SIMPRO, SPACE DEBRIS SIMULATOR AND PROPAGATION – USER GUIDE

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1. Introduction

SIMPRO is a space debris simulator of break-up events, based on NASA's model EVOLVE 4.0 ([3], see also [1]); it also allows to propagate the orbits using different formalisms (Cartesian or Hamiltonian). SIMPRO represents a useful tool in the analysis of satellites and space debris dynamics, with the aim to provide information on break-up events, either collisions or explosions, and their subsequent dynamics. The application is written in JAVA and can be executed on a wide set of operating systems.

These guidelines are intended to give the user basic information to run the program; details can be found in the accompanying paper [2].

The executable program is publicly available and it can be downloaded from the following link:

SIMPRO GitHub repository

IMPORTANT NOTE: When using the results of this simulator in articles, books, videos, or any other mean, acknowledge the use making reference to:

M. Apetrii, A. Celletti, E. Efthymiopoulos, C. Gales, T. Vartolomei, *Simulating a breakup event and propagating the orbits of space debris*, Celestial Mechanics and Dynamical Astronomy 136 (5), 35 (2024).

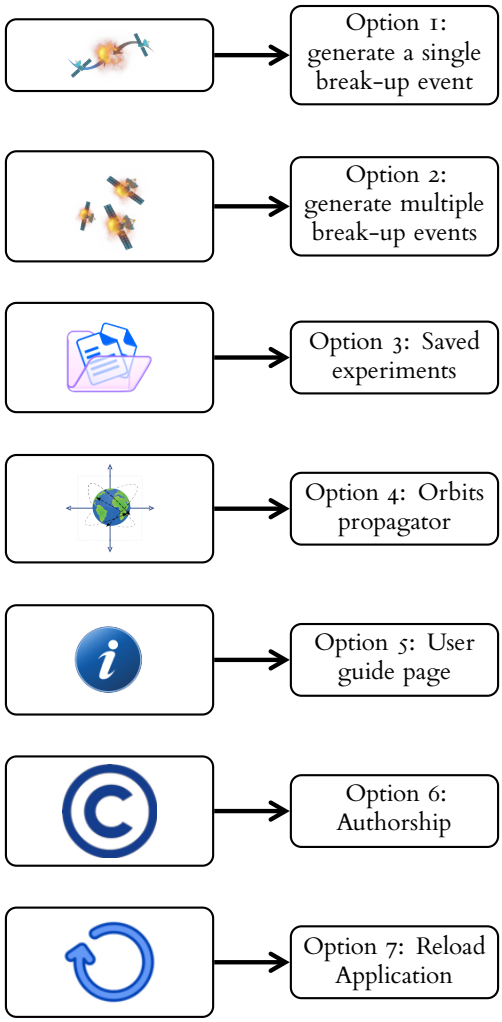
Any question on SIMPRO can be addressed on GitHub or writing to:

simpro.project@gmail.com

Refer to these notes as: Version 1.0 - September 2024.

2. Quick description of the main menu

This section reproduces the left column that appears when opening SIMPRO and explains the meaning of the symbols, which correspond to the different options that the user can select. The following sections will provide further details on each option.

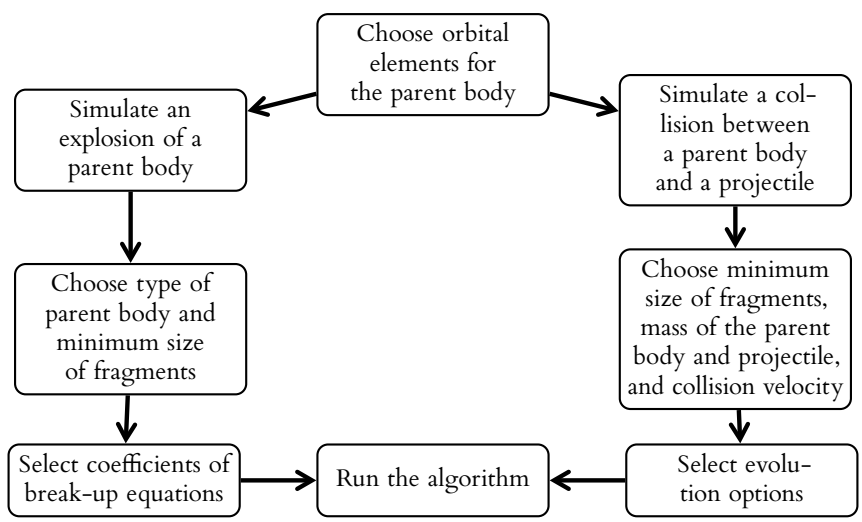


3. Option 1: generate a single break-up event

The first option of SIMPRO reproduces the break-up model Evolve 4.0 provided by NASA for a single break-up event.

It allows one to determine the cross-sections, masses, and imparted velocities of the fragments after an explosion or a collision. Section 3.1 describes the work-flow, Section 3.2 illustrates how to choose the initial orbital elements, Sections 3.3 and 3.4 explain, respectively, the procedure to simulate a collision or an explosion, Section 3.5 shows how to get the evolution of each fragment on a given time interval, Section 3.6 explains how to change some settings with respect to [3], Section 3.7 describes the different outputs generated by SIMPRO, Section 3.8 shows how to save the data of an experiment.

3.1. **Work-flow.** The work-flow of SIMPRO is illustrated below.



3.2. **Choosing Orbital Elements.** Choose Mean elements (TLE) and provide the orbital elements of the parent body (where the break-up event will happen).

- Semi-major axis in km: $a > 6400$ km and $a < 45000$ km.
- Eccentricity $e \in [0, 0.75]$.
- Inclination in degrees: $i \in [0, 180^o]$.
- Mean anomaly in degrees: $M \in [0, 360^o]$.
- Argument of perigee in degrees: $\omega \in [0, 360^o]$.
- Argument of the ascending node in degrees: $\Omega \in [0, 360^o]$.

An example is given in Figure 1.

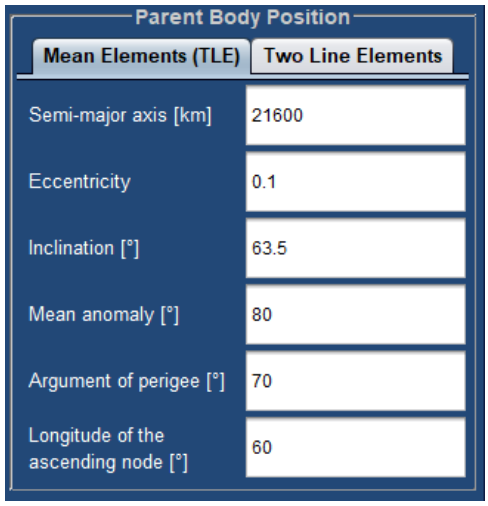


FIGURE 1. Orbital Elements of Parent Body.

Alternatively, choose Two Line Elements and provide the data in LINE 1 and LINE 2 using the NORAD format from CelesTrak.

3.3. Collisions options.

- Choose the size of the smallest fragment generated, with the constraint ≥ 1 cm.
- Set the masses of parent body between 300 and 15 000 kg.
- Set the masses of parent body between 0.001 and 5 kg.
- Choose the impact velocity between 1 and 10 000 m/s.
- Select the type of parent body: Drop down menu > Upper Stage or Drop down menu > Spacecraft

An example is given in Figure 2.

The "Output" frame gives the number of generated fragments and the number of fragments with elliptic orbits, taking into account that some fragments can fall on the Earth. Besides, it gives "Catastrophic: false" or "Catastrophic: true", the latter case occurring whenever the energy of break-up is greater than 40 kJ, which means that the parent body is completely disintegrated. This could happen only in case of a collision with a heavy projectile at a high relative velocity.

3.4. Explosions options.

After having chosen the mean elements of the parent body as in Section 3.3, proceed to fix the parameters of break-up.

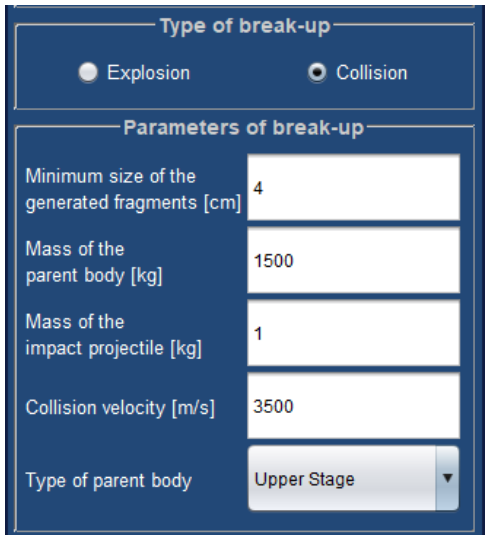


FIGURE 2. Collision options.

