Implementing a Neural Network

In this exercise we will develop a neural network with fully-connected layers to perform classification, and test it out on the CIFAR-10 dataset.

```
In [1]:
```

```
# A bit of setup
import numpy as np
import matplotlib.pyplot as plt
from cs175.classifiers.neural net import TwoLayerNet
from __future__ import print_function
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'
# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipytho
n
%load ext autoreload
%autoreload 2
def rel error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

We will use the class TwoLayerNet in the file cs175/classifiers/neural_net.py to represent instances of our network. The network parameters are stored in the instance variable self.params where keys are string parameter names and values are numpy arrays. Below, we initialize toy data and a toy model that we will use to develop your implementation.

```
In [2]:
```

```
# Create a small net and some toy data to check your implementations.
# Note that we set the random seed for repeatable experiments.
input size = 4
hidden size = 10
num classes = 3
num_inputs = 5
def init toy model():
    np.random.seed(0)
    return TwoLayerNet(input size, hidden size, num classes, std=1e-1)
def init_toy_data():
    np.random.seed(1)
    X = 10 * np.random.randn(num inputs, input size)
    y = np.array([0, 1, 2, 2, 1])
    return X, y
net = init toy model()
X, y = init_toy_data()
```

Forward pass: compute scores

Open the file cs175/classifiers/neural_net.py and look at the method TwoLayerNet.loss. This function is very similar to the loss functions you have written for the SVM and Softmax exercises: It takes the data and weights and computes the class scores, the loss, and the gradients on the parameters.

Implement the first part of the forward pass which uses the weights and biases to compute the scores for all inputs.

```
In [3]:
scores = net.loss(X)
print('Your scores:')
print(scores)
print()
print('correct scores:')
correct scores = np.asarray([
  [-0.81233741, -1.27654624, -0.70335995],
  [-0.17129677, -1.18803311, -0.47310444],
  [-0.51590475, -1.01354314, -0.8504215],
  [-0.15419291, -0.48629638, -0.52901952],
  [-0.00618733, -0.12435261, -0.15226949]])
print(correct scores)
print()
# The difference should be very small. We get < 1e-7
print('Difference between your scores and correct scores:')
print(np.sum(np.abs(scores - correct_scores)))
Your scores:
[[-0.81233741 -1.27654624 -0.70335995]
 [-0.17129677 -1.18803311 -0.47310444]
 [-0.51590475 -1.01354314 -0.8504215]
 [-0.15419291 -0.48629638 -0.52901952]
```

```
[[-0.81233741 -1.27654624 -0.70335995]
[-0.17129677 -1.18803311 -0.47310444]
[-0.51590475 -1.01354314 -0.8504215 ]
[-0.15419291 -0.48629638 -0.52901952]
[-0.00618733 -0.12435261 -0.15226949]]

correct scores:
[[-0.81233741 -1.27654624 -0.70335995]
[-0.17129677 -1.18803311 -0.47310444]
[-0.51590475 -1.01354314 -0.8504215 ]
[-0.15419291 -0.48629638 -0.52901952]
[-0.00618733 -0.12435261 -0.15226949]]

Difference between your scores and correct scores:
3.6802720496109664e-08
```

Forward pass: compute loss

In the same function, implement the second part that computes the data and regularization loss.

```
In [4]:

loss, _ = net.loss(X, y, reg=0.05)
correct_loss = 1.30378789133

# should be very small, we get < 1e-12
print('Difference between your loss and correct loss:')
print(np.sum(np.abs(loss - correct_loss)))</pre>
```

Difference between your loss and correct loss: 1.7985612998927536e-13

Backward pass

Implement the rest of the function. This will compute the gradient of the loss with respect to the variables W1, b1, W2, and b2. Now that you (hopefully!) have a correctly implemented forward pass, you can debug your backward pass using a numeric gradient check:

In [5]:

```
from cs175.gradient_check import eval_numerical_gradient

# Use numeric gradient checking to check your implementation of the backward pas
s.

# If your implementation is correct, the difference between the numeric and
# analytic gradients should be less than 1e-8 for each of W1, W2, b1, and b2.

