

26/7/2017

System Programming

System - Consists of hardware components and s/w components or programs.

System Programming

Involves designing & writing computer programs that allow computer hardware to interface with programmer & user, leading to effective execution of application s/w on the computer system.

Language Processors

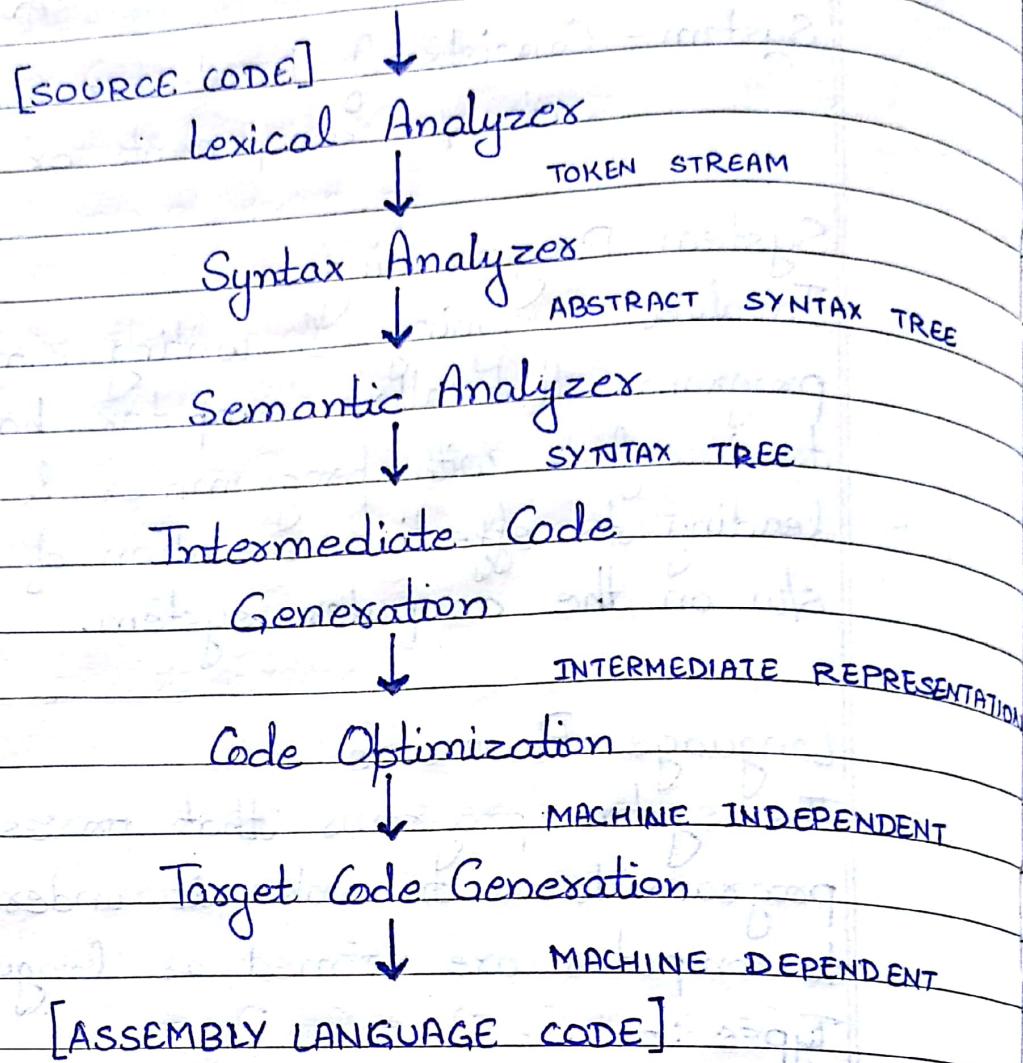
The system programs that process HLL program to as to make it understandable to computer are termed as language processor

Types :-

1. Assembler - Converts program written in assembly language into machine language.
2. Interpreter - Converts HLL program into machine language, by converting & executing it line by line.
3. Compiler - Also converts HLL program into machine language but converts entire program in one go.

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Compiler Architecture



1. Lexical Analyzer

- Works as text scanner. It scans the source code as a stream of characters & converts into tokens.

2. Syntax Analysis

- Takes token produced by lexical analysis as input & generates a parse tree.
- In this phase, token arrangements are checked against the source code grammar (i.e. checks if expression made by tokens is

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syntactically correct)

Semantic Analysis

3.

- Checks whether the parse tree constructed follows the rules of language.
eg- datatypes are compatible or not.
- Also keeps track of identifiers, their types & expressions.

4.

Intermediate Code Generation

- In this phase, the compiler generates a intermediate code of source code for the target code machine.
- It is in b/w HLL & machine language

5.

Code Optimisation

- Some unnecessary code lines are removed from the intermediate code.

6.

Target Code Generation

- In this phase, the code generator takes the optimised code & maps it to target machine language.
- The code generator translates the intermediate code into sequence of instructions or machine code.

Symbol Table

- A data structure maintained throughout all the phases of compiler.
- All the identifier's names & their types are stored here.

Error Handling

- Each phase can encounter errors. After detecting an error, a phase must handle the error so that compilation can proceed.

Illustrative Example

Source code :- $x = a + b * 6.5;$

1. > Lexical analyzer

$$(id_1) = (id_2) + (id_3) * (6.5);$$

Symbol Table

symbol name	type	address
x	int	---
a	int	---
b	int	---

2. > Syntax Analysis

→ PRODUCTION RULE

$$S \rightarrow id = E$$

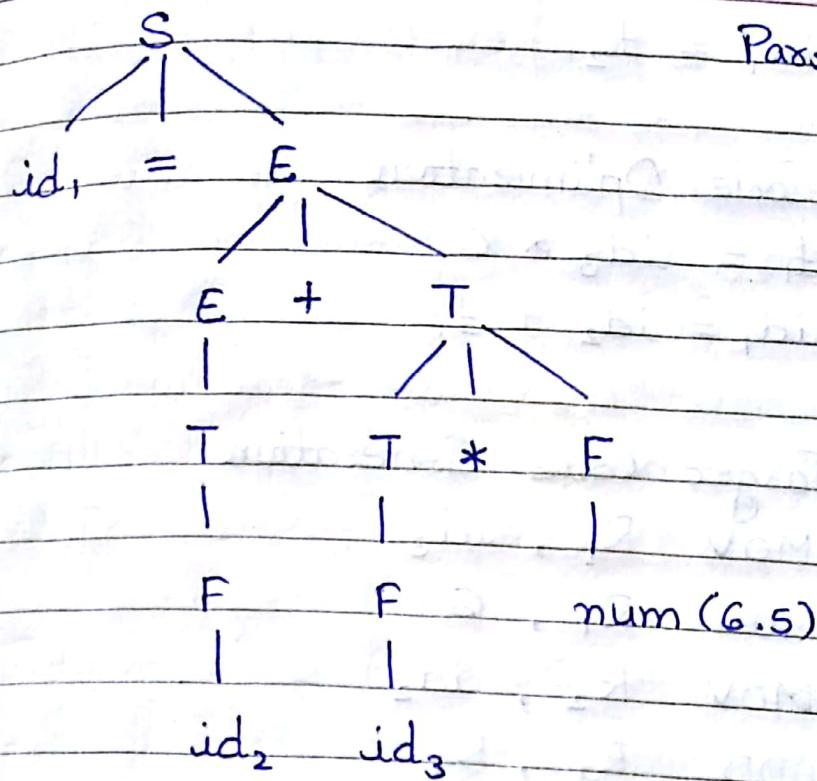
$$E \rightarrow E + T / T$$

$$T \rightarrow T * F / F$$

$$F \rightarrow id / num$$

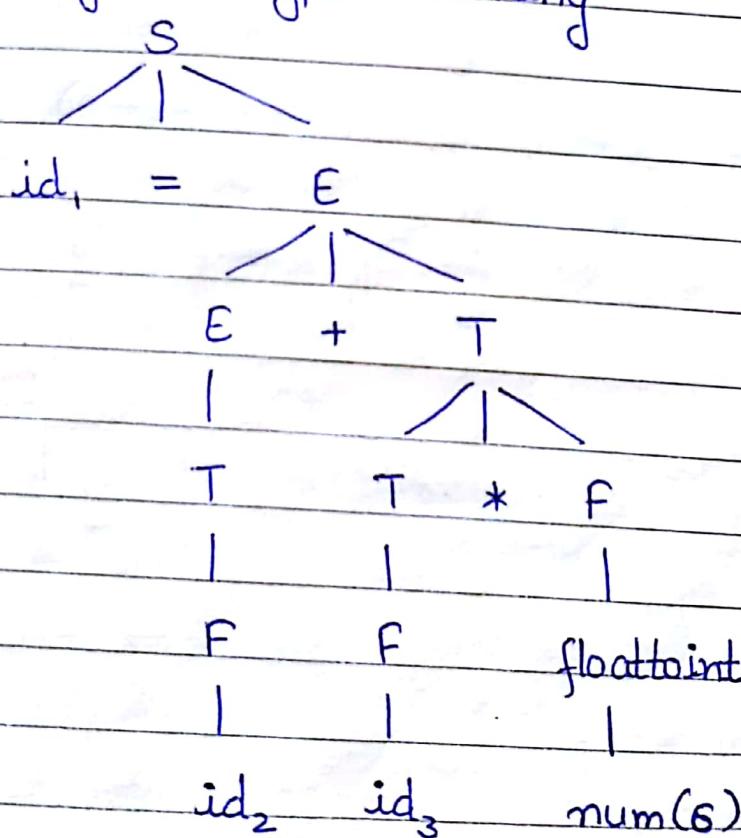
} Starting symbol(s)
} Terminating symbol
} (small letters)
} Non-terminating

Parse Tree



3.) Semantic Analysis

→ Performs type checking



4.) Intermediate Code Generation

$$t_1 = id_3 * \cancel{num\ 6}$$

$$t_2 = id_2 + t_1$$

$$id_1 = t_2$$

5.) Code Optimization

$$t_1 = id_3 * 6$$

$$id_1 = id_2 + t_1$$

6.) Target Code Generation

MOV R₁, id₃

MUL R₁, 6

MOV R₂, id₂

ADD R₂, R₁

MOV id₁, R₂

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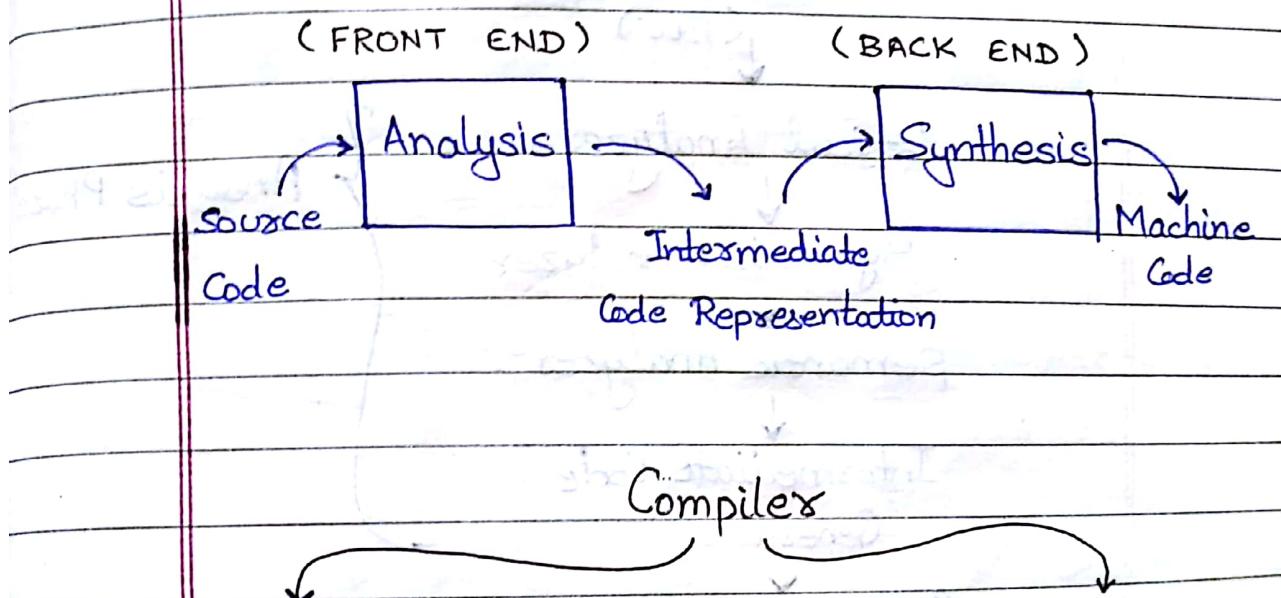
Phases of Compilation

1. Analysis Phase

- Known as front end of compiler
- Reads the source code, checks for lexical grammar & syntax errors.
- Then generates an intermediate representation of source code & a symbol table.

2. Synthesis Phase

- Known as back end of compiler.
- Generates target program with the help of intermediate source code representation.



Single Pass Compiler

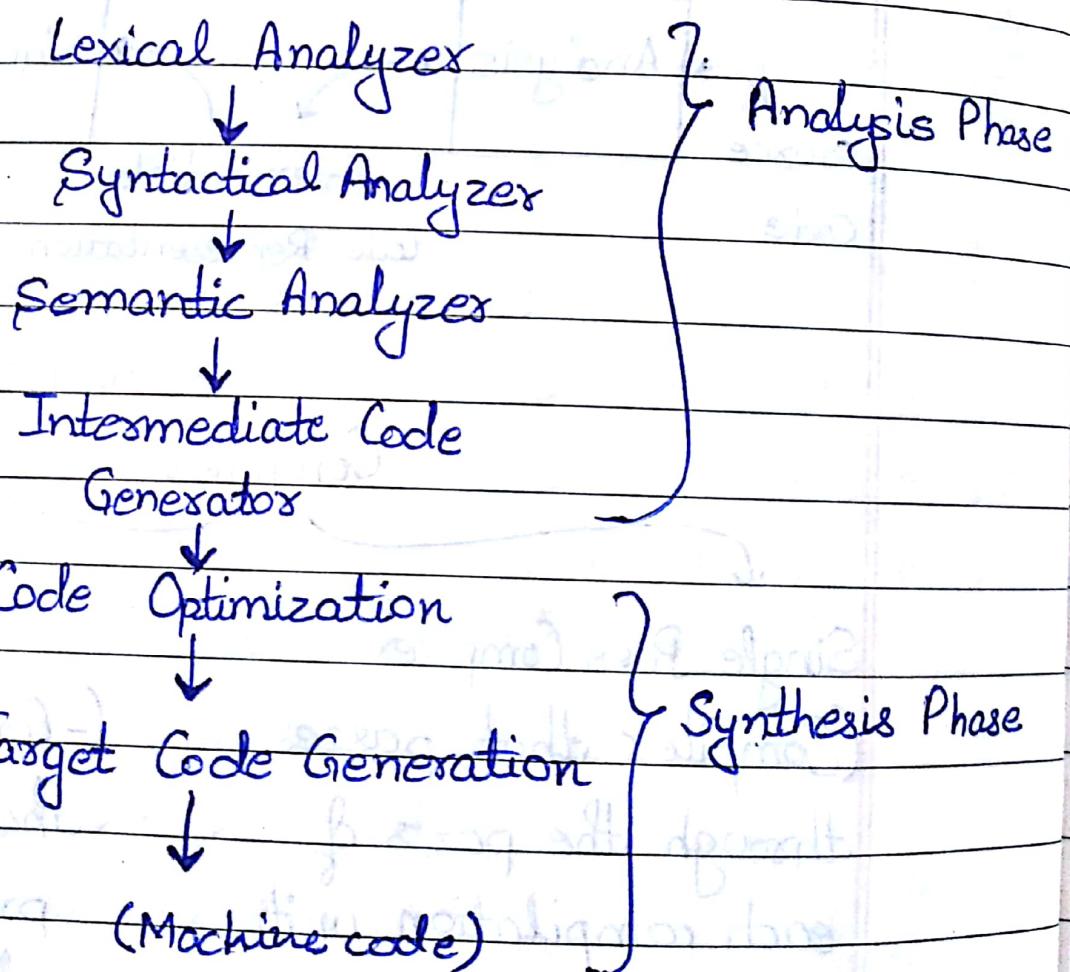
(Compiler that passes through the parts of each compilation unit only once, immediately translating each part into its final machine code.)