- Choose the size L_c of the smallest fragment generated, with the constraint ≥ 1 cm.
- Select the type of parent body:

Drop down menu » Molniya Satellite | Ukranian Tsyklan | Soviet Antisatellite | Soviet Battery

Drop down menu (continued) » Soviet Eorsat | Regular Body | Titan Transtage

The "Output" frame gives the number of generated fragments and the number of fragments with elliptic orbits, taking into account that some fragments can fall on the Earth.

3.5. **Fragments' propagation.** To activate the propagation of the fragments, select Toggle activation with a LEFT CLICK and set the options with a RIGHT CLICK. One can choose "short-term" and "long-term" propagation, providing the period and step, the initial time and selecting the forces one wants to include in the propagation, namely the J_2 and J_3 terms of the geopotential, the effects of Moon and Sun, the Solar radiation pressure, and the drag effect due to the Earth's atmosphere, see Figure 3.

3.6. **Setting equations' parameters.** You may change the original coefficients and parameters of the NASA Evolve 4.0 equations described in [1], [3], see Figure 5.

- Open the pop-up window by pressing Set Parameters - More Info button.

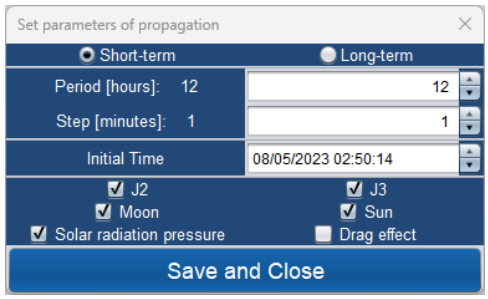


FIGURE 3. Options for the propagation of each fragment for a period of time.

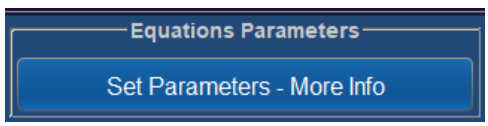


FIGURE 4. Set NASA Evolve 4.0 parameters.

- Find the equation you want to modify and set the value of the parameter(s) within the editable boxes. The boxes provide the default values; a pop-up window that opens passing on the editable boxes provides the allowed intervals for each parameter.
- You may change one or more parameters.
- Save your choice parameters using Save and close button on top of the window.

Notice that a slightly change in the NASA Evolve 4.0 parameters could give major differences in the results. Please refer to [1] and [2] for more details

3.7. **Output.** The output panel has two different frameworks, according to whether the orbits are propagated or not.

3.7.1. *Orbital Elements Plots.* The orbital elements a, e, i are plotted in the 2-dimensional planes of $a - i$, $a - e$, and $e - i$; Figure 6 shows the output without (left panel) and with propagation of the orbits (right panel).

3.7.2. *Data Analysis.* It provides a statistical analysis of the data after a break-up event by computing mean, median, min, max, range, variance, standard deviation, mean standard error, coefficient of variation of the orbital elements, size, area-to mass ratio and velocity distributions. Figure 7 shows the output after a propagation.

The output in Figure 7 is described as follows:

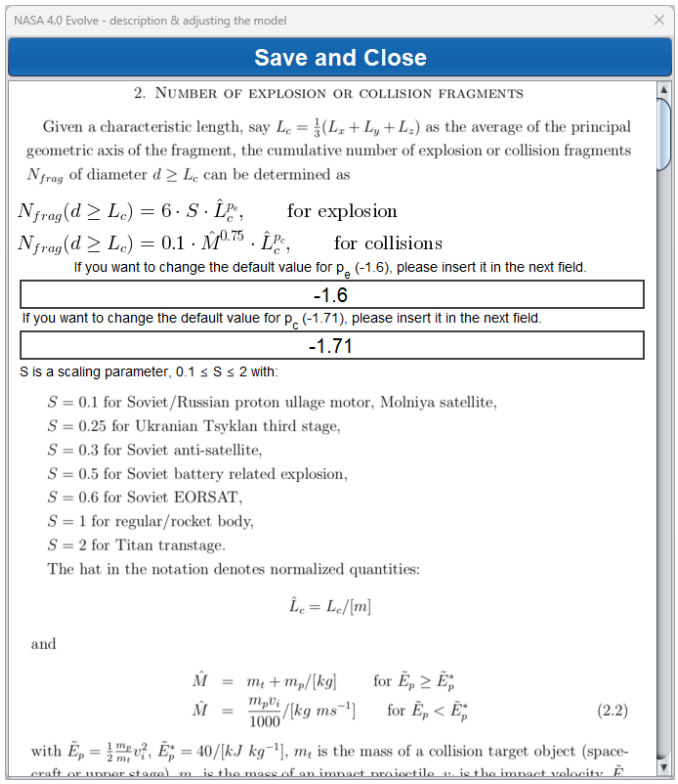


Figure 5. Set parameters window

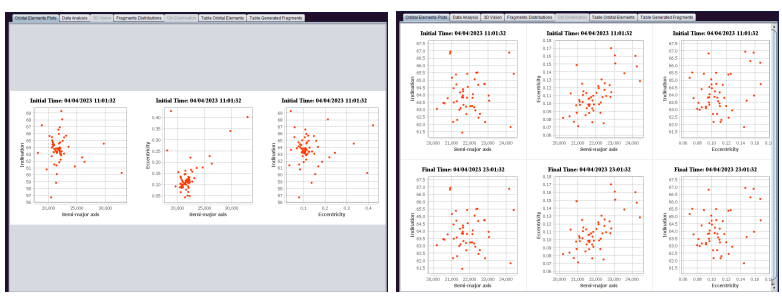
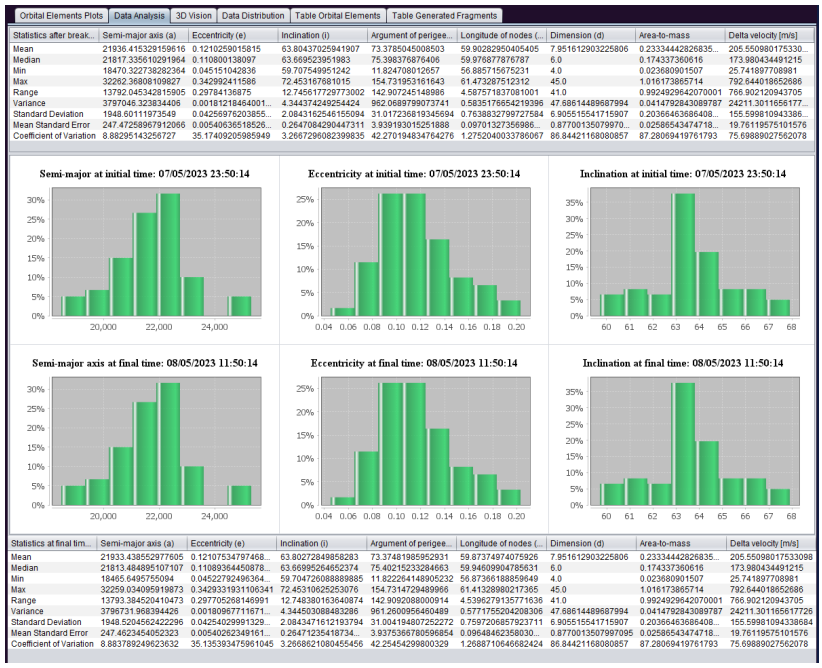


Figure 6. Orbital elements plots.

- First row: statistics at break-up time;
- Second row: histograms of a, e, i at break-up;
- Third row: histograms of a, e, i after evolution period;
- Forth row: statistics after evolution period.