loss, grads = net.loss(X, y, reg=0.05)

# these should all be less than 1e-8 or so
for param_name in grads:
    f = lambda W: net.loss(X, y, reg=0.05)[0]
    param_grad_num = eval_numerical_gradient(f, net.params[param_name], verbose=
False)
    print('%s max relative error: %e' % (param_name, rel_error(param_grad_num, g
rads[param_name])))
```

```
W2 max relative error: 3.333333e-01
b2 max relative error: 3.865091e-11
W1 max relative error: 8.002490e-01
b1 max relative error: 1.555470e-09
```

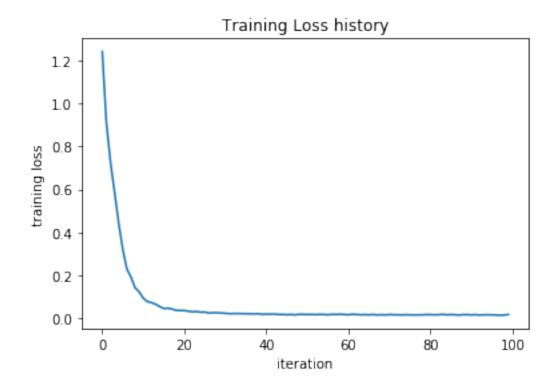
Train the network

To train the network we will use stochastic gradient descent (SGD), similar to the SVM and Softmax classifiers. Look at the function <code>TwoLayerNet.train</code> and fill in the missing sections to implement the training procedure. This should be very similar to the training procedure you used for the SVM and Softmax classifiers. You will also have to implement <code>TwoLayerNet.predict</code>, as the training process periodically performs prediction to keep track of accuracy over time while the network trains.

Once you have implemented the method, run the code below to train a two-layer network on toy data. You should achieve a training loss less than 0.2.

In [6]:

Final training loss: 0.017149085837733297



Load the data

Now that you have implemented a two-layer network that passes gradient checks and works on toy data, it's time to load up our favorite CIFAR-10 data so we can use it to train a classifier on a real dataset.

```
from cs175.data utils import load CIFAR10
def get CIFAR10 data(num training=49000, num validation=1000, num test=1000):
    Load the CIFAR-10 dataset from disk and perform preprocessing to prepare
    it for the two-layer neural net classifier. These are the same steps as
    we used for the SVM, but condensed to a single function.
    # Load the raw CIFAR-10 data
    cifar10 dir = 'cs175/datasets/cifar-10-batches-py'
    X train, y train, X test, y test = load CIFAR10(cifar10 dir)
    # Subsample the data
    mask = list(range(num training, num training + num validation))
    X val = X train[mask]
    y val = y train[mask]
    mask = list(range(num training))
    X train = X train[mask]
    y_train = y_train[mask]
    mask = list(range(num test))
    X test = X test[mask]
    y_test = y_test[mask]
    # Normalize the data: subtract the mean image
    mean image = np.mean(X train, axis=0)
    X train -= mean image
    X val -= mean image
    X test -= mean image
    # Reshape data to rows
    X train = X train.reshape(num training, -1)
    X val = X val.reshape(num validation, -1)
    X test = X test.reshape(num test, -1)
    return X train, y train, X val, y val, X test, y test
# Invoke the above function to get our data.
X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: ', X val.shape)
print('Validation labels shape: ', y_val.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y test.shape)
```

```
Train data shape: (49000, 3072)
Train labels shape: (49000,)
Validation data shape: (1000, 3072)
Validation labels shape: (1000,)
Test data shape: (1000, 3072)
Test labels shape: (1000,)
```

Train a network

To train our network we will use SGD with momentum. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate.

In [8]:

```
iteration 0 / 1000: loss 2.302954
iteration 100 / 1000: loss 2.302550
iteration 200 / 1000: loss 2.297603
iteration 300 / 1000: loss 2.259162
iteration 400 / 1000: loss 2.203468
iteration 500 / 1000: loss 2.117619
iteration 600 / 1000: loss 2.050917
iteration 700 / 1000: loss 1.987152
iteration 800 / 1000: loss 2.005458
iteration 900 / 1000: loss 1.950105
Validation accuracy: 0.287
```

Debug the training

With the default parameters we provided above, you should get a validation accuracy of about 0.29 on the validation set. This isn't very good.

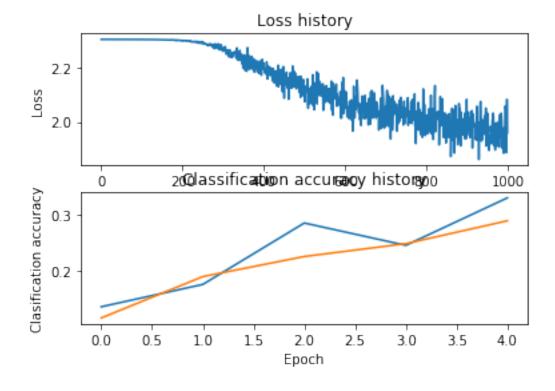
One strategy for getting insight into what's wrong is to plot the loss function and the accuracies on the training and validation sets during optimization.

Another strategy is to visualize the weights that were learned in the first layer of the network. In most neural networks trained on visual data, the first layer weights typically show some visible structure when visualized.

In [9]:

```
# Plot the loss function and train / validation accuracies
plt.subplot(2, 1, 1)
plt.plot(stats['loss_history'])
plt.title('Loss history')
plt.xlabel('Iteration')
plt.ylabel('Loss')

plt.subplot(2, 1, 2)
plt.plot(stats['train_acc_history'], label='train')
plt.plot(stats['val_acc_history'], label='val')
plt.title('Classification accuracy history')
plt.xlabel('Epoch')
plt.ylabel('Clasification accuracy')
plt.show()
```



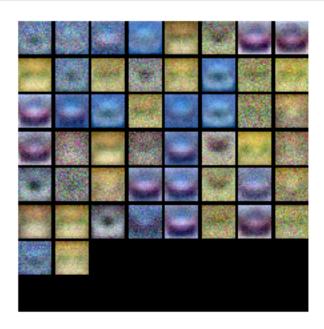
In [10]:

```
from cs175.vis_utils import visualize_grid

# Visualize the weights of the network

def show_net_weights(net):
    W1 = net.params['W1']
    W1 = W1.reshape(32, 32, 3, -1).transpose(3, 0, 1, 2)
    plt.imshow(visualize_grid(W1, padding=3).astype('uint8'))
    plt.gca().axis('off')
    plt.show()

show_net_weights(net)
```



Tune your hyperparameters

What's wrong?. Looking at the visualizations above, we see that the loss is decreasing more or less linearly, which seems to suggest that the learning rate may be too low. Moreover, there is no gap between the training and validation accuracy, suggesting that the model we used has low capacity, and that we should increase its size. On the other hand, with a very large model we would expect to see more overfitting, which would manifest itself as a very large gap between the training and validation accuracy.

Tuning. Tuning the hyperparameters and developing intuition for how they affect the final performance is a large part of using Neural Networks, so we want you to get a lot of practice. Below, you should experiment with different values of the various hyperparameters, including hidden layer size, learning rate, numer of training epochs, and regularization strength. You might also consider tuning the learning rate decay, but you should be able to get good performance using the default value.

Approximate results. You should be aim to achieve a classification accuracy of greater than 48% on the validation set. Our best network gets over 52% on the validation set.

Experiment: You goal in this exercise is to get as good of a result on CIFAR-10 as you can, with a fully-connected Neural Network. For every 1% above 52% on the Test set we will award you with one extra bonus point. Feel free implement your own techniques (e.g. PCA to reduce dimensionality, or adding dropout, or adding features to the solver, etc.).

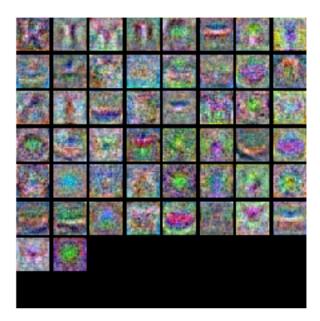
In [11]:

```
best net = None # store the best model into this
best val = 0
results = {}
#
# TODO: Tune hyperparameters using the validation set. Store your best trained
#
#
 model in best net.
#
#
 To help debug your network, it may help to use visualizations similar to the
#
#
 ones we used above; these visualizations will have significant qualitative
#
# differences from the ones we saw above for the poorly tuned network.
#
#
#
 Tweaking hyperparameters by hand can be fun, but you might find it useful to
#
 write code to sweep through possible combinations of hyperparameters
```

```
# automatically like we did on the previous exercises.
learning rates = [1e-3, 5e-4]
regularization strengths = [0.1,0.2]#0.3,0.4,0.5]
for lr in learning rates:
   for reg in regularization strengths:
       neural net = TwoLayerNet(input size, hidden size, num classes)
      neural_net.train(X_train, y_train, X_val, y_val,
                 num iters=3000, batch size=200,
                 learning rate=lr, learning rate decay=0.95,
                 reg=reg)
      y train pred = neural net.predict(X train)
       acc_train = np.mean(y_train == y_train_pred)
       y val pred = neural net.predict(X val)
       acc_val = np.mean(y_val == y_val_pred)
      results[(lr, reg)] = (acc train, acc val)
       if best val < acc val:</pre>
          best val = acc val
          best net = neural net
# Print out results.
for lr, reg in sorted(results):
   train accuracy, val accuracy = results[(lr, reg)]
   print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
              lr, reg, train accuracy, val accuracy))
print('best validation accuracy achieved during cross-validation: %f' % best val
)
#
#
                           END OF YOUR CODE
lr 5.000000e-04 reg 1.000000e-01 train accuracy: 0.526673 val accura
cy: 0.492000
lr 5.000000e-04 reg 2.000000e-01 train accuracy: 0.523286 val accura
cy: 0.471000
lr 1.000000e-03 reg 1.000000e-01 train accuracy: 0.562408 val accura
cy: 0.505000
lr 1.000000e-03 reg 2.000000e-01 train accuracy: 0.553490 val accura
cy: 0.493000
best validation accuracy achieved during cross-validation: 0.505000
```

In [12]:

visualize the weights of the best network
show net weights(best net)



Run on the test set

When you are done experimenting, you should evaluate your final trained network on the test set; you should get above 48%.

We will give you extra bonus point for every 1% of accuracy above 52%.

```
In [13]:

test_acc = (best_net.predict(X_test) == y_test).mean()
print('Test accuracy: ', test_acc)

Test accuracy: 0.497

In [ ]:
In [ ]:
```

Image features exercise

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For more details see the <u>assignments page</u> (http://vision.stanford.edu/teaching/cs175/assignments.html) on the course website.

We have seen that we can achieve reasonable performance on an image classification task by training a linear classifier on the pixels of the input image. In this exercise we will show that we can improve our classification performance by training linear classifiers not on raw pixels but on features that are computed from the raw pixels.

All of your work for this exercise will be done in this notebook.

```
In [1]:
```

```
import random
import numpy as np
from cs175.data_utils import load_CIFAR10
import matplotlib.pyplot as plt

from __future__ import print_function

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading extenrnal modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipytho
n
%load_ext autoreload
%autoreload 2
```

Load data

Similar to previous exercises, we will load CIFAR-10 data from disk.

