```
Problem(19) --> Data file name : DB_01_KingNakornchai(1982)_5x7.cfp
< Machines visited by parts: Process route numbers(PRN) >
                   2,
                        3,
Part[
                              5 }
Part[
        2]
3]
4]
5]
                   1,
2,
                        4
                          }
            =
Part[
Part[
            =
                        3
                        4
                   1,
           =
                        5
Part[
                   1,
                        3
Part[
         6]
7]
                   1,
                              4 }
            =
Part[
                          ______
< Block Diagonal Solution Matrix >
             < Locations >
               0 0 0 0
               0 0 0 0 0
               1 2 3 4 5
             < Machines >
               0 0 0 0 0
               0 0 0 0
            1
* *
                 4 2 3 5
< Parts >
             * 1 1
          2
    1)
             * 1 1
    2)
          4
             * 1
    3)
          5
                        1
            * 1 1
    4)
          6
                      1
    ======= * = = = = *
             *
                    1 1 1 *
    5)
          3
7
             *
                    1 1
                          *
    6)
             *
    7)
                      1 1
                          *
< Machine cells and Part families >
______
Machine Cell[ 1] = \{ 1, 4 \}
Machine Cell[ 2] = \{ 2, 3, 5 \}
_____
      Family[ 1] = \{ 2, 4, 5, 6 \}
Family[ 2] = \{ 1, 3, 7 \}
Part
Part
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
Machine cell size
                                                = 7
                                                 =
              size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                 = 0.457
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                   14
                                                   3
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                                = 87.50 %
= 85.62 %
= 73.68 %
Machine utilization (MU)
                                                = 82.35 %
No. of redundant machines (RMs)
                                                = 0
```

```
< Machines visited by parts: Process route numbers(PRN) >
                         }
                  2,
Part[
Part[
Part[
Part[
         2]
3]
4]
5]
                  1,
2,
                        2
           =
                        3,
           =
                             6
           =
                         '}
Part[
                        5
                        3,
Part[
                  2,
        6]
                             5
           =
Part[
Part[
         8]
            =
                                 _____
< Block Diagonal Solution Matrix >
             < Locations >
               0 0 0 0 0
               0 0 0 0 0
               1 2 3 4 5 6
             < Machines >
               0 0 0 0 0
               0 0 0 0 0
               1 4 6 2
< Parts >
* 1
         2
                     1
(
            * 1 1 1
          4
    2)
            * 1 1 1 1
    3)
         7
    ====== * = = = = =
             *
                            *
                     1
             *
                     1
                       1 1
    5)
                            *
             *
    6)
                     1
             *
                       1 \overline{1}
                            *
                     1
          6
            *
                            *
    8)
          8
                     1 1 1
    ======= * * * *
< Machine cells and Part families >
Machine Cell[ 1] = { 1, 4, Machine Cell[ 2] = { 2, 3,
                             5 }
Part Family[ 1] = { 2, 4, 7 }
Part Family[ 2] = { 1, 3, 5, 6, 8 }
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
                                               = 6
                                                 8
                                               =
                                               =
Machine cell size Total no. of 1's in the original MPIM : |A|
                                                 0.458
Matrix density
Total no. of within-block 1's
                                                 20
No. of exceptional elements (EEs)
                                                 2
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                 4
                                                 6
                                               = 90.91 %
                                               = 87.50 %
= 76.92 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                               = 83.33
No. of redundant machines (RMs)
                                               = 0
______
```