3.7.3. *3D Orbit Vision.* This page allows to visualize the position of the generated fragments in a 3-dimensional space, whenever the propagation



Statistics after break...	Semi-major axis (a)	Eccentricity (e)	Inclination (i)	Argument of perigee...	Longitude of nodes (...	Dimension (d)	Area-to-mass	Delta velocity [m/s]
Mean	21936.415329159616	0.1210259015815	63.80437025941907	73.3785045008503	59.90282950405405	7.951612903225806	0.23334442826835...	205.550980175330...
Median	21817.335610291964	0.1108001380097	63.669523951983	75.398376876406	59.976877876787	6.0	0.174337360616	173.980434491215
Min	18470.322738282364	0.045151042836	59.70754995124 2	11.824708012657	56.885715675231	4.0	0.023680901507	25.741897708981
Max	32262.36808109827	0.342992411586	72.453167681015	154.731953161643	61.473287512312	45.0	1.016173865714	792.644018652686
Range	13792.045342815905	0.29784136875	12.745617729773002	142.907245148986	4.587571837081001	41.0	0.992492964207000 1	766.902120943705
Variance	3797046.323834406	0.00181218464001...	4.344374249254424	962.0689799073741	0.583517665429396	47.68614489687994	0.0414792843089787	24211.3011655177...
Standard Deviation	1948.60111973549	0.0425697520385 5...	2.0843162546155094	31.017236819345694	0.763883279972758 4	6.905515541715907	0.203664636864084...	155.599810943386...
Mean Standard Error	247.47258967912066	0.00540636518526...	0.2647084290447311	3.939193015251888	0.09701327356986...	0.8770013507997 70...	0.0258654347471 8...	19.76119575101576
Coefficient of Variation	8.88295143256727	35.17409205985949	3.2667296082399835	42.270194834764276	1.2752040033786067	86.84421168080857	87.28069419761793	75.69889027562078

Statistics at final tim...	Semi-major axis (a)	Eccentricity (e)	Inclination (i)	Argument of perigee...	Longitude of nodes (...	Dimension (d)	Area-to-mass	Delta velocity [m/s]
Mean	21933.438552977605	0.1210753479746 8...	63.80272849858283	73.37481985952931	59.87374974075926	7.951612903225806	0.23334442826835...	205.550980175330 98
Median	21813.484895107107	0.1108936445087 8...	63.66995264552374	75.40215233284663	59.94609904785631	6.0	0.174337360616	173.980434491215
Min	18465.6495755094	0.0452279249636 4...	59.70472608888985	11.82226414890523 2	56.87366188859649	4.0	0.023680901507	25.741897708981
Max	32259.034095919873	0.3429331931106341	72.45310625253076	154.73147729489968	61.41328980217365	45.0	1.016173865714	792.644018652686
Range	13793.384520410473	0.29770526814991	12.74838016364087 4	142.9092088000914	4.539627913577163 6	41.0	0.992492964207000 1	766.902120943705
Variance	3796731.968394426	0.0018096771167 1...	4.344503088483286	961.2600956460489	0.577175520420830 6	47.68614489687994	0.0414792843089787	24211.301165617726
Standard Deviation	1948.5204562422296	0.0425402999132 9...	2.0843471612193794	31.004194807252272	0.759720685792371 1	6.905515541715907	0.203664636864084...	155.599810943386 84
Mean Standard Error	247.46234540952323	0.0054026234916 1...	0.2647123541973 4...	3.937536678059685 4	0.09648462358030...	0.8770013507997095	0.0258654347471 8...	19.76119575101576
Coefficient of Variation	8.883789249623632	35.13539347596104 5	3.2668621080455456	42.2545429980032 9	1.2688710646682424	86.84421168080857	87.28069419761793	75.69889027562078

FIGURE 7. Data analysis window.

has been computed. An example is given in Figure 8 with the following description, where the blue dots make the contour plot of the Earth surface:

- Top-left: parent body position at break-up time.
- Top-right: fragments' orbits after one fourth of period.
- Bottom-left: fragments' position after three fourths of period.
- Bottom-right: fragments' orbits at final time.

Each panel has additional options to zoom and move the graphs, rotate the plot, reset the zoom, modify the scale settings, save the picture, have a list of Cartesian coordinates (X, Y, Z) of each fragment at a given time, the coordinates of the parent body that gives the orbit, the coordinates of the blue dots representing the Earth. An option allows one to decide whether visualize the fragments, parent body, and the Earth.

3.7.4. *Data Distribution.* This page shows the ξ-distribution described in the NASA model ([3]), where $\chi = \log_{10} \frac{A}{m}$, see Figure 9. This page is activated only for catastrophic events, which are obtained for a large mass of the impact projectile and a large collision velocity. The page shows:

- First row: Histograms of size, area-to-mass ratio and Δv;

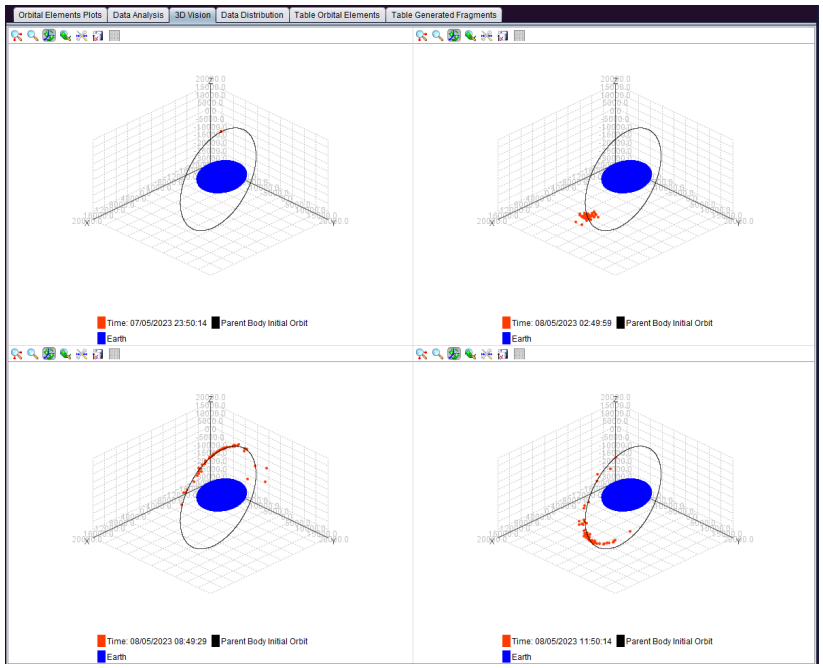


FIGURE 8. 3D plots.

- Second row (only for catastrophic events): Histograms of χ for the generated data and for different values of L_c versus the theoretical Probability density function (PDF) of χ.

3.7.5. *Table of Orbital Elements.* This page gives the data about the orbital position $(a, e, i, M, \omega, \Omega)$, the area-to-mass ratio, the dimension, and the ID sequence number of each generated fragment after the break-up, see Figure 10.

3.7.6. *Table of Generated Fragments.* This page gives the state vector and the characteristics of each generated fragment after the break-up; the ID sequence number, the size, the area-to-mass ratio, the area, the mass, the delta velocity, the components of the velocity (V_x, V_y, V_z), the observation dynamical type, which could be elliptic or hyperbolic orbits, and escape or re-entry orbits, see Figure 11.

3.8. **Save Experiment.** To save the current experiment (including the evolution), press the button below the output text, see Figure 12.

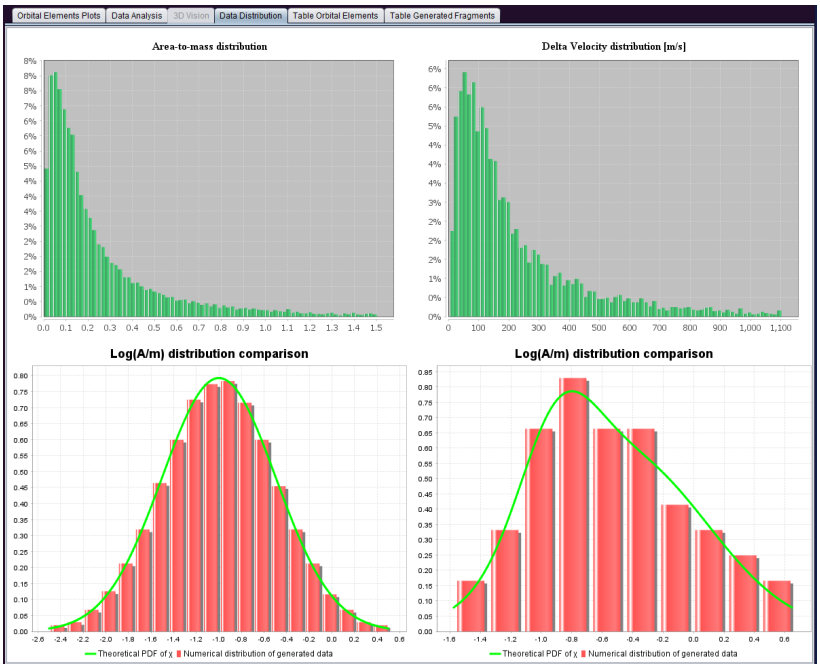
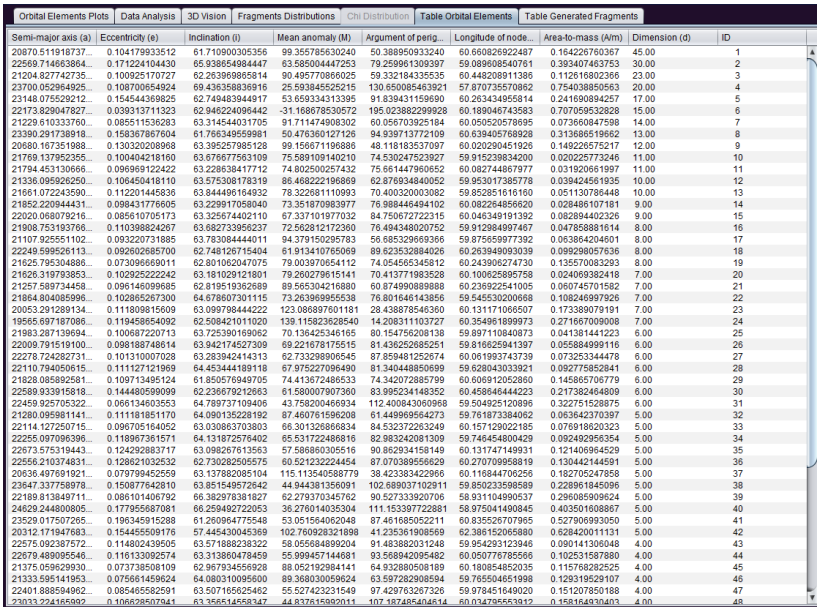


FIGURE 9. Data distribution window.