Multi Pass Compiler

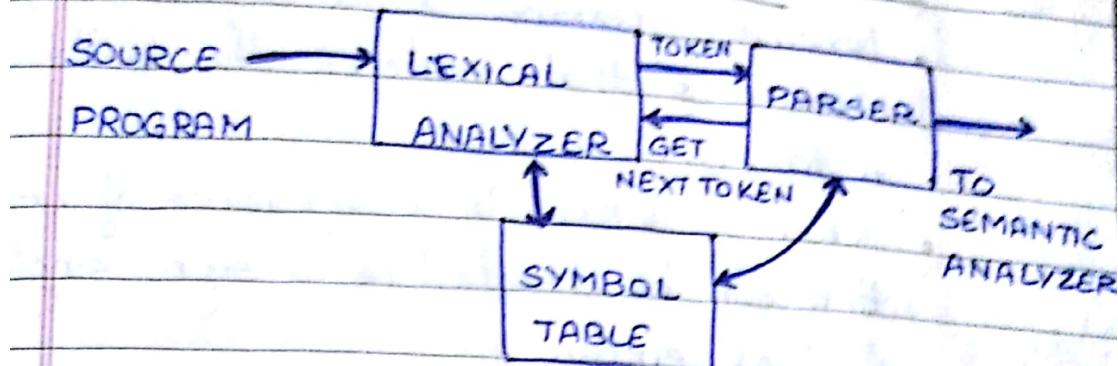
(Compiler that processes the source code of a program several times)

Single Pass Compiler	Multipass Compiler
- Takes less time for compilation	- Takes more time for compilation.
- Limited scope of passes	- Wide scope of passes
- Produces less efficient programs.	- Helpful in optimizing code.
- Machine Dependent	- Machine Independent
- Requires more memory space.	- Requires less memory space.
- Used by languages like C++, Java	- Java compilers are multipass compilers

(ANSI - IEEE) (HLL) (ANSI - IEEE)



ECE LEXICAL ANALYSER



Role of Lexical Analyzer

- It reads the input characters of source code & group them into lexemes.
- Then breaks these lexemes into a series of tokens, by removing any whitespace or comments in the source code.
- If it finds a token invalid, it generates an error message, with its occurrence by specifying its line no.

Lexical analysis consists of 2 stages of processing -

- Scanning - Reading input characters & removing whitespaces & comments.
- Tokenization - Produce tokens as output.

Need of Lexical Analyzer

- Simplicity of design of compiler
- Compiler efficiency is improved
- Compiler portability is enhanced.

Lexeme and Tokens

- Lexeme - Lexeme is a sequence of characters that matches the pattern for a token.
- Token - Token is a sequence of characters that can be treated as a single logical entity.

Common tokens in a programming language are :-

- Keywords
- constants
- Identifiers
- Numbers
- Punctuation symbols

Specification & Recognition of Tokens

There are some predefined rules for a lexeme to be a token.

- Valid tokens - keywords, punctuation marks, semicolon, numbers etc.
- Non tokens - Comments, blanks, tabs, macros etc.

eg- int a, b ;

has 4 tokens.

printf("Hello");

has 5 tokens

Practice Question

1. Count no. of tokens

a) int max(i, j)

{ // max of i & j

return i > j ? i : j;

}

18 tokens

b) int main()

{ int a = 10, b = 20;

printf("sum is : %d", a+b);

return 0;

}

27 Tokens

c) printf("i = %.d, &i = %x", i, &i);

10 Tokens

1) Lexical Analyzer

→ Scanner
→ Lexcial Analysis

TOKEN	INFORMAL DESCRIPTION	EXAMPLE
IF	characters i, f	if
ELSE	characters e, l, s, c	else
comparison	< or > or <= or =>	>, =>, =<
id	letter followed by letter / digit	variable name
number	constant	23
literal	inside "	"total=%d"

Input Buffering

eg -

if(2>3)

i	f	(2	>	3)	[eof]
---	---	---	---	---	---	---	-------

↓ ↗
lexeme forward
begin Pointer

Terms related to strings

- Prefix
- Suffix
- Substring
- Proper prefix
- Proper suffix
- Proper substring
- Subsequence

- 1) Prefix - string obtained by removing zero or more trailing symbols from a string.
eg- pre is prefix in present prepaid
- 2) Suffix - string obtained by removing zero or more leading symbols from a string.
- 3) Substring - string obtained by removing prefix & suffix
- 4) Proper prefix or proper suffix - string obtained by ~~then~~ removing leading or trailing symbols that are not null.
- 5) Subsequence - string obtained by deleting zero or more arbitrary symbols.
eg- strn is a subsequence of string.

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Transition Diagram.

Relational Operation

Lexeme Attribute

> (GE) greater than

Token Name

RELOP

< (LT) less than

>= (GE) greater than/equal to

"

<= (LE) less than /equal to

"

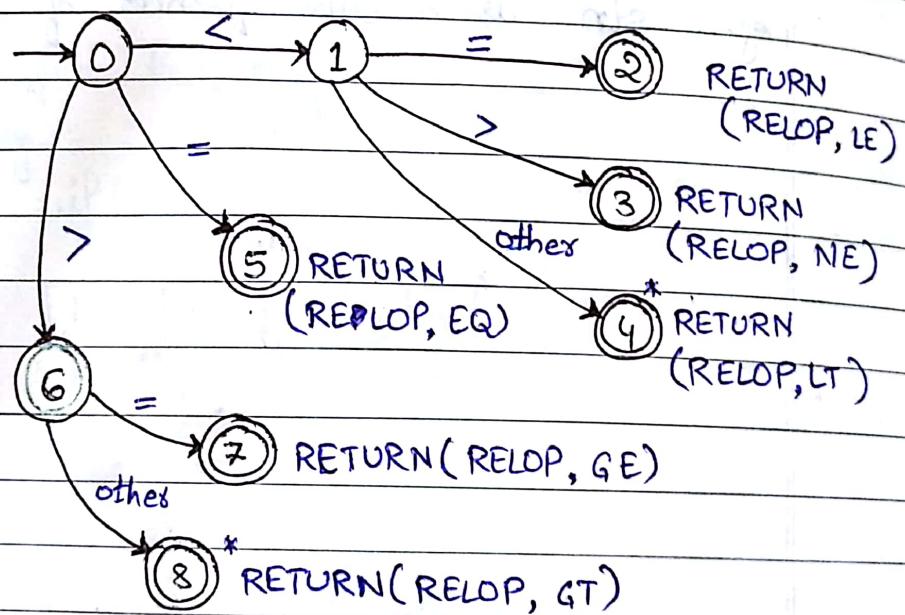
<> (NE) not equal to

"

= (EQ) equal to

"

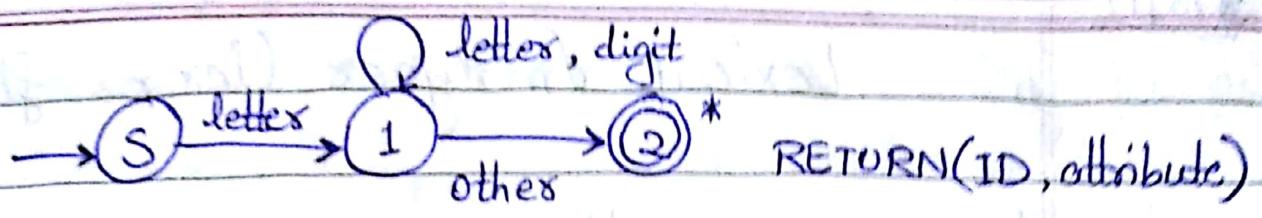
FA Transition Diagram.



* → Represents we need to go a step back

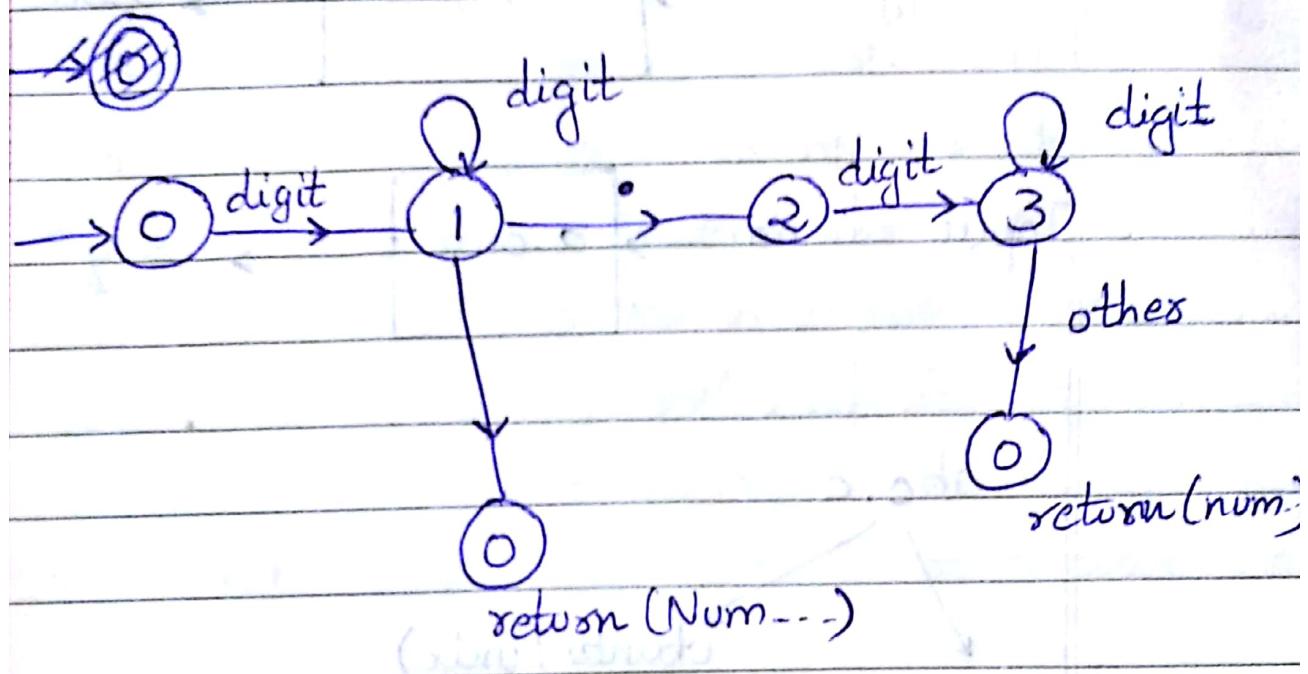
Transition Diagram for Reserve word & Identifier

id → (letter) (letter*)/digit)*

Number

$\text{num} \rightarrow \text{digit}(\cdot / \text{digit})$

$\text{digit} \rightarrow \text{digit}^+$

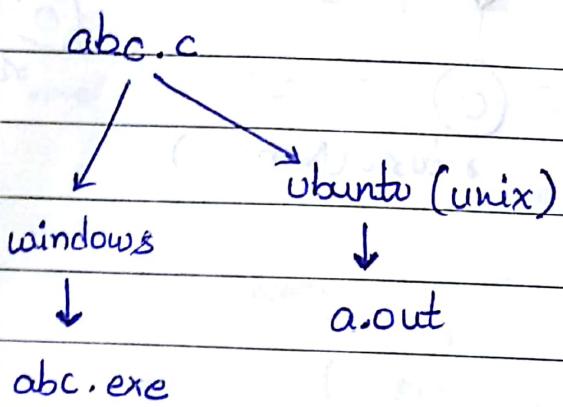
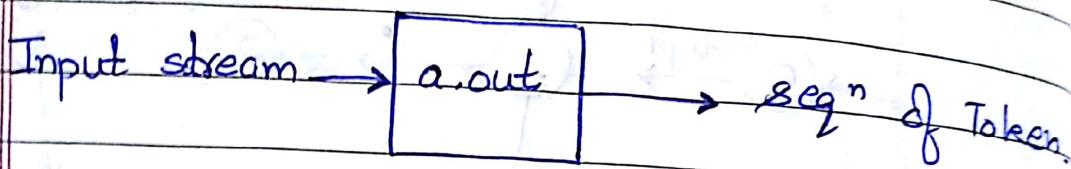
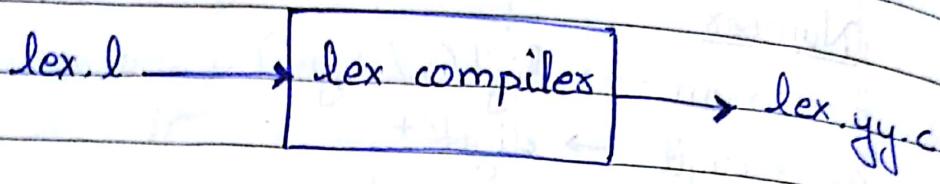


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Lexical Analyzers (lex or flex)

- Lex is a compiler



What is lex?

- Lex is a computer program that generates lexical analyzers.
- Its main job is to break up an input stream into more usable elements.

Regular Expressions (REGEX)

SYMBOL	DESCRIPTION
.	any character
^	beginning of line
\$	end of line
[abc]	any of a, b or c
[^abc]	neither a, b nor c
x*	zero or more string matching x
x ⁺	one or more string matching x
x?	zero or one more x
x ₁ x ₂	x ₁ , followed by x ₂
x ₁ x ₂	x ₁ , or x ₂
x ^{m,n}	b/w m & n occurrences of x
" s "	matching string s

- * In unix, "grep" command is used for REGEX searching.

ex - \$ grep a.pple fruit
 ↓ ↓
 for matching filename

⇒ a.pple will look for such matchings where starting letter is 'a' & last 4 letters are 'pple' & second letter can be any character.

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Example - A filename "fruits", that has contents as :-

Apple

Apple Red

apple

An Apple

aPPLE

mango

aPple

abple

Write the correct answers for the following -

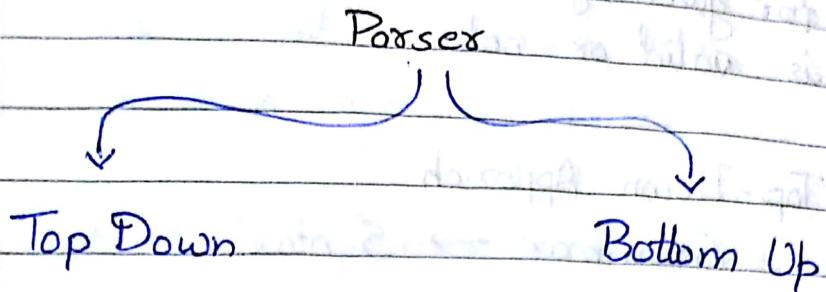
a) a.ble - apple, aPple, abple

b) [aA]bble - Apple, apple

c) apple/Apple - Apple, apple

d) ^Apple - Apple, Apple Red

e) Apple \$ - Apple, An Apple

2) Parsing

Grammar - A grammar can be defined as

$$G = (V, T, S, P)$$

Starting symbol set
 Production rule
 Set of terminal symbols

Set of non-terminal

Symbol

$S \rightarrow$ starting symbol

Capital letter \rightarrow non-terminal symbol (V)

Small letter \rightarrow set of Terminal symbol (T)

$$\text{eg} - S = \{S\}$$

$$T = \{a, b, c, d, \dots\}$$

$$V = \{S, A, B, \dots\}$$

$$P = \{S \rightarrow cAd\}$$

$$A \rightarrow abId\}$$

Example - $E \rightarrow TE'$

$$E' \rightarrow + TE' / E$$

$$T \rightarrow FT'$$

$$T' \rightarrow * FT' / \epsilon$$

$$F \rightarrow (E) / id$$

E is starting symbol

T₀ Terminal symbol = {+, *, ε, (,)}

Non-terminal symbols = { E, T, E', T', F }
 for given grammar check id + id * id
 is valid or not.

a) Top-Down Approach

Grammar \rightarrow Syntax

\Rightarrow Root \rightarrow Leaf

$$E \Leftrightarrow E$$

T E'

[left most derivative
is taken first]

E
T E'

F T'

E

T E'

F T' ± T E'
 \Rightarrow Parse (Syntax)
 \Rightarrow Tree

id \in F T'

id * F T'

id

E

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Thus, given syntax satisfied by the grammar

$$\begin{aligned} id &\in + id * id \\ &= id + id + id \end{aligned}$$

b) Bottom - Up Approach

Syntax \rightarrow Grammar

Leaf \rightarrow Root

$id * id$



Example: Grammar

$$E \rightarrow E + T \mid T$$

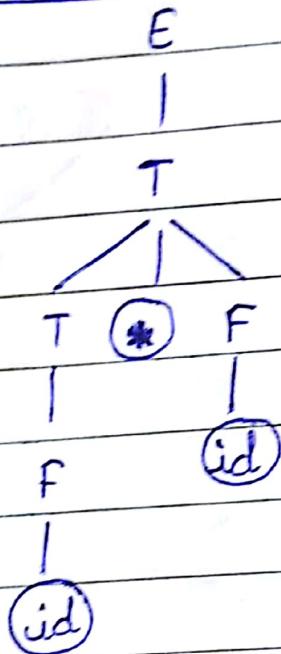
$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid id$$

