c = (1.0f, 1.1f, 2.0f, 2.1f)

|  |  |
| --- | --- |
| **method** | compress\_saturated |
| **defined for** | Vec8s, Vec8us, Vec4i, Vec4ui, Vec2q, Vec2uq  Vec16s, Vec16us, Vec8i, Vec8ui, Vec4q, Vec4uq, Vec16i, Vec16ui, Vec8q, Vec8uq |
| **description** | reduces integers to a lower number of bits per element. Overflow and underflow saturates |
| **efficiency** | medium (worse than compress in most cases) |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(20, 21, 22, 23);

Vec8s c = compress\_saturated(a, b);

// c = (10,11,12,13,20,21,22,23)

## *Conversion between boolean vector types*

|  |  |
| --- | --- |
| **method** | to\_bits |
| **defined for** | all boolean vectors, except Vec128b, Vec256b, Vec512b |
| **description** | converts a boolean vector to an integer with one bit per element. |
| **efficiency** | good for Vec8qb, Vec16ib, Vec8db, Vec16fb when AVX512 used. Medium otherwise |

Example:

Vec4i a(10, 11, 12, 13);

Vec4i b(12, 11, 10, 9);

Vec4ib f = a > b; // (false, false, true, true) uint8\_t g = to\_bits(f); // = 0x0C (1100 binary)

(The order is not reversed, but in the comments above, the vector elements are listed in little endian order, while the binary number is written in big endian order)

|  |  |
| --- | --- |
| **method** | to\_Vec4ib, to\_Vec8ib, to\_Vec16ib, to\_Vec2qb, to\_Vec4qb, to\_Vec8qb, to\_Vec4fb, to\_Vec8fb, to\_Vec16fb, to\_Vec2db, to\_Vec4db, to\_Vec8db |
| **defined for** | all boolean vectors for 32-bit and 64-bit integers, float and double |
| **description** | converts an integer bit-field to a boolean vector |
| **efficiency** | good for Vec8qb, Vec16ib, Vec8db, Vec16fb when AVX512 used. Medium or poor otherwise |

Example:

uint8\_t a = 0xC2; // 11000010 binary Vec8qb b = to\_vec8qb(a);

// = false, true, false, false, false, false, true, true

(The order is not reversed, but in the comments above, the vector elements are listed in little endian order, while the binary number is written in big endian order)

|  |  |
| --- | --- |
| **method** | conversion between boolean vectors of same size and element size |
| **defined for** | Vec4ib ↔ Vec4fb Vec8ib ↔ Vec8fb Vec16ib ↔ Vec16fb Vec2qb ↔ Vec2db Vec4qb ↔ Vec4db Vec8qb ↔ Vec8db |
| **description** | Boolean vectors for use with different types of vectors with the same bit size can be converted to each other. |
| **efficiency** | good |

Example:

Vec4i a(0,1,2,3);

Vec4i b(4,3,2,1);

Vec4ib f = a > b; // f = (false,false,false,true) Vec4fb g = Vec4fb(f); // g = (false,false,false,true)

|  |  |
| --- | --- |
| **method** | conversion from boolean vectors to integer vectors of the same size and element size |
| **defined for** | Vec16cb → Vec16c Vec32cb → Vec32c Vec8sb → Vec8s Vec16sb → Vec16s Vec4ib, Vec4fb → Vec4i Vec8ib, Vec8fb → Vec8i Vec2qb, Vec2db → Vec2q Vec4qb, Vec4db → Vec4q  Not defined for vectors bigger than 256 bits. |
| **description** | Boolean vectors can be converted to integer vectors of the same size and bit size. The result will be -1 for true and 0 for false. |
| **efficiency** | good |

Example:

Vec4i a(0,1,2,3);

Vec4i b(4,3,2,1);

Vec4ib f = a > b; // f = (false,false,false,true) Vec4i g = Vec4i(f); // g = (0, 0, 0, -1)

Conversion the other way, e.g. from Vec4i to Vec4ib is possible for vector types smaller than 512 bits if the input vector contains -1 for true and 0 for false, but the result is implementation dependent and possibly wrong and inconsistent if the input vector contains any other values than 0 and -1. To prevent errors, it is recommended to use a comparison instead for converting an integer vector to a boolean vector. For example:

Vec4i a(-1,0,1,2);

Vec4ib f = (a != 0); // f = (true,false,true,true)

# Random number generator

The files ranvec1.h and ranvec1.cpp define a high quality pseudo-random number generator with vector output. These files are contained in the sub-archive named "special.zip". This generator is useful for producing random numbers for simulation and other Monte Carlo applications. Add the file ranvec1.cpp to your project and compile for the appropriate instruction set. This example shows a simple use of the random number generator:

// Example for random number generator

// Remember to link ranvec1.cpp into the project #include <stdio.h>

#include "vectorsimd.h" #include "ranvec1.h"

int main() {

// Arbitrary seed int seed = 1;

// Create an instance of Ranvec1 class with type 3 Ranvec1 ran(3);

// Initialize with seed ran.init(seed);

// Generate a vector of 8 random integers below 100 Vec8i ri = ran.random8i(0,99);

// Generate a vector of 8 random floats Vec8f rf = ran.random8f();

int i;

// Output the 8 random integers

printf("\nRandom integers in interval 0 - 99\n"); for (i=0; i<ri.size(); i++) printf("%3i ", ri[i]);

// Output the 8 random floats

printf("\nRandom floats in interval 0 - 1\n");

for (i=0; i<rf.size(); i++) printf("%7.4f ", rf[i]); printf("\n");

return 0;

}

The optional parameter for the constructor of the class Ranvec1 defines the type of random number generator to use:

|  |  |
| --- | --- |
| Parameter for constructor | Generator type |
| 1 | MWC. Multiply-With-Carry Generator. Use this for small applications where speed is important. (cycle length > 4∙1019) |
| 2 | MTGP. A variant of Mersenne Twister. Use this for applications with multiple threads.  (cycle length > 103375) |
| 3 | MWC + MTGP combined. Use this for the best possible randomness and for large applications with many threads.  (cycle length > 103395) |

It is necessary to initialize the random number generator with a seed, using either the function init or initByArray. The generator will produce only zeroes if it has not been initialized with any of the init functions.

The random number sequence depends on the seed. A different seed will produce a different sequence of random numbers. You can reproduce a random number sequence exactly after initializing again with the same seed. You may use simple values like 1, 2, 3,... for seeds in a series of simulations if you want to be able to reproduce the results later. If you want a non-reproducible sequence then you need a seed from some source of genuine randomness. The function PhysicalSeed in the [asmlib](http://www.agner.org/optimize/#asmlib) library is useful for this purpose.

If the application has multiple threads then it is necessary to make a separate instance of the class Ranvec1 for each thread that uses random numbers. It is not safe to access the same Ranvec1 object from more than one thread. The separate objects must have different seeds. Applications with many threads or many random number streams may specify generator type 3 for the constructor and use the init function with two seeds, one for the MWC generator and one for the MTGP generator. At least the second seed must be different for each instance. A theoretical discussion of this is given in the theory article cited below.

The generator can produce vector outputs with different vector sizes. The best performance is obtained when the vector size fits the instruction set: SSE2 or higher for 128 bit vectors. AVX2 or higher for 256 bit vectors. AVX512 or higher for 512 bit vectors. The define MAX\_VECTOR\_SIZE determines whether the higher vector sizes are available. Depending on details of the application, it may or may not be possible to reproduce a simulation result exactly when the vector size is changed.