Problem(20) --> Data file name : DB_02_KusiakCho(1992)_6x8.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                   2,
1}
Part[
                              6 }
Part[
         2]
3]
4]
            =
Part
            =
                   1,
                         4,
                              7 }
                          6,
                         7
5
7
7
6
Part
            =
Part[
        6]
7]
8]
                   4,
Part[
            =
Part[
Part[
                         7
Part[
         9]
                   6,
Part[
Part[
                   3,
                         6
                         6 }
3 }
        107
            =
        11] =
                   2,
______
< Block Diagonal Solution Matrix >
             < Locations >
                0 0 0 0 0 0 0
                0 0 0 0 0 0
                1 2 3 4 5 6 7
              < Machines
               0 0 0 0 0 0
               0 0 0 0 0 0
             1 4 7 3 6 2 5
< Parts >
             *
    1)
                  1
                        1 1
             * 1
          2
                               *
    2)
          3
             *
               1 1 1
    3)
             *
          6
                  1 1
          7
             * 1
                    1
    5)
             * = = = = =
             *
          4
                    1
                        1
    6)
             *
                         1
          9
                    1
                        1
             *
                               *
    9)
         10
                      1 1
         === * = = =
                        = = =
   10)
             *
                           1 1
                               *
             *
                           1
                      1 * *
         11
   11)
  ======= * * * *
< Machine cells and Part families >
Machine Cell[1] = \{1, 4, 7\}
Machine Cell[ 2] = { 3, Machine Cell[ 3] = { 2,
                          6 }
5 }
Part Family[ 1] = { 1, Part Family[ 2] = { 4, Part Family[ 3] = { 5,
                          2,
                           8,
                              9, 10 }
                          11 }
< Summary of the performance measures >
_____
No. of machines
No. of part types
                                                 = 7
                                                 = 11
No. of cells
                                                 = 3
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                   23
Matrix density
                                                   0.299
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
                                                   17
                                                   6
                                                   10
                                                   16
Group Cability Index (GCI)
                                                 = 73.91 %
                                                 = 75.48
= 51.52
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                 = 62.96 %
No. of redundant machines (RMs)
                                                 = 0
______
```

Problem(21) --> Data file name : DB_03_KusiakChow(1987)_7x11.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                                 -----
                         3
Part[
Part[
         2]
3]
4]
                   1,
                           }
                         2
            =
Part[
--+[
                   3,
                         4,
                              5 }
                         6
7
2
Part
            =
Part[
                   6,
        6]
Part[
            =
                   1,
                   3,
7 }
2 }
Part[
Part[
         7]
8]
Part[
         9]
Part[
Part[
                         7 }
5 }
        107
                   6,
            =
                   3,
        11] =
______
< Block Diagonal Solution Matrix >
              < Locations >
                0 0 0 0 0 0
                0 0 0 0 0 0
                1 2 3 4 5 6 7
              < Machines
                0 0 0 0 0 0
                0 0 0 0 0 0
             1 2 3 4 5 6 7
< Parts >
             * 1 1
    1)
          2
             * 1 1
                                *
    2)
(
          9
             *
                  1
    3)
             * = = = = = =
             * 1
          1
                    1
(
             *
    5)
                    1 1 1
             *
    6)
                    1 1
             *
         11
                    1
                        1
    7)
    *
                               *
    8)
                         1 1
             *
    9)
          5
                           1 1
                             1
1
*
                               *
   10)
          8
             *
                                *
         10
   11)
  ======= * * * * * *
< Machine cells and Part families >
Machine Cell[ 1] = \{ 1, 2 \}
Machine Cell\begin{bmatrix} 2 \end{bmatrix} = \{ 3, 4, \\ \text{Machine Cell} \begin{bmatrix} 3 \end{bmatrix} = \{ 6, 7 \}
                              5
Part Family[ 1] = { 2, Part Family[ 2] = { 1, Part Family[ 3] = { 4,
                           6,
                              9 }
                           3, 7, 11 }
                           5, 8, 10 }
< Summary of the performance measures >
_____
No. of machines
No. of part types
                                                 = 7
                                                  = 11
No. of cells
                                                  = 3
Machine cell size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                    0.273
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
                                                    19
                                                    9
Group Cability Index (GCI)
                                                  = 90.48 %
                                                 = 84.58 %
= 67.86 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                  = 73.08 %
No. of redundant machines (RMs)
                                                 = 0
______
```

Problem(22) --> Data file name : DB_04_Boctor(1991)_7x11.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                                 _____
                     1,
1 }
Part[
Part[
          2]
3]
4]
5]
             =
                     1,
Part
                           2,
3
                                 3
Part
             =
Part[
                             `}
          6]
7]
8]
                           3,
             = {
= {
= {
                     2,
2,
3,
                                   }
PartL
                                 4
                           3,
                                 4,
                                       5,
6 }
6 }
Part
                                              6 }
                           4,
Part
                           4,
Part[
          9]
        10]
                           4,
                     2,
Part[
             =
Part[
Part[
         11
        12]
                           8
                             }
             =
< Block Diagonal Solution Matrix >
               < Locations >
                 0 0 0 0 0 0 0 0
                 0 0 0 0 0 0 0 0
                      3 4 5 6 7 8
               < Machines
                            >
                 0 0 0 0 0 0 0 0
                   0 0 0 0 0 0 0
                   2 3 4 5 6 7
< Parts >
              * *
              * 1 1
                                     *
1
1
     2)
3)
           2
               *
               * 1 1 1
* 1 1 1
              *
     4)
           4
              *
     5)
           5
                   1 1
              *
           6
                   1 1 1
     6)
              * =
                   _ _ _ _ _ _ _
(
                   1 1 1 1 1
              *
                                     *
     8)
                      1 1 1 1
                      1 1 1 1
     9)
           9
                   1
   10)
         10
              *
                        1 1
         ==== *
                = = = = = =
              *
                                     *
    11)
          11
                             1 1 1
              *
                                1
    12)
          12
                                  1
         ==== * * * * * * * *
< Machine cells and Part families >
Machine Cell[ 1] = { 1, Machine Cell[ 2] = { 4, Machine Cell[ 3] = { 7,
      Family[ 1] = { 1, 2, 3, Family[ 2] = { 7, 8, 9, Family[ 3] = { 11, 12 }
                                     4, 5, 6 }
10 }
Part
Part
Part
< Summary of the performance measures >
______
No. of machines
                                                      = 8
No. of part types No. of cells
                                                        12
                                                      =
                                                        3
Machine cell size
Total no. of 1's in the original MPIM: |A|
                                                        35
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
                                                        0.365
                                                         28
No. of voids
                                                        6
Sum of EEs and voids
                                                        13
Group Cability Index (GCI) grouping efficiency (GE)
                                                        80.00 %
                                                      = 85.53 %
= 68.29 %
Grouping efficacy (GF)
Machine utilization (MU)
                                                      = 82.35 %
```

Problem(23) --> Data file name : DB_05_Seifoddiniwolfe(1986)_8x12.cfp

Problem(24) --> Data file name : DB_06_ChandraRaja(1989a)_8x20.cfp

< Summary of the performance measures >

