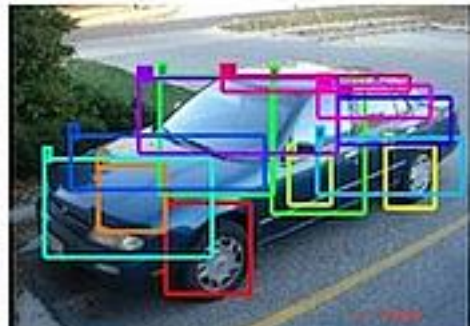
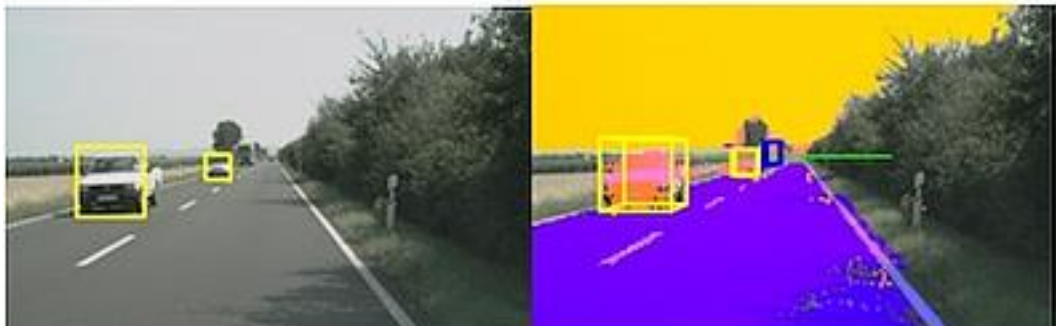
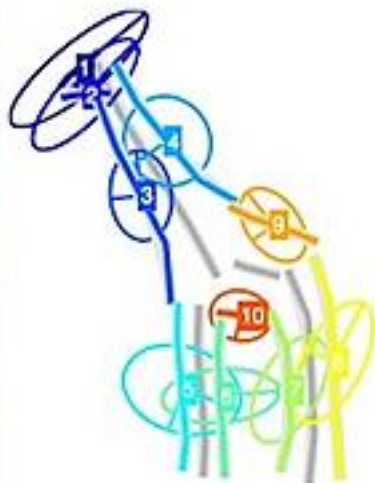
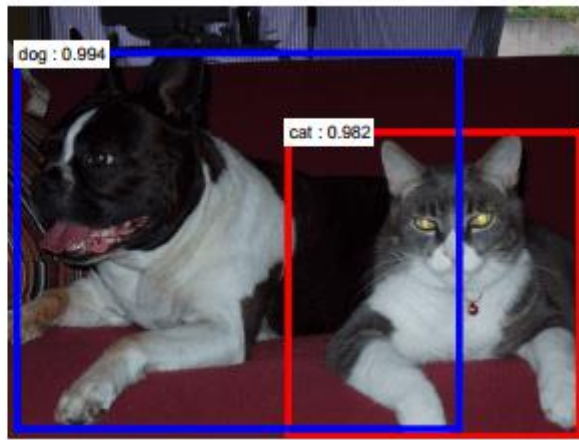
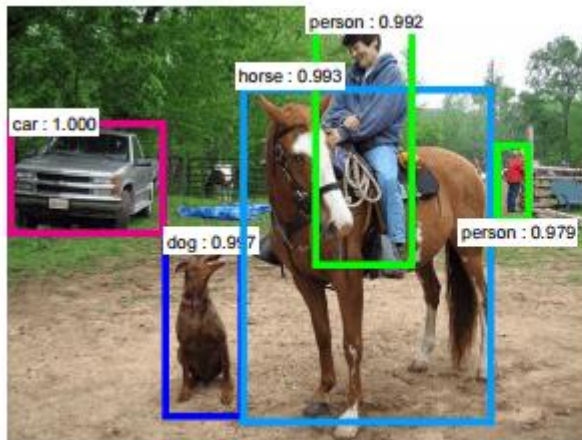
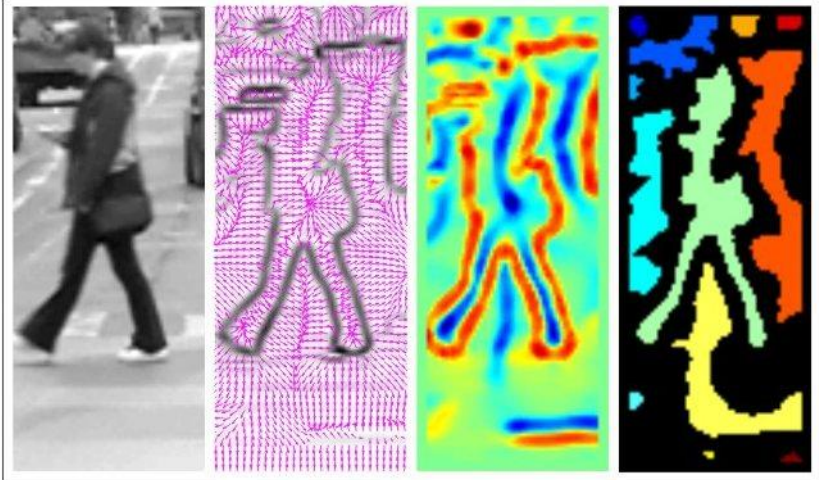


