

Dijkstra's Algorithm

Juggling Algorithm

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Array Rotation in Place

Suppose we have given an array of n integers and we have to rotate it by k positions to the left with in place. Complexity $O(1)$ i.e. within the same array (in-place)

1 2 3 4 5 6 $n=6$

$k=2$

3 4 5 6 1 2

1. Divide the array into sets/cycles

2. Shift every element in a set k places to the left.

3. Then move to the next set and repeat the process.

Step 1
1 2 3 4 5 6

temp=1
3 2 3 4 5 6

temp=1
3 2 5 4 5 6

Using temp we place 1

3 2 5 4 1 6

→ End of cycle 1

3 2 5 4 1 6

temp=2

3 4 5 4 1 6

// temp=2

3 4 5 6 1 6

Replace with temp

3 4 5 6 1 2

Step 1

Array Rotation in - Place

Divide the array into sets & rotate each element in set k position to left

Two loops

1. Outer loop - No. of sets

2. Inner loop - rotate elements of a set k positions to the left

1. How to find the no. of sets?

→ $\text{gcd}(n, k)$

2. How to ensure we shift the elements in a set k positions to the left?

3. When to move to the next set?

$$k=8 \quad n=9$$

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| A | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

O/P - should be

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 4 | 5 | 6 | 7 | 8 | 9 | 1 | 2 | 3 |
|---|---|---|---|---|---|---|---|---|

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| A | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

temp = 1

↑
j

↑
d

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

temp = 1

↑
d

↑
j

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

temp = 1

↑
d

↑
j

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

→ for wise. (array on)

- No. of sets will depend on the value of n & k
- no. of sets = $\text{gcd}(n, k)$
- gcd = greatest common divisor
- Outer loop $i = 0$ to $i < \text{no. of sets}$
- $A[i] = A[(j+k) \% n]$
 - ↳ so that we move in a cyclic way.
- Inner loop ends when $d = i$
- Increment i to move to next step

Set 1: 0, 3, 6
Set 2: 1, 4, 7
Set 3: 2, 5, 8

| i | j | d = (j+k) % n | A[j] = A[d] |
|---|---|----------------------|---------------|
| 0 | 0 | $d = (0+3) \% 9 = 3$ | $A[0] = A[3]$ |
| 0 | 3 | $d = (3+3) \% 9 = 6$ | $A[3] = A[6]$ |
| 0 | 6 | $d = (6+3) \% 9 = 0$ | $A[6] = A[0]$ |
| | | | ↳ temp = A[6] |
| 1 | 1 | $d = (1+3) \% 9 = 4$ | $A[1] = A[4]$ |
| 1 | 4 | $d = (4+3) \% 9 = 7$ | $A[4] = A[7]$ |
| 1 | 7 | $d = (7+3) \% 9 = 1$ | $d = i$ |
| | | | ↳ temp = A[7] |
| 2 | 2 | $d = (2+3) \% 9 = 5$ | $A[2] = A[5]$ |
| 2 | 5 | $d = (5+3) \% 9 = 8$ | $A[5] = A[8]$ |
| 2 | 8 | $d = (8+3) \% 9 = 2$ | $d = i$ |
| | | | ↳ temp = A[8] |