```
No. of machines = 8
No. of part types = 20
No. of cells = 3
Machine cell size = 4
Total no. of 1's in the original MPIM : |A| = 61
Matrix density = 0.381
Total no. of within-block 1's = 52
No. of exceptional elements (EEs) = 9
No. of voids = 0
Sum of EEs and voids = 9
Group Cability Index (GCI) = 85.25 %
grouping efficiency (GE) = 95.83 %
Grouping efficacy (GF) = 85.25 %
Machine utilization (MU) = 100.00%
No. of redundant machines (RMS) = 0
```

```
< Machines visited by parts: Process route numbers(PRN) >
                                            }
}
                                    6,
Part[
Part[
          2]
3]
4]
                      2,
                                    6,
                                          8
                             5,
              =
                                    4,
Part
                                                 8 }
                                          5
8
8
7
Part
              =
                             6,
Part[
                      2,
2,
3,
          6]
7]
                             3,
                                    5
Part[
              = {
Part[
Part[
                                    4,
                                                 7 }
8 }
                                          6,
          81
                                    6,
                             ż,
                                          8
                                    4,
                                             `}
Part[
          9]
                                   5,
                                          6,
7
7,
                             4,
Part[
         10]
                      1,
2,
3,
                                                 8 }
              =
                             3,
5,
4,
                                    6,
Part
         11
Part
         12]
                                    6,
              =
                                    5,
Part[
                                                 8 }
         13]
                             4,
                                          8
6
         14]
                      1,
                                    6,
PartL
              =
Part[
         15]
16]
                             3,
                                          6,
7,
Part
                                                        8 }
                      3,
Part[
         17]
                                    4,
         18]
19]
                      1,
                             2,
                                          6
Part[
              =
                             3,
                                    4,
                                                 6,
7)
Part[
              =
                             3,
                                    4,
         20]
                      2,
Part[
              =
< Block Diagonal Solution Matrix >
                < Locations >
                  0 0 0 0 0 0 0 0
                  \begin{smallmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \end{smallmatrix}
                < Machines
                  0 0 0 0 0 0 0 0
                     000000
                  0
                     2 4 3 5 6 7
< Parts >
                  1
               * *
                * 1 1 1
                                     1
     2)
3)
            4
                * 1 1 1
* 1 1 1
* 1 1 1
                *
(
                                     1
            9
     4)
          18
                                1
               * = = = = = = =
                                       *
    -----
               * 1
           1
                             1 1
                                     1
               *
            2
                     1
                             1 1
                                     1
     6)
            5
                                1 1 1
                          1
                                        *
            6
7
                *
                     1
                          1 1
                                  1
                *
     9)
                     1 1 1
                                1 1
                        \overline{1} \overline{1}
                             1
1
            8
    10)
                *
           10
                  1
                                     1
                                1 1
    12)
          11
                *
          12
13
    13)
                          1 1 1 1
    14)
15)
               *
                        1 1 1
                * 1
                        1
                                     1
               * 1
                             1 1
    16)
          15
                        1
               * 1
          16
                          1 1 1 1 1
    17)
                                  \begin{array}{ccc} 1 & \overline{1} \\ 1 & \end{array}
    18)
          17
                *
                        1
                          1 1
                          1
                        1
    19)
          19
                  1
                             1 1
                       \frac{1}{*}
          20
                *
                     1
                          1 1
    20)
< Machine cells and Part families >
Machine Cell[ 1] = \{ 1, 2, 4 \}
Machine Cell[ 2] = \{ 3, 5, 6, 7, 8 \}
                  -----
Part Family[ 1] = \{ 3, 4, 9, 18 \}
Part Family[ 2] = \{ 1, 2, 5, 6, 7 \}
                                2, 5, 6, 7, 8, 10, 11, 12, 13, 14, 15, 16, 17, 19, 20 }
< Summary of the performance measures >
______
No. of machines
                                                          = 8
```

Problem(25) --> Data file name : DB_07_ChandraRaja(1989b)_8x20.cfp

```
No. of part types

No. of cells

Machine cell size

Total no. of 1's in the original MPIM: |A| = 91

Matrix density

Total no. of within-block 1's

No. of exceptional elements (EEs)

No. of voids

Sum of EEs and voids

Group Cability Index (GCI)

grouping efficiency (GE)

Grouping efficacy (GF)

Machine utilization (MU)

No. of redundant machines (RMS)

= 20

= 20

= 20

= 55

FOR TOTAL MPIM: |A| = 91

= 0.569

= 66

EES)