Orbital Elements Plots | Data Analysis | 3D Vision | Fragments Distributions | Chi Distribution | Table Orbital Elements | Table Generated Fragments

Semi-major axis (a)	Eccentricity (e)	Inclination (i)	Mean anomaly (M)	Argument of perig...	Longitude of node...	Area-to-mass (A/m)	Dimension (d)	ID
20870.511918737...	0.104179933512	61.710900305356	99.355785630240	50.388950933240	60.660826922487	0.164226760367	45.00	1
22569.714663864...	0.171224104430	65.938654984447	63.585004447253	79.259961309397	59.089608540761	0.393407463753	30.00	2
21204.827742735...	0.100925170727	62.263969865814	90.495770866025	59.332184335535	60.448208911386	0.112616802366	23.00	3
23700.052964925...	0.108700654924	69.436358836916	25.593945525215	130.650085463921	57.870735570862	0.754038850563	20.00	4
23148.075529212...	0.154544369825	62.749483944917	53.659334313395	91.839431159690	60.263434955814	0.241690894257	17.00	5
22173.829047827...	0.039313711323	62.946224096442	-31.168678530572	195.023882299928	60.189046743583	0.707059532828	15.00	6
21229.610333760...	0.085511536283	63.314544031705	91.711474908302	60.056703925184	60.050520578695	0.073660847598	14.00	7
23390.291738918...	0.158367867604	61.766349959981	50.476360127126	94.939713772109	60.639405768928	0.313686519662	13.00	8
20680.167351988...	0.130320208968	63.395257985128	99.156671196886	48.118183537097	60.020290451926	0.149226575217	12.00	9
21769.137952355...	0.100404218160	63.876677563109	75.589109140210	74.530247523927	59.915239834200	0.020225773246	11.00	10
21794.453130666...	0.096969122422	63.228638417712	74.802500257432	75.661447960652	60.082744867977	0.031920661997	11.00	11
21336.095926250...	0.106450418110	63.575308178319	86.468222196869	62.876934840052	59.953017385778	0.039424561935	10.00	12
21661.072243590...	0.112201445836	63.844496164932	78.322681110993	70.400320003082	59.852851616160	0.051130786448	10.00	13
21852.220944431...	0.098431776605	63.229917058040	73.351870983977	76.988446494102	60.082264856620	0.028486107181	9.00	14
22020.068079216...	0.085610705173	63.325674402110	67.337101977032	84.750672722315	60.046349191392	0.082894402326	9.00	15
21908.753193766...	0.110398824267	63.682733956237	72.562812172360	76.494348020752	59.912984997467	0.047858881614	8.00	16
21107.925551102...	0.093220731885	63.783084444011	94.379150295783	56.685329669366	59.875659977392	0.063864204601	8.00	17
22249.599526113...	0.092602685700	62.748126715404	61.913410765069	89.623532884026	60.263949093039	0.099298057636	8.00	18
21625.795304886...	0.073096669011	62.801062047075	79.003970654112	74.054565345812	60.243906274730	0.135570083293	8.00	19
21626.319793853...	0.102925222242	63.181029121801	79.260279615141	70.413771983528	60.100625895758	0.024069382418	7.00	20
21257.589734458...	0.096146099685	62.819519362689	89.565304216880	60.874990889888	60.236922541005	0.060745701582	7.00	21
21864.804085996...	0.102865267300	64.678607301115	73.263969955538	76.801646143856	59.545530200668	0.108246997926	7.00	22
20053.291289134...	0.111809815609	63.099798444222	123.086897601181	28.438878546360	60.131171066507	0.173380079191	7.00	23
19565.697187086...	0.119458654092	62.508421011020	139.115823628540	14.208311103727	60.354961899973	0.271667009008	7.00	24
21983.287139694...	0.100687220713	63.725390169062	70.136425346165	80.154756208138	59.897110840873	0.041381441223	6.00	25
22009.791519100...	0.098188748614	63.942174527309	69.221678175515	81.436252685251	59.816625941397	0.055884999116	6.00	26
22278.724282731...	0.101310007028	63.283942414313	62.733298906545	87.859481252674	60.061993743739	0.073253344478	6.00	27
22110.794050615...	0.111127121969	64.453444189118	67.975227096490	81.340448850699	59.628043033921	0.092775852841	6.00	28
21828.085892581...	0.109713495124	61.850576949705	74.413672486533	74.342072885799	60.606912052860	0.145865706779	6.00	29
22589.933915818...	0.144480599099	62.236679212663	61.580007907360	83.995234148352	60.458464444223	0.217382464809	6.00	30
22459.925705322...	0.066134603553	64.789737109406	43.758200466934	112.400843060968	59.504925120896	0.322751528875	6.00	31
21280.095981141...	0.111181851170	64.090135228192	87.460761596208	61.449969564273	59.761873384062	0.063642370397	5.00	32
22114.127250715...	0.096705164052	63.030863703803	66.301326866834	84.532372263249	60.157129022185	0.076918620323	5.00	33
22255.097096396...	0.118967361571	64.131872576402	65.531722486816	82.993242081309	59.746454800429	0.092492956354	5.00	34
22673.575319443...	0.124292883717	63.098267613563	57.588860305516	90.862934158149	60.131747149931	0.121406964529	5.00	35
22556.210374831...	0.128621032532	62.730282505575	60.521232224454	87.070389556629	60.270709958819	0.130442144591	5.00	36
20636.497691921...	0.079799452559	63.137882085104	115.113540588779	38.423383422966	60.116844706256	0.182705247858	5.00	37
23647.337758978...	0.150877642810	63.851549572642	44.944381356091	102.689037102911	59.850233598589	0.228961845096	5.00	38
22189.813849711...	0.086101406792	66.382978381827	62.279370345762	90.527333920706	58.931104990537	0.296085909624	5.00	39
24629.244800805...	0.177955687081	66.259492722053	36.276014035304	111.153397722881	58.975041490845	0.403501608867	5.00	40
23529.017507265...	0.196345915288	61.260964775548	53.051564062048	87.461685052211	60.835526707965	0.527906993050	5.00	41
20312.171947683...	0.154455509176	57.445430045369	102.760928321898	41.235361908569	62.386152065880	0.628420011131	5.00	42
22575.092387572...	0.114802439505	63.571888238322	58.055684899204	91.483882031248	59.954293123946	0.090141306048	4.00	43
22679.489095546...	0.116133092574	63.313860478459	55.999457144681	93.568942095482	60.050776785566	0.102531587880	4.00	44
21375.059629930...	0.073738508109	62.967934556928	88.052192984141	64.932880508189	60.180854852035	0.115768282525	4.00	45
21333.595141953...	0.075661459624	64.080310095600	89.368030059624	63.597282908594	59.765504651998	0.129319529107	4.00	46
22401.888594962...	0.085465582591	63.507165625462	55.527423231549	97.429763267326	59.978451649020	0.151207950188	4.00	47
23033.224165992...	0.106628507941	63.356514558347	44.837615992011	107.187485404614	60.034795553912	0.158164930403	4.00	48

FIGURE 10. Table of orbital elements.