Convolutional Neural Networks



Convolution

- Convolution is a pointwise multiplication of two functions to produce a third function.
- Primary purpose of convolution in CNN is to extract features from the input image.
- matrix formed by sliding the filter over the image and computing the dot product is called the 'Convolved Feature' or 'Activation Map' or the 'Feature Map'.

CNNs Vs. ANNs

- ANNs suffer from curse of dimensionality when it comes to high resolution images
- CNNs do a little pre-processing, that means the network learns the filters before doing the real classification.
- We use filters (receptive fields) to exploit spatial locality by enforcing a local connectivity pattern between neurons of adjacent layers

Detecting Vertical edges

3	0	1	2	7	4
1	5	8	9	3	1
2	7	2	5	1	3
0	1	3	1	7	8
4	2	1	6	2	8
2	4	5	2	3	9

6X6 Matrix (nXn)

Convolution

*	1	0	-1
	1	0	-1
	1	0	-1

3X3 Filter (fXf)

=

-5	-4	0	8

(n-f+1)X(n-f+1)

Detecting Vertical edges

10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0



*

1	0	-1
1	0	-1
1	0	-1



0	30	30	0
0	30	30	0
0	30	30	0
0	30	30	0



Filter Weights

1	1	1
0	0	0
-1	-1	-1

Horizontal Filter

1	0	-1
2	0	-2
1	0	-1

Sobel Filter

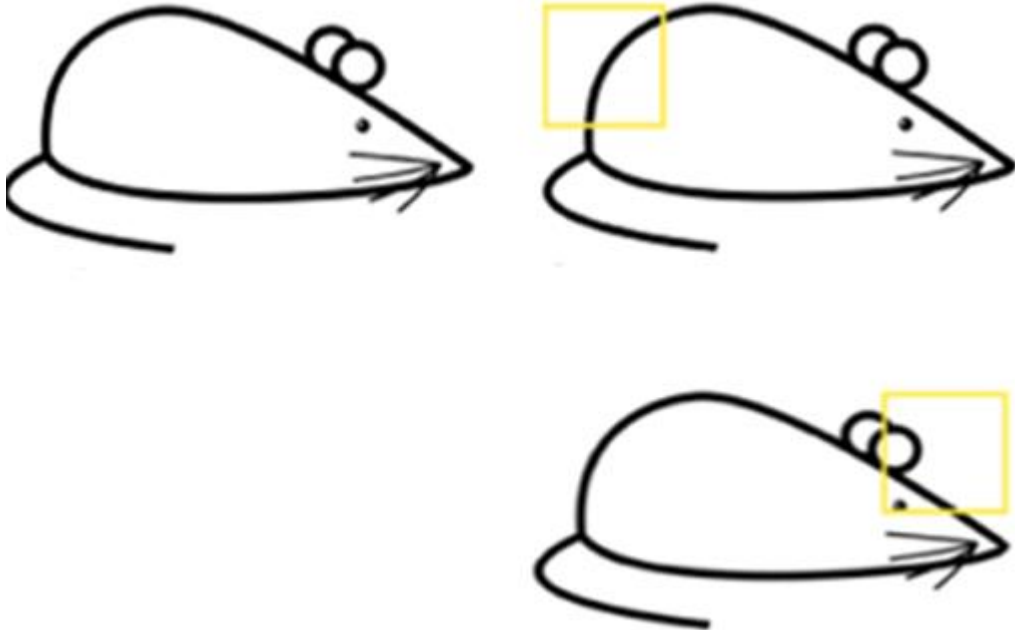
3	0	-3
10	0	-10
3	0	-3

Schorr Filter

w_1	w_2	w_3
w_4	w_5	w_6
w_7	w_8	w_9

Convolutional Neural Networks
automatically estimates the
weights of the filter

More Intuition



0	0	0	0	0	30	0
0	0	0	0	30	0	0
0	0	0	30	0	0	0
0	0	0	30	0	0	0
0	0	0	30	0	0	0
0	0	0	30	0	0	0
0	0	0	0	0	0	0