= 25

E 25

E 26

E 30

E 31

E 31

E 32

E 44

E 34

E 35

E 36

E 37

E 37

E 38

E 37

E 37

E 38

E 38
```

```
Problem(26) --> Data file name : DB_08_Carrie(1973)_20x35.cfp
< Machines visited by parts: Process route numbers(PRN) >
                                          8,
Part[
                                               17
Part
                             4,
          2]
3]
4]
                      2,
                                  13,
                                         14,
                                               18
              =
                                                   ~
                                   7,
                                          8,
Part
              =
                      1,
                             3,
                                                17
                                        16,
17 }
16 }
                            12,
                                  15
                                               19
Part
                     11,
              =
                      3,
                                   8,
Part[
                                  15,
14 }
          6]
7]
                            12
PartL
                     11,
              =
                      2,
                            4,
Part
                                   9,
                             6,
                                         10,
          81
                                               20
Part
                                               20 }
19 }
              =
                                  15,
                            12,
Part[
          9]
                     11,
                                         16,
Part[
         10]
                      2,
                            14,
                                  18 }
              =
                                               19 }
18 }
18 }
20 }
                            12,
                                  15,
                                         16,
Part
         11
              =
                     11,
                             4,
4,
                                  13,
Part
         12]
                      2,
2,
5,
                                         14,
              =
                                         ī4,
                                  13,
Part[
         13]
                                        14,
10,
17 }
                                   ġ,
         14]
                             6,
PartL
              =
                             7,
6,
                                  8,
10 }
Part
         15]
                      5,
3,
Part
         16]
              =
                             7,
                                  8,
18 }
                                         17 }
Part[
         17]
         18]
                      2,
                           14,
Part[
              =
                             9,
7,
                      6,
                                  10,
Part
         19
              =
                                         20 }
                                      `}
         20]
                      1,
                                   8
Part
              =
Part
         21]
                     11,
                            12,
                                  15,
                                         16,
                                               19 }
                             9,
         22]
                      6,
                                  10 }
Part[
              =
Part[
                      1,
                                   8,
         23]
                                         17 }
              =
                                  13,
17,}
         24]
                      2,
                             4,
                                         14,
                                               18 }
Part
              =
                      1,
                             8,
Part[
         25]
                                 1,
10,
14 }
                             9,
         26]
27]
                      6,
                                         20 }
Part[
              =
                             4,
                      2,
Part
              =
         281
                                         19
                                  16,
Part
                     11,
                            15,
              =
                                        17 }
19 }
18 }
                      1,
                             3,
                                   8,
Part
         291
                                  16,
                     11,
                           15,
Part[
         30]
              =
Part[
         31]
32]
                      2,
                            3,
                                  14,
19 }
              =
                     11,
                           16,
Part[
              =
                     12´}
         33]
Part[
                     5,
11 }
Part[
         34]
                             6 }
              =
Part[
         35]
              =
< Block Diagonal Solution Matrix >
                < Locations >
                  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
                  0\; 0\; 0\; 0\; 0\; 0\; 0\; 0\; 0\; 1\; 1\; 1\; 1\; 1\; 1\; 1\; 1\; 1\; 2\; 2
                       3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9 0
                  1 2
                < Machines
                     1 0
7 5
* *
                                               2
                                                  1 1
1 2
* *
                                                       1
5
                       1 1 1 0 0 0 0
                                                          1
                                                            1
                                                               0 0
                                                                    1
                          4 8 1 3 7 8
                                                            9
                                                          6
< Parts >
                  2
                     4 3
               *
                  1 1 1 1 1
     1)
               * 1 1
                                                                       *
     2)
                          1
               *
                                                                       *
          10
     3)
                  1
                          1 1
          12
13
                    \begin{array}{cc} 1 & 1 \\ 1 & 1 \end{array}
                          1
                             1
1
                *
                  1
                                                                       *
     4)
                  1
                *
     5)
     6)
7)
               * 1
          18
                          1
                            1
                *
                    1 1 1 1
          24
                  1
               *
     8)
          27
                  1 1
                          1
                *
     9)
          31
                  1
                          1
                            1
                                  1
               *
                               =
                                  = = = =
                *
                                                                       *
    10)
                                  1
                               1
                                     1 1 1
   11)
12)
            3
5
                *
                               1 1
                                                                       *
                                     1
                                       1
                                          1
                *
                                     \overline{1}
                                  1
                                       1
                                          1
   13)
          15
                *
                                  1
                                    1 1 1
                                                                       *
                *
                                                                       *
          17
                                    1 1 1
    14)
                                  1
          20
23
                *
   15)
                               1
                                     1
                                       1
                               1
                                     1
                                       1
                                          1
    16)
                                                                       *
    17)
          25
                ÷
                               1
                                       1 1
               *
                               1 1
                                       1 1
    18)
          29
```

= = = =

=

*

= = = = =