Syntax

$id * id$

a) Top-Down Parsing

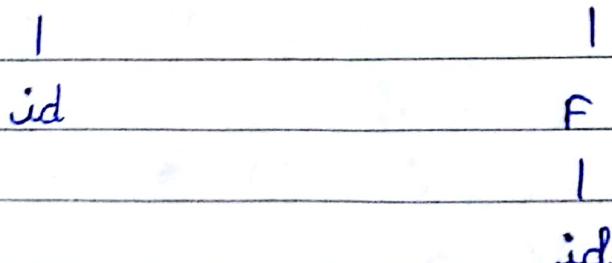


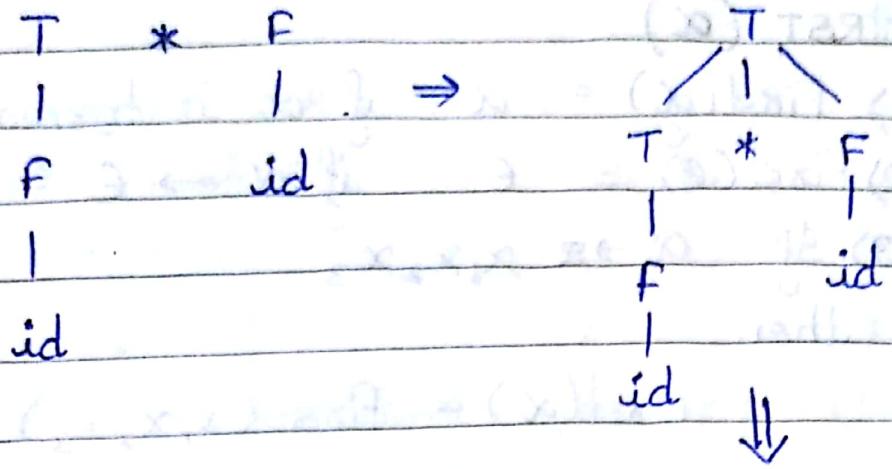
b) Bottom-Up Parsing

$id * id$

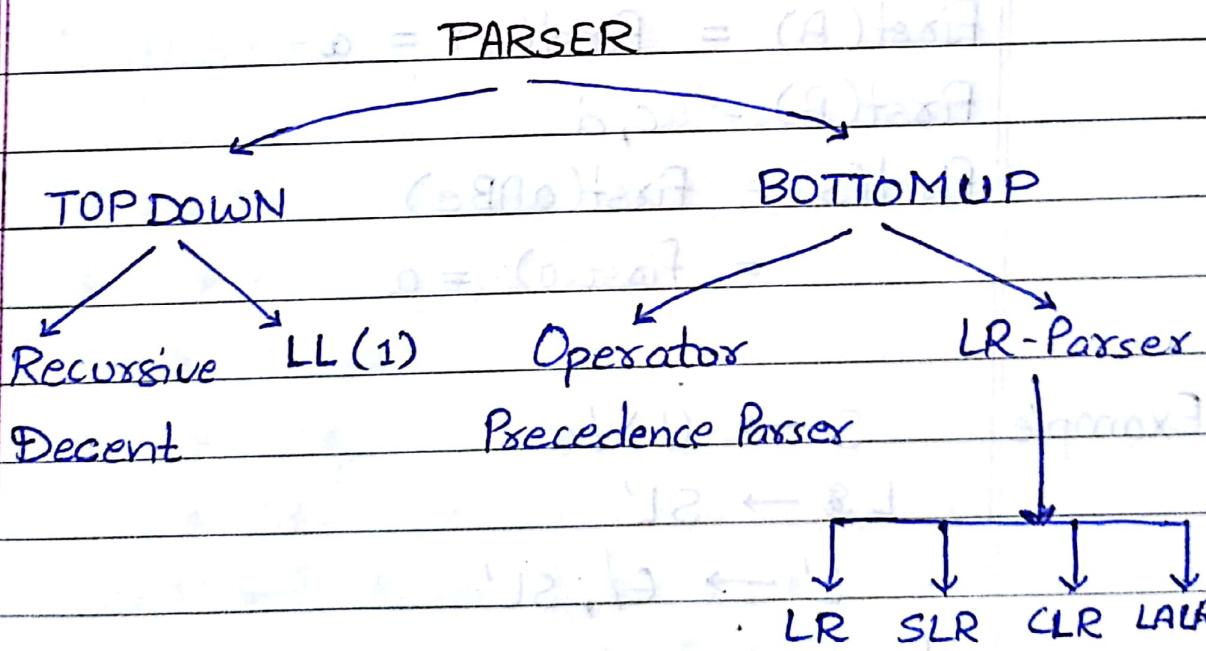
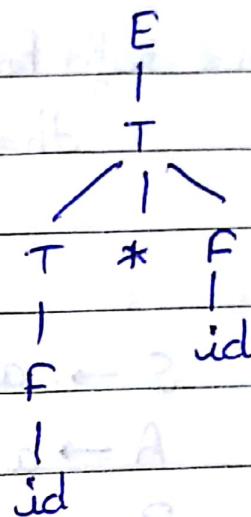


$$f \cancel{id} * id \Rightarrow T * id$$





We reached the root
(Starting symbol).



First * First & Follow

FIRST (α)

1) $\text{First}(\alpha) = \alpha$ if α is terminal symbol

2) $\text{First}(\overset{\alpha}{\text{E}}) = \epsilon$ if $\alpha \rightarrow \epsilon$

3) If $\alpha \rightarrow x_1 x_2 x_3$

then

$$\begin{aligned}\text{First}(\alpha) &= \text{First}(x_1 x_2 x_3) \\ &= \text{First}(x_1)\end{aligned}$$

if $\text{First}(x_1)$ contain ϵ

$$\text{then } \text{First}(\alpha) = (\text{First}(x_1) - \epsilon) \cup \text{First}(x_2 x_3)$$

Example-

$$S \rightarrow aABe$$

$$A \rightarrow a$$

$$B \rightarrow c/d$$

$$\text{First}(A) = \text{First}(a) = a$$

$$\text{First}(B) = c, d$$

$$\text{First}(S) = \text{First}(aABe)$$

$$= \text{First}(a) = a$$

Example

$$S \rightarrow (L) / a$$

$$L \rightarrow SL'$$

$$L' \rightarrow \epsilon / ; SL'$$

$$\text{First}(S) = (, a$$

$$\text{First}(L) = \text{First}(SL')$$

$$= \text{First}(S)$$

$$= (, a$$

$$\text{Q: } \text{First}(L') = \text{Q, } \epsilon, ,$$

Example: $A \rightarrow aA \mid bB \mid c \mid d$

Find $\text{First}(A)$

$$\text{First}(a) = c$$

$$\text{First}(d) = d$$

$$\begin{aligned}\text{First}(A) &= \text{First}(aA) = \text{First}(a) \\ &= a\end{aligned}$$

$$\text{First}(bB) = \text{First}(b) = b$$

$$\Rightarrow \text{First}(A) = \{a, b, c, d\}$$

Example: $S \rightarrow aABE$

$B \rightarrow cld$

$A \rightarrow a$

$$\text{First}(S) = \{a\}$$

$$\text{First}(B) = \{c, d\}$$

$$\text{First}(A) = \{a\}$$

Example: $E \rightarrow TE'$

$E' \rightarrow \epsilon \mid + \mid TE'$

$T \rightarrow FT'$

$T' \rightarrow \epsilon \mid * \mid FT'$

$F \rightarrow id \mid (E)$

$$\text{First}(A) = \{ \text{First}(E) = \epsilon, + \}$$

$$\text{First}(T') = \epsilon, *$$

$$\text{First}(F) = id, ($$

$$\text{First}(T) = \text{First}(F) = id, C$$

$$\text{First}(E) = \text{First}(T) = id, C$$

Example - $S \rightarrow aBDh$

$B \rightarrow cC$

$C \rightarrow bC / \epsilon$

$E \rightarrow g / \epsilon$

$F \rightarrow f / \epsilon$

$D \rightarrow EF$

$\text{First}(S) = \{a\}$

$\text{First}(B) = \{c\}$

$\text{First}(C) = \{b\}$

$\text{First}(E) = \{g, \epsilon\}$

$\text{First}(F) = \{f, \epsilon\}$

$\text{First}(D) = \text{First}(EF)$

$$\begin{aligned}
 &= \text{First}(E) = \{g, \epsilon\} \quad \because \text{First}(E) \\
 &= (\{g, \epsilon\} - \epsilon) \cup \text{First}(F) \quad \text{contains } \epsilon \\
 &= \{g, f, \epsilon\}
 \end{aligned}$$

Example $S \rightarrow (L)/a$

$L \rightarrow SL'$

$L' \rightarrow \epsilon / SL'$

$\text{First}(S) = (, a$

$\text{First}(L) = (, a$

$\text{First}(L') = \epsilon, ,$

Follow (A)

- 1) If A is starting symbol, then
 $\text{Follow}(A) = \$$
 - 2) If $x \rightarrow \alpha AB$, then
 $\text{Follow}(A) = \text{First}(B)$
 - 3) If $(x \rightarrow \alpha A) \cup (x \rightarrow \alpha AB)$ and
 $B \rightarrow \epsilon$

Example- $S \rightarrow (L)/a$

$l \rightarrow SL$

$$L' \rightarrow \epsilon /, sL$$

$$\text{Follow}(S) = \{\$, , ,)\}$$

$$\text{Follow}(L) = \{ \text{First}(S) \mid S \in T \}$$

$$\text{Follow}(L') = \text{follow}(L) = (\text{Follow}(L))^+ \quad (\text{Rule 3})$$

$$\text{follow}(s) = \text{follow } \text{First}(s')$$

二

= \bullet (Follow(L))

= , ,)

$$\text{follow}(S) = \$ \quad (\because S \text{ is starting pt.})$$

Example $S \rightarrow aABe$

$A \rightarrow a$

$B \rightarrow c/d$

First(S) = a

$$\text{first}(B) = c, d$$

First(A) = a

Follow(S) = \$

Follow(A) = First(B) = c, d

Follow(B) = First(e) = e

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Example: Find Follow(x)

$E \rightarrow TE'$

$E' \rightarrow E / +TE'$

$T \rightarrow FT'$

$T' \rightarrow \epsilon / *FT'$

$F \rightarrow id / (CE)$

First(E) = id, (

First(T) = id, ϵ

First(E') = $\epsilon, +$

First($\emptyset T'$) = $\epsilon, *$

First(F) = id, (

Follow(E) = \$,)

Follow(T) = +, \$,)

Follow(E') = Follow(E) = \$,)

Follow($\emptyset T'$) = First($\emptyset T'$) = \emptyset Follow(+, \$,)

Follow(F) = First(T')

= *, ϵ

= *, Follow(T)

= *, +, \$,)

Left Recursion

If $A \rightarrow A\alpha_1 | A\alpha_2 | A\alpha_3 | \dots | \beta_1 | \beta_2 | \beta_3 \dots$ is in production rule, then problems are created. So this has to be removed.

e.g. $A \rightarrow Aa$



Aa



$Aa \dots$

Thus, new production rule is defined as

$$A \rightarrow \beta_1 | \beta_2 | \beta_3 | \dots$$

$$A' \rightarrow \alpha_1 | \alpha_2 | \alpha_3 | \dots | \epsilon$$

Example:- $E \rightarrow E + T | T$

Here $A \Rightarrow E$

$\alpha_1 \Rightarrow + T$

$\beta_1 \Rightarrow T$

Thus,

$$E \rightarrow E + T | T$$



~~$\Rightarrow E \rightarrow TE'$~~

$$E' \rightarrow + TE' | \epsilon$$

Example:- $F \rightarrow F * T | T$

Here $A \Rightarrow F$ $\alpha_1 = * T$ $\beta_1 = T$

$\Rightarrow F \rightarrow TF'$

$$F' \rightarrow * TF' | \epsilon$$

Remark

For direct conversion,

$$A \rightarrow A\alpha/\beta \Rightarrow \begin{cases} A \rightarrow BA' \\ A' \rightarrow \alpha A'/\epsilon \end{cases}$$

LL(1) Parser (Top down)

Left to Right String Parsing

Use Left most derivative.

Procedure :

1. Make grammar free from left recursion
2. Find First & Follow
3. Make the following table as -

Non-Terminal	Terminal Symbols ...				
	T	I	F	E	S

Table

1. Add $A \rightarrow \alpha F$ under $M[A, b]$ where $b \in \text{First}(A)$

2. If $\text{First}(A)$ contain Non-terminal/ ϵ , then add

$A \rightarrow \alpha$ under $M[A, c]$

$A \rightarrow \epsilon$ where $c \in \text{Follow}(A)$

Example- Consider the following set of rules -

$$S \rightarrow (L) / a$$

$$L \rightarrow S / L'$$

$$L' \rightarrow , SL' / \epsilon$$

First

S	(, a	\$, , ,)
L	(, a)
L'	, , E)

Follow

	a	()	.	\$
S	$S \rightarrow a$	$S \rightarrow (L)$			
L	$L \rightarrow SL'$	$\$ \rightarrow SL'$			
L'			$L' \rightarrow \epsilon$	$L' \rightarrow SL'$	

Since, one cell contains only one entry
then it has LL(1) Parsing.

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LL(1) Parser

Example - $E \rightarrow E + T / T$ $T \rightarrow T * F / F$ $F \rightarrow id / (E)$

Remove left
 $S \rightarrow S\alpha_1 | S\alpha_2 | \beta_1 | \beta_2$

↓

 $S \rightarrow \beta_1 S' | \beta_2 S'$ $S' \rightarrow \alpha_1 S' | \alpha_2 S' | \epsilon$

STEP 1 - Using above formula to remove left recursion
 $E \rightarrow TE'$

 $E' \rightarrow +TE' / \epsilon$ $T \rightarrow FT'$ $T' \rightarrow *FT' / \epsilon$ $F \rightarrow id / (E)$

STEP 2 -

First

Follow

E	$id, ($	$\$,)$
E'	$+, \epsilon$	$\$,)$
ϵT	$id, ($	$+, \$,)$
T'	$*, \epsilon$	$+, \$,)$
F	$id, ($	$*, +, \$,)$

	<u>id</u>	<u>+</u>	<u>*</u>	<u>(</u>	<u>)</u>	<u>\$</u>
E	$E \rightarrow TE'$				$E \rightarrow TE'$	
E'		$E' \rightarrow +TE'$				$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$		\emptyset			$E' \rightarrow \epsilon$
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$				$F \rightarrow (E)$	

Example $S \rightarrow iEtSS'la$
 $S' \rightarrow eS/E$
 $E \rightarrow b$

Is LL(1) Parser?

	First	Follow
S	i, a	$\$, e*$
S'	e, E	$\$, e$
E	b	t

	<u>i</u>	<u>a</u>	<u>the</u>	<u>b</u>	<u>at</u>	<u>+</u>	<u>\$</u>
S	$s \rightarrow iEtSS'$	$s \rightarrow a$					
S'		$s' \rightarrow eS$					$s' \rightarrow E$
E'				$E \rightarrow b$			

* This is not a LL(1) parser

NOTE:

① If $A \rightarrow \alpha_1 | \alpha_2 | \alpha_3$ then it is said to be LL(1) iff -

$$\text{First}(\alpha_1) \cap \text{First}(\alpha_2) = \emptyset$$

$$\text{First}(\alpha_2) \cap \text{First}(\alpha_3) = \emptyset$$

$$\text{First}(\alpha_3) \cap \text{First}(\alpha_1) = \emptyset$$

② If $A \rightarrow \alpha_1 | \alpha_2 | t$ then it is said to be in LL(1) iff -

$$\text{First}(\alpha_1) \cap \text{Follow}(A) = \emptyset$$

$$\text{Follow}(A) \cap \text{First}(\alpha_2) = \emptyset$$

$$\text{First}(\alpha_1) \cap \text{Follow}(A) = \emptyset$$

Example-

$$S \rightarrow E/a$$

$$E \rightarrow a$$

Check LL(1) parser or not?

$$\text{First}(E) \neq \emptyset \quad \text{First}(a) = \{a\} \cap \{a\} \\ \neq \emptyset$$

\Rightarrow Thus, given grammar is not in LL(1) parser.

Example-

$$S \rightarrow aSA/\epsilon$$

$$A \rightarrow c/E$$

$$\text{First}(aSA) \cap \text{Follow}(S) = \{a\} \cap \{\$, c\} \\ = \neq \emptyset$$

$$\text{First}(c) \cap \text{Follow}(A) = \{\$\}, c \cap \{c\} = \{c\} \\ \neq \emptyset$$

\Rightarrow Thus, this is not in LL(1) parser

Example-

$$S \rightarrow aABb$$

$$A \rightarrow a/E$$

$$B \rightarrow d/E$$

	First	Follow
A	a, E	d, b
B	d, E	b

$$\text{First}(a) \cap \text{Follow}(A) = \{a\} \cap \{d, b\} = \emptyset$$

$$\text{First}(d) \cap \text{Follow}(B) = \{d\} \cap \{b\} = \emptyset$$

\Rightarrow Thus, the given grammar is in LL(1) parser.

LR(R) Parser

- Bottom-up parser
- 'L' → left to right scanning
- 'R' → constructing rightmost derivative in reverse order
- 'k' → # lookahead symbol

- Let G be a grammar with start symbol S . then augmented grammar G' with a new start symbol S' s.t. $S' \rightarrow S$.
- An augmented Grammar is used to announce the acceptance of input.

Example: G is given by

$$S \rightarrow A$$

$$A \rightarrow aA/b$$

Find G' (augmented grammar)

Sol-

G' is given as

$$S' \rightarrow S$$

$$S \rightarrow A$$

$$A \rightarrow aA/b$$

* LR item

Contains production rule.