Pixel representation of filter

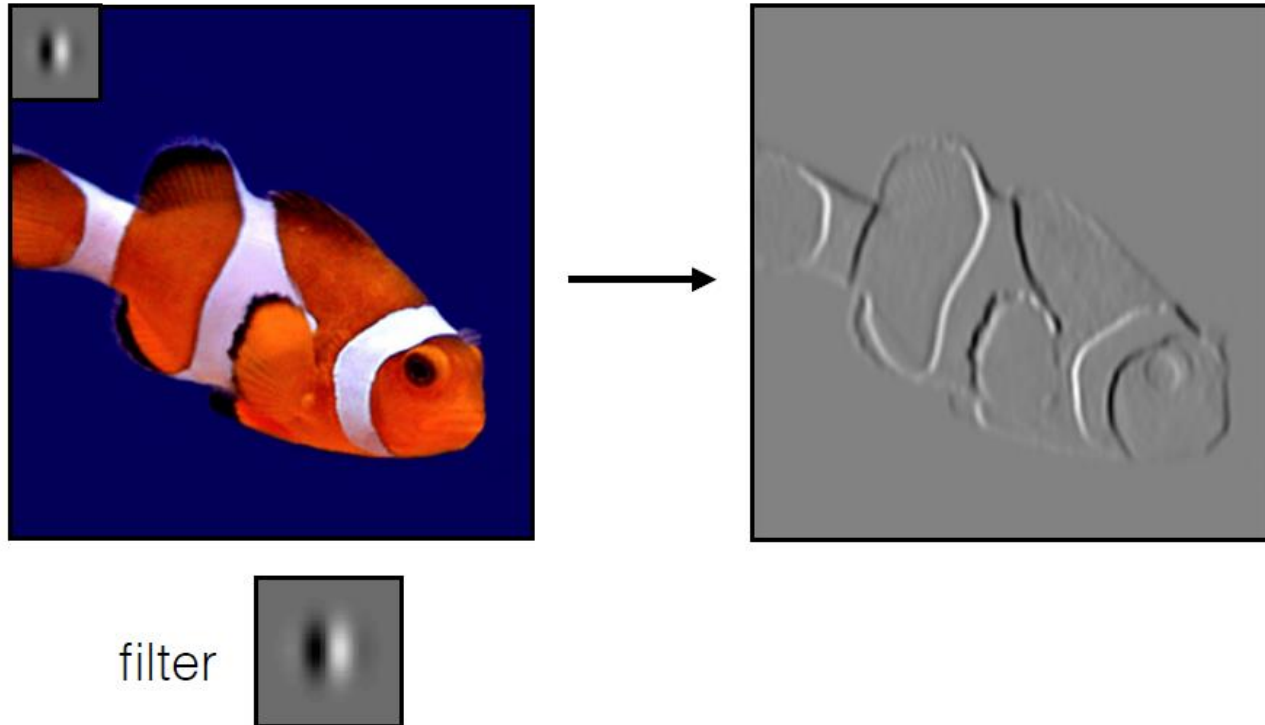


Visualization of a curve detector filter

Interpretation

Convolution is just another way of computing $W^T X$

In CNN, **input** is **image**, **kernel** is **convolution filter** to be learned, **response** is the **feature map**



Padding

Padding is used to preserve the original dimensions of the input

Zeros are added to outside of the input

Number of zero layers depend upon the size of the kernel

0	0	0	0	0	0	0
0	1	1	1	0	0	0
0	0	1	1	1	0	0
0	0	0	1	1	1	0
0	0	1	1	1	0	0
0	0	1	1	0	0	0
0	0	0	0	0	0	0

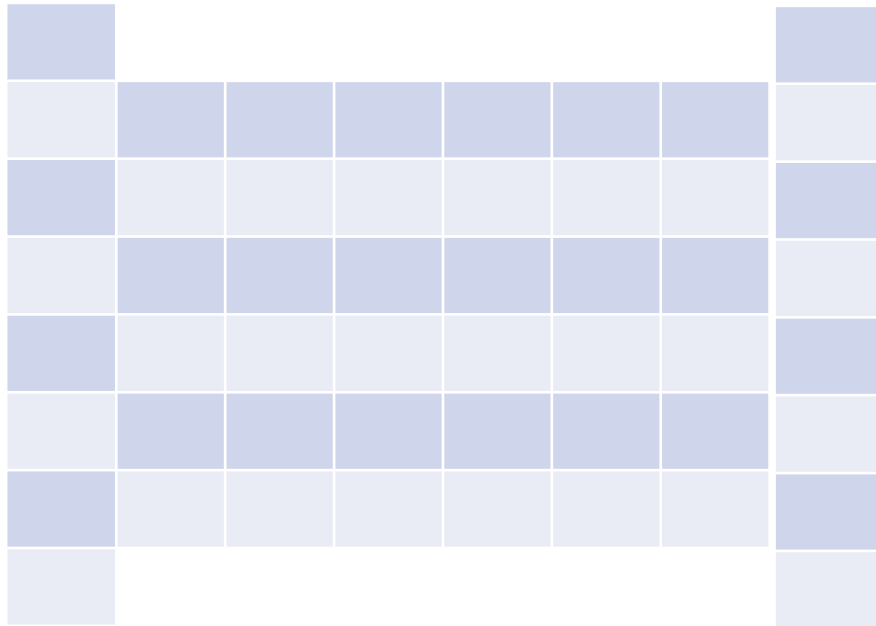
5X5 (with padding)