```
*
    19)
                                                       1 1 1 1 1
    20)
                                                             1
    21)
                                                       1 1 1 1 1
    22)
                  *
            11
                                                          1 1 1 1
                                                          1111
            21
                  *
    23)
                                                       1
    24)
25)
                  *
            28
                  *
            30
                                                       1
                  *
     26)
                                                                1 1
            32
            33
                  *
    27)
                                                          1
    28)
                  *
                                                        1
                                                       _ _ _ _ _ _ _ _
    ====
           ====
                 *
            8
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< Machine cells and Part families >
______
Machine Cell[ 1] = { 2, 4, 13, 14, 18 }
Machine Cell[ 2] = { 1, 3, 7, 8, 17 }
Machine Cell[ 3] = { 5, 20 } --> Residual cell
Machine Cell[ 4] = { 11, 12, 15, 16, 19 }
Machine Cell[ 5] = { 6, 9, 10 }
        Family[ 1] = { 2, 7, 10, 12, 13, 18, 24, 27, 31 }
Family[ 2] = { 1, 3, 5, 15, 17, 20, 23, 25, 29 }
Family[ 3] --> Empty Part family
Family[ 4] = { 4, 6, 9, 11, 21, 28, 30, 32, 33, 35 }
Family[ 5] = { 8, 14, 16, 19, 22, 26, 34 }
Part
Part
Part
< Summary of the performance measures >
No. of machines
No. of part types
No. of cells
                                                                = 20
                                                                   35
                                                                =
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                                   135
                                                                = 0.193
Matrix density
Total no. of within-block 1's
                                                                  126
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                                = 9
                                                                =
                                                                  35
                                                                  44
                                                                  93.33 %
grouping efficiency (GE)
                                                                = 88.30 %
Grouping efficacy (GF)
                                                                = 74.12
                                                                           %
                                                                = 78.26
Machine utilization (MU)
No. of redundant machines (RMs)
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< Machine cells and Part families >
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Machine Cell[ 1] = { 3, 20 Machine Cell[ 2] = { 4, 16
                                  16 }
Machine Cell[ 2] = { 4, Machine Cell[ 3] = { 2, Machine Cell[ 4] = { 6, Machine Cell[ 5] = { 1, Machine Cell[ 6] = { 9, Machine Cell[ 7] = { 7,
                             2, 5, 11, 19 }
6, 8, 12, 15, 1
1, 13, 21, 22 }
9, 10, 17 }
                                                 18 }
                                       23,
                                  14,
        Family[ 1] = { 2, 11, 12, 15, 23, 24, 31, 34 }
Family[ 2] = { 8, 19, 21, 28, 37, 38, 39 }
Family[ 3] = { 10, 13, 14, 22, 35, 36 }
Family[ 4] = { 4, 5, 18, 26, 27, 30 }
Family[ 5] = { 1, 9, 16, 17, 33 }
Family[ 6] = { 6, 7, 20, 29, 40 }
Family[ 7] = { 3, 25, 32 }
Part
Part
Part
Part
Part
Part
Part
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
                                                              = 24
                                                              = 40
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                                 130
                                                                 0.135
Matrix density
Total no. of within-block 1's
                                                                 120
No. of exceptional elements (EEs)
                                                                 10
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                                 11
                                                                 21
                                                                 92.31 %
grouping efficiency (GE)
                                                              = 95.20 %
Grouping efficacy (GF)
                                                              = 85.11 %
Machine utilization (MU)
                                                                 91.60
No. of redundant machines (RMs)
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< Machine cells and Part families >
_____
Machine Cell[ 1] = { 6, 8, 12, 15, 18 }
Machine Cell[ 2] = { 3, 20 }
Machine Cell[ 3] = { 2, 5, 11, 19 }
Machine Cell[ 4] = { 7, 14, 23, 24 }
Machine Cell[ 5] = { 1, 13, 21, 22 }
Machine Cell[ 6] = { 4, 16 }
Machine Cell[ 7] = { 9, 10, 17 }
        Family[ 1] = { 4, 5, 18, 26, 27, 30, 37 }
Family[ 2] = { 2, 11, 12, 15, 23, 24, 31, 34 }
Family[ 3] = { 10, 13, 14, 22, 35, 36 }
Family[ 4] = { 3, 25, 32 }
Family[ 5] = { 1, 9, 16, 17, 33 }
Family[ 6] = { 8, 19, 21, 28, 38, 39 }
Family[ 7] = { 6, 7, 20, 29, 40 }
Part
Part
Part
Part
Part
Part
Part
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
                                                                 = 24
                                                                 = 40
                                                                 = 7
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                                 = 131
Matrix density
Total no. of within-block 1's
                                                                  = 111
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                                  = 20
                                                                    23
                                                                    43
                                                                  = 84.73 %
grouping efficiency (GE)
                                                                  = 90.21 %
Grouping efficacy (GF)
                                                                 = 72.08 %
Machine utilization (MU)
                                                                 = 82.84 %
No. of redundant machines (RMs)
______
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< Machines visited by parts: Process route numbers(PRN) >