Orbital Elements Plots | Data Analysis | 3D Vision | Framgents Distributions | Table Orbital Elements | Table Cartesian Elements

ID	Size	Area-to-Mass	area	mass	delta velocity	Vx	Vy	Vz	X	Y	Z
1	128.00	0.12589253...	0.91355975...	7.25666345...	46.7735136...	-42.53991795...	-5.96619002...	-18.50733743...	13462.530324...	-31555.27064...	-28154.63143...
2	83.00	0.13039122...	0.38334300...	2.93994476...	47.1031198...	36.33672361...	10.62813003...	-28.02479740...	14544.200487...	-31327.70542...	-28285.14856...
3	64.00	0.13996591...	0.22764588...	1.62643803...	47.7754138...	-35.96383349...	30.50114898...	7.66633950...	13552.711069...	-31055.17795...	-27795.70026...
4	54.00	0.14902753...	0.16193473...	1.08660947...	48.3786010...	-19.03845574...	-43.75070121...	-7.99389686...	13784.816237...	-32073.42631...	-28010.45599...
5	47.00	0.15868947...	0.12259262...	0.77253159...	48.9902462...	-9.25315686...	-6.25222876...	47.70045022...	13919.006355...	-31559.19322...	-27246.69485...
6	42.00	0.16845508...	0.09784468...	0.58083548...	49.5788928...	-23.66699551...	-39.71676007...	17.90304178...	13721.343030...	-32018.10709...	-27655.31985...
7	38.00	0.17899216...	0.08005735...	0.44726738...	50.1841767...	25.56794327...	41.88715740...	10.49751971...	14396.523454...	-30899.03659...	-27756.87504...
8	35.00	0.18925078...	0.06788940...	0.35872721...	50.7466684...	-3.20554524...	43.37589722...	26.14345770...	14001.939919...	-30878.62085...	-27542.31539...
9	32.00	0.20242297...	0.05672606...	0.28023530...	51.4341967...	-8.84715552...	-2.60162188...	-50.60075100...	13924.574030...	-31509.13084...	-28544.74256...
10	30.00	0.20768998...	0.04984174...	0.23998146...	51.6991155...	-44.27210096...	-6.26592587...	25.95222135...	13438.776134...	-31559.38105...	-27544.93790...
11	28.00	0.21217121...	0.04340360...	0.20456874...	51.9203120...	7.73466104...	45.42786495...	23.92076319...	14151.967792...	-30850.48131...	-27572.79618...
12	27.00	0.21457573...	0.04035179...	0.18805386...	52.0374638...	-31.98773889...	-36.60045123...	-18.57657581...	13607.237008...	-31975.37178...	-28155.58093...
13	25.00	0.21975407...	0.03458262...	0.15736968...	52.2862372...	43.46326604...	-24.47354244...	15.67931218...	14641.929905...	-31809.07013...	-27685.81483...
14	24.00	0.22254739...	0.03186522...	0.14318400...	52.4184894...	-7.20333277...	51.68306955...	-4.96692655...	13947.116496...	-30764.70093...	-27968.94581...
15	23.00	0.22549143...	0.02925924...	0.12975770...	52.5564483...	-20.52121820...	7.33360517...	-47.82549630...	13764.482462...	-31372.88469...	-28556.68427...
16	22.00	0.22859912...	0.02676467...	0.11708127...	52.7005214...	42.84948321...	-5.57125712...	-30.16998251...	14633.512830...	-31549.85476...	-28314.56643...
17	21.00	0.23195189...	0.02438148...	0.10564607...	48.0857918...	37.99317866...	8.22516175...	-29.30385954...	14566.916185...	-31360.65838...	-28288.97546...
18	21.00	0.23197654...	0.02438148...	0.10564607...	59.5741235...	-47.60898778...	-3.92261151...	-35.59597721...	13393.015934...	-31527.24615...	-28388.97548...
19	20.00	0.23536458...	0.02210964...	0.09393785...	53.0088305...	21.56707842...	-6.95844519...	-47.92053093...	14341.657830...	-31568.87788...	-28557.98752...
20	19.00	0.23898904...	0.02000000...	0.08511380...	48.2578998...	-40.16075125...	26.55568358...	-3.27637427...	13495.156886...	-31109.28385...	-27945.76252...
21	19.00	0.23898904...	0.02000000...	0.08511380...	59.9216486...	-28.49183061...	28.61607908...	-44.27120495...	13655.177939...	-31081.02874...	-28507.94271...
22	18.00	0.24286375...	0.01789993...	0.07614188...	48.3543084...	15.64836747...	37.33574776...	26.44446413...	14260.491937...	-30961.45208...	-27538.18756...
23	18.00	0.24286375...	0.01789993...	0.07614188...	60.1047739...	10.46134035...	-42.80466726...	40.87670078...	14189.359947...	-32060.45292...	-27340.27193...
24	17.00	0.24691344...	0.01596200...	0.06791404...	48.4587489...	-8.85566021...	9.34927863...	46.71636349...	13924.457402...	-31345.24287...	-27260.19006...
25	17.00	0.24691344...	0.01596200...	0.06791404...	60.2949693...	-48.37266361...	-24.38447126...	-26.47576828...	13382.543311...	-31807.84866...	-28263.90604...
26	16.00	0.25136985...	0.01413531...	0.06017441...	46.2029143...	12.64183016...	-33.03482764...	-29.72530216...	14219.261965...	-31926.47481...	-28308.46833...
27	16.00	0.25136985...	0.01413531...	0.06017441...	53.7224909...	32.76450385...	41.69117107...	8.62783734...	14495.213062...	-30901.72424...	-27782.51482...
28	16.00	0.25136985...	0.01413531...	0.06017441...	64.8627223...	25.46965737...	-5.39764781...	59.40820399...	14395.175616...	-31547.47397...	-27086.14126...
29	15.00	0.25583104...	0.01241984...	0.05285191...	46.2760744...	-14.38080913...	-21.85161944...	38.17295011...	13848.688598...	-31773.11454...	-27377.34966...
30	15.00	0.25583104...	0.01241984...	0.05285191...	53.9256003...	-31.49773917...	1.75762826...	43.73526663...	13813.956590...	-31449.35052...	-27301.07116...
31	15.00	0.25583104...	0.01241984...	0.05285191...	65.0491605...	-32.98434996...	56.04405443...	1.57794389...	13593.570041...	-30704.89682...	-27879.19311...
32	14.00	0.26040631...	0.01081554...	0.04594153...	48.3585508...	-3.11296226...	-28.52734169...	36.40900267...	14003.209551...	-31864.66166...	-27401.53945...
33	14.00	0.26040631...	0.01081554...	0.04594153...	54.1406386...	-46.32602375...	24.45569809...	-13.67578957...	13410.609786...	-31138.08188...	-28088.37423...
34	14.00	0.26040631...	0.01081554...	0.04594153...	65.2449219...	58.36978873...	-9.12792025...	-27.68661555...	14846.349623...	-31598.62885...	-28280.51092...
35	13.00	0.26495050...	0.00932239...	0.03961180...	43.7344528...	20.32577108...	18.06276015...	-34.25349757...	14324.635235...	-31225.75106...	-28370.56547...
36	13.00	0.26495050...	0.00932239...	0.03961180...	48.9805422...	5.23643051...	-48.45310253...	4.89593437...	14117.708455...	-32137.91241...	-27833.69205...
37	13.00	0.26495050...	0.00932239...	0.03961180...	54.3689854...	38.54328587...	34.52790271...	16.68009662...	14574.460048...	-30999.95730...	-27672.09063...
38	13.00	0.26495050...	0.00932239...	0.03961180...	61.1436489...	16.91644225...	14.01406546...	57.06124563...	14277.881606...	-31281.27259...	-27118.32613...
39	13.00	1.01144714...	0.00932239...	0.03961180...	70.9559204...	44.41314830...	20.18638526...	-51.52402119...	14654.956059...	-31196.62885...	-28607.40377...
40	12.00	0.09040545...	0.00794035...	0.03376180...	43.7762874...	-1.38164681...	43.73866677...	-1.17619167...	14026.951843...	-30873.64603...	-27916.96179...
41	12.00	0.16121449...	0.00794035...	0.03376180...	49.1451670...	9.47644241...	-39.89026790...	-27.09632829...	14175.853608...	-32020.48648...	-28272.41605...
42	12.00	0.27318155...	0.00794035...	0.03376180...	54.6122758...	-50.11509094...	-1.19235750...	21.66925505...	13958.648637...	-31489.80497...	-27603.67211...
43	12.00	0.49007679...	0.00794035...	0.03376180...	61.3836667...	48.67898558...	28.51437828...	24.19175752...	14713.455367...	-31082.42341...	-27569.07992...
44	12.00	1.02545622...	0.00794035...	0.03376180...	71.1513960...	-1.71620431...	-13.54908257...	-69.82834780...	14022.363908...	-31659.25819...	-28858.41907...
45	11.00	0.02400097...	0.00666937...	0.02835180...	33.5773012...	-15.03143473...	-29.28277500...	6.63401975...	13839.766283...	-31875.02125...	-27809.85692...
46	11.00	0.04331183...	0.00666937...	0.02835180...	41.2729484...	-14.20538381...	38.61495768...	-3.24782850...	13851.094283...	-30943.90971...	-27945.37106...
47	11.00	0.06734843...	0.00666937...	0.02835180...	44.6683567...	20.92693429...	24.96772968...	-30.56039907...	14332.879251...	-31131.06016...	-28319.92038...
48	11.00	0.09999997...	0.00666937...	0.02835180...	48.3431049...	-14.95686629...	-40.01451408...	-22.63154010...	13840.788873...	-32022.19032...	-28211.18844...
49	11.00	0.14848162...	0.00666937...	0.02835180...	52.8054351...	49.90476542...	5.88115990...	16.22776399...	14730.265026...	-31392.80271...	-27678.29367...
50	11.00	0.23088362...	0.00666937...	0.02835180...	59.4229555...	13.53905718...	-28.23133986...	-50.50493688...	14231.578377...	-31860.60246...	-28593.42862...
51	11.00	0.41664986...	0.00666937...	0.02835180...	33.0992961...	4.61492059...	-16.44638735...	-28.35105391...	14109.185416...	-31698.99021...	-28289.62266...
52	10.00	0.02234054...	0.00550940...	0.02331180...	37.0206213...	8.37872001...	-15.00189586...	-32.79125762...	14160.800056...	-31679.18126...	-28350.51313...
53	10.00	0.03910375...	0.00550940...	0.02331180...	40.1849032...	28.19688674...	-19.59225235...	-20.97835417...	14432.575315...	-31742.13084...	-28187.14623...
54	10.00	0.05892704...	0.00550940...	0.02331180...	43.1618343...	-21.87341848...	36.83751150...	5.24359190...	13745.939143...	-30968.28461...	-27828.92447...
55	10.00	0.08429633...	0.00550940...	0.02331180...	46.2274673...	16.10696817...	28.76357710...	-32.40680396...	14266.780931...	-31079.00604...	-28345.24094...
56	10.00	0.11871360...	0.00550940...	0.02331180...	49.6520366...	21.67115770...	-2.30338186...	44.61367614...	14343.085115...	-31505.04094...	-27289.02514...
57	10.00	0.16970136...	0.00550940...	0.02331180...	53.9666667...	43.16680910...	20.91006100...	7.00314330...	14534.149449...	-31232.20364...	-27600.00000...