```
from cs175.features import color histogram hsv, hog feature
def get CIFAR10 data(num training=49000, num validation=1000, num test=1000):
    # Load the raw CIFAR-10 data
    cifar10 dir = 'cs175/datasets/cifar-10-batches-py'
    X train, y train, X test, y test = load CIFAR10(cifar10 dir)
    # Subsample the data
   mask = list(range(num_training, num training + num validation))
   X val = X train[mask]
   y_val = y_train[mask]
   mask = list(range(num training))
   X_train = X_train[mask]
   y train = y train[mask]
   mask = list(range(num test))
   X_test = X_test[mask]
   y_test = y_test[mask]
    return X train, y train, X val, y val, X test, y test
X train, y train, X val, y val, X test, y test = get CIFAR10 data()
```

Extract Features

For each image we will compute a Histogram of Oriented Gradients (HOG) as well as a color histogram using the hue channel in HSV color space. We form our final feature vector for each image by concatenating the HOG and color histogram feature vectors.

Roughly speaking, HOG should capture the texture of the image while ignoring color information, and the color histogram represents the color of the input image while ignoring texture. As a result, we expect that using both together ought to work better than using either alone. Verifying this assumption would be a good thing to try for the bonus section.

The hog_feature and color_histogram_hsv functions both operate on a single image and return a feature vector for that image. The extract_features function takes a set of images and a list of feature functions and evaluates each feature function on each image, storing the results in a matrix where each column is the concatenation of all feature vectors for a single image.

```
from cs175.features import *
num color bins = 10 # Number of bins in the color histogram
feature fns = [hog feature, lambda img: color histogram hsv(img, nbin=num color
bins)]
X_train_feats = extract_features(X_train, feature_fns, verbose=True)
X_val_feats = extract_features(X_val, feature_fns)
X test feats = extract features(X test, feature fns)
# Preprocessing: Subtract the mean feature
mean feat = np.mean(X train feats, axis=0, keepdims=True)
X train feats -= mean feat
X_val_feats -= mean_feat
X test feats -= mean feat
# Preprocessing: Divide by standard deviation. This ensures that each feature
# has roughly the same scale.
std feat = np.std(X train feats, axis=0, keepdims=True)
X_train_feats /= std_feat
X val feats /= std feat
X test feats /= std feat
# Preprocessing: Add a bias dimension
X train feats = np.hstack([X train_feats, np.ones((X_train_feats.shape[0], 1))])
X_val_feats = np.hstack([X_val_feats, np.ones((X_val_feats.shape[0], 1))])
X_test_feats = np.hstack([X_test_feats, np.ones((X_test_feats.shape[0], 1))])
```

```
Done extracting features for 1000 / 49000 images
Done extracting features for 2000 / 49000 images
Done extracting features for 3000 / 49000 images
Done extracting features for 4000 / 49000 images
Done extracting features for 5000 / 49000 images
Done extracting features for 6000 / 49000 images
Done extracting features for 7000 / 49000 images
Done extracting features for 8000 / 49000 images
Done extracting features for 9000 / 49000 images
Done extracting features for 10000 / 49000 images
Done extracting features for 11000 / 49000 images
Done extracting features for 12000 / 49000 images
Done extracting features for 13000 / 49000 images
Done extracting features for 14000 / 49000 images
Done extracting features for 15000 / 49000 images
Done extracting features for 16000 / 49000 images
Done extracting features for 17000 / 49000 images
Done extracting features for 18000 / 49000 images
Done extracting features for 19000 / 49000 images
Done extracting features for 20000 / 49000 images
Done extracting features for 21000 / 49000 images
Done extracting features for 22000 / 49000 images
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Done extracting features for 30000 / 49000 images
Done extracting features for 31000 / 49000 images
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Done extracting features for 37000 / 49000 images
Done extracting features for 38000 / 49000 images
Done extracting features for 39000 / 49000 images
Done extracting features for 40000 / 49000 images
Done extracting features for 41000 / 49000 images
Done extracting features for 42000 / 49000 images
Done extracting features for 43000 / 49000 images
Done extracting features for 44000 / 49000 images
Done extracting features for 45000 / 49000 images
Done extracting features for 46000 / 49000 images
Done extracting features for 47000 / 49000 images
Done extracting features for 48000 / 49000 images
```

Train SVM on features

Using the multiclass SVM code developed earlier in the assignment, train SVMs on top of the features extracted above; this should achieve better results than training SVMs directly on top of raw pixels.