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[ 2] = {

21, 23,

[ 3] = {

33, 35 }

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Part[ 15] = {

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 < Machine cells and Part families
Machine Cell[ 1] = { 1, 2, 5, 6, 7, 9, 12, 13, 16, 22, 24, 25, 29, 34, 35, 36, 37 } --> Residual cell
Machine Cell[ 2] = { 3, 4, 8, 10, 11, 14, 15, 17, 18, 19, 20, 21, 23, 26, 27, 28, 30, 31,
 32, 33 }
Part Family[ 1] --> Empty Part family
Part Family[ 2] = { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53 }
 < Summary of the performance measures >
No. of machines
No. of part types
No. of cells
                                                                                        = 37
= 53
= 2
= 20
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                                                             977
Total no. of 1's in the original Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
No. of redundant machines (RMS)
                                                                                            0.498
                                                                                        = 763
= 214
= 297
                                                                                         = 511
                                                                                         = 78.10 %
= 74.11 %
                                                                                        = 59.89 %
= 71.98 %
= 17
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No. of redundant machines (RMs)

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< Machines visited by parts: Process route numbers(PRN) >
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< Machine cells and Part families >
Machine Cell[ 1] = { 1, 2, 3, 4, 11, 12 } Machine Cell[ 2] = { 5, 6, 7 } Machine Cell[ 3] = { 8, 9, 10 }
Part Family[ 1]
Part Family[ 2]
Part Family[ 3]
                        = { 1,
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                                   9, 10 }
< Summary of the performance measures >
No. of machines
No. of part types
No. of cells
                                                                = 12
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                                                                  3
Machine cell
                   size
                                                                   6
Total no. of 1's in the original MPIM : |A|
Matrix density
Total no. of within-block 1's
                                                                  0.317
                                                                  33
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
                                                                  5
9
                                                                  14
Group Cability Index (GCI) grouping efficiency (GE)
                                                                   86.84 %
                                                                = 86.08 %
= 70.21 %
Grouping efficacy (GF)
Machine utilization (MU)
                                                                = 78.57 %
No. of redundant machines (RMs)
                                                                = 0
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Problem(30) --> Data file name : DB_12_McAuley(1972)_12x10.cfp

Problem(31) --> Data file name : DB_13_King(1980)_14x24.cfp

```
Machine Cell[ 1] = { 4, 5, 7 }
Machine Cell[ 2] = { 6, 8, 9, 14 }
Machine Cell[ 3] = { 2, 3, 10, 11 }
Machine Cell[ 4] = { 1, 12, 13 }
______
Part Family[ 1] = { 1, 2, 17, 19, 20, 23 } 

Part Family[ 2] = { 5, 9, 10, 11, 12, 13, 14, 15, 16, 22 } 

Part Family[ 3] = { 3, 4, 21, 24 } 

Part Family[ 4] = { 6, 7, 8, 18 }
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
                                                                = 14
                                                                = 24
                                                                = 4
Machine cell size
                                                                = 4
Total no. of 1's in the original MPIM : |A|
                                                                = 59
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of exceptional crements
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                                = 29
                                                                = 31
                                                                = 96.61 %
                                                                = 82.74 %
                                                                = 64.77 %
Grouping efficacy (GF)
Machine utilization (MU)
                                                                = 66.28 %
```

= 0

No. of redundant machines (RMs)

```
< Machines visited by parts: Process route numbers(PRN) >
                                4,
Part[
                                       8 }
Part[
                     3,
                          6,
                               10
                                   }
          2]
3]
4]
5]
             =
                     1,
                          4,
Part
             =
                                 8
                           9
                     5,
Part
             =
Part[
                          6,
                                 7
                                /
4,
1 }
                    1,
                          2,
Part<u></u>
          6]
             =
                                       8 }
Part[
Part[
                          9,
                               10
                    1,
                          3,
          8]
                                 6,
                                       7 }
             =
                                      _____
< Block Diagonal Solution Matrix >
               < Locations >
                 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0
                 0 0 0 0 0 0 0 0 0 1
                     3 4 5 6 7 8 9 0
               < Machines
                 0000000000
                 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0
                                      1
                               3 6
< Parts >
                     4 8
                          5
                             9
              *
                     * *
========
              * 1 1 1 1
                                         *
              *
           3
                1
(
     2)
                      1 1
              *
                1 1 1 1
     3)
           6
          ===
                = = = =
                          =
                             =
              *
                                         *
                           1 1
(
           7
              *
                           1
                             1
     5)
                                       1
                                         *
              *
           2
                               1
                                  1
                                       1
     6)
                                         *
              *
     7)
                               1 1 1
              *
           8
     8)
                 1
                               1
                                  1
                   * *
                        * *
                 *
< Machine cells and Part families >
                            <del>2</del>,
9,}
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
                   = {
= {
= {
                         1,
                         5,
                             6, 7, 10 }
       Family[ 1] = { 1, 3, 6 }
Family[ 2] = { 4, 7 }
Family[ 3] = { 2, 5, 8 }
Part
Part
Part
                          _____
< Summary of the performance measures >
No. of machines
                                                     = 10
No. of part types
No. of cells
                                                     = 8
= 3
Machine cell size
Total no. of 1's in the original MPIM: |A|
                                                       26
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
                                                       0.325
                                                        24
                                                       2
                                                     =
No. of voids
                                                     =
                                                        4
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                        6
                                                        92.31 %
                                                     = 90.93 %
Grouping efficacy (GF)
                                                     = 80.00 %
Machine utilization (MU)
                                                     = 85.71 %
No. of redundant machines (RMs)
                                                     = 0
______
```