FIGURE 11. Table of generated fragments.

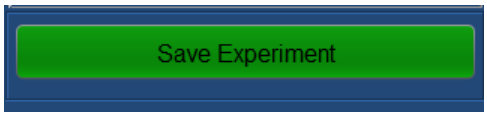


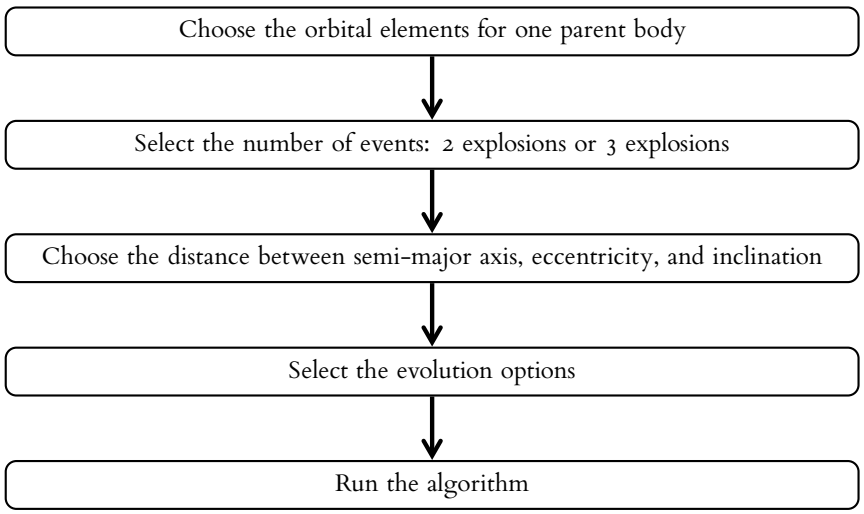
FIGURE 12. Save experiment button.

4. Option 2: generate multiple break-up events

The first option of SIMPRO reproduces the break-up model Evolve 4.0 provided by NASA in [3] to generate two or three explosions and to analyze their evolution.

The work-flow is described in Section 4.1, the choice of the orbital elements is shown in Section 4.2, the selection of the number of break-up events is found in Section 4.3, while Section 4.4 shows how to get the evolution of the generated fragment on a given time interval, and Section 6.7 describes the different outputs generated by SIMPRO for multiple break-up events.

4.1. **Work-flow.** The work-flow below reproduces the left column that appears when opening SIMPRO for the second option of multiple break-up events.



4.2. **Choosing Orbital Elements.** Choose the orbital elements of the parent body (where the break-up event will happen), see Figure 1.

- Semi-major axis in km: $a > 6400$ km and $a < 45000$ km.
- Eccentricity $e \in [0, 0.75]$.
- Inclination in degrees: $i \in [0, 180^o]$.
- Mean anomaly in degrees: $M \in [0, 360^o]$.
- Argument of perigee in degrees: $\omega \in [0, 360^o]$.
- Argument of the ascending node in degrees: $\Omega \in [0, 360^o]$.

4.3. **Number and Distance between Events.** Select the number of break-up events, either 2 or 3 bodies (see Figure 14).

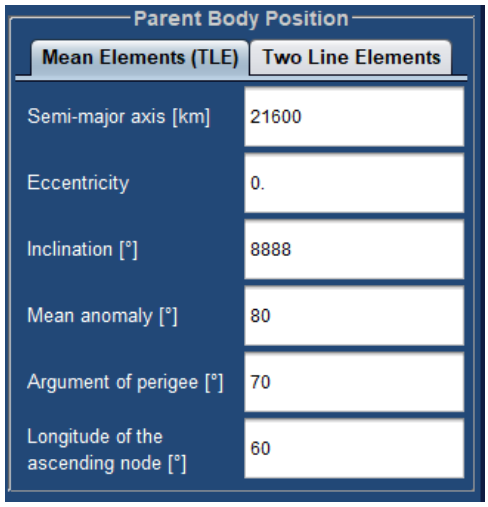


FIGURE 13. Choice of the orbital elements.

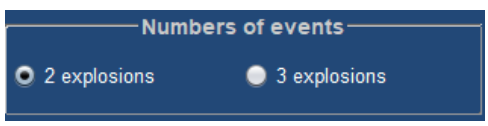


FIGURE 14. Selection of the number of break-up events.

Choose the distance in terms of a, e, i from the orbital elements of the first parent body (see Figure 15).

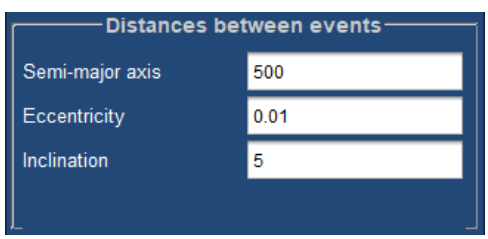


FIGURE 15. Distances of the orbital elements.

4.4. **Fragments' propagation.** To propagate the generated fragments, select Toggle activation with a LEFT CLICK and set the options with a RIGHT CLICK. One can choose "short-term" and "long-term" propagation, providing the period and step, the initial time and selecting the forces one wants to include in the propagation, namely the J_2 and J_3 terms of the geopotential, the effects of Moon and Sun, the Solar radiation pressure, and the drag effect due to the Earth's atmosphere, see Figure 16.

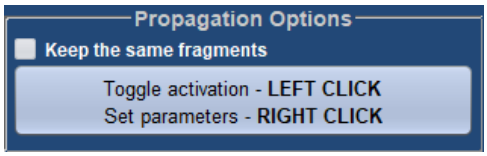


FIGURE 16. Propagation options.

4.5. **Output.** The output panel has two different frameworks, according to whether the orbits are propagated or not.

4.5.1. *Orbital Elements Plots.* The orbital elements a, e, i are plotted in the 2-dimensional planes of $a-e$, $a-i$, and $e-i$; Figure 17 shows the output without (left panel) and with propagation of the orbits (right panel).