Closure of any item

Closure (I) = is defined / obtained by -

1. Adds item I to closure(I)

2. If $\alpha \rightarrow \beta A \gamma$, $\beta A \gamma$ is Item I

and $A \rightarrow BC$

then add

$A \rightarrow BC$ to closure (I)

3: Repeat 1 & 2 for newly added item

Example

$S \rightarrow \text{ } AA$

$A \rightarrow aA/b$

~~Closure ($S \rightarrow S$)~~ Find closure ($S' \rightarrow S$)

1. Make augmented grammar

$S' \rightarrow S$

$S \rightarrow AA$

$A \rightarrow aA/b$

2. Closure ($S' \rightarrow S$) \Rightarrow $S' \rightarrow .S$
 $S \rightarrow .AA$
 $A \rightarrow .aA/b$

Item I₀

Example - $E' \rightarrow E$

$E \rightarrow E + T / T$

$T \rightarrow T * F / F$

$F \rightarrow (E) / \text{id}$

Closure ($E' \rightarrow E$)

$= E' \rightarrow .E$

$E \rightarrow .E + T / T$

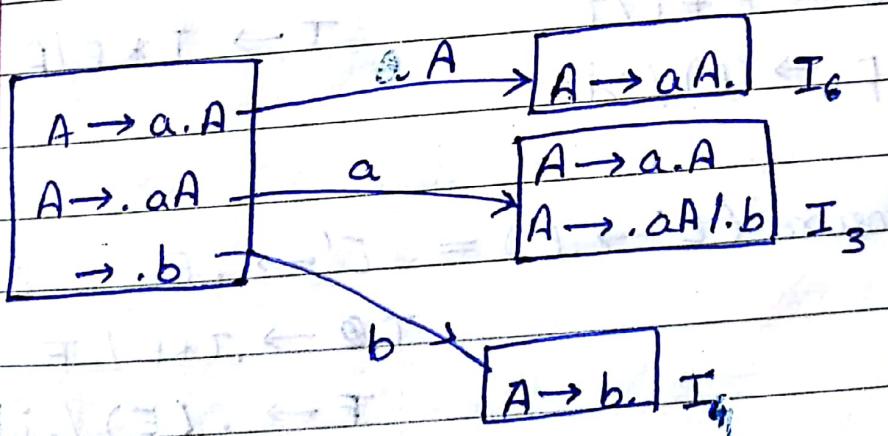
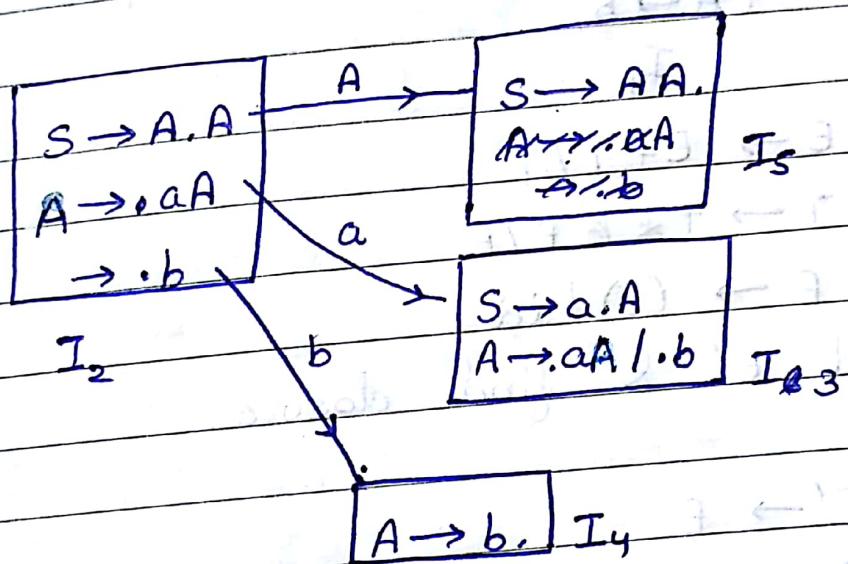
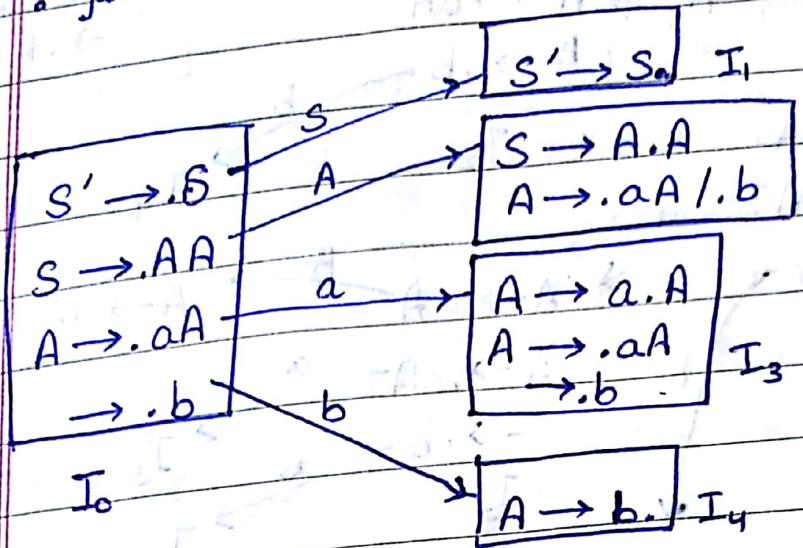
$T \rightarrow .T * F / F$

$F \rightarrow .(E) / \text{id}$

LR Algo for G

- Create G'
- find closure of $(S' \rightarrow^* S)$ & say it item I_0

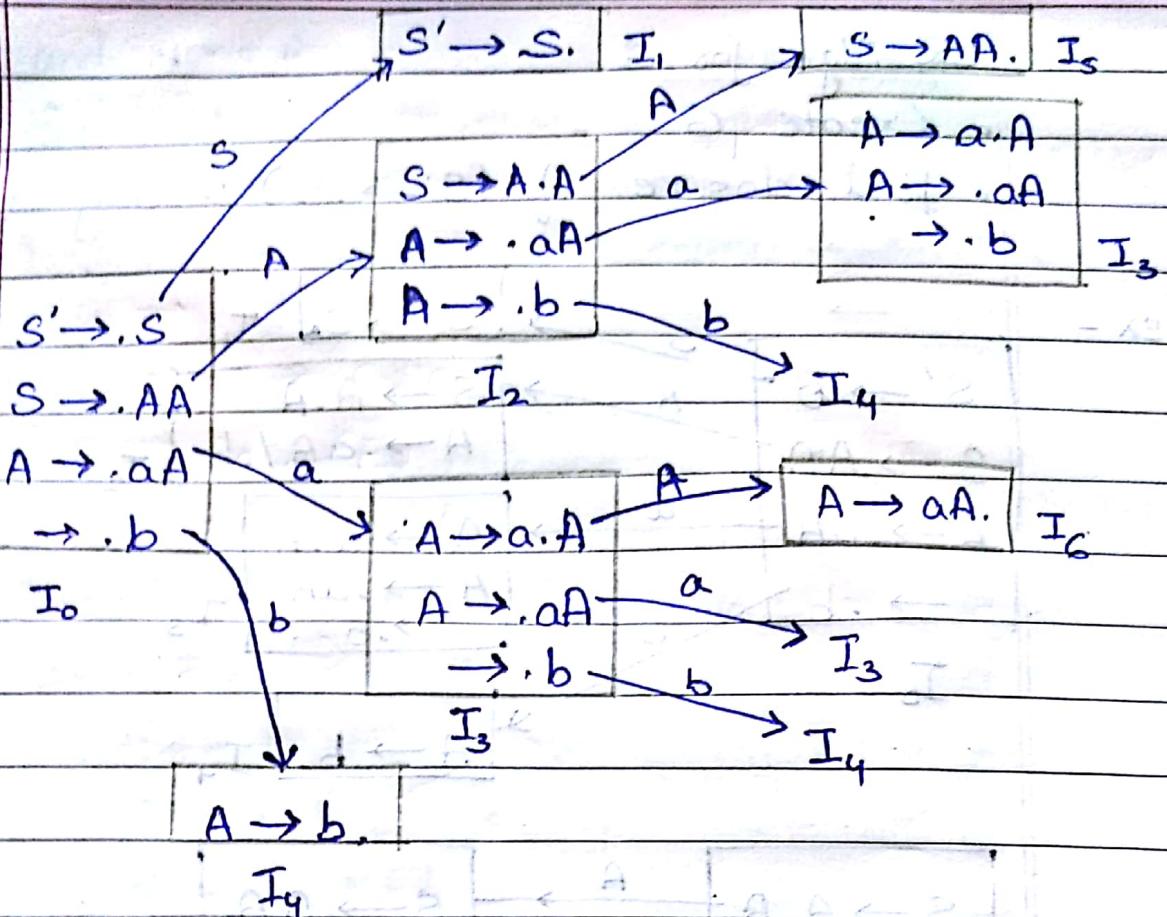
ex -



Reduce = I_1, I_5, I_4, I_6

↓

(Cannot go further)



Example-

$$E \rightarrow E + T / T$$

$$T \rightarrow T * F / F$$

$$F \rightarrow (E) / id$$

* Add E' & find closure.

$$E' \rightarrow E$$

$$E \rightarrow E + T / T$$

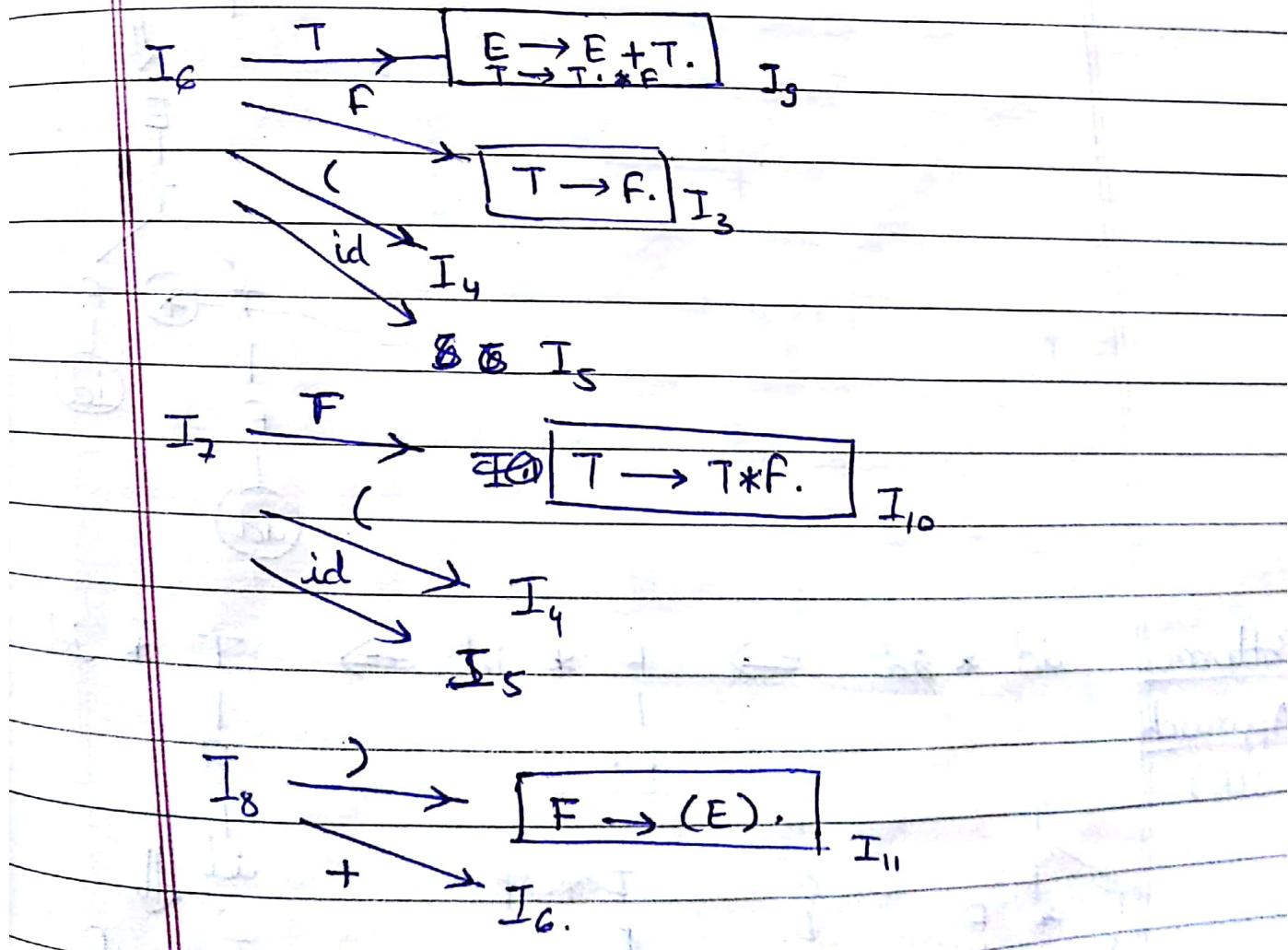
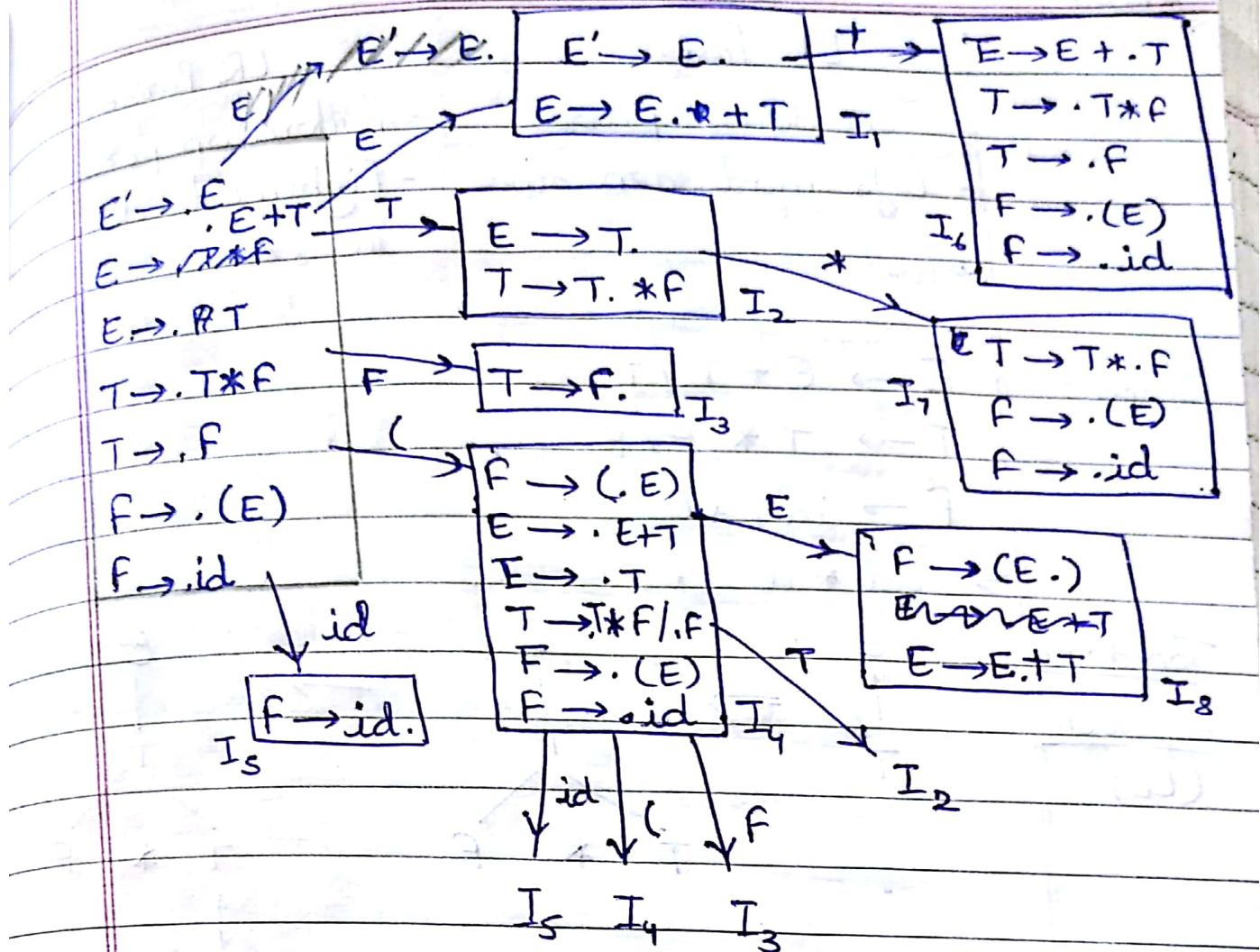
$$T \rightarrow T * F / F$$

$$F \rightarrow (E) / id$$

$$\text{Closure } (E' \rightarrow .E) = E' \rightarrow .E \cup E \rightarrow .E + T / T$$

$$T \rightarrow .T * F / F$$

$$F \rightarrow .(E) / id$$



LL ParserLR Parser

- Top down parser - Bottom up parser
- left most derivative - Rightmost derivative
in reverse order.