Problem(32) --> Data file name : DB_14_Ham(1985)_10x8.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                                21,
                          15,
Part[
                    13,
                                      22 }
Part
                                24 }
24 }
          2]
3]
4]
                     3,
                          20,
             =
                          23,
12,
Part
             =
                    14,
                                15,
12,
                                      18 }
Part
                     8,
             =
                     6,
                           8,
                                      15,
                                            18 }
Part[
         6]
7]
                          10 }
PartL
                     9
             =
                     9,
                          10,
16 }
Part
                                17,
                                      19 }
                     4,
          81
Part
             =
                     1,
                          13,
                                21 }
Part[
          9]
                         5,
20 }
20 }
                     2,
3,
Part[
         10]
                                      19,
                                11,
                                            21 }
             =
Part
         11
             =
         12]
                     3,
2,
2,
Part
             =
                                19 }
Part[
         13]
                          11,
                          5,
20 }
        14]
                                      19 }
PartL
                                14,
             =
Part
         15]
                                21, 22 }
                          14,
        16]
                     1,
Part
                                      22,
                                            31 }
             =
                          ī3,
                     1,
Part[
         17]
                                15,
         18]
                     6,
                          12,
                                      18 }
20 }
                                      18
Part[
             =
                          4,
                                16,
17 }
                     1,
Part
         19]
             =
        20]
                    10,
                          12,
Part
             =
Part
         21]
                     4,
                          16 }
                          .6
5,
1 }
                     2,
        22]
                                11,
                                      19 }
Part[
             =
Part[
        23]
24]
                     3,
                          20
             =
                     3,
7,
                          12,
                                20 }
23 }
                                20
Part
             =
                          14,
         25]
Part[
                          8,
        26]
27]
                     6,
                                10,
                                      15,
12,
Part[
             =
                     5,
4 }
                           6,
                                 8,
                                            15,
                                                  18 }
Part
             =
         281
Part
             =
                     9,
Part
         291
                          17 }
                          8,
20 }
                     6,
                                12,
                                      18,
                                            22 }
Part[
         30]
             =
Part[
                    17,
7,
        31]
             =
        32 🗍
                          16,
                                23,
                                      24 }
Part[
             =
                          2, 20 }
                                 9,
                                            21,
         33]
                                      13,
                                                 22 }
Part[
                     3,
         34]
Part[
             =
Part[
         35]
36]
                     5,
2,
                          11,
                                19 }
             =
                          5,
16 }
                                      19 }
                                11,
Part
             =
Part[
         371
                    15,
             =
                          4,
16 }
         38]
                     6,
Part[
             =
                                16 }
                ₹{
Part[
                     4,
         391
             =
         40]
                           9,
                                17 }
Part[
             =
< Block Diagonal Solution Matrix >
               < Locations
                 2
1
                 1 1
3 4
                                                                2
                                                   1
5
                                                      1
6
                                                        1
7
                                                           1
                                                             1
9
               < Machines
                 0 0 0
                     1 1 1 0 2 0 0 1 1 0
2 5 8 3 0 2 5 1 9 4
* * * * * * * * * * *
                                              1 0 1
6 7 4
* * *
                                                      2 3 *
                                                         2
                                                             1
                                                                1
7
                                                                   0
                                                                     1
                                                                          2
                                                           0
                 0
                   0
                   8 2
                                                         4
                                                           9
                                                                   1
< Parts >
                 6
               *
                    1 1 1 1
              * 1 1 1 1 1
     2)
     3)
4)
              *
                      1 1 1
          18
                 1
                 1
          26
27
               *
                   1
                                                              1
                         1
              * 1 1 1 1 1
     5)
                                     1
              *
                 1 1 1
          30
     6)
                           1
                                                                           1
                        1
          37
               *
     7)
                                               1
              *
                        = =
                             = = = = = = = = =
     8)
           2
              *
                             1 1
                                                         1
               *
                              1 1
    9)
          11
         12
15
   10)
               *
                              1
                                1
                                1
               *
                              1
   11)
12)
          23
              *
                              1 1
               *
    13)
          24
                      1
                              1 1
    14)
          31
               *
                                                                1
```

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```
(
    15)
                                  1 1
           34
   _____
                                       1
    16)
                                          1 1 1
                 *
                                        1
    17)
           13
                                             1 1
                 *
                                        1 1
           14
    18)
                                                            1
           22
35
                 *
                                        1
                                          19)
                                        20)
           36
                 *
    21)
                *
    22)
                 *
             8
                                                   1 1
    23)
                 *
                                                   1
                                                      1
            19
                                                                             1
    24)
           21
                 *
                                                   1
                                                      1
                 *
    25)
           28
           38
                 *
                                                   1
                                                      1
    26)
                 *
    27)
           39
                                                      1
   ====
          ====
                 *
(
    28)
                                                           1 1
    29)
           25
                 *
           32
                                                      1
                                                         1
                                                               1 1
    30)
    ====
           ====
                 *
                                                                    1 1
    31)
    32)
33)
                 *
                                                1
                                                                    1
                                                                       1 1
           20
                 *
                                                                       1
                                                                          1
                          1
    34)
                 *
           29
                                                                          1
                 *
    35)
           40
                                                                          1
   =======
    36)
                            1
    37)
             9
                                                                               1
                                                                                  1
                                                                             1
                 *
    38)
           16
                                                                             1
                                                                                   1
           17
                 *
                                                                             1
1
                                                                               1
1
                                                                                     1
1
    39)
                 *
    40)
           33
< Machine cells and Part families >
_____
Machine Cell[ 1] = { 6, 8, 12, 15, 18 }
Machine Cell[ 2] = { 3, 20 }
                              3,
                                  2Ó
5,
Machine Cell[ 2] = { 3, 20 }
Machine Cell[ 3] = { 2, 5, 11, 19 }
Machine Cell[ 4] = { 4, 16 }
Machine Cell[ 5] = { 7, 14, 23, 24 }
Machine Cell[ 6] = { 9, 10, 17 }
Machine Cell[ 7] = { 1, 13, 21, 22 }
        Family[ 1] = { 4, 5, 18, 26, 27, 30, 37 }
Family[ 2] = { 2, 11, 12, 15, 23, 24, 31, 34 }
Family[ 3] = { 10, 13, 14, 22, 35, 36 }
Family[ 4] = { 8, 19, 21, 28, 38, 39 }
Family[ 5] = { 3, 25, 32 }
Family[ 6] = { 6, 7, 20, 29, 40 }
Family[ 7] = { 1, 9, 16, 17, 33 }
Part
Part
Part
Part
Part
Part
Part
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
                                                              = 24
                                                              = 40
                                                              = 7
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                              = 130
Matrix density
Total no. of within-block 1's
                                                                 110
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                               = 20
                                                                 24
                                                                 44
                                                              = 84.62 %
grouping efficiency (GE)
                                                               = 89.83 %
Grouping efficacy (GF)
                                                              = 71.43 %
Machine utilization (MU)
                                                              = 82.09 %
No. of redundant machines (RMs)
______
```