```
In [4]:
# Use the validation set to tune the learning rate and regularization strength
from cs175.classifiers.linear classifier import LinearSVM
learning rates = [1e-9, 1e-8, 1e-7]
regularization strengths = [5e4, 5e5, 5e6]
results = {}
best val = -1
best svm = None
# TODO:
# Use the validation set to set the learning rate and regularization strength. #
# This should be identical to the validation that you did for the SVM; save
                                                                 #
# the best trained classifer in best svm. You might also want to play
                                                                 #
# with different numbers of bins in the color histogram. If you are careful
                                                                 #
# you should be able to get accuracy of near 0.44 on the validation set.
                                                                 #
for lr in learning rates:
   for reg in regularization strengths:
      svm=LinearSVM()
      svm.train(X train feats, y train, learning rate=lr, reg=reg, num iters=8
00)
      y train pred = svm.predict(X train feats)
      y val pred=svm.predict(X val feats)
      accuracy train=np.mean(y train==y train pred)
      accuracy val=np.mean(y val==y val pred)
      results[(lr, reg)] = (accuracy train, accuracy val)
      if accuracy val > best val:
         best val = accuracy val
         best svm = svm
END OF YOUR CODE
# Print out results.
for lr, reg in sorted(results):
   train accuracy, val accuracy = results[(lr, reg)]
   print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
             lr, reg, train accuracy, val accuracy))
print('best validation accuracy achieved during cross-validation: %f' % best val
```

```
lr 1.000000e-09 reg 5.000000e+04 train accuracy: 0.089122 val accura
cy: 0.089000
lr 1.000000e-09 reg 5.000000e+05 train accuracy: 0.098878 val accura
cy: 0.086000
lr 1.000000e-09 reg 5.000000e+06 train accuracy: 0.080653 val accura
cy: 0.066000
lr 1.000000e-08 reg 5.000000e+04 train accuracy: 0.102286 val accura
cy: 0.097000
lr 1.000000e-08 reg 5.000000e+05 train accuracy: 0.146102 val accura
cy: 0.158000
lr 1.000000e-08 reg 5.000000e+06 train accuracy: 0.417408 val accura
cy: 0.419000
lr 1.000000e-07 reg 5.000000e+04 train accuracy: 0.203388 val accura
cy: 0.202000
lr 1.000000e-07 reg 5.000000e+05 train accuracy: 0.411429 val accura
cy: 0.418000
lr 1.000000e-07 reg 5.000000e+06 train accuracy: 0.360224 val accura
cy: 0.348000
best validation accuracy achieved during cross-validation: 0.419000
```

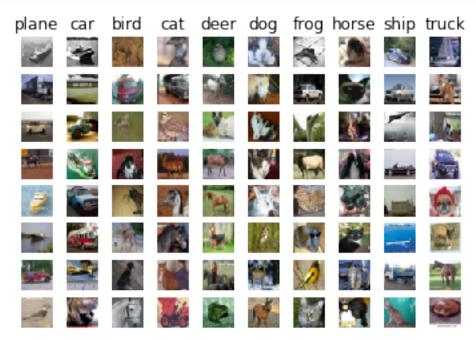
In [5]:

```
# Evaluate your trained SVM on the test set
y_test_pred = best_svm.predict(X_test_feats)
test_accuracy = np.mean(y_test == y_test_pred)
print(test_accuracy)
```

0.427