Ques -

$$E \rightarrow E + T / T$$

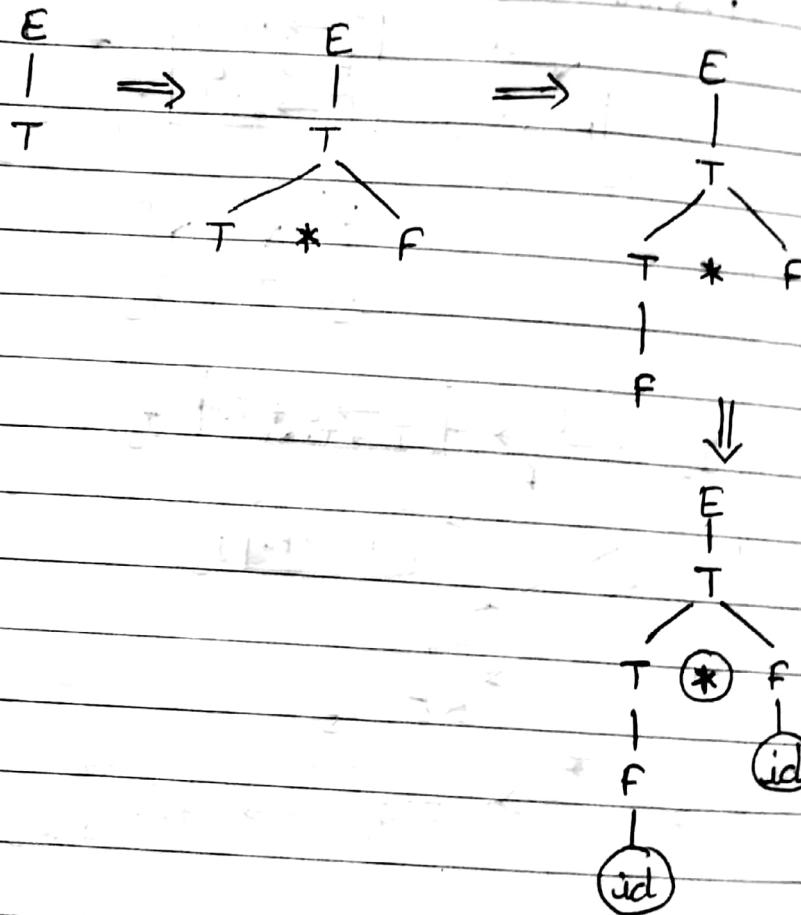
$$T \rightarrow T * F / F$$

$$F \rightarrow id / (E)$$

$$\Rightarrow id * id$$

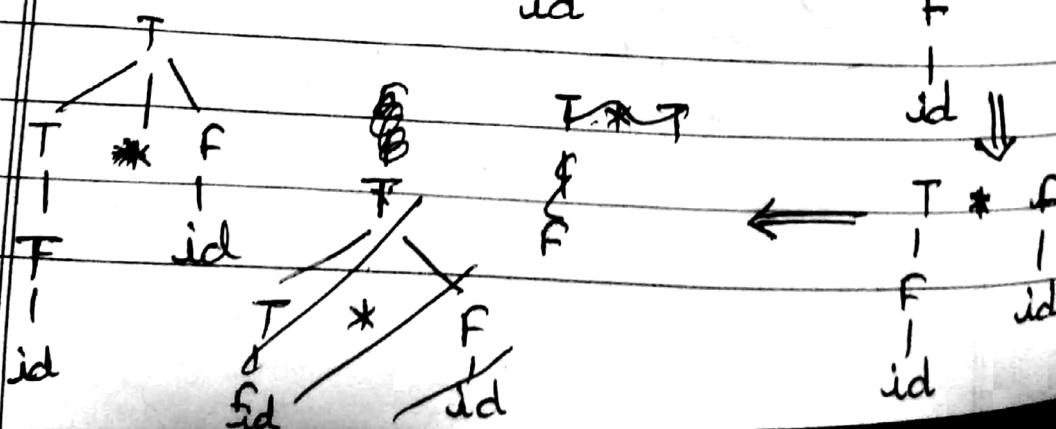
Top downApproach

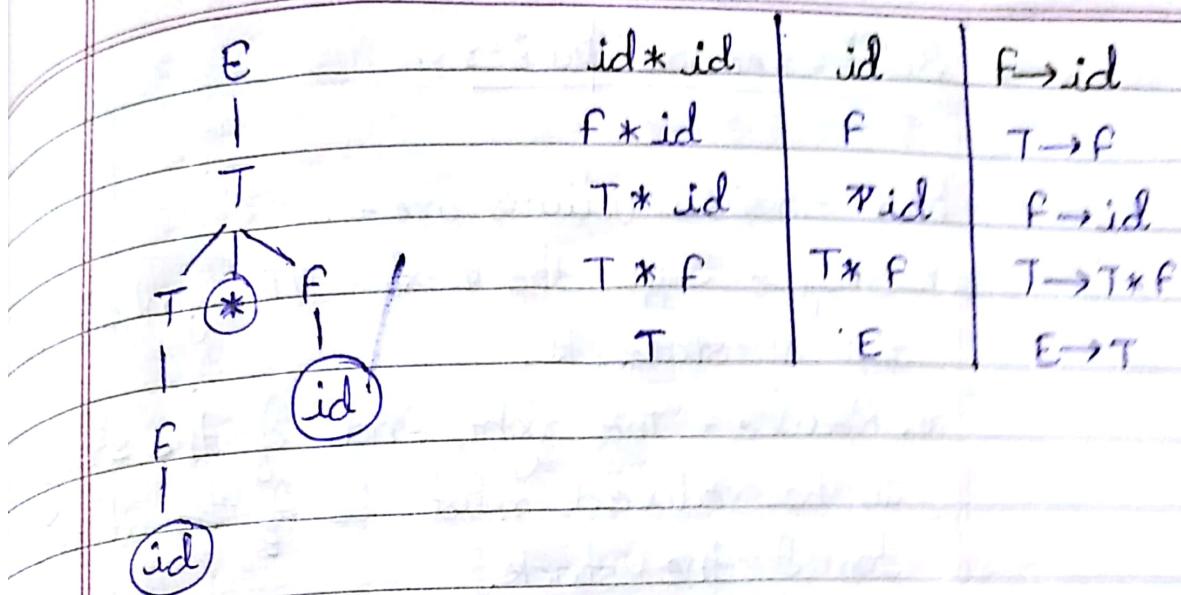
(LL)

Bottom upApproach

(LR)

$$id * id \Rightarrow F * id \Rightarrow T * id$$





Top-down using rightmost derivation -

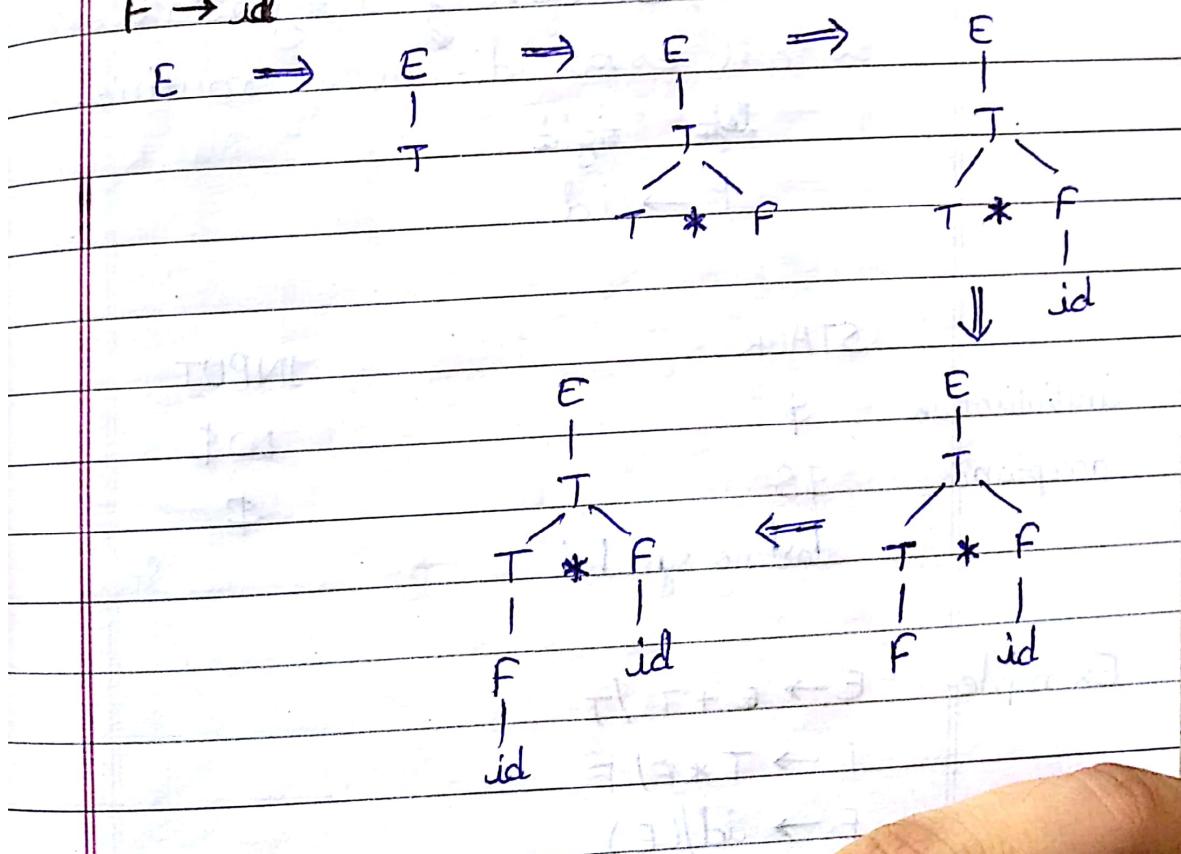
E → T

$$T\mathcal{E} \rightarrow T^*F$$

f → id

$T \rightarrow F$

F → id



Shift-reduce parser

Four possible actions are -

1. Shift - Shift the next I/P symbol on top of stack.

2. Reduce - The right end of the string to be reduced must be at the top of the stack.

Locate left end of the string within the stack & decide with that non-terminal to replace the string.

3. Accept - Successful completion of parsing.

4. Error - Discovery of a syntax error & call error discover routine.

left right

$F \rightarrow id$

STACK

initialisation \$

acceptance \$S

↓
starting symbol

INPUT

w\$

\$

Example: $E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow id \mid (E)$

$w = id * id$

STACK	INPUT	ACTION
\$	id * id \$	} shift
\$ id	* id \$	} Reduce by F → id
\$ F	* id \$	} F → T
\$ T	* id \$	Shift
\$ T *	id \$	Shift
\$ T * id	\$	Reduce F → id
\$ T * F	\$	T → T * F
\$ T	\$	E → T
\$ E	\$	Accept

Hence $w = \text{id} * \text{id}$ is acceptable by the parser.

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Example: $E \rightarrow E + T / T$
 $T \rightarrow T * F / F$
 $F \rightarrow (E) / id$

Augmented grammar.

$E' \rightarrow E$
 $E \rightarrow E + T$
 $E \rightarrow T$
 $T \rightarrow T * F$
 $T \rightarrow F$
 $F \rightarrow (E)$
 $F \rightarrow id$

Create LR zero item (I_0)

$E' \rightarrow .E$
 $E \rightarrow .E + T$
 $E \rightarrow .T$
 $T \rightarrow .T * F$
 $T \rightarrow .F$
 $F \rightarrow .(E)$
 $F \rightarrow .id$

Kernel Item

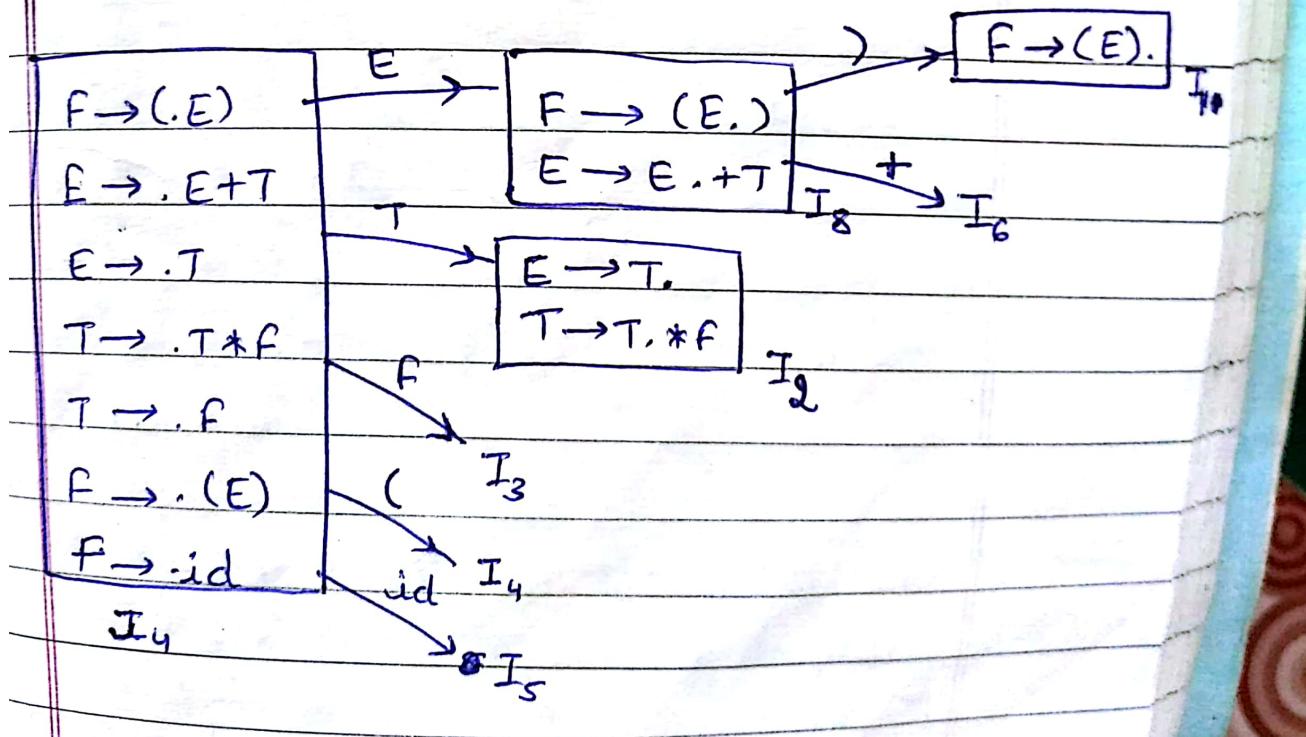
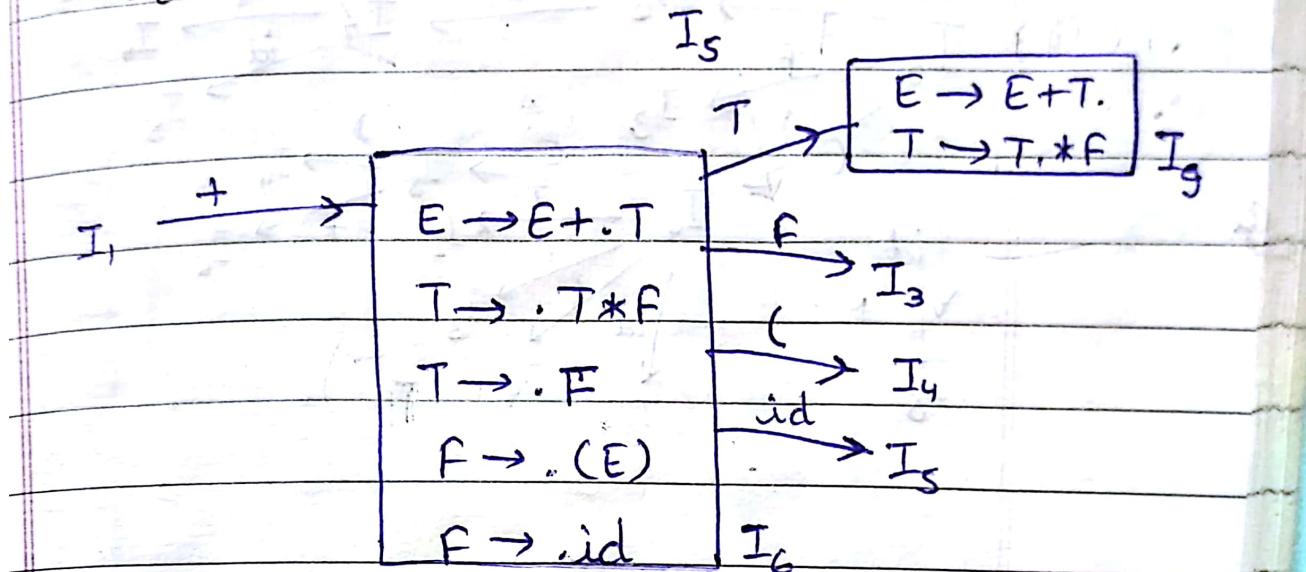
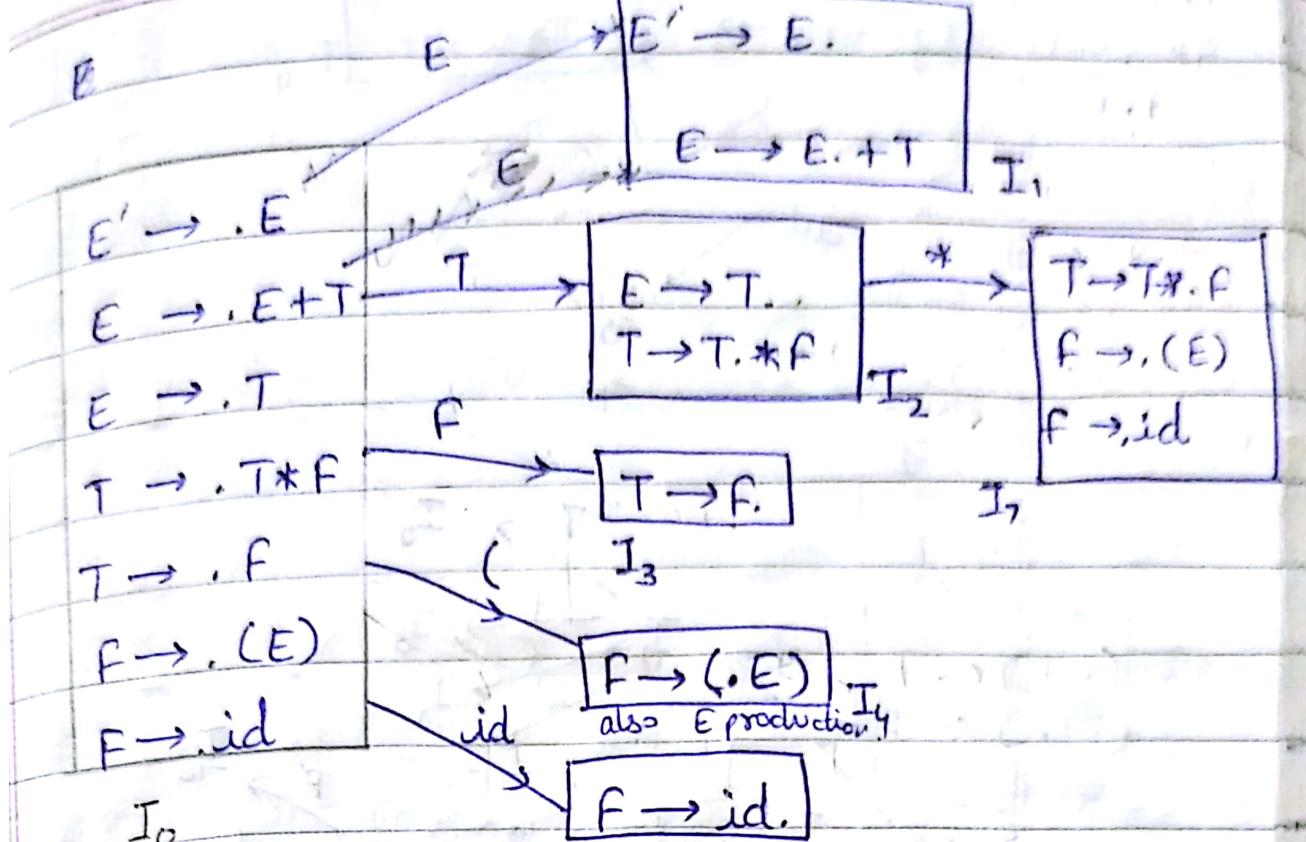
Non Kernel Item