The theory of the Ranvec1 package including the different generators, multiprocessing and vector processing is described in the article:

Fog, Agner: “Pseudo-Random Number Generators for Vector Processors and Multicore Processors.” *Journal of Modern Applied Statistical Methods* vol. 14, no. 1, 2015, article 23. <http://digitalcommons.wayne.edu/jmasm/vol14/iss1/23/>

Member functions for class Ranvec1:

|  |  |
| --- | --- |
| **constructor** | Ranvec1(int gtype) |
| **description** | Constructor for Ranvec1 class. See the table above for values of the generator type gtype. |
| **efficiency** | medium |

|  |  |
| --- | --- |
| **method** | void init(int seed) |
| **description** | Initialization with one seed. Any value is allowed for seed. Use a different value of seed each time to get a different random number sequence. |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **method** | void init(int seed1, int seed2) |
| **description** | Initialization with two seeds. The random number sequence depends on both seeds. If the generator type is 3 then seed1 is used for the MWC generator and seed2 is used for the MTGP generator. The value of seed2 should be different for each thread in multithreaded applications. |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **method** | void initByArray(int const seeds[], int numSeeds) |
| **description** | Initialization with multiple seeds. The seeds array must contain numSeed integers. The random number sequence depends on all these integer seeds. This can be useful for security applications in order to make it difficult to guess the seeds. The best security is obtained with generator type 3. The generators are not guaranteed to be cryptographically safe. |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **method** | uint32\_t random32b() uint64\_t random64b() |
| **description** | Returns an integer of 32 or 64 random bits |
| **efficiency** | medium |

|  |  |
| --- | --- |
| **method** | Vec4ui random128b() Vec8ui random256b() Vec16ui random512b() |
| **description** | Returns an integer vector of 128, 256 or 512 random bits (MAX\_VECTOR\_SIZE determines which of these functions are available) |
| **efficiency** | medium |

|  |  |
| --- | --- |
| **method** | int random1i(int min, int max) Vec4i random4i(int min, int max) Vec8i random8i(int min, int max) Vec16i random16i(int min, int max) |
| **description** | Returns a random integer or a vector of random integers with uniform distribution in the interval min ≤ x ≤ max. (The distribution may be slightly inaccurate when the interval size is large and not a power of 2. See below for a more accurate version. MAX\_VECTOR\_SIZE determines which of these functions are available) |
| **efficiency** | medium |

|  |  |
| --- | --- |
| **method** | int random1ix(int min, int max) Vec4i random4ix(int min, int max) Vec8i random8ix(int min, int max) Vec16i random16ix(int min, int max) |
| **description** | Same as above, but accurate.  (The accurate version of these functions use a rejection method as described in the theory article mentioned above. To reproduce a sequence, the same function with the same vector size must be called. MAX\_VECTOR\_SIZE determines which of these functions are available) |
| **efficiency** | somewhat slower than the above |

|  |  |
| --- | --- |
| **method** | float random1f() Vec4f random4f() Vec8f random8f() Vec16f random16f() |
| **description** | Returns a random floating point number or a vector of random floating point numbers with uniform distribution in the interval 0 ≤ x < 1. The resolution is 2-24.  (A value in the interval 0 < x ≤ 1 can be obtained as 1 - x. MAX\_VECTOR\_SIZE determines which of these functions are available) |
| **efficiency** | medium |

|  |  |
| --- | --- |
| **method** | double random1d() Vec2d random2d() Vec4d random4d() Vec8d random8d() |
| **description** | Returns a random double precision number or a vector of random double precision numbers with uniform distribution in the interval 0 ≤ x < 1. The resolution is 2-52.  (A value in the interval 0 < x ≤ 1 can be obtained as 1 - x. MAX\_VECTOR\_SIZE determines which of these functions are available) |
| **efficiency** | medium |

# Special applications

## 3-dimensional vectors

The header file "vector3d.h" in the sub-archive named "special.zip" defines 3- dimensional vectors for use in geometry and physics.

Vector classes defined in vector3d.h:

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| **vector class** | **precision** | **elements per vector** | **total bits** | **recommended instruction set** |
| Vec3f | single | 3 | 128 | SSE3 |
| Vec3d | double | 3 | 256 | AVX |

These vector classes are actually using vector registers that can hold 4 floats or 4 doubles, respectively. The last element in the vector register is not used.

Most operators and functions are similar to those of Vec4f and Vec4d. A constructor with the three coordinates is defined:

|  |  |
| --- | --- |
| **method** | constructor with 3 elements as parameter |
| **defined for** | Vec3f, Vec3d |
| **description** | contents is initialized with x, y, z coordinates |

Note that some operators and functions inherited from Vec4f and Vec4d make little or no sense. For example, the > operator will make a not very useful element-by-element comparison rather than comparing vector lengths:

Vec3f a(10,11,12); Vec3f b(12,11,10);

Vec4fb c = a > b; // c = (false,false,true,false)

bool d = vector\_length(a) > vector\_length(b); // d = false

Member functions:

|  |  |
| --- | --- |
| **member function** | get\_x(), get\_y(), get\_z() |
| **defined for** | Vec3f, Vec3d |
| **description** | extract a single coordinate |

|  |  |
| --- | --- |
| **member function** | extract(index) |
| **defined for** | Vec3f, Vec3d |
| **description** | extracts coordinate x, y or z for index = 0, 1 or 2, respectively |

Arithmetic operators:

|  |  |
| --- | --- |
| **operators** | +, -, \*, / |
| **defined for** | Vec3f, Vec3d |
| **description** | element-by-element operation |

Comparison operators:

|  |  |
| --- | --- |
| **operators** | ==, != |
| **defined for** | Vec3f, Vec3d |
| **description** | returns a boolean telling if vectors are equal or not equal. The unused fourth element is ignored. |

There are several different ways to multiply 3-dimensional vectors:

|  |  |
| --- | --- |
| **operator** | vector \* vector |
| **defined for** | Vec3f, Vec3d |
| **description** | element-by-element multiplication |

|  |  |
| --- | --- |
| **operator** | vector \* scalar, scalar \* vector |
| **defined for** | Vec3f, Vec3d |
| **description** | all elements are multiplied by the scalar |

|  |  |
| --- | --- |
| **function** | dot\_product(vector, vector) |
| **defined for** | Vec3f, Vec3d |
| **description** | returns the dot-product as a scalar |

|  |  |
| --- | --- |
| **function** | cross\_product(vector, vector) |
| **defined for** | Vec3f, Vec3d |
| **description** | returns the cross-product as a vector perpendicular to the two input vectors |

Other functions:

|  |  |
| --- | --- |
| **function** | vector\_length(vector) |
| **defined for** | Vec3f, Vec3d |
| **description** | returns the length as a scalar |

|  |  |
| --- | --- |
| **function** | normalize\_vector(vector) |
| **defined for** | Vec3f, Vec3d |
| **description** | returns a vector with unit length and same direction as the input vector |

|  |  |
| --- | --- |
| **function** | rotate(vector c0, vector c1, vector c2, vector a) |
| **defined for** | Vec3f, Vec3d |
| **description** | rotates vector a by multiplying with the matrix defined by the columns (c0,c1,c2). (If the rotation matrix is defined by rows then it must first be transposed to get the column vectors, see page [111](#_bookmark67) for an example). |

Example:

Vec3f a(11,22,33);

Vec3f c0(0,1,0), c1(0,0,1), c2(1,0,0);

Vec3f b = rotate(c0, c1, c2, a); // b = (22,33,11)

|  |  |
| --- | --- |
| **function** | to\_single |
| **defined for** | Vec3d |
| **description** | converts to Vec3f |

|  |  |
| --- | --- |
| **function** | to\_double |
| **defined for** | Vec3f |
| **description** | converts to Vec3d |

## *Complex number vectors*

The header file "complexvec.h" in the sub-archive named "special.zip" defines classes for complex numbers and complex vectors for use in mathematics and electronics.

