# 50.021 – Artificial Intelligence

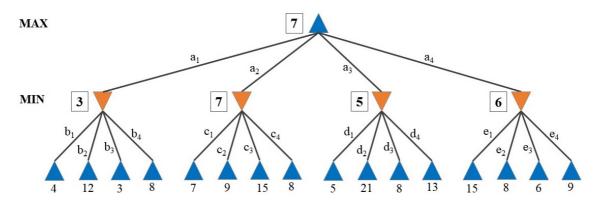
#### Kwan Hui

#### Week 9 Theory Homework - Adversarial/Game Search

[The following notes are compiled from various sources such as textbooks, lecture materials, Web resources and are shared for academic purposes only, intended for use by students registered for a specific course. In the interest of brevity, every source is not cited. The compiler of these notes gratefully acknowledges all such sources. ]

These answers are provided only as a brief guide. There could be more than one way to answer the questions.

### 1 Minimax Search



Consider the above game tree for a 2-ply game between two players, with the utility scores as listed. Apply the Minimax algorithm on this search, where the exploration of moves/actions is based on alphabetical order (i.e.,  $a_1, a_2, a_3, ...$ ). Answer the following:

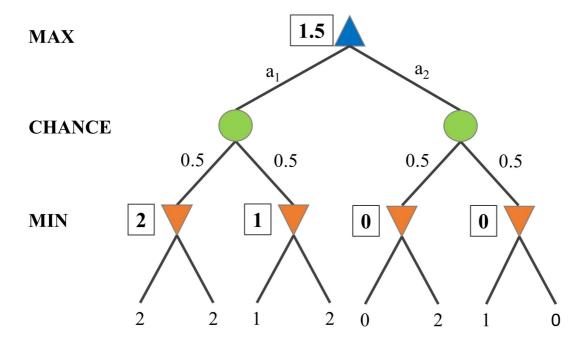
- (a) List down the Minimax values at each level (i.e., the square boxes with the question mark). As above
- (b) Briefly explain why those values are chosen. As per the lecture and exercise examples, the minimum value among the child nodes for the MIN node, etc
- (c) Which move/action would be chosen?  $a_2$

## 2 $\alpha - \beta$ Pruning

Using the same search tree from Task  $\boxed{1}$  apply  $\alpha - \beta$  pruning with the same move ordering as before. Answer the following:

- (a) Which moves/actions are pruned (if any)? List them in the order they were remove.  $d_2, d_3, d_4, e_4$
- (b) Briefly explain why these moves/actions were removed (if any). As per the lecture and exercise examples.

### 3 ExpectiMinimax Search



Consider the above game tree for a probabilistic game between two players, with the utility scores as listed at the leaf nodes. In this game, there are chance nodes (denoted by circles) that are based on a fair coin toss. Apply the ExpectiMinimax algorithm on this search, where the exploration of moves/actions is based on alphabetical order. Answer the following:

- (a) List down the ExpectiMinimax values at each level (i.e., the square boxes with the question mark). As above.
- (b) Which move/action would be chosen?  $a_1$