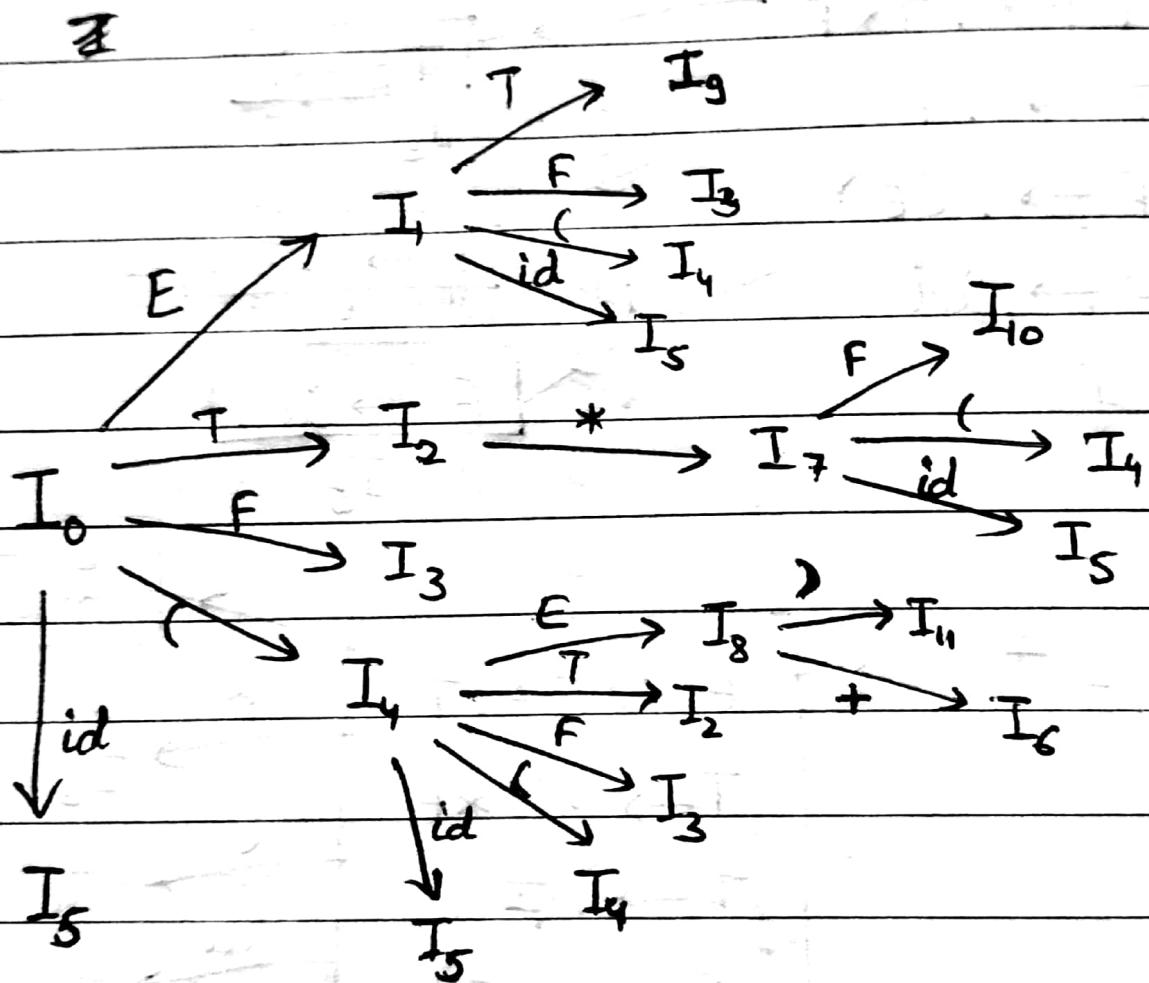
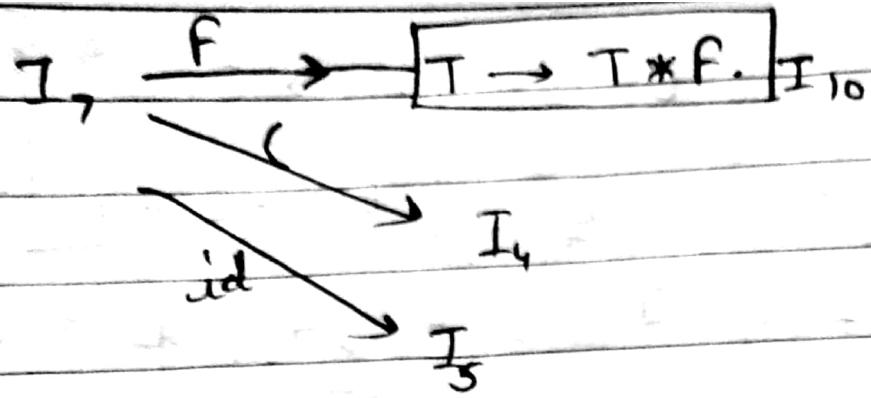
Kernel Item

- The initial item $S' \rightarrow .S$ & all item whose ' $.$ ' are not left end.

Non-Kernel Item

- Except $S' \rightarrow S$ where ' $.$ ' on left side





* Acceptance only for $E' \rightarrow E$.

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Create corresponding table.

Item	id	ACTION						GOTO		
		*	+	*	()	\$	E	T	F
0	S5				S4			1	2	3
1		SG					($E' \rightarrow E$) accept			
2	x2	x2	x2	x2	x2	x2				
3	x4	x4	x4	x4	x4	x4				
4	S5			S4			8	2	3	
5	x6	x6	x6	x6	x6	x6		g	3	
6	S5			S4			g	3		
7	S5			S4			10			
8		SG			S11					
9	x1	x1	x1	x1	x1	x1				
10	x3	x3	x3	x3	x3	x3				
11	x5	x5	x5	x5	x5	x5				

Reduce.

1 $E \rightarrow E + T$.

2 $E \rightarrow T$.

3 $T \rightarrow T * F$.

4 $T \rightarrow F$.

5 $F \rightarrow (E)$.

6 $F \rightarrow id$.

* If any cell in the table has multiple values then the string is not accepted by LR(0) parser.

else

it is in LR(0) PA

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SLR (Simple LR)

- Write reduce entry only in follow of that production.

State	id	+	*	()	\$	E	T	F
0	S_3				S_4		1	2	3
12		S_6				accept			
23		x_2	S_1			x_2	x_2		
34		x_4	x_4			x_4	x_4		
45	S_5				S_4		8	2	3
56		x_6	x_6			x_6	x_6		
6	S_5				S_4		9	3	
78	S_5				S_4				10
8		S_6				S_{11}			
910		x_1	S_7			x_1	x_1		
10		x_3	x_3			x_3	x_3		
11		x_5	x_5			x_5	x_5		

Thus, the grammar is accepted by SLR parser.

e.g. check for id * id

STACK	Symbol	Input	ACTION
0	\$	id * id \$	shift
05	\$ id	* id \$	Reduce $F \rightarrow id$ R: $T \rightarrow F$
03	\$ F	* id \$	shift
02	\$ T	* id \$	shift
027	\$ T *	id \$	shift to S
0275	\$ T * id	\$	R: $F \rightarrow id$
02710	\$ T * F	\$	R: $T \rightarrow T * F$
02	\$ T	\$	R: $E \rightarrow T$
01	\$ E	\$	accept

Ques-

Check whether the given grammars are acceptable by LR or SLR parser.

$$S \rightarrow AA$$

$$A\$ \rightarrow aA/b$$

Augmented grammar

$$S' \rightarrow S$$

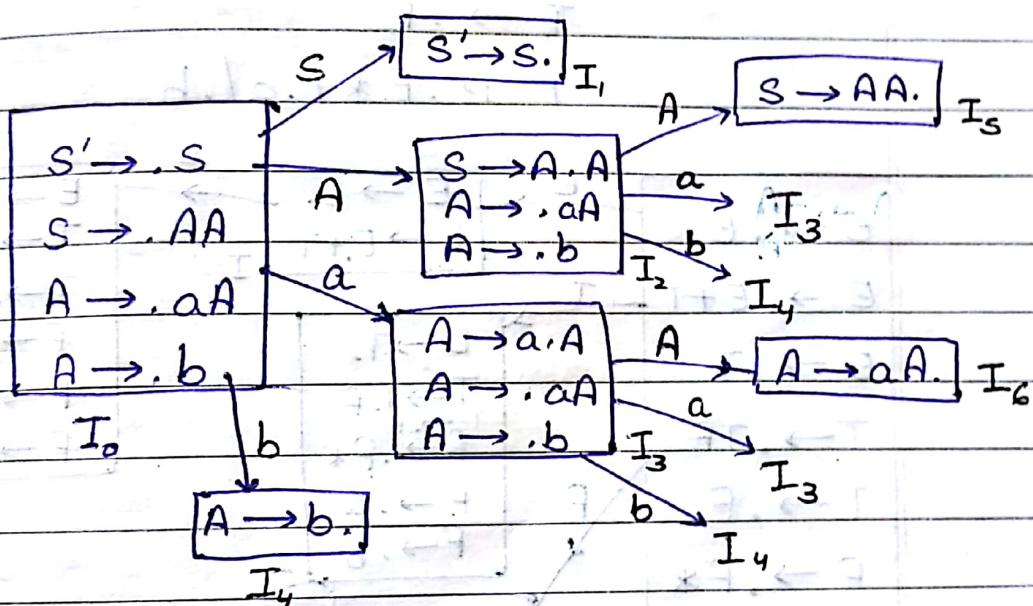
$$S \rightarrow AA$$

$$A \rightarrow aA/b$$

$$\text{Closure } A \quad S' \rightarrow S \quad] \quad I_0$$

$$S \rightarrow .AA \quad] \quad I_0$$

$$A \rightarrow .aA/b \quad] \quad I_0$$



State	a	b	,	\$	S.	A
0	S_3		S_4		1	2
1						5
2	S_3		S_4			6
3	S_3		S_4			
4	γ_3		γ_3		γ_3	
5	γ_1		γ_1		γ_1	
6	γ_2		γ_2		γ_2	

Ans: Yes the given grammar is LR parser acceptable.

Ques-

$$E \rightarrow E + T \mid T$$

$$T \rightarrow TF \mid F$$

$$F \rightarrow F^* \mid a \mid b$$

• Make augmented grammar

• Closure of $E' \rightarrow .E$

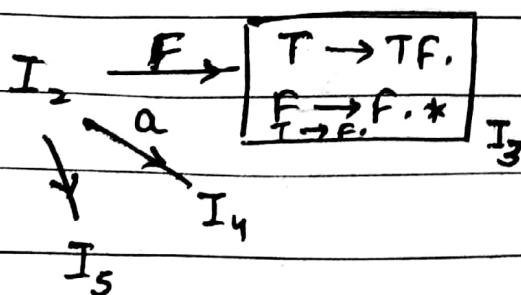
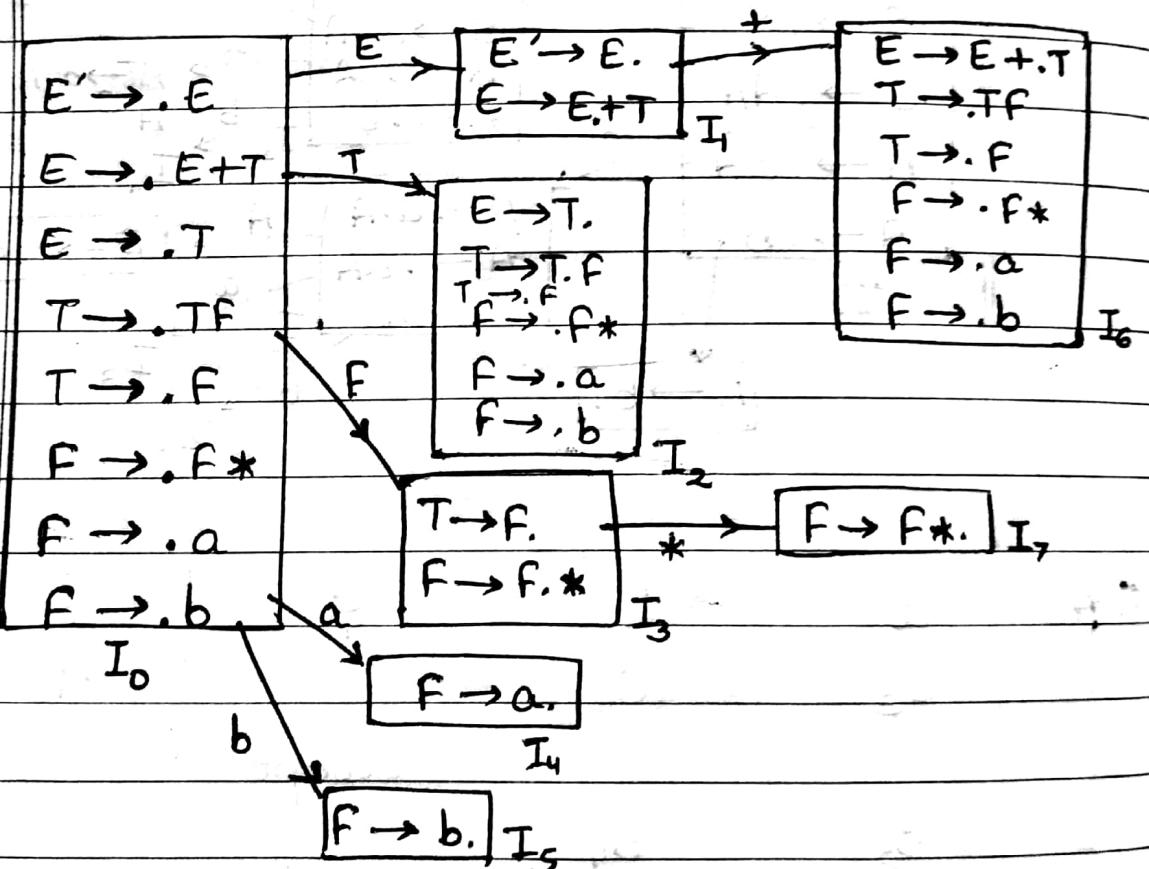
$$E \rightarrow .E + T$$

$$E \rightarrow .T$$

$$T \rightarrow .TF$$

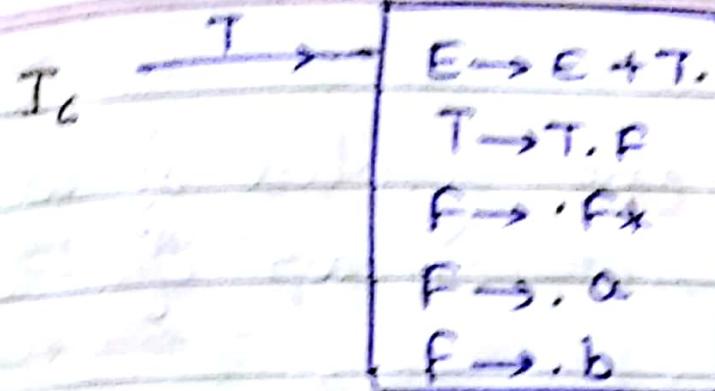
$$T \rightarrow .F$$

$$F \rightarrow .F^* \mid .a \mid .b$$



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LR Parser Algo

Let a be the first symbol of $w\$$
 Let S be the state on top of stack.