Classes defined in complexvec.h:

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| **vector class** | **precision** | **complex numbers per vector** | **total bits** | **recommended instruction set** |
| Complex2f | single | 1 | 128 | SSE2 |
| Complex4f | single | 2 | 128 | SSE2 |
| Complex8f | single | 4 | 256 | AVX |
| Complex2d | double | 1 | 128 | SSE2 |
| Complex4d | double | 2 | 256 | AVX |

The class Complex2f uses the lower half of a 128-bit register, while the upper half of the register is unused. The other complex classes use a full 128-bit or 256-bit register.

The minimum instruction set is SSE2. The performance of multiplication is improved by compiling for the SSE3 instruction set. The performance of multiplication and division is improved by compiling for the FMA3 or FMA4 instruction set.

Constructors:

|  |  |
| --- | --- |
| **method** | default constructor |
| **defined for** | all complex classes |
| **description** | contents is not initialized |

|  |  |
| --- | --- |
| **method** | constructor with real and imaginary parts |
| **defined for** | all complex classes |
| **description** | all elements are initialized with real and imaginary parts |

Example:

Complex4f a(1.0f, 2.0f, 3.0f, 4.0f);

// a = (1+2i, 3+4i)

|  |  |
| --- | --- |
| **method** | constructor with one real and one imaginary part |
| **defined for** | all complex classes |
| **description** | all elements are initialized with the same (real,imaginary) pair |

|  |  |
| --- | --- |
| **method** | constructor with one real part only |
| **defined for** | all complex classes |
| **description** | all elements are initialized with the same real number. The imaginary parts are set to zero |

|  |  |
| --- | --- |
| **method** | constructor with one Complex2f or Complex2d |
| **defined for** | Complex4f, Complex8f, Complex4d |
| **description** | all elements are initialized with the same (real,imaginary) pair |

|  |  |
| --- | --- |
| **method** | constructor with two Complex4f or four Complex2f |
| **defined for** | Complex8f |
| **description** | vectors are concatenated |

Member functions:

|  |  |
| --- | --- |
| **method** | load |
| **defined for** | all complex classes |
| **description** | all elements are initialized from a float or double array containing alternating real and imaginary parts |

Example:

double x[4] = {1.0, 2.0, 3.0, 4.0};

Vec4d a;

a.load(x); // a = (1+2i, 3+4i)

|  |  |
| --- | --- |
| **method** | get\_low, get\_high |
| **defined for** | Complex4f, Complex8f, Complex4d |
| **description** | get lower or upper half or the vector as a Complex2f, Complex4f, Complex2d, respectively |

|  |  |
| --- | --- |
| **method** | extract(index) |
| **defined for** | all complex classes |
| **description** | extract a single real or imaginary part. index = 0 gives real part of first element, index = 1 gives imaginary part of first element, etc. |

Operators:

|  |  |
| --- | --- |
| **operators** | +, +=, -, -=, unary minus, \*, \*=, /, /= |
| **defined for** | all complex classes |
| **description** | arithmetic functions between two complex numbers:  (a+i\*b) + (c+i\*d) = ((a+c) + i\*(b+d))  (a+i\*b) - (c+i\*d) = ((a-c) + i\*(b-d))  (a+i\*b) \* (c+i\*d) = ((a\*c-b\*d) + i\*(a\*d+b\*c)) (a+i\*b) / (c+i\*d) = ((a\*c+b\*d)+i\*(b\*c-a\*d))/(c2+d2) |

Operators combining complex and real

|  |  |
| --- | --- |
| **operators** | +, +=, -, -=, \*, \*=, /, /= |
| **defined for** | all complex classes |
| **description** | arithmetic functions between a complex number and a real:  (a+ib) + c = ((a+c) + i\*b) (a+ib) - c = ((a-c) + i\*b)  (a+ib) \* c = ((a\*c) + i\*(b\*c))  (a+ib) / c = ((a/c) + i\*(b/c))  c / (a+ib) = ((a\*c) - i\*(b\*c))/(a2+b2) |

Complex conjugate:

|  |  |
| --- | --- |
| **operators** | ~ |
| **defined for** | all complex classes |
| **description** | complex conjugate of all vector elements:  ~(a+i\*b) = (a-i\*b) |

Comparison operators:

|  |  |
| --- | --- |
| **operators** | ==, != |
| **defined for** | all complex classes |
| **description** | returns a boolean for Complex2f and Complex2d. returns a boolean vector for Complex4f, Complex8f,  Complex4d. The output can be used in the select function |

Functions:

|  |  |
| --- | --- |
| **function** | abs |
| **defined for** | all complex classes |
| **description** | abs(a+i\*b) = sqrt(a\*a+b\*b) |

|  |  |
| --- | --- |
| **function** | sqrt |
| **defined for** | all complex classes |
| **description** | square root of complex number |

|  |  |
| --- | --- |
| **function** | select |
| **defined for** | all complex classes |
| **description** | selects between the elements of two vectors |

Example:

Complex4f a(1,2,3,4); Complex4f b(1,2,5,6);

Complex4f c = select(a == b, Complex4f(0), b);

// c = (0+i\*0, 5+i\*6)

|  |  |
| --- | --- |
| **function** | to\_single |
| **defined for** | Complex2d, Complex4d |
| **description** | converts to Complex2f, Complex4f |

|  |  |
| --- | --- |
| **function** | to\_double |
| **defined for** | Complex2f, Complex4f |
| **description** | converts to Complex2d, Complex4d |

|  |  |
| --- | --- |
| **function** | cexp |
| **defined for** | all complex classes |
| **description** | complex exponential function:  cexp(a+i\*b) = exp(a)\*(cos(b)+i\*sin(b))  For best performance, include vectormath.h before complexvec.h and use Intel SVML library as explained on pag[e 40](#_bookmark31). |

## *Quaternions*

The header file "quaternion.h" in the sub-archive named "special.zip" defines classes for quaternions (hypercomplex numbers) for use in mathematics and geometry.

Classes defined in quaternion.h:

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| **vector class** | **precision** | **quaternions per vector** | **total bits** | **recommended instruction set** |
| Quaternion4f | single | 1 | 128 | SSE2 |
| Quaternion4d | double | 1 | 256 | AVX |

Constructors:

|  |  |
| --- | --- |
| **method** | default constructor |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | contents is not initialized |

|  |  |
| --- | --- |
| **method** | constructor with real and imaginary parts |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | initialized with real and imaginary parts |

Example:

Quaternion4f a(1.0f, 2.0f, 3.0f, 4.0f);

// a = (1 + 2\*i + 3\*j + 4\*k)

|  |  |
| --- | --- |
| **method** | constructor with one real part only |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | initialized with the real number. The imaginary parts are set to zero |

|  |  |
| --- | --- |
| **method** | constructor with two Complex2f or two Complex2d |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | The quaternion is constructed from two complex numbers: Quaternion((a+b\*i),(c+d\*i)) = (a+b\*i) + (c+d\*i)\*j  = a+b\*i+c\*j+d\*k |

|  |  |
| --- | --- |
| **method** | constructor with vector |
| **defined for** | Quaternion4f(Vec4f), Quaternion4d(Vec4d) |
| **description** | The four vector elements go into the real part and the three imagniary parts |

|  |  |
| --- | --- |
| **method** | constructor from 3-dimensional vector |
| **defined for** | Quaternion4f(Vec3f), Quaternion4d(Vec3d) |
| **description** | (x,y,z) is converted to (x\*i+y\*j+z\*k). Conversion from quaternion to 3-dimensional vector is also possible. The cross\_product function for Vec3f and Vec3d corresponds to the operator \* for Quaternion4f and Quaternion4d.  Note that these conversions are only available if vector3d.h is included before quaternion.h |