x1	x0	x1
x0	x1	x0
x1	x0	x1

2	2	3	1	1
1	4	3	4	1
2	2	4	3	3
1	2	3	4	1
1	2	3	1	1

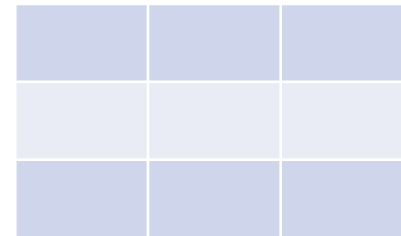
5X5

Padding



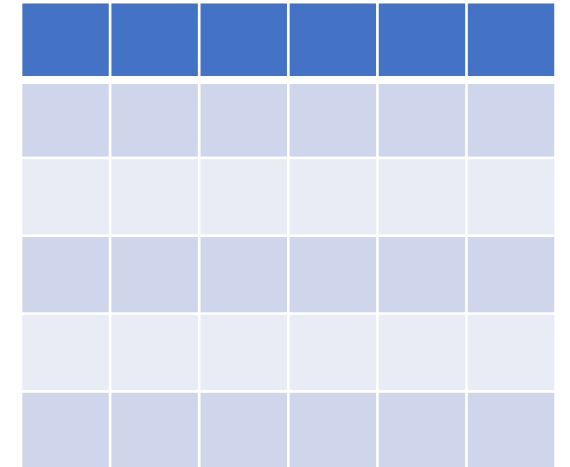
$n \times n$ 6X6 to 8X8 Padding=1

*



f 3X3

=



$(n-f+1) \times (n-f+1)$ to $(n+2p-f+1) \times (n+2p-f+1)$
Valid to same

Stride= s

$$\text{Floor}\left(\frac{n+2p-f}{s} + 1\right) \times \text{Floor}\left(\frac{n+2p-f}{s} + 1\right)$$

Stride

3	0	1	2	7	4
1	5	8	9	3	1
2	7	2	5	1	3
0	1	3	1	7	8
4	2	1	6	2	8
2	4	5	2	3	9

6X6 Matrix

1	0	-1
1	0	-1
1	0	-1

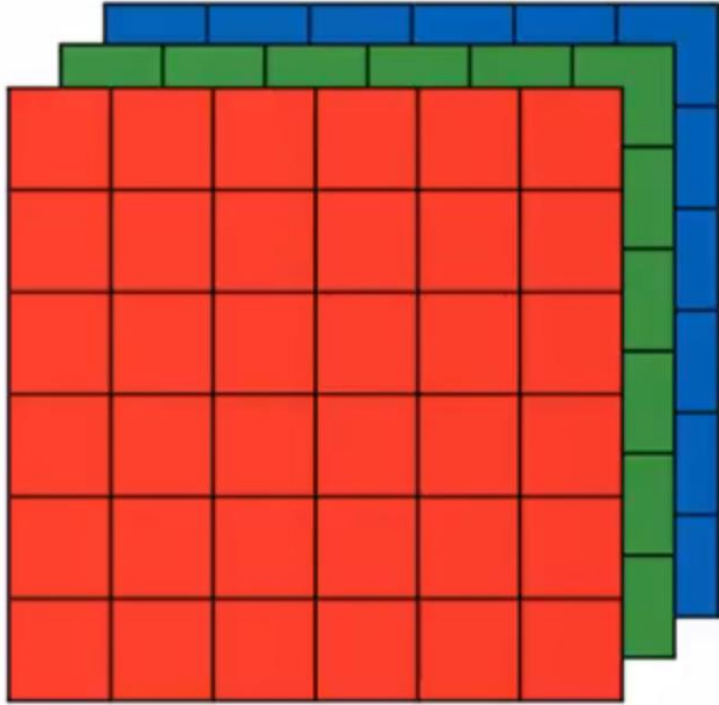
3X3 Filter

-5	8
-3	-16

2X2

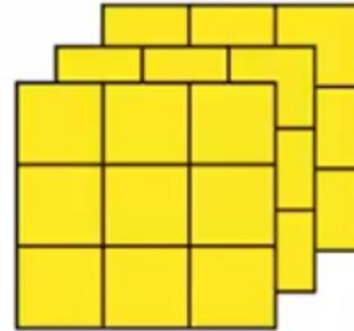
Stride=s (3 Here) $\text{Floor}(\frac{n+2p-f}{s} + 1) \times \text{Floor}(\frac{n+2p-f}{s} + 1)$