if (Action $[\$, a] = \text{Shift}$) {

Push \bullet onto the stack;

let a be the next input symbol

}

else if (Action $[S, a] = \text{reduce } A \rightarrow B$)

{

Pop $[B]$ symbol of the stack;

let state t now on top of stack

Push Goto $[t, A]$ onto stack;

output the production $A \rightarrow B$

}

else if (Action $[S, a] = \text{accept}$)

break;

* else call error-recovery routine

}

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LR(1) Item

LR(0) item + Look Ahead Symbol

Algorithm

LR(1)closure (I) \Rightarrow 1. Add I to closure (I)2. If I is $\alpha \rightarrow B.ABC, \$$
&& $A \rightarrow EFG$ then add ~~$A \rightarrow EFG, first(B)$~~ $A \rightarrow .EFG, first(BC, \$)$

3. Repeat it for newly added number.

LR(0) closure (I) \Rightarrow 1. Add I to closure (I)2. If I is $\alpha \rightarrow B.ABC, &$ $A \rightarrow EFG$

then add,

 $A \rightarrow .EFG$

3. Repeat for new number.

Example $S \rightarrow AA$ $A \rightarrow aA/b$

Find LR(1) Closure

Closure ($S' \rightarrow .S, \$$) * $\Rightarrow S' \rightarrow .S, \$$ $S \rightarrow .A | A, \$$ { $S' \rightarrow .A, first(\$)$ } $A \rightarrow .aA, a/b$ $A \rightarrow .b, alb$

Ques - 1

$$S' \rightarrow S$$

$$S \rightarrow CC$$

$C \rightarrow CC \cup d$ Check for CLR₉

Closure ($S' \rightarrow .S, \$$)

$$\Rightarrow S' \rightarrow .S, \$$$

$$S \rightarrow .CC, \$$$

$$C \rightarrow .CC, \& C \cup d$$

$$C \rightarrow .d, C \cup d$$

 I_0

$$S' \rightarrow S, \$$$

 I_1

$$S^* \rightarrow C.C, \$$$

$$C \rightarrow .CC, C \cup d, \$$$

$$C \rightarrow .d, C \cup d, \$$$

 I_2

$$C \rightarrow d, C \cup d$$

 I_4

$$C \rightarrow c.C, C \cup d$$

$$C \rightarrow .cC, C \cup d$$

$$C \rightarrow .d, C \cup d$$

 I_3

$$I_2 \xrightarrow{C} S \rightarrow CC, \$ I_5$$

$$C \rightarrow c.C, \$$$

$$C \rightarrow .cC, \$$$

$$C \rightarrow d, \$$$

$$C \rightarrow .d, \$$$

 I_6 I_7

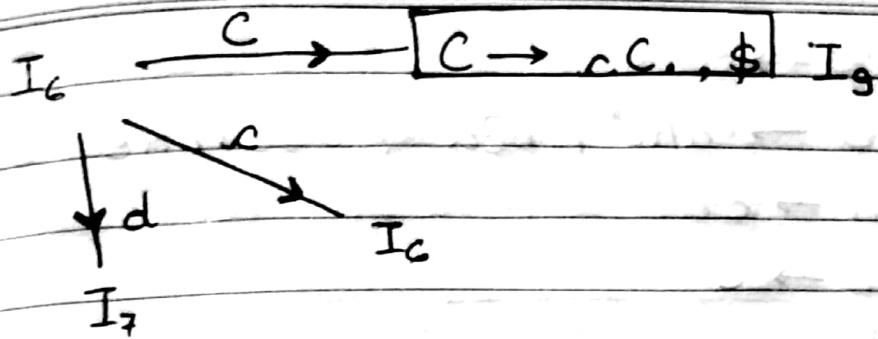
$$I_3 \xrightarrow{C} C \rightarrow CC, \$ I_8$$

$$C \rightarrow c.C, C \cup d$$

$$C \rightarrow .cC, C \cup d$$

$$C \rightarrow .d, C \cup d$$

 I_3 I_4



1. $S \rightarrow CC.$
 2. $SC \rightarrow CC.$
 3. $C \rightarrow d.$
- $\} \text{Reduce}$

	ACTION			GOTO	
STATE	c	d	\$	s	c
0	s_3	s_4		1	2
1			accept		
2	s_6	s_7			5
3	s_3	s_4			8
4	x_3	x_3			
5			x_1		9
6	s_6	s_7			
7			x_3		
8	x_2	x_2			
9			x_2		

* Fill x_n where under the look ahead symbol column.

for CLR, this has no conflict. Thus, the grammar is in CLR. (Canonical LR)

Ques-2. $S' \rightarrow S$

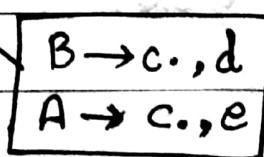
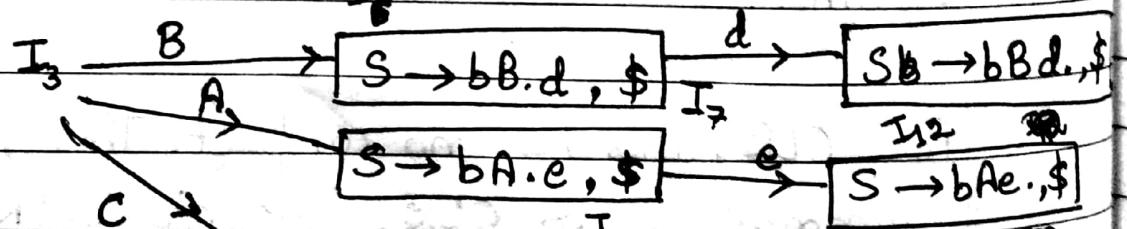
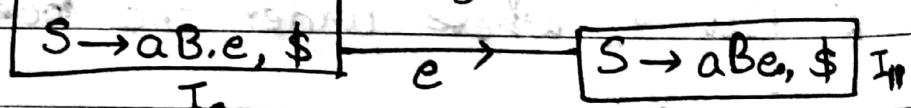
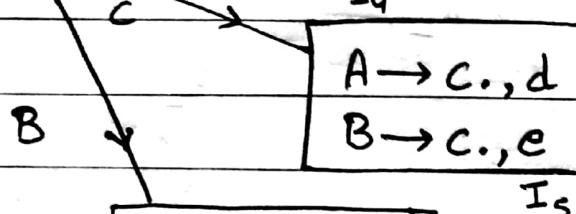
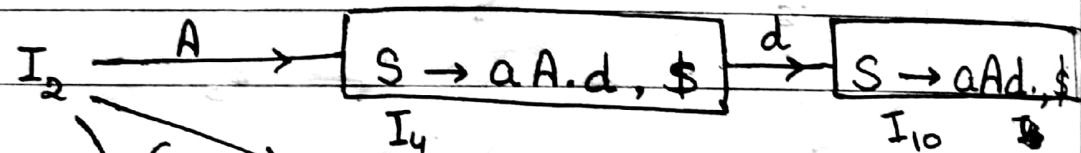
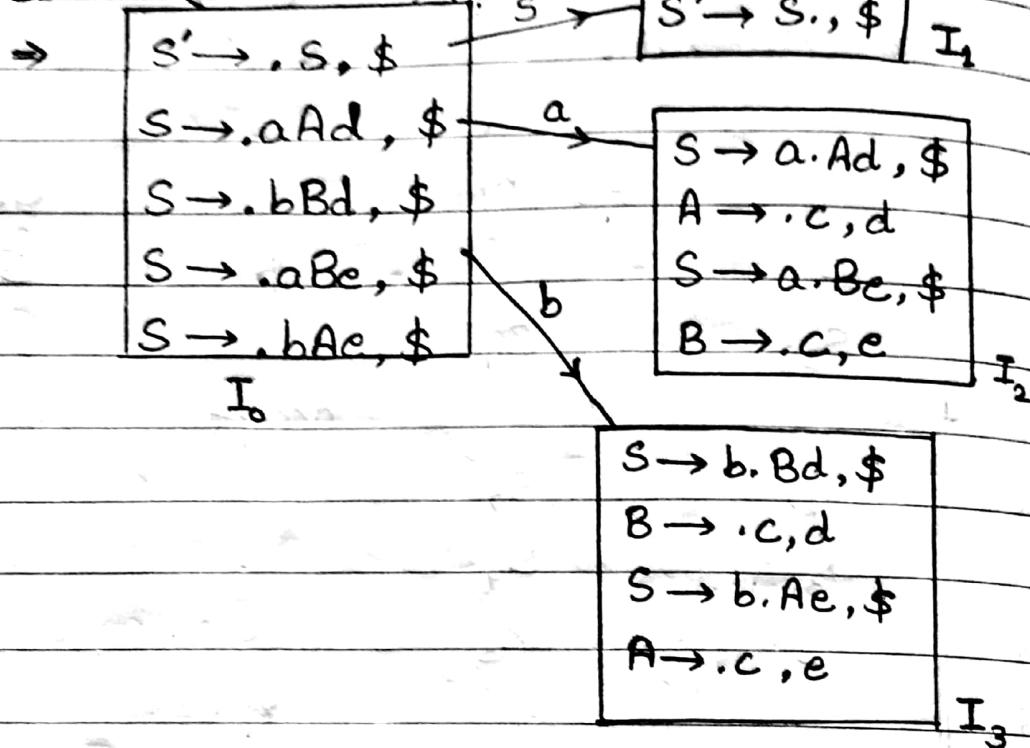
$S \rightarrow aAd / bBd / aBe / bAe$

$A \rightarrow c$

$B \rightarrow c$

Check for CLR Parser.

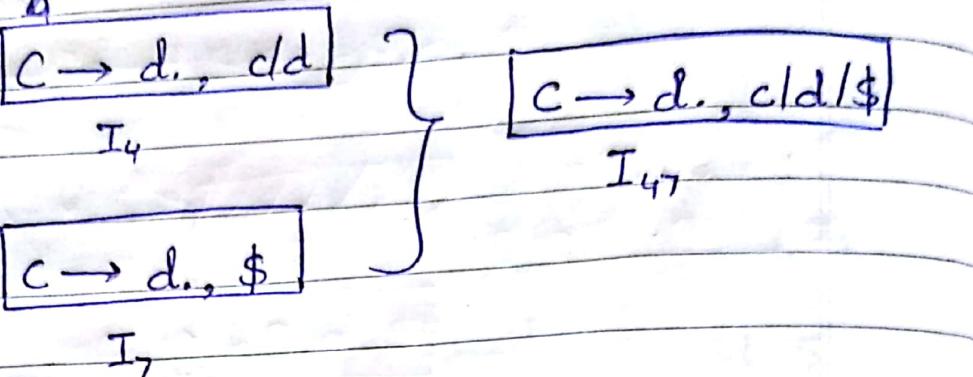
Closure ($S' \rightarrow .S, \$$)



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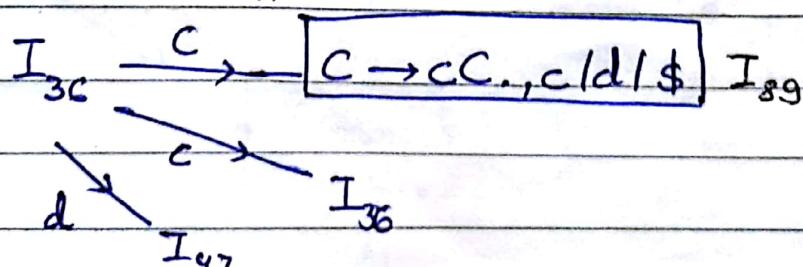
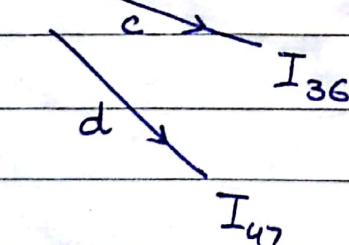
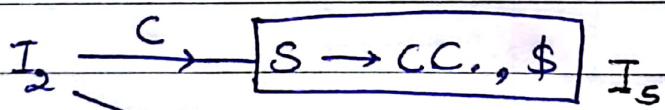
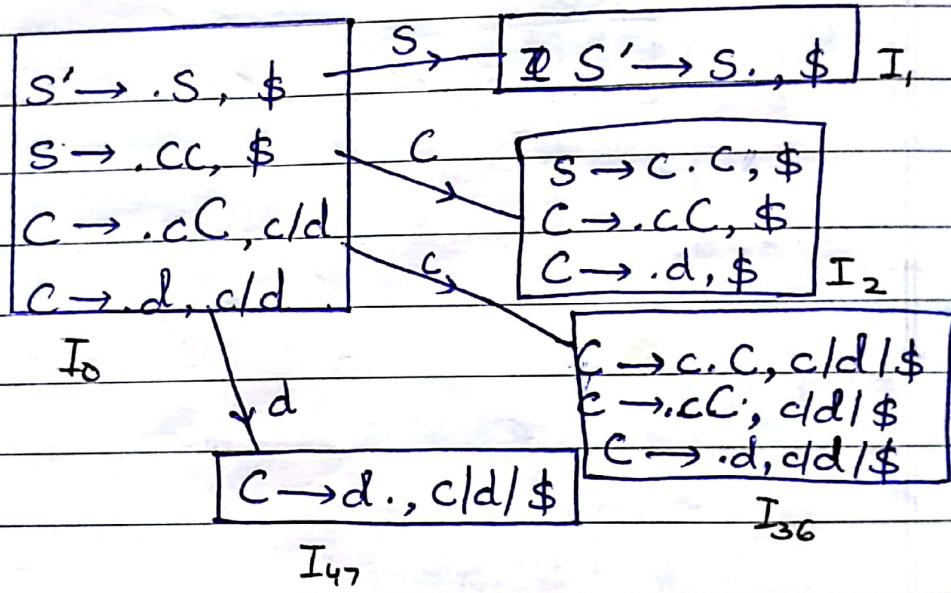
LALR

Ref Quest: In LALR, merge stat stage 1 item which have only diff. look ahead symbol.

eg- $\boxed{C \rightarrow d., c/d}$ I_4 

- Replace I_4 & I_7 with I_{47}

- Do it this for all such items.