Member functions:

|  |  |
| --- | --- |
| **method** | load(pointer) |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | The quaternion is read from a float or double array containing the real part followed by the imaginary parts |

|  |  |
| --- | --- |
| **method** | store(pointer) |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | The quaternion is stored as four values in a float or double array |

|  |  |
| --- | --- |
| **method** | get\_low(), get\_high() |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | Split the quaternion into two complex numbers. q = q.get\_low() + q.get\_high()\*j |

|  |  |
| --- | --- |
| **method** | real() |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | Get the real part as a float or double |

|  |  |
| --- | --- |
| **method** | imag() |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | Get the imaginary parts, with the real part set to zero |

|  |  |
| --- | --- |
| **method** | extract(index) |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | extract a single real or imaginary part. index = 0 gives real part of first element, index = 1 gives first imaginary part, etc. |

|  |  |
| --- | --- |
| **method** | to\_vector() |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | Convert to a vector Vec4f or Vec4d containing the real part and the imaginary parts. |

Operators:

|  |  |
| --- | --- |
| **operators** | +, +=, -, -=, unary minus, \*, \*=, /, /= |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | Arithmetic functions between two quaternions. Multiplication is not commutative. Division of quaternions is ambiguous. Here, devision is defined as  q / r = q \* reciprocal(r). |

Operators combining quaternion and real

|  |  |
| --- | --- |
| **operators** | +, +=, -, -=, \*, \*=, /, /= |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | Arithmetic functions between a quaternion and a real |

Complex conjugate:

|  |  |
| --- | --- |
| **operators** | ~ |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | The conjugate is defined as  ~(a+b\*i+c\*j+d\*k) = (a-b\*i-c\*j-d\*k) |

Comparison operators:

|  |  |
| --- | --- |
| **operators** | ==, != |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | returns a boolean |

Functions:

|  |  |
| --- | --- |
| **function** | abs |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | abs(a + b\*i + c\*j + d\*k) = sqrt(a\*a + b\*b + c\*c + d\*d) |

|  |  |
| --- | --- |
| **function** | select |
| **defined for** | Quaternion4f, Quaternion4d |
| **description** | selects between two quaternions |

|  |  |
| --- | --- |
| **function** | to\_single |
| **defined for** | Quaternion4d |
| **description** | converts Quaternion4d to Quaternion4f |

|  |  |
| --- | --- |
| **function** | to\_double |
| **defined for** | Quaternion4f |
| **description** | converts Quaternion4f to Quaternion4d |

# Instruction sets and CPU dispatching

Almost every new generation of microprocessors has a new extension to the instruction set. Most of the new instructions relate to vector operations. We can take advantage of these new instructions to make vector code more efficient. The vector class library requires the SSE2 instruction set as a minimum, but it makes more efficient code when a higher instruction set is used. The following table indicates things that are improved for each successive instruction set extension.

|  |  |  |
| --- | --- | --- |
| **Instruction set** | **Year introduce d** | **Functions that are improved** |
| SSE2 | 2001 | minimum requirement for vector class library |
| SSE3 | 2004 | floating point horizontal\_add |
| SSSE3 | 2006 | permute, blend and lookup functions, integer horizontal\_add, integer abs |
| SSE4.1 | 2007 | select, blend, horizontal\_and, horizontal\_or, integer max/min, integer multiply (32 and 64 bit), integer divide (32 bit), 64-bit integer compare (==, !=), floating point round, truncate, floor, ceil. |
| SSE4.2 | 2008 | 64-bit integer compare (>, >=, <, <=). 64 bit integer max, min |
| AVX | 2011 | all operations on 256-bit floating point vectors: Vec8f, Vec4d |
| XOP  AMD only | 2011 | on 128-bit integer vectors: compare, horizontal\_add\_x, rotate\_left, blend, lookup |
| FMA4  AMD only | 2011 | floating point code containing multiplication followed by addition |
| FMA3 | 2012 | floating point code containing multiplication followed by addition |
| AVX2 | 2013 | All operations on 256-bit integer vectors: Vec32c, Vec32uc, Vec16s, Vec16us, Vec8i, Vec8ui, Vec4q, Vec4uq. Gather. |
| AVX512F | 2016 | All operations on 512-bit integer and floating point vectors: Vec16i, Vec16ui, Vec8q, Vec8uq, Vec16f, Vec8d. |
| AVX512ER | 2016 | Only on some processors. Fast exponential functions. Better precision on approx\_recipr and approx\_rsqrt. |
| AVX512BW AVX512VL | Expected 2017 | 512 bit vectors with 8-bit and 16-bit elements. Not yet implemented in vector class library. |

The vector class library makes it possible to compile for different instruction sets from the same source code. Different versions are made simply by recompiling the code with different compiler options. The desired instruction set can be specified on the compiler command line as follows:

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| **Instruction set** | **Gnu and Clang compiler** | **Intel compiler Linux** | **Intel compiler Windows** | **MS compiler** |
| SSE2 | -msse2 | -msse2 | /arch:sse2 | /arch:sse2 |
| SSE3 | -msse3 | -msse3 | /arch:sse3 | /arch:sse2  -D SSE3 |
| SSSE3 | -mssse3 | -mssse3 | /arch:ssse3 | /arch:sse2  -D SSSE3 |
| SSE4.1 | -msse4.1 | -msse4.1 | /arch:sse4.1 | /arch:sse2  -D SSE4\_1 |
| SSE4.2 | -msse4.2 | -msse4.2 | /arch:sse4.2 | /arch:sse2  -D SSE4\_2 |
| AVX | -mavx  -fabi-version=0 | -mavx | /arch:avx | /arch:avx |
| XOP | -mavx  -mxop  -fabi-version=0 | not available | not available | /arch:avx  -D XOP |
| FMA4 | -mfma4 | not available | not available | not available |
| FMA3 | -mfma | -mfma | /Qfma | not available |
| AVX2 | -mavx2  -fabi-version=0 | -mavx2 | /arch:avx2 | /arch:avx  -D AVX2 |
| AVX512F | -mavx512f | -xCOMMON- AVX512 | /arch:COMMON- AVX512 | not available |
| AVX512ER | -mavx512er | -xMIC- AVX512 | /arch:MIC- AVX512 | not available |

The Microsoft compiler supports only a few of the instruction sets, but other instruction sets can be specified as defines which are detected in the preprocessing directives of the vector class library.

The FMA3 and FMA4 instruction sets are not always handled directly by the code in the vector class library, but by the compiler. The compiler may automatically combine a floating point multiplication and a subsequent addition or subtraction into a single instruction, unless you have specified a strict floating point model.

There is no advantage in using the biggest vector classes unless the corresponding instruction set is specified, but it can be convenient to use these classes anyway if the same source code is compiled for multiple versions with different instruction sets. Each large vector will simply be split up into two or four smaller vectors when compiling for a lower instruction set.

It is recommended to make an automatic CPU dispatcher that detects at run time which instruction sets are supported by the actual CPU and operating system, and selects the best version of the code accordingly. For example, you may compile the code four times for four different instruction sets: SSE2, SSE4.1, AVX2 and AVX512F. The CPU dispatcher will then set a function pointer to point to the appropriate version. You can use the function instrset\_detect (see below, page [95](#_bookmark51)) to detect the supported instruction set. The file dispatch\_example.cpp shows an example of how to make a CPU dispatcher that selects the appropriate code version. The critical part of the program is called through a function pointer. This function pointer initially points to the CPU dispatcher, which is activated the first time the function is called. The CPU dispatcher changes the function pointer to point to the best version of the code, and then continues in the selected code. The next time the function is called, the call goes directly to the right version of the code without calling the CPU dispatcher first. It is probably not necessary to make a branch for instruction sets prior to SSE2 because old computers without SSE2 are rarely in use today, and certainly not for demanding applications.