*

*

Part

< Summary of the performance measures >

```
No. of machines = 12
No. of part types = 19
No. of cells = 3
Machine cell size = 5
Total no. of 1's in the original MPIM : |A| = 74
Matrix density = 0.325
Total no. of within-block 1's = 57
No. of exceptional elements (EEs) = 17
No. of voids = 38
Sum of EEs and voids = 38
Sum of EEs and voids = 55
Group Cability Index (GCI) = 77.03 %
grouping efficiency (GE) = 73.61 %
Grouping efficacy (GF) = 50.89 %
Machine utilization (MU) = 60.00 %
No. of redundant machines (RMs) = 2
```

*

8 *

*

*

*

===

19

21

28

3

17) 18) 19)

20)

21)

= = = = = = = =

1

= =

= = =

1 1

1 1

1 1

1

= =

1 1 1

1

*

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```
22) 25
                                                                     1 1 1
    _____
     23)
                                  1
                                                                                     1 1 1
     24)
                                                                                  1 1 1
                    *
     25)
                                                                                  1 1 1 1
              16
     26)
                     *
             17
                                                                                  1 1
                                                                                            1
                                                                                                1 1
                    *
                                                                                                ar{1} \ ar{1} \ 1
     28)
     29)
                    *
              20
                                                                                                   1 1
                               1
                    * * * * * * * * *
< Machine cells and Part families >
______
Machine Cell[ 1] = { 6, 8, 12, 15, 18 }
Machine Cell[ 2] = { 3, 20 }
Machine Cell[ 3] = { 2, 5, 11, 19 }
Machine Cell[ 4] = { 4, 16 }
Machine Cell[ 5] = { 7, 14, 23, 24 }
Machine Cell[ 6] = { 1, 13, 21, 22 }
Machine Cell[ 7] = { 9, 10, 17 }
_____
Part Family[ 1] = { 4, 5, 18, 26, 27, 30 }
Part Family[ 2] = { 2, 11, 12, 15, 23, 24 }
Part Family[ 3] = { 10, 13, 14, 22 }
Part Family[ 4] = { 8, 19, 21, 28 }
Part Family[ 5] = { 3, 25 }
Part Family[ 6] = { 1, 9, 16, 17 }
Part Family[ 7] = { 6, 7, 20, 29 }
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
                                                                           = 24
                                                                           = 30
Machine cell size = Total no. of 1's in the original MPIM : |A| = =
                                                                           = 0.138
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                                           = 12
                                                                              15
                                                                           = \frac{1}{27}
                                                                           = 87.88 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                                           = 91.68 %
                                                                           = 76.32 %
= 85.29 %
No. of redundant machines (RMs)
```

```
< Machines visited by parts: Process route numbers(PRN) >
                                4