Channels



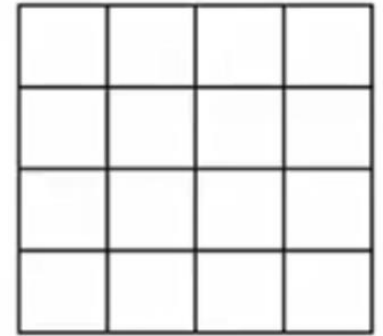
6X6 Matrix

*



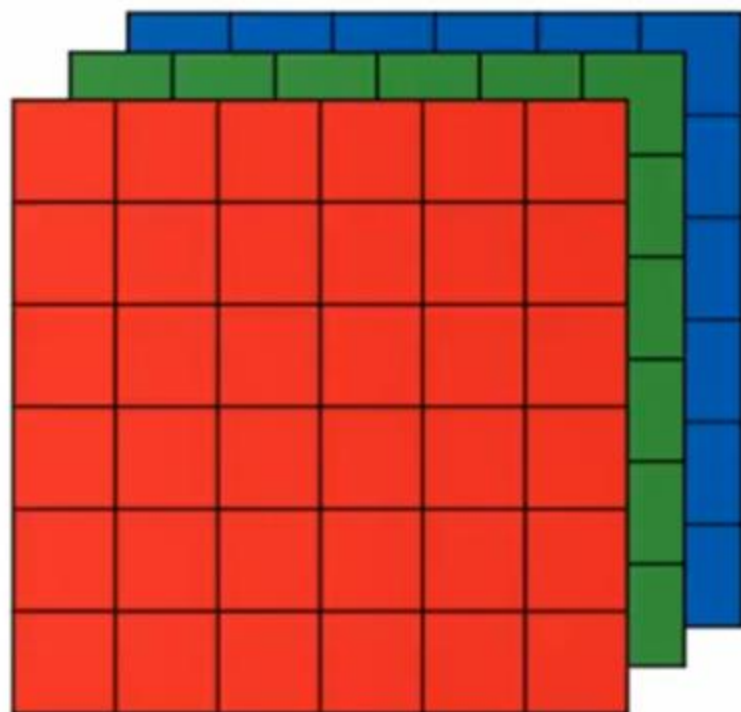
3X3 Filter

=



4 x 4

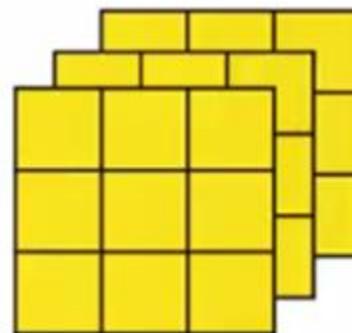
Padding =0 Stride=1



$6 \times 6 \times 3$

$n \times n \times n_c$

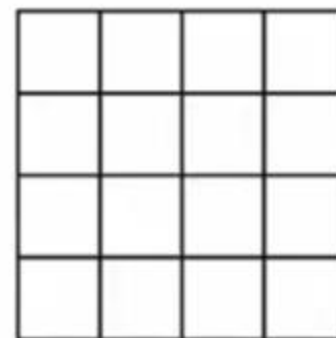
*