There is an important restriction when you are combining code compiled for different instruction sets: Do not transfer any data *as vector objects* between different pieces of code that are compiled for different instruction sets, because the vectors may be represented differently under the different instruction sets. It is recommended to transfer the data as arrays instead between different parts of the program that are compiled for different instruction sets.

The following functions, defined in the file instrset\_detect.cpp, can be used for detecting at run time which instruction set is supported.

|  |  |
| --- | --- |
| **function** | int instrset\_detect(void) |
| **description** | returns one of these values:   1. 80386 instruction set 2. or above = SSE supported by CPU (not testing for O.S. support) 3. or above = SSE2 4. or above = SSE3 5. or above = Supplementary SSE3 (SSSE3) 6. or above = SSE4.1 7. or above = SSE4.2 8. or above = AVX supported by CPU and O.S. 9. or above = AVX2 10. or above = AVX512F 11. or above = AVX512VL, AVX512BW, AVX512DQ |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | bool hasFMA3(void) |
| **description** | returns true if FMA3 is supported |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | bool hasFMA4(void) |
| **description** | returns true if FMA4 is supported |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | bool hasXOP(void) |
| **description** | returns true if XOP is supported |
| **efficiency** | poor |

|  |  |
| --- | --- |
| **function** | bool hasAVX512ER(void) |
| **description** | returns true if AVX512ER is supported |
| **efficiency** | poor |

# Performance considerations

## *Comparison of alternative methods for writing SIMD code*

The SIMD (Single Instruction Multiple Data) instructions play an important role when software performance has to be optimized. Several different ways of writing SIMD code are discussed below.

### Assembly code

Assembly programming is the ultimate way of optimizing code. Almost everything is possible in assembly code, but it is quite tedious and error-prone. There are far more than a thousand different instructions, and it is quite difficult to remember which instruction belongs to which instruction set extension. Assembly code is difficult to document, difficult to debug and difficult to maintain.

### Intrinsic functions

Several compilers support intrinsic functions that are direct representations of machine instructions. A big advantage of using intrinsic functions rather than assembly code is that the compiler takes care of register allocation, function calling conventions and other details which are often difficult to keep track of when writing assembly code. Another advantage is that the compiler can optimize the code further by such methods as scheduling, interprocedural optimization, function inlining, constant propagation, common subexpression elimination, loop invariant code motion, induction variables, etc. Many of these optimizations are rarely used in assembly code because they make the code unwieldy and unmanageable. Consequently, the combination on intrinsic functions and a good optimizing compiler can often produce more efficient code than what a decent assembly programmer would do.

A disadvantage of intrinsic functions is that these functions have long names that are difficult to remember and which make the code look awkward.

### Intel vector classes

Intel has published a number of vector classes in the form of three C++ header files named fvec.h, dvec.h and ivec.h. These are simpler to use than the intrinsic functions, but unfortunately the Intel vector class files are not always kept up to date, they provide only the most basic functionality, and Intel has done very little to promote, support or develop them. The Intel vector classes have no way of converting data between arrays and vectors. This leaves us with no way of putting data into a vector other than specifying each element separately - which pretty much destroys the advantage of using vectors. The Intel vector classes work only with Intel and MS compilers.

### The BIGMATH SIMD vector class library

The present vector class library has several important features, listed on page [3](#_bookmark2). It provides the same level of optimization as the intrinsic functions, but it is much easier to use. This makes it possible to make optimal use of the SIMD instructions without the need to remember the thousands of different instructions or intrinsic functions. It also takes away the hassle of remembering which instruction belongs to which instruction set extension and making different code versions for different instruction sets.

### Automatic vectorization

A good optimizing compiler is able to automatically transform linear code to vector code in simple cases. Typically, a good compiler will vectorize an algorithm that loops through an array and does some calculations on each array element.

Automatic vectorization is the easiest way of generating SIMD code, and I would recommend to use this method when it works. Automatic vectorization may fail or produce suboptimal code in the following cases:

* + when the algorithm is too complex.
  + when data have to be re-arranged in order to fit into vectors and it is not obvious to the compiler how to do this or when other parts of the code needs to be changed to handle the re-arranged data.
  + when it is not known to the compiler which data sets are bigger or smaller than the vector size.
  + when it is not known to the compiler whether the size of a data set is a multiple of the vector size or not.
  + when the algorithm involves calls to functions that are defined elsewhere or cannot be inlined and which are not readily available in vector versions.
  + when the algorithm involves many branches that are not easily vectorized.
  + when floating point operations have to be reordered or transformed and it is not known to the compiler whether these transformations are permissible with respect to precision, overflow, etc.
  + when functions are implemented with lookup tables.

The present vector class library is intended as a good alternative when automatic vectorization fails to produce optimal code for any of these reasons.

## *Choice of compiler and function libraries*

The vector class library has support for the following four compilers:

### Microsoft Visual Studio

This is a very popular compiler for Windows because it has a good and user friendly IDE (Integrated Development Environment). Make sure you are compiling for the "unmanaged" version, i. e. not using the .net framework.

The Microsoft compiler optimizes reasonably well, but not as good as the other compilers, and it does not support all instruction sets.

### Intel Studio / Intel Composer

This compiler optimizes very well. Intel also provides some of the best optimized function libraries for mathematical and other purposes. Unfortunately, the Intel compilers and some of the function libraries favor Intel CPUs, and often produce code that runs slower than necessary on CPUs of any other brand than Intel. It is possible to work around this limitation for the Intel function libraries and in some cases also for the compiler. See [my blog](http://www.agner.org/optimize/blog/read.php?i=49) and [my C++ manual](http://www.agner.org/optimize/#manual_cpp) for details. Intel's compilers are available for Windows, Linux and Mac platforms.

### Gnu C++ compiler

This compiler produced the best optimizations in my tests. The g++ compiler is available for all x86 and x86-64 platforms. The math functions in the glibc library are currently not fully optimized.

### Clang C++ compiler

This compiler has now been developed to a stage where it is feasible for our purpose. The performance is similar to the Gnu compiler and it supports the same platforms. Unfortunately, the Clang developers are not very effective in fixing reported bugs, so you may encounter problems. Compile with option

-std=c++0x or higher.

## *Choosing the optimal vector size and precision*

The time it takes to make a vector operation such as addition or multiplication typically depends on the total number of bits in the vector rather than the number of elements. For example, it takes the same time to make a vector addition with vectors of eight single precision floats (Vec8f) as with vectors of four double precision floats (Vec4d). Likewise, it takes the same time to add two integer vectors whether the vectors have eight 32-bit integers (Vec8i) or sixteen 16-bit integers (Vec16s). Therefore, it is advantageous to use the lowest precision or resolution that fits the data. It may even be worthwhile to modify a floating point algorithm to reduce loss of precision if this allows you to use single precision rather than double precision. However, you should also take into account the time it takes to convert data from one precision to another. Therefore, it is not good to mix different precisions. The 8-bit and 16-bit integers can not be used with vectors bigger than 256 bits.

The total vector size is 128 bits, 256 or 512 bits. Whether it is advantageous to use the biggest vector size depends on the instruction set. The 256-bit floating point vectors (Vec8f and Vec4d) are only advantageous when the AVX instruction set is available and enabled. The 256-bit integer vectors (Vec32c, Vec16s, Vec8i, Vec4q, etc.) are only advantageous under the AVX2 instruction set. The 512-bit integer and floating point vectors (Vec16f, Vec8d, Vec16i, Vec8q, etc.) will be available with the future AVX512F instruction set, expected in 2016.