STATE	ACTION			GOTO	
	c	d	\$	s	c
0	S_{36}	S_{47}		1	2
1			accept		
2	S_{36}	S_{47}			5
36	S_{36}	S_{47}			89
47	γ_3	γ_3	γ_3		89
5			γ_1		
89	γ_2	γ_2	γ_2		

Ques 3- $S' \rightarrow S$

$S \rightarrow Aa$

$S \rightarrow bAc$

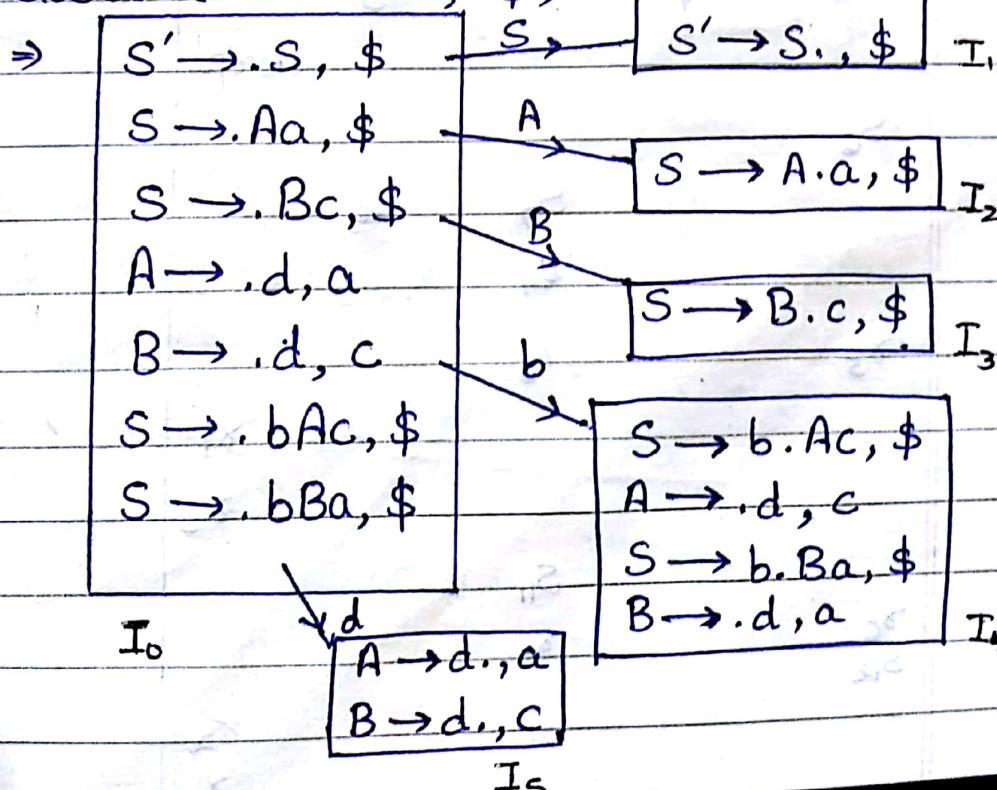
$S \rightarrow Bc$

$S \rightarrow bBa$

$A \rightarrow d$

$B \rightarrow d$

Closure ($S' \rightarrow .S, \$$)



$I_2 \xrightarrow{a} [S \rightarrow Aa., \$] I_6$

$I_3 \xrightarrow{c} [S \rightarrow Bc., \$] I_7$

$I_4 \xrightarrow{A} [S \rightarrow bA.c, \$] I_8$

$\begin{array}{l} d \\ B \end{array} \xrightarrow{\quad} [PA/PA/a./c] \quad \begin{array}{l} A \rightarrow d., c \\ B \rightarrow d., a \end{array} I_9$

$S \rightarrow bB.a, \$ I_{10}$

$I_8 \xrightarrow{c} [S \rightarrow bAc., \$] I_{11}$

$I_{10} \xrightarrow{a} [S \rightarrow bBa., \$] I_{12}$

STATE	ACTION					GOTO		
	a	b	c	d	\$	S	A	B
0		s_4		s_5		1	2	3
1						accept		
2	s_6							
3			s_7	s_8		8	10	
4			s_7	s_9		8	10	
5	s_5		s_6					
6						s_1		
7						s_3		
8					s_{11}			
9	s_6			s_5				
10	s_{12}					s_2		
11						s_4		
12								

\Rightarrow Solving for LALR Parser

- I_5 & I_g are identical irrespective of lookahead symbols.

$$\begin{array}{l} A \rightarrow d, c/a \\ B \rightarrow d, c/a \end{array}$$

I_{5g} .

New Table.

STATE	ACTION					GOTO		
	a	b	c	d	\$	S	A	B
0	S_4			S_{5g}		1	2	3
1						accept		
2	S_6							
3			S_7					
4				S_{5g}			8	10
6						x_1		
7						x_3		
8			S_{11}					
10	S_{12}		x_5					
11						x_2		
12						x_4		
59	x_5		x_6					

Yes, the grammar is LALR parser.

Syntax Directed Translation (SDT)

$$S \rightarrow S + T$$

$s \rightarrow s + t$ { $T.value = F.value$ }
 printf("f") $\xrightarrow{\text{semantic attribute}}$

Calculation of + & *

$$L \rightarrow E_n \quad \{ \quad L.\text{val} = E.\text{val} \quad \}$$

$$E \rightarrow E_1 + T \quad \{ \quad E.\text{val} = E_1.\text{val} + T.\text{val} \quad \}$$

$$E \rightarrow T \quad \{ E.\text{val} = T.\text{val} \}$$

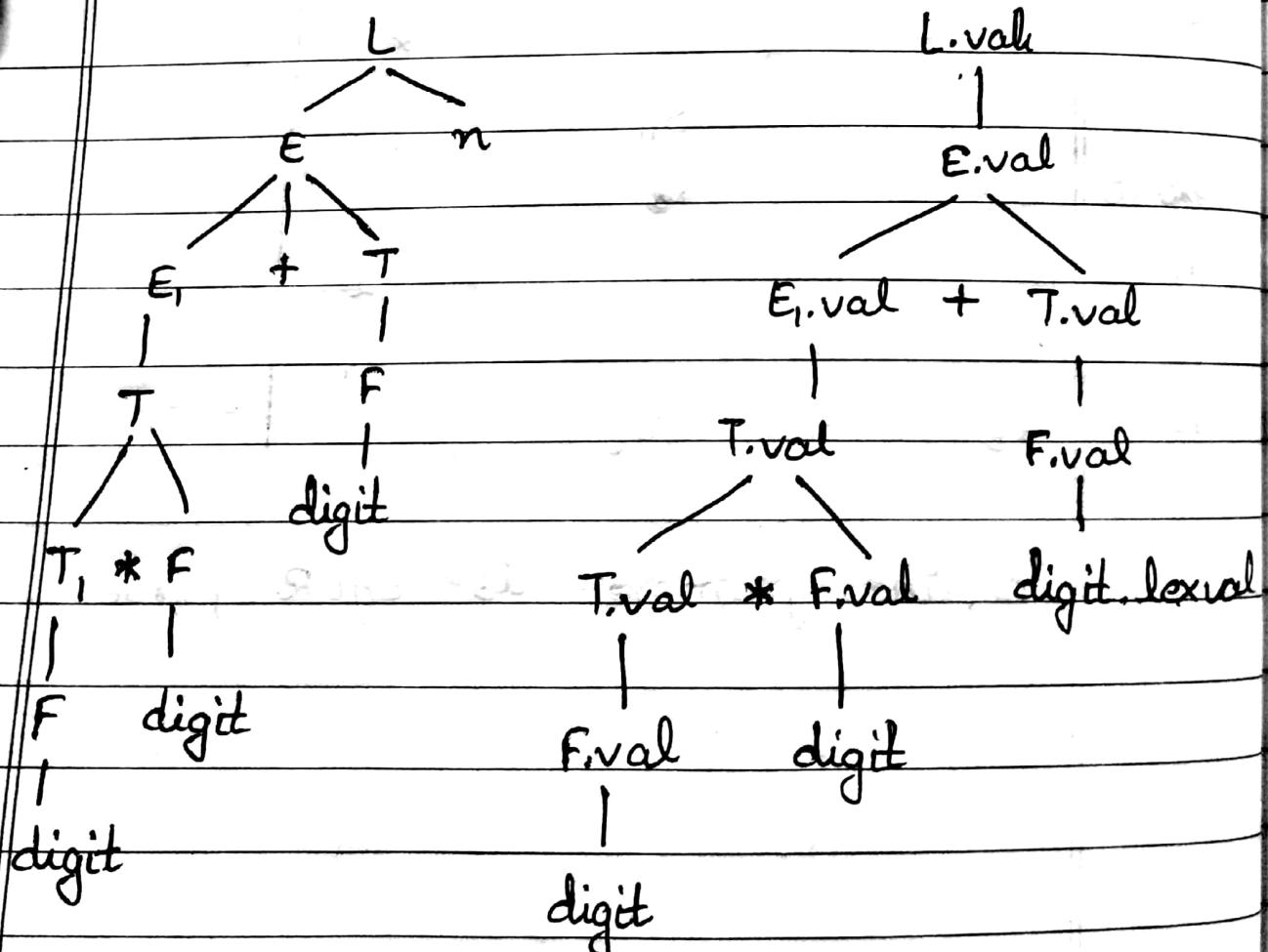
$$T \rightarrow T_1 * F \quad \left\{ \begin{array}{l} T.\text{val} = T_1.\text{val} * F.\text{val} \end{array} \right.$$

$$T \rightarrow F \quad \{ T.\text{val} = F.\text{val} \}$$

$$F \rightarrow (E) \quad \{ F.\text{val} = E.\text{val} \}$$

$f \rightarrow \text{digit} \quad \{ \quad f.\text{val} = \text{digit.lexval} \}$

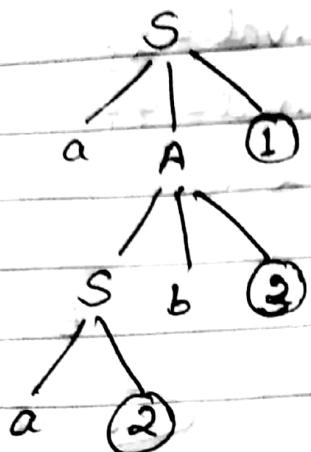
$$3 * 5 + 4n$$



Ex-

$$\begin{array}{l} S \xrightarrow{} aA \quad \{ \text{point 1} \} \\ S \xrightarrow{} a \quad \{ \text{point 2} \} \\ A \xrightarrow{} Sb \quad \{ \text{point 3} \} \end{array}$$

Parse "aab"

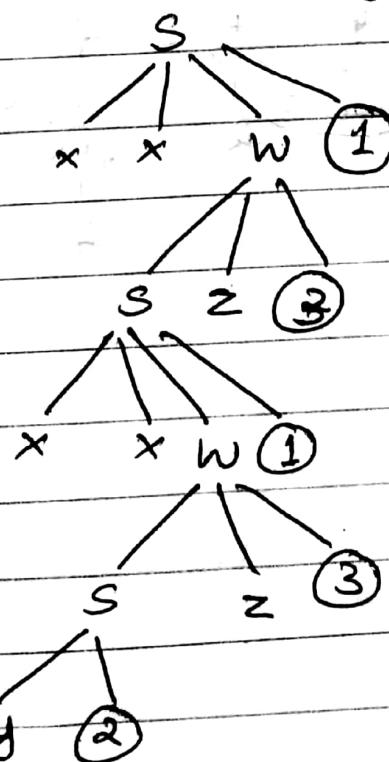


→ 2 3 1

Ex-

$$\begin{array}{l} S \xrightarrow{} xxw \quad \{ \text{point 1} \} \\ S \xrightarrow{} y \quad \{ \text{point 2} \} \\ w \xrightarrow{} Sz \quad \{ \text{point 3} \} \end{array}$$

Parse "xxxxyzz"



→ 2 3 1 3 1

Ex-

$$E \rightarrow E_1 * T$$

$$\{ E.val = E_1.val \times T.val \}$$

E → T

$\{ E.val = T.val \}$

$$T \rightarrow F - T_1$$

$\{ T.val = F.val - T.val \}$

T → F

$\{ T.val = F.val \}$

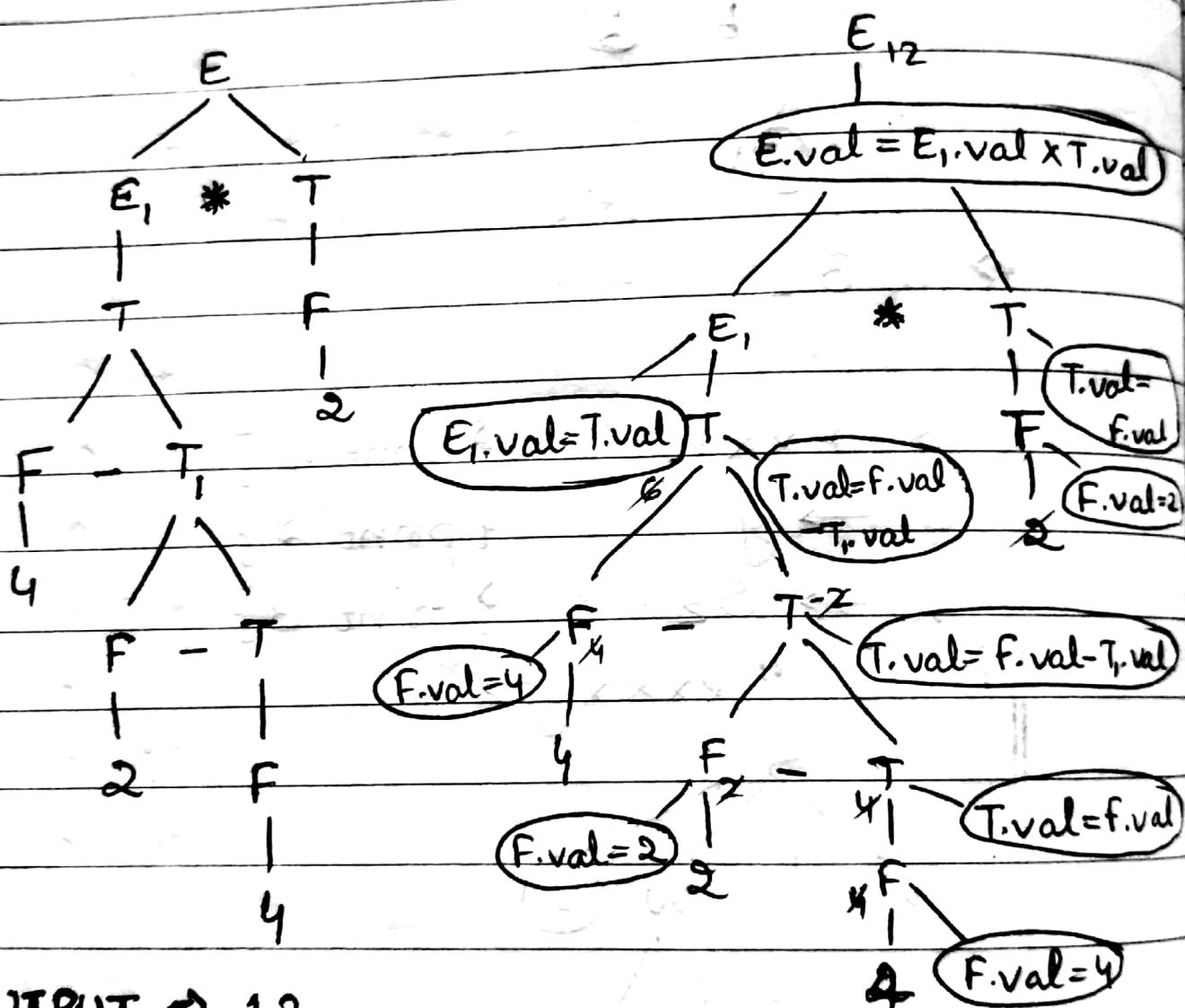
F-2

$\{ F.val = 2 \}$

F → 4

$\{ f.val = 4 \}$

INPUT \Rightarrow 4 - 2 - 4 * 2



OUTPUT → 12

22/9/17

SDTSyntax Directed Definition

- It is a CFG together with attributes & rules.
- Attributes are associated to grammar symbols & rules are associated with productions

eg- $\frac{x.a}{\text{Symbol}} \quad \frac{x \rightarrow a}{\text{Production rule}}$

Attributes of many types - number, String, type, table reference

Type of Attributes -

1. Synthesised Attribute -

2. Inherited Attribute -

Synthesized Attribute for a non-terminal A

At a parse tree node N is defined by semantic rule associated with the production of A at N.

- The production must have A at its head

A synthesised attribute at node N is defined only in term of attribute value at its children of N & at N itself.

$$\text{eg- } E.\text{value} = T.\text{val} + F.\text{val}$$

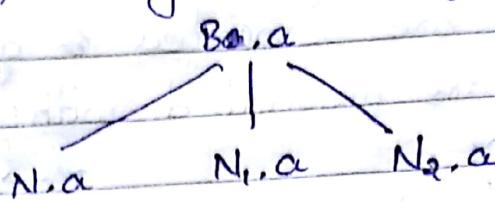
Inherited Attribute for non-terminal B

At a parse tree node N is defined by semantic rule associated with the production at the

parent of N.

A inherited attribute at Node N is defined only in term of attribute values at N's parent, siblings & itself.

e.g. $B.a$



Application of SDT

1. Converting infix to postfix
2. Converting infix to prefix.
3. Binary to decimal conversion

Example- $L \rightarrow E_n$

$E \rightarrow E, + T \quad \{ \text{point}(+) \}$

$E \rightarrow T$

$T \rightarrow T * F \quad \{ \text{point}(*) \}$

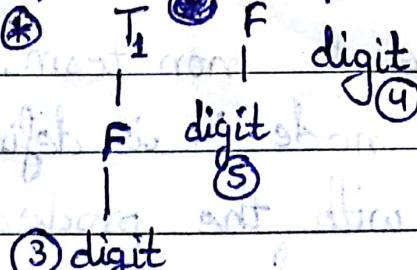
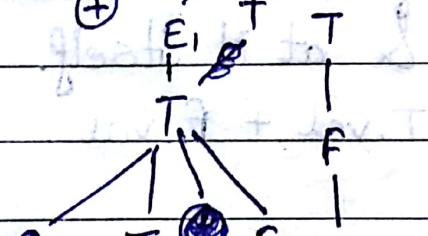
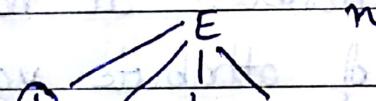
$T \rightarrow F$

$F \rightarrow (E)$

$F \rightarrow \text{digit} \quad \{ \text{point(digit.lexval)} \}$

INPUT $\Rightarrow 3 * 5 + 4$

Board it to A sword to L



OUTPUT $\Rightarrow 3 * 4 + 5$

(3) digit

More Applications of SDT

- Draw DAG (Directed Acyclic Graph)
- Generate Intermediate Code