$3 \times 3 \times 3$

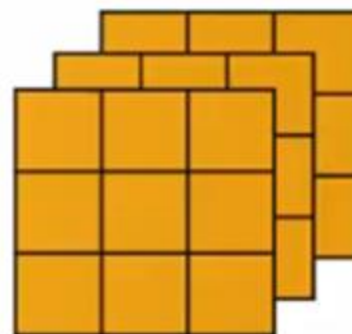
$f \times f \times n_c$

=



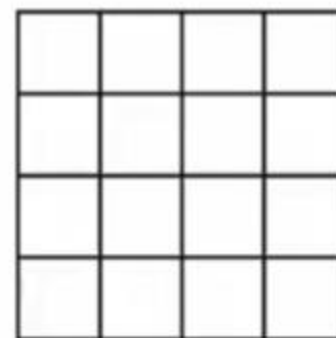
4×4

*



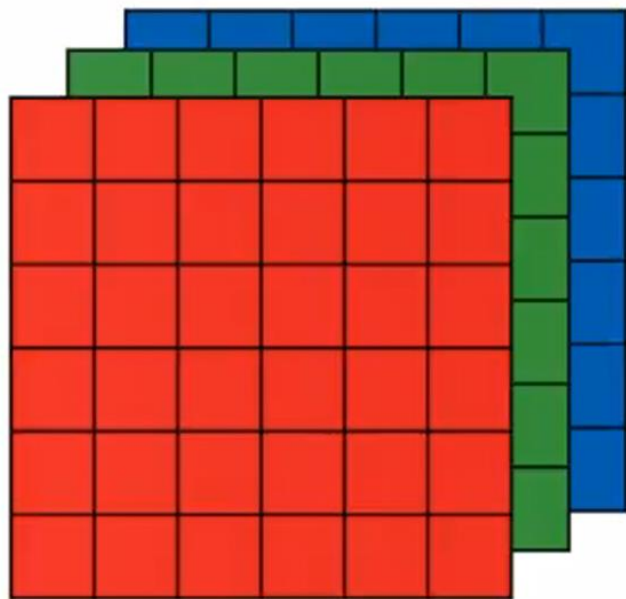
$3 \times 3 \times 3$

=



4×4

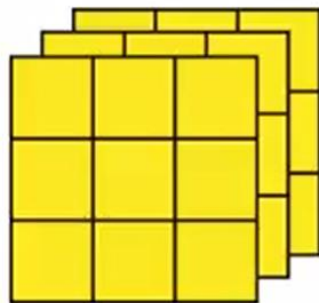
$n-f+1 \times n-f+1 \times n_{c'}$ c' =no of filters