## *Putting data into vectors*

The different ways of putting data into vectors are listed on page [10](#_bookmark14). If the vector elements are constants known at compile time, then the fastest way is to use a constructor:

Vec4i a(1); // a = (1, 1, 1, 1)

Vec4i b(2, 3, 4, 5); // b = (2, 3, 4, 5)

If the vector elements are not constants then the fastest way is to load from an array with the method load or load\_a. However, it is not good to load data from an array immediately after writing the data elements to the array one by one,

because this causes a "store forwarding stall" (see my [microarchitecture](http://www.agner.org/optimize/#manual_microarch) [manual](http://www.agner.org/optimize/#manual_microarch)). This is illustrated in the following examples:

// Example 1. Make vector with constructor

int MakeMyData(int i); // make whatever data we need void DoSomething(Vec4i & data); // handle these data const int datasize = 1000; // total number data elements

...

for (int i = 0; i < datasize; i += 4) {

Vec4i d(MakeMyData(i), MakeMyData(i+1), MakeMyData(i+2), MakeMyData(i+3));

DoSomething(d);

}

// Example 2. Load from small array

int MakeMyData(int i); // make whatever data we need void DoSomething(Vec4i & data); // handle these data const int datasize = 1000; // total number data elements

...

for (int i = 0; i < datasize; i += 4) {

int data4[4];

for (int j = 0; j < 4; j++) { data4[j] = MakeMyData(i+j);

}

// store forwarding stall here! Vec4i d = Vec4i().load(data4); DoSomething(d);

}

// Example 3. Make array a little bigger

int MakeMyData(int i); // make whatever data we need void DoSomething(Vec4i & data); // handle these data const int datasize = 1000; // total number data elements

...

for (int i = 0; i < datasize; i += 8) {

int data8[8];

for (int j = 0; j < 8; j++) { data8[j] = MakeMyData(i+j);

}

Vec4i d;

for (int k = 0; k < 8; k += 4) {

d.load(data8 + k); DoSomething(d);

}

}

// Example 4. Make array full size

int MakeMyData(int i); // make whatever data we need void DoSomething(Vec4i & data); // handle these data const int datasize = 1000; // total number data elements

...

int data1000[datasize]; int i;

for (i = 0; i < datasize; i++) {

data1000[i] = MakeMyData(i);

}

Vec4i d;

for (i = 0; i < datasize; i += 4) {

d.load(data1000 + i); DoSomething(d);

}

In example 1, we are combining four data elements into vector d by calling a constructor with four parameters. This may not be the most efficient way because it requires several instructions to combine the four numbers into a single vector.

In example 2, we are putting the four values into an array and then loading the array into a vector. This is causing the so-called store forwarding stall. A store forwarding stall occurs in the CPU hardware when doing a large read (here 128 bits) immediately after a smaller write (here 32 bits) to the same address range. This causes a delay of 10 - 20 clock cycles.

In example 3, we are putting eight values into an array and then reading four elements at a time. If we assume that it takes more than 10 - 20 clock cycles to call MakeMyData four times then the first four elements of the array will have sufficient time to make it into the level-1 cache while we are writing the next four elements. This delay is sufficient to avoid the store forwarding stall.

In example 4, we are putting a thousand elements into an array before loading them. This is certain to avoid the store forwarding stall.

Example 3 and 4 are likely to be the best solutions. A disadvantage of example 3 is that we need an extra loop. A disadvantage of example 4 is that the large array takes more cache space.

## *When the data size is not a multiple of the vector size*

It is obviously easier to vectorize a data set when the number of elements in the data set is a multiple of the vector size. Here, we will discuss different way of handling the situation when the data do not fit into an integral number of vectors. We will use the simple example of adding 134 integers stored in an array.

### handling the remaining data one by one

const int datasize = 134; const int vectorsize = 8;

const int regularpart = datasize & (-vectorsize); // = 128

// (AND-ing with -vectorsize will round down to nearest

// lower multiple of vectorsize. This works only if

// vectorsize is a power of 2) int mydata[datasize];

... // initialize mydata

Vec8i sum1(0), temp; int i;

// loop for 8 numbers at a time

for (i = 0; i < regularpart; i += vectorsize) {

temp.load(mydata+i); // load 8 elements sum1 += temp; // add 8 elements

}

int sum = 0;

// loop for the remaining 6 numbers for (; i < datasize; i++) {

sum += mydata[i];

}

sum += horizontal\_add(sum1); // add the vector sum

### handling the remaining data with a smaller vector size

const int datasize = 134; const int vectorsize = 8;

const int regularpart = datasize & (-vectorsize); // = 128 int mydata[datasize];

... // initialize mydata

Vec8i sum1(0), temp; int sum = 0;

int i;

// loop for 8 numbers at a time

for (i = 0; i < regularpart; i += vectorsize) {

temp.load(mydata+i); // load 8 elements sum1 += temp; // add 8 elements

}

sum = horizontal\_add(sum1); // sum of first 128 numbers if (datasize - i >= 4) {

// get four more numbers Vec4i sum2; sum2.load(mydata+i);

i += 4;

sum += horizontal\_add(sum2);

}

// loop for the remaining 2 numbers for (; i < datasize; i++) {

sum += mydata[i];

}

### use partial load for the last vector

const int datasize = 134;

const int vectorsize = 8; int mydata[datasize];

... // initialize mydata

Vec8i sum1(0), temp;

// loop for 8 numbers at a time

for (int i = 0; i < datasize; i += vectorsize) {

if (datasize - i >= vectorsize) {

temp.load(mydata+i); // load 8 elements

}

else {

// load the last 6 elements temp.load\_partial(datasize-i, mydata+i);

}

sum1 += temp; // add 8 elements

}

int sum = horizontal\_add(sum1); // vector sum

### read past the end of the array and ignore excess data

const int datasize = 134; const int vectorsize = 8; int mydata[datasize];

... // initialize mydata

Vec8i sum1(0), temp;

// loop for 8 numbers at a time, reading 136 numbers for (int i = 0; i < datasize; i += vectorsize) {

temp.load(mydata+i); // load 8 elements if (datasize - i < vectorsize) {

// set excess data to zero

// (this is faster than load\_partial) temp.cutoff(datasize - i);

}

sum1 += temp; // add 8 elements

}

int sum = horizontal\_add(sum1); // vector sum

### make array bigger and set excess data to zero

const int datasize = 134; const int vectorsize = 8;

// round up datasize to 136 const int arraysize =

(datasize + vectorsize - 1) & (-vectorsize); int mydata[arraysize];

int i;

... // initialize mydata

// set excess data to zero

for (i = datasize; i < arraysize; i++) {

mydata[i] = 0;

}

Vec8i sum1(0), temp;

// loop for 8 numbers at a time, reading 136 numbers for (i = 0; i < arraysize; i += vectorsize) {

temp.load(mydata+i); // load 8 elements sum1 += temp; // add 8 elements

}

int sum = horizontal\_add(sum1); // vector sum

It is clearly advantageous to increase the array size to a multiple of the vector size, as in case 5 above. Likewise, if you are storing vector data to an array, then it is an advantage to make the result array bigger to hold the excess data. If this is not possible then use store\_partial to write the last partial vector to the array.

It is usually possible to read past the end of an array, as in case 4 above, without causing problems. However, there is a theoretical possibility that the array is placed at the very end of the readable data area so that the program will crash when attempting to read from an illegal address past the end of the valid data area. To consider this problem, we need to look at each possible method of data storage:

* 1. An array declared inside a function, and not static, is stored on the stack. The subsequent addresses on the stack will contain the return address and parameters for the function, followed by local data, parameters, and return address of the next higher function all the way up to main. In this case there is plenty of extra data to read from.
  2. A static or global array is stored in static data memory. The static data area is often followed by library data, exception handler tables, link tables, etc. These tables can be seen by requesting a map file from the linker.
  3. Data allocated with the operator new are stored on the heap. I have no information of the size of the end node in a heap.
  4. If an array is declared inside a class definition then case (a), (b) or (c) above applies, depending on how the class instance (object) is created.