```
In [6]:
```

```
# An important way to gain intuition about how an algorithm works is to
# visualize the mistakes that it makes. In this visualization, we show examples
# of images that are misclassified by our current system. The first column
# shows images that our system labeled as "plane" but whose true label is
# something other than "plane".
examples_per_class = 8
classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 'ship'
, 'truck'l
for cls, cls name in enumerate(classes):
    idxs = np.where((y test != cls) & (y test pred == cls))[0]
    idxs = np.random.choice(idxs, examples per class, replace=False)
    for i, idx in enumerate(idxs):
        plt.subplot(examples per class, len(classes), i * len(classes) + cls + 1
)
        plt.imshow(X test[idx].astype('uint8'))
        plt.axis('off')
        if i == 0:
            plt.title(cls name)
plt.show()
```



Inline question 1:

Describe the misclassification results that you see. Do they make sense?

From the above classification we can see that HOG feature is not able to classify the images to correct classes as different images grouped together under a particular class have something in common with respect to each other for instance colors seem to be somewhat similar.

Neural Network on image features

Earlier in this assignment we saw that training a two-layer neural network on raw pixels achieved better classification performance than linear classifiers on raw pixels. In this notebook we have seen that linear classifiers on image features outperform linear classifiers on raw pixels.

For completeness, we should also try training a neural network on image features. This approach should outperform all previous approaches: you should easily be able to achieve over 55% classification accuracy on the test set; our best model achieves about 60% classification accuracy.

```
In [7]:
print(X_train_feats.shape)
(49000, 155)
In [8]:
from cs175.classifiers.neural_net import TwoLayerNet
input dim = X train feats.shape[1]
hidden dim = 500
num classes = 10
best net = None
# TODO: Train a two-layer neural network on image features. You may want to
                                                                   #
# cross-validate various parameters as in previous sections. Store your best
                                                                   #
# model in the best net variable.
                                                                   #
# get rid of this line for lr in learning rates:
best val = -1
results = {}
learning rates = [1e-2,1e-1,1]
regularization_strengths = [1e-4,1e-5]
for lr in learning rates:
   for reg in regularization strengths:
      net = TwoLayerNet(input dim, hidden dim, num classes)
      net.train(X train feats, y train, X val feats, y val,
                 num iters=3000, batch size=200,
                 learning rate=lr, learning rate decay=0.95,
                 reg=reg)
      y train pred = net.predict(X train feats)
```

```
acc_train = np.mean(y_train == y_train_pred)
       y val pred = net.predict(X val feats)
       acc_val = np.mean(y_val == y_val_pred)
       results[(lr, reg)] = (acc train, acc val)
       if best val < acc val:</pre>
          best val = acc val
          best net = net
# Print out results.
for lr, reg in sorted(results):
   train accuracy, val accuracy = results[(lr, reg)]
   print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
              lr, reg, train accuracy, val accuracy))
print('best validation accuracy achieved during cross-validation: %f' % best val
END OF YOUR CODE
lr 1.000000e-02 reg 1.000000e-05 train accuracy: 0.260327 val accura
cy: 0.272000
lr 1.000000e-02 reg 1.000000e-04 train accuracy: 0.256694 val accura
cy: 0.272000
lr 1.000000e-01 reg 1.000000e-05 train accuracy: 0.588980 val accura
cy: 0.559000
lr 1.000000e-01 reg 1.000000e-04 train accuracy: 0.588857 val accura
cy: 0.564000
lr 1.000000e+00 reg 1.000000e-05 train accuracy: 0.864816 val accura
cy: 0.557000
lr 1.000000e+00 reg 1.000000e-04 train accuracy: 0.844449 val accura
cy: 0.573000
best validation accuracy achieved during cross-validation: 0.573000
In [9]:
# Run your neural net classifier on the test set. You should be able to
# get more than 55% accuracy.
test acc = (net.predict(X test feats) == y test).mean()
```

print(test acc)

0.57

Bonus: Design your own features!

You have seen that simple image features can improve classification performance. So far we have tried HOG and color histograms, but other types of features may be able to achieve even better classification performance.

For bonus points, design and implement a new type of feature and use it for image classification on CIFAR-10. Explain how your feature works and why you expect it to be useful for image classification. Implement it in this notebook, cross-validate any hyperparameters, and compare its performance to the HOG + Color histogram baseline.

Bonus: Do something extra!

Use the material and code we have presented in this assignment to do something interesting. Was there another question we should have asked? Did any cool ideas pop into your head as you were working on the assignment? This is your chance to show off!