$6 \times 6 \times 3$

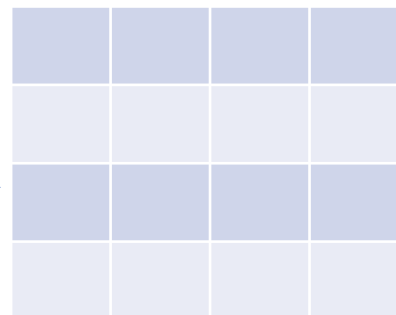
$a^{[0]}$

*

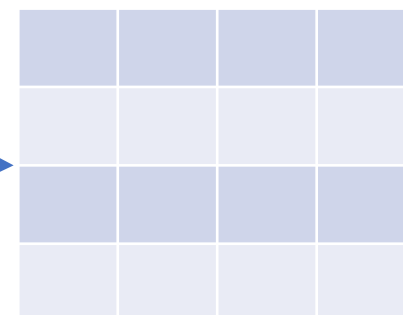


$3 \times 3 \times 3$

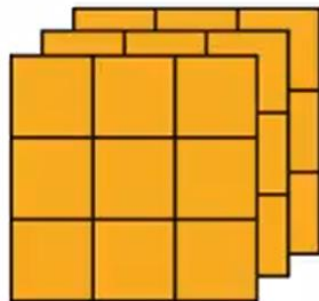
ReLU



+b1

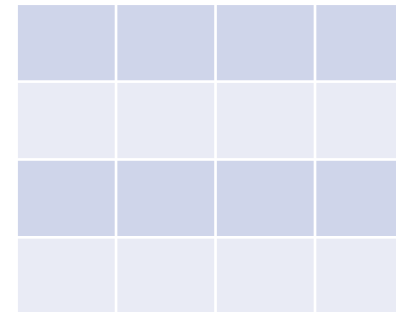


*

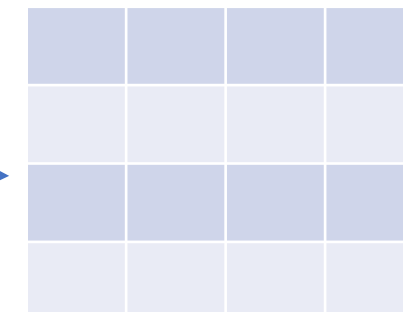


$3 \times 3 \times 3$

ReLU



+b1



$w^{[1]} a^{[0]}$

$a^{[1]} 4 \times 4 \times 2$

$w^{[1]}$ 2 filters means two units here

Pooling

1	4	6	3
1	8	9	7
2	9	1	2
3	4	4	3

8	9
9	4

Max Pooling : One example of pooling layer

$f=2$