These problems can be avoided either by making the array bigger or by aligning the array to an address divisible by 16 for 128-bit vectors or divisible by 32 for 256-bit vectors. The memory page size is at least 4 kbytes, and always a power of 2. If the array is aligned by the vector size (16 or 32) then the page boundaries are certain to coincide with vector boundaries. This makes sure that there is no memory page boundary between the end of the array and the next vector-size boundary. Therefore, we can read up to the next vector-size boundary without the risk of crossing a boundary to an invalid memory page.

A further advantage of aligning the array by 16, 32 or 64 is that reading and writing vectors from an aligned array may be faster. To align an array by 16 in Windows, write:

declspec(align(16)) int mydata[1000];

In Unix-like systems, write:

int mydata[1000] attribute ((aligned(16)));

It is always recommended to align large arrays for performance reasons if the code uses vectors. Unfortunately, it may be more complicated to align arrays created with operator new.

## *Using multiple accumulators*

Consider this function which adds a long list of floating point numbers:

double add\_long\_list(double const \* p, int n) {

int n1 = n & (-4); // round down n to multiple of 4 Vec4d sum(0.0);

int i;

for (i = 0; i < n1; i += 4) {

sum += Vec4d().load(p + i); // add 4 numbers

}

// add any remaining numbers

sum += Vec4d().load\_partial(n - i, p + i); return horizontal\_add(sum);

}

In this example, we have a loop-carried dependency chain (see my [C++ manual](http://www.agner.org/optimize/#manual_cpp)). The vector addition inside the loop has a latency of typically 3 - 5 clock cycles. As each addition has to wait for the result of the previous addition, the loop will take 3 - 5 clock cycles per iteration.

However, the throughput of floating point additions is typically one vector addition per clock cycle. Therefore, we are far from fully utilizing the capacity of the floating point adder. In this situation, we can double the speed by using two accumulators:

double add\_long\_list(double const \* p, int n) {

int n2 = n & (-8); // round down n to multiple of 8 Vec4d sum1(0.0), sum2(0.0);

int i;

for (i = 0; i < n2; i += 8) {

sum1 += Vec4d().load(p + i); // add 4 numbers sum2 += Vec4d().load(p + i + 4); // 4 more numbers

}

if (n - i >= 4) {

// add 4 more numbers

sum1 += Vec4d().load(p + i); i += 4;

}

// add any remaining numbers

sum2 += Vec4d().load\_partial(n - i, p + i); return horizontal\_add(sum1 + sum2);

}

Here, the addition to sum2 can begin before the addition to sum1 is finished. The loop still takes 3 - 5 clock cycles per iteration, but the number of additions done per loop iteration is doubled. It may even be worthwhile to have three or four accumulators in this case if n is very big.

In general, if we want to predict whether it is advantageous to have more than one accumulator, we first have to see if there is a loop-carried dependency chain. If the performance is not limited by a loop-carried dependency chain then there is no need for multiple accumulators. Next, we have to look at the latency and throughput of the instructions inside the loop. Floating point addition, subtraction and multiplication all have latencies of typically 3 - 5 clock cycles and a throughput of one vector addition or subtraction plus one vector multiplication per clock cycle. Therefore, if the loop-carried dependency chain involves floating point addition, subtraction or multiplication; and the total number of floating point operations per loop iteration is lower than the maximum throughput, then it may be advantageous to have two accumulators, or perhaps more than two.

There is rarely any reason to have multiple accumulators in integer code, because an integer vector addition has a latency of just 1 or 2 clock cycles.

## *Using multiple threads*

Performance can be improved by dividing the work between multiple threads on processors with multiple CPU cores. This technique is outside the scope of the present manual. The vector class library is thread-safe as long as the same vector is not accessed from multiple threads simultaneously. The floating point control word (see p. [36](#_bookmark29)) is not shared between threads.

# Error conditions

## *Runtime errors*

The vector class library is generally not producing runtime error messages. An index that is out of range produces behavior that is implementation-dependent.

This means that the output may be different for different instruction sets or for different versions of the vector class library.

For example, an attempt to read a vector element with an index that is out of range may result in various behaviors, such as producing zero, taking the index modulo the vector size, giving the last element, or producing an arbitrary value. Likewise, an attempt to write a vector element with an index that is out of range may variously take the index modulo the vector size, write the last element, or do nothing. This applies to functions such as insert, extract, load\_partial, store\_partial, cutoff, permute, blend, lookup and gather. The same applies to a bit-index that is out of range in functions like set\_bit, get\_bit, rotate, and shift operators (<<, >>).

Boolean vectors for instruction sets lower than AVX512 are stored as integer vectors. The only allowed values for boolean vector elements in this case are 0 (false) and -1 (true). The behavior for other values is implementation dependent and possibly inconsistent. For example, the behavior of the select function when the boolean selector input is a mixture of 0 and 1 bits depends on the instruction set. For instruction sets prior to SSE4.1, it will select between the operands bit-by-bit. For SSE4.1 and higher it will select integer vectors byte-by- byte, using the leftmost bit of each byte in the selector input. For floating point vectors under SSE4.1 and higher, it will use only the leftmost bit (sign bit) of the selector. Boolean vectors for the biggest vector size compiled under the AVX512 instruction set have only one bit for each element.

An integer division by a variable that is zero will usually produce a runtime exception.

A floating point overflow will usually produce infinity, floating point underflow produces zero, and an invalid floating point operation may produce not-a-number (NAN). Floating point exceptions can occur only if exceptions are unmasked.

Unmasking floating point exceptions does not guarantee that BIGMATH SIMD floating point functions will generate exceptions in case of error.

Mathematical functions will signal an error by producing INF or NAN, not by raising exceptions or setting an errno variable.

A program crash may be caused by alignment errors. This can happen if a BIGMATH SIMD vector is stored in a dynamic array or an STL container or other data container that does not have correct alignment. See page [16](#_bookmark16).

## *Compile-time errors*

Integer vector division by a const\_int or const\_uint can produce a compile- time error message when the divisor is zero or out of range. The error message may not be as informative as we could wish, due to the limitations of template metaprogramming. The error message may possibly contain the text "Static\_error\_check<false>".

Combination of incompatible vector classes, or other syntax errors produce compile-time error messages. These error messages may be quite long and confusing due to overloading and templates, but generally indicating the line number of the error.

"error C2719: formal parameter with declspec(align('16')) won't be aligned". The Microsoft compiler cannot handle vectors as function parameters. The easiest solution is to change the parameter to a const reference, e. g.:

Vec4f my\_function(Vec4f const & x) {

... }

"ambiguous call to overloaded function". Make sure all parameters have the correct type, e.g.:

Vec4f a, b;

b = pow(a,0.8);

// this should be: b = pow(a,0.8f);

The same can happen with operators, e.g.

Vec4ui a; a >>= 2;

// this should be: a >>= 2u;

## *Link errors*

"unresolved external symbol intel\_cpu\_indicator". This link error occurs when you are using Intel's SVML library without including a CPU dispatcher. Link in the library libircmt.lib to use Intel's own CPU dispatch function for Intel processors, or use an object file from the [asmlib library](http://www.agner.org/optimize/#asmlib) under "inteldispatchpatch" for best performance on all brands of processors. See [my blog](http://www.agner.org/optimize/blog/read.php?i=49) and [my C++ manual](http://www.agner.org/optimize/#manual_cpp) for details.