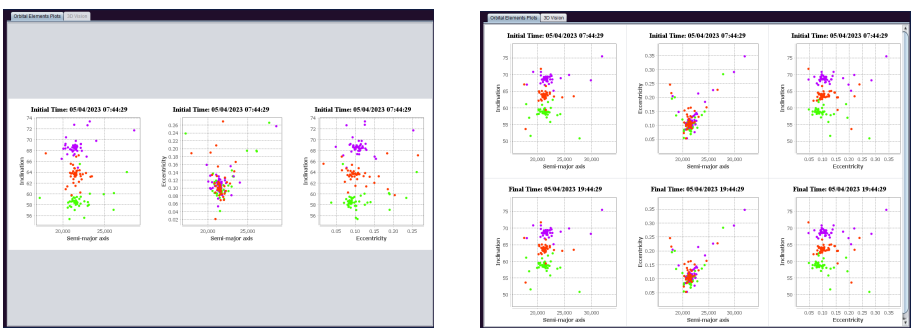


FIGURE 17. Plots of the orbital elements without and with propagation.

4.5.2. *3D Orbit Vision.* This page allows to visualize the position of the generated fragments in a 3-dimensional space, whenever the propagation has been computed. An example is given in Figure 18 with the following description, where the blue dots make the contour plot of the Earth surface:

- Top-left: parent body position at break-up time.
- Top-right: fragments' orbits after 3 hours.
- Bottom-left: fragments' position after 6 more hours.
- Bottom-right: fragments' orbits after 3 more hours.

Each panel has additional options to zoom and move the graphs, rotate the plot, reset the zoom, modify the scale settings, save the picture, have a list of Cartesian coordinates (X, Y, Z) of each fragment at a given time, the coordinates of the parent body that gives the orbit, the coordinates of the blue dots representing the Earth. An option allows to decide whether visualize the fragments, parent body, and the Earth.

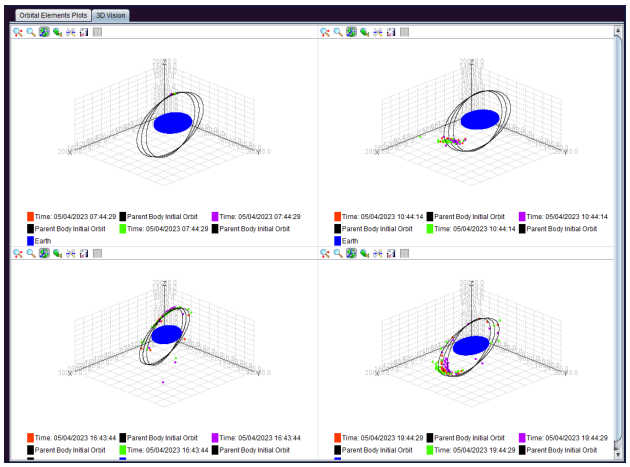


FIGURE 18. 3D plots.

5. OPTION 3: SAVED EXPERIMENTS

If an experiment is saved using Option 1, it can be retrieved using the third option, which allows one to see the elements and plots of the saved experiment, see Figure 19.

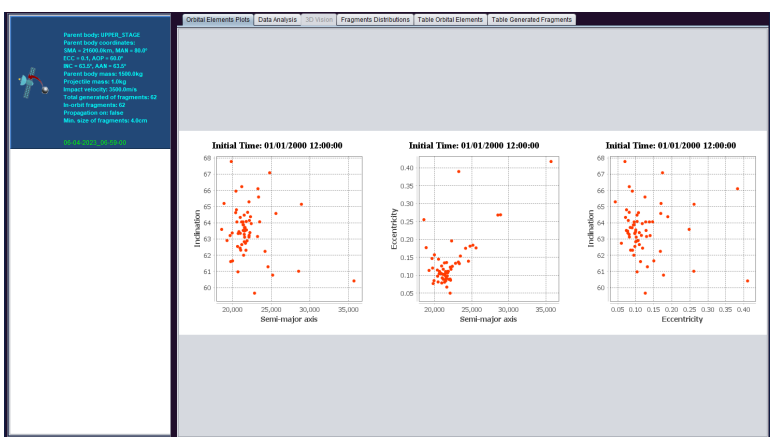


FIGURE 19. Saved experiments.

Pressing double click on one element on the left list will open the page from Option 1 using the input data of the selected experiment.

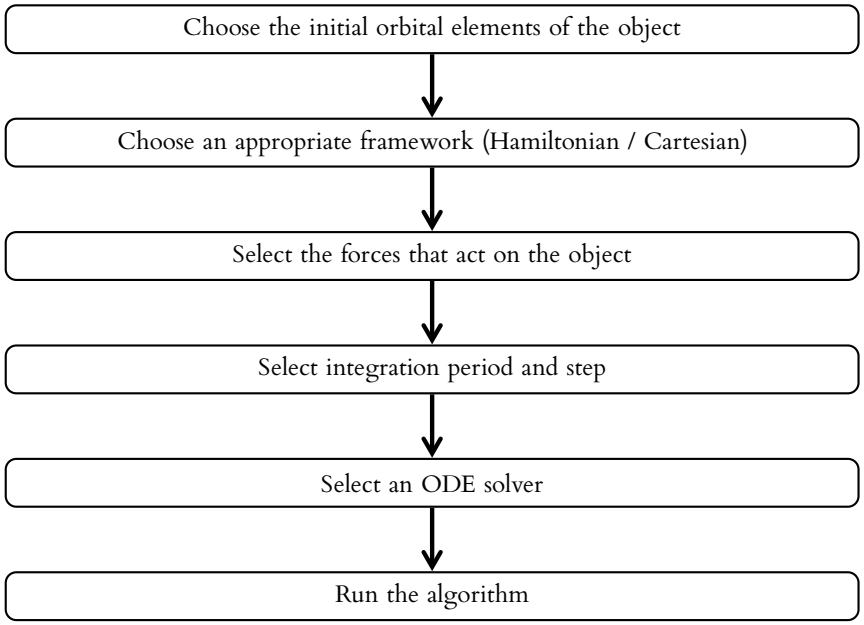
6. Option 4: Orbits' propagator

This option allows one to propagate the orbit of an object around the Earth, taking into account different forces.

The work-flow is described in Section 6.1, the choice of the orbital elements is given in Section 6.2, the selection of the forces is shown in Section 6.4, the selection of the framework, either Cartesian or Hamiltonian, is given in Section 6.3, the choice of the parameters is described in Section 6.5, the integration method can be chose as described in Section 6.6, Section 6.7 describes the different outputs generated by SIMPRO, while Section 6.8 gives the propagation history.

6.1. **Workflow.**

This section reproduces the left column that appears when opening SIMPRO for the fourth option.



A summary of the equations and parameters used to propagate the orbits is shown when clicking on Formulas - More Info, see Figure 20.

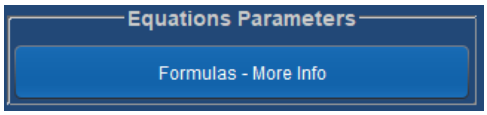


Figure 20. Equations and parameters for the propagation.

6.2. **Choosing Orbital Elements.** Choose Mean elements (TLE), which allows to select the orbital elements to be propagated.

- Semi-major axis in km: $a > 6400$ km and $a < 45000$ km.
- Eccentricity $e \in [0, 0.75]$.
- Inclination in degrees: $i \in [0, 180^o]$.
- Mean anomaly in degrees: $M \in [0, 360^o]$.
- Argument of perigee in degrees: $\omega \in [0, 360^o]$.
- Argument of the ascending node in degrees: $\Omega \in [0, 360^o]$.

An example is given in Figure 21.

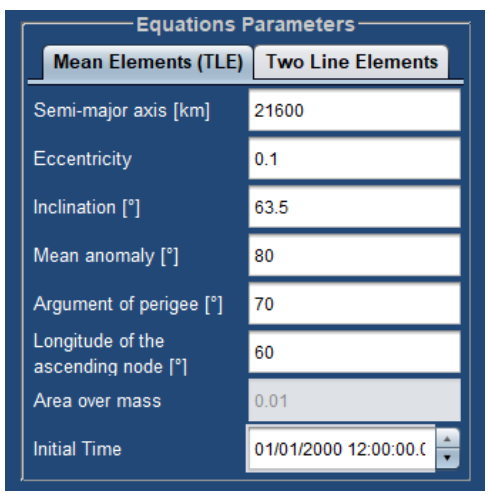


FIGURE 21. Orbital elements of the parent body.

Alternatively, choose Two Line Elements and provide the data in LINE 1 and LINE 2 using the NORAD format from CelesTrak.

6.3. **Selecting the framework.** Select the framework to be used for the propagation of the orbits (see Figure 22).

(1) For a long-period integration, select Hamilton's equations.
(2) For a short-period integration, select Cartesian equations.
(3) For a simplified perturbation model, select SGP4.
(4) For a comparison between Hamiltonian and Cartesian propagation, select "Hamiltonian vs Cartesian".
(5) For a comparison between Cartesian and SGP4 propagation, select "Cartesian vs SGP4".