$s=2$ 4X4 converted to 2X2

Function of Pooling is to progressively reduce the spatial size of the representation to reduce the amount of parameters and computation in the network.

Pooling

1	4	6	3
1	8	9	7
2	9	1	2
3	4	4	3

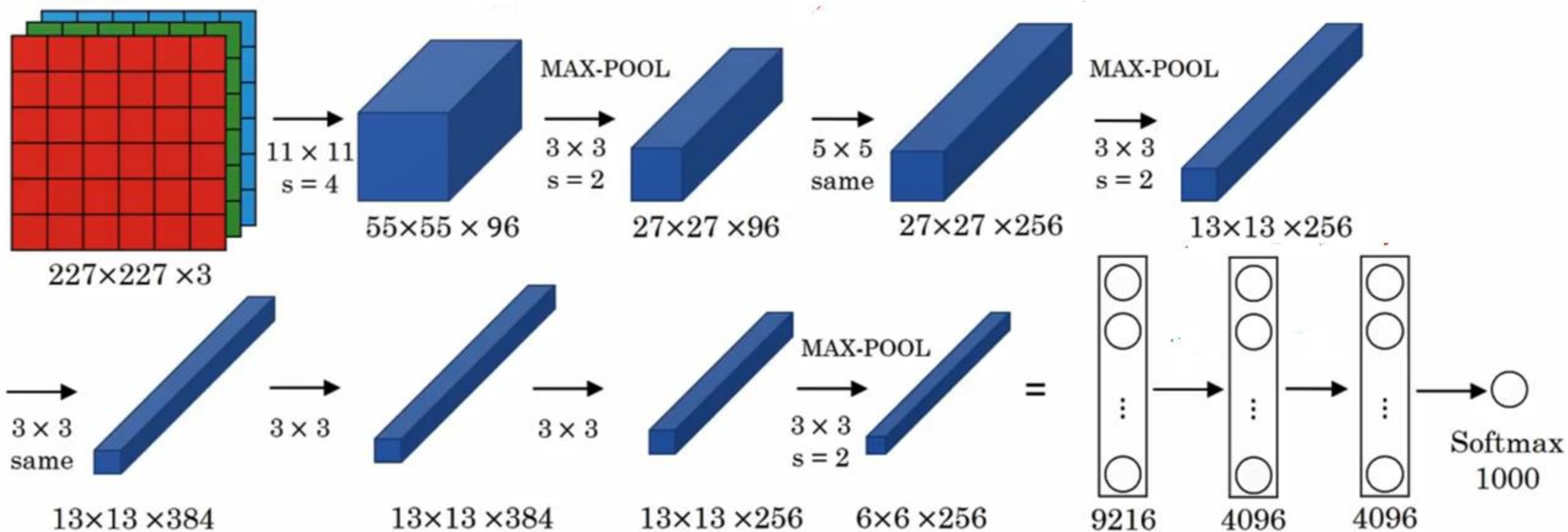
3.5	6.25
4.5	2.5

Average Pooling : Another example of pooling layer

$f=2$

$s=2$ 4X4 converted to 2X2

AlexNet



Famous CNN Models

LeNet - 1990

AlexNet - 2012

ZFNet - 2013

GoogLeNet - 2014

VGGNet - 2014

ResNet - 2015

Inception v3 - 2016

MobileNet - 2017