# Implementation-dependent behavior

A big advantage of the BIGMATH SIMD library is that you can compile the same source code for different instruction set extensions. A higher instruction set will generally give faster code, but produce the same results. There may, however, be special cases where the same code generates different results with different instruction sets or different compilers. These cases include:

* An index out of range produces implementation-dependent results. Functions such as insert, extract, load\_partial, store\_partial, cutoff, permute, blend, lookup and gather may produce different results for an index out of range depending on the instruction set. No exception or error message is generated, only a meaningless number.
* permute and blend functions allow a *"don't care"* index to be specified. The result for a *don't care* element may depend on the instruction set.
* Negative zero. The floating point values of 0.0 and -0.0 should be regarded as equal. Some functions may return 0.0 or -0.0 depending on the instruction set, e.g. when rounding a negative number. The sign of a zero can be detected by the functions sign\_bit and sign\_combine.
* NANs. An error code can be propagated through NAN (not-a-number) values and retrieved by the function nan\_code. When two NAN values with different codes are combined, for example by adding them together, the result may be either of the two values, or an OR-combination of the two, depending on the compiler and the CPU. The sign of a NAN has no meaning and may vary. The min and max functions may fail to propagate NAN values.

# File list

|  |  |
| --- | --- |
| **file name** | **purpose** |
| Simd.pdf | instructions (this file) |
| vectorsimd.h | top-level C++ header file. This will include several other header files, according to the indicated instruction set. |
| instrset.h | detection of which instruction set the code is compiled for, and various common definitions. Included by vectorsimd.h |
| vectori128.h | defines classes, operators and functions for integer vectors with a total size of 128 bits. Included by vectorsimd.h |
| vectori256.h | defines classes, operators and functions for integer vectors with a total size of 256 bits for the AVX2 instruction set. Included by vectorsimd.h if appropriate |
| vectori256e.h | defines classes, operators and functions for integer vectors with a total size of 256 bits for instruction sets lower than AVX2. Included by vectorsimd.h if appropriate |
| vectori512.h | defines classes, operators and functions for integer vectors with a total size of 512 bits for the AVX512 instruction set. Included by vectorsimd.h if appropriate |
| vectori512e.h | defines classes, operators and functions for integer vectors with a total size of 512 bits for instruction sets lower than AVX512. Included by vectorsimd.h if appropriate |
| vectorf128.h | defines classes, operators and functions for floating point vectors with a total size of 128 bits. Included by vectorsimd.h |
| vectorf256.h | defines classes, operators and functions for floating point vectors with a total size of 256 bits for the AVX and later instruction sets. Included by vectorsimd.h if appropriate |
| vectorf256e.h | defines classes, operators and functions for floating point vectors with a total size of 256 bits for instruction sets lower than AVX. Included by vectorsimd.h if appropriate |
| vectorf512.h | defines classes, operators and functions for floating point vectors with a total size of 512 bits for the AVX512 and later instruction sets. Included by vectorsimd.h if appropriate |
| vectorf512e.h | defines classes, operators and functions for floating point vectors with a total size of 512 bits for instruction sets lower than AVX512. Included by vectorsimd.h if appropriate |
| vectormath\_lib.h | optional header file for external mathematical vector function libraries |
| math/exp.h | optional inline mathematical functions: power, logarithms and exponential functions |
| vectormath\_trig.h | optional inline mathematical functions: trigonometric and inverse trigonometric functions |
| math/hyp.h | optional inline mathematical functions: hyperbolic and inverse hyperbolic functions |
| vectormath\_common.h | common definitions for math/exp.h, vectormath\_trig.h and math/hyp.h |
| special.zip/ranvec1.h | random number generator header file |
| special.zip/ranvec1.cpp | random number generator |
| special.zip/decimal.h | optional header file for conversion of integer vectors to decimal and hexadecimal ASCII number strings and vice versa |
| special.zip/vector3d.h | optional header file for 3-dimensional vectors |
| special.zip/complexvec.h | optional header file for complex numbers and complex vectors |
| special.zip/quaternion.h | optional header file for quaternions |
| instrset\_detect.cpp | optional functions for detecting which instruction set is supported at runtime |
| dispatch\_example.cpp | example of how to make automatic CPU dispatching |
| license.txt | Gnu general public license |
| changelog.txt | change log |

# Examples

This example calculates the polynomial x3 + 2∙*x*2 - 5∙*x* + 1 on a floating point vector. The function parameter x is declared as a const reference in order to avoid problems in the Microsoft compiler. The constants a, b and c are declared static so that they don't need to be initialized at every function call. The order of calculation is specified by parentheses in order to make shorter dependency chains.

Vec4f polynomial (Vec4f const & x) {

static const Vec4f a(2.0f), b(-5.0f), c(1.0f); return (a + x) \* (x \* x) + (b \* x + c);

}

The next example transposes a 4x4 matrix.

void transpose(float matrix[4][4]) { Vec8f row01, row23, col01, col23;

// load first two rows row01.load(&matrix[0][0]);

// load next two rows row23.load(&matrix[2][0]);

// reorder into columns

col01 = blend8f<0,4, 8,12,1,5, 9,13>(row01, row23); col23 = blend8f<2,6,10,14,3,7,11,15>(row01, row23);

// store columns into rows col01.store(&matrix[0][0]); col23.store(&matrix[2][0]);

}

or with AVX512:

void transpose(float matrix[4][4]) {

Vec16f rows, columns;

// load entire matrix as rows rows.load(&matrix[0][0]);

// reorder into columns

columns = permute16f<0,4,8,12,1,5,9,13, 2,6,10,14,3,7,11,15>(rows);

// store columns into rows columns.store(&matrix[0][0]);

}

The next example makes a matrix multiplication of two 4x4 matrixes.

void matrixmul(float A[4][4],float B[4][4],float M[4][4]){

// calculates M = A\*B Vec4f Brow[4], Mrow[4]; int i, j;

// load B as rows

for (i = 0; i < 4; i++) {

Brow[i].load(&B[i][0]);

}

// loop for A and M rows for (i = 0; i < 4; i++) {

Mrow[i] = Vec4f(0.0f);

// loop for A columns, B rows for (j = 0; j < 4; j++) {

Mrow[i] += Brow[j] \* A[i][j];

}

}

// store M

for (i = 0; i < 4; i++) {

Mrow[i].store(&M[i][0]);

}

}

The next example makes a table of the sin function and gets sin(x) and cos(x) by table lookup.

#include <math.h>

#ifndef M\_PI // define pi if not defined #define M\_PI 3.14159265358979323846

#endif

// length of table. Must be a power of 2. #define sin\_tablelen 1024

// the accuracy of table lookup is +/- pi/sin\_tablelen

class SinTable {

protected:

float table[sin\_tablelen]; float resolution;

float rres; // 1./resolution public:

SinTable(); // constructor Vec4f sin(Vec4f const & x); Vec4f cos(Vec4f const & x);

};

SinTable::SinTable() { // constructor

// compute resolution

resolution = float(2.0 \* M\_PI / sin\_tablelen); rres = 1.0f / resolution;

// initialize table (no need to use vectors

// here because this is calculated only once) for (int i = 0; i < sin\_tablelen; i++) {

table[i] = sinf((float)i \* resolution);

}

}

Vec4f SinTable::sin(Vec4f const & x) {

// calculate sin by table lookup Vec4i index = round\_to\_int(x \* rres);

// modulo tablelen equivalent to modulo 2\*pi index &= sin\_tablelen - 1;

// look up in table

return lookup<sin\_tablelen>(index, table);

}

Vec4f SinTable::cos(Vec4f const & x) {

// calculate cos by table lookup

Vec4i index = round\_to\_int(x \* rres) + sin\_tablelen/4;

// modulo tablelen equivalent to modulo 2\*pi index &= sin\_tablelen - 1;

// look up in table

return lookup<sin\_tablelen>(index, table);

}

int main() {

SinTable sintab;

Vec4f a(0.0f, 0.5f, 1.0f, 1.5f);

Vec4f b = sintab.sin(a);

// b = (0.0000 0.4768 0.8416 0.9973)

// accuracy +/- 0.003

...

return 0;

}