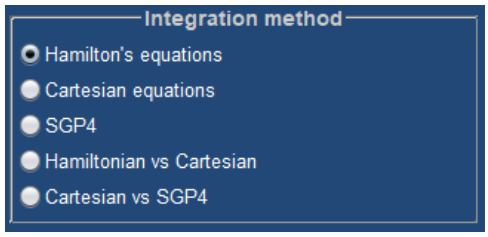


FIGURE 22. Selection of the integration framework.

6.4. **Selecting the forces.** Choose the forces that act on the object, among the following options (see Figure 23).

(1) Geopotential: J2 and J3 effects.
(2) Moon and Sun attraction.
(3) Solar radiation pressure (for a given A/m).
(4) Drag effect.

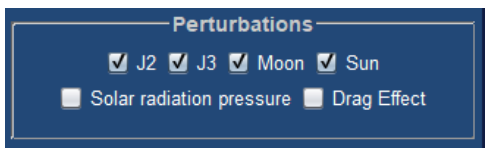


FIGURE 23. Selection of the forces.

6.5. **Choosing the integration time and step.** In the box shown in Figure 24, select the integration period in days and the integration step in minutes.

(1) In case of Cartesian equations, it is convenient to select a time period between 1 day and 366 days with a time step of 1-5 minutes.
(2) In case of Hamilton's equations, it is convenient to select a time period between 1 year and 500 years with a time step of 1-10 days.

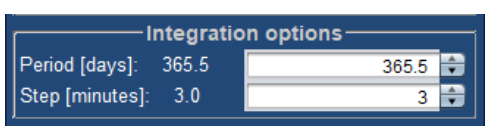


FIGURE 24. Select the integration options.

6.6. **Choosing the integration method.** In the box shown in Figure 25, select the integration method: Runge-Kutta or Adams-Bashforth-Moulton.

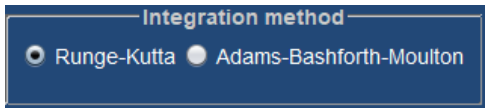


FIGURE 25. Integration method.

6.7. **Output.** The output of the integration consists in plotting the time evolution of the orbital elements $a, e, i, M, \omega, \Omega$, see Figure 27. For each run, one experiment page is created.

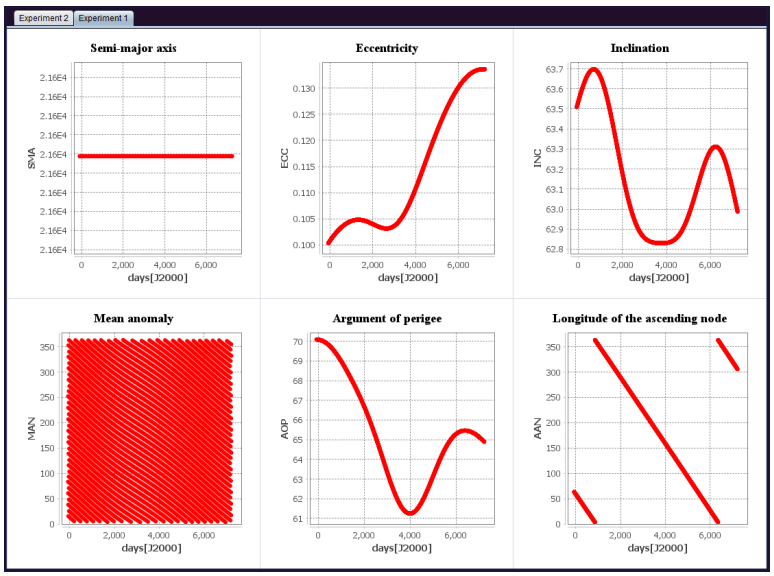


FIGURE 26. Output of the propagation.

6.8. **Propagation history.** The propagator stores up to 10 experiments on a single session (see Figure 27). Once the application is closed, all the experiments are erased.

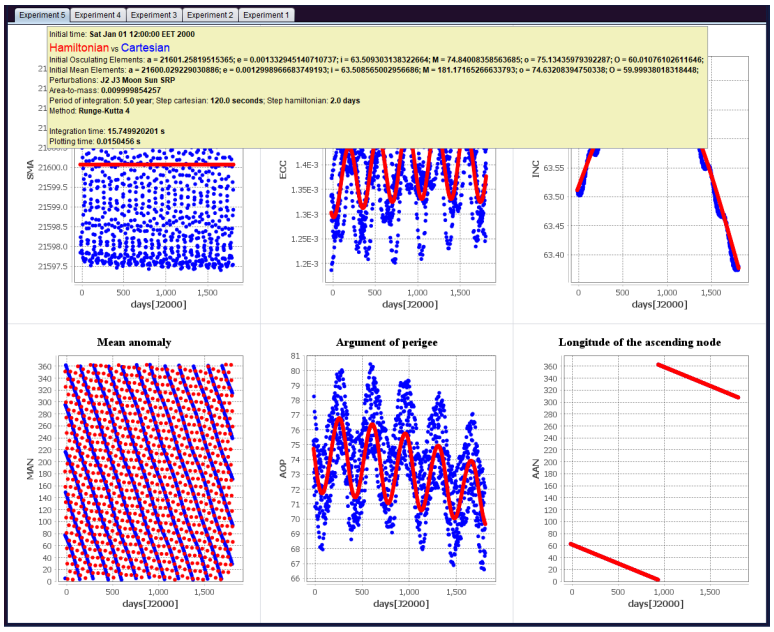


FIGURE 27. Different saved experiments.

7. Option 5: User guide page

The option n. 5 allows the user to get access to an information page containing slides to illustrate graphically the overall program and each option, see Figure 29.

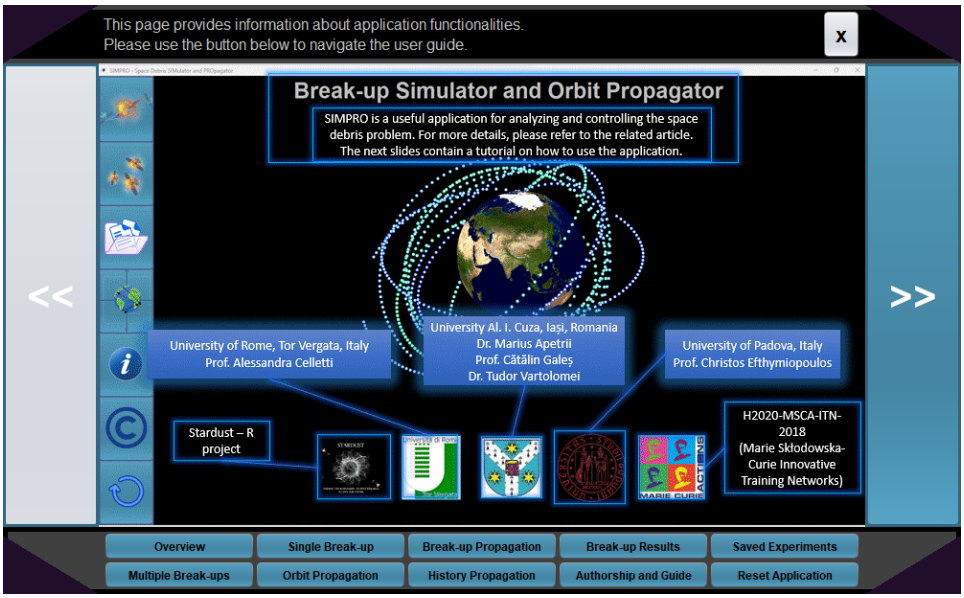


Figure 28. User guide page.

8. Option 5: Copyright page

This page displays the detail of the related article and authorship of SIMPRO, see Figure29.

Figure 29. Copyright and contact page.

9. Option 6: Reload application button

The last option reloads the program, removing any existing experiment from Option 1 and Option 2 and erasing all experiments from Option 4, see Figure 30.

Figure 30. The reload button.

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References

[1] AAVV, *NASA Standard Breakup Model 1998 Revision,* prepared by Lockheed Martin Space Mission Systems & Services for NASA, July 1998.
[2] M. Apetrii, A. Celletti, E. Efthymiopoulos, C. Gales, T. Vartolomei, *Simulating a breakup event and propagating the orbits of space debris*, Preprint (2023)
[3] N. L. Johnson, P. H. Krisko, J.-C. Lieu, and P. D. Am-Meador, *NASA's new breakup model of EVOLVE 4.0,* Adv. Space Res., 28, n. 9, 1377-1384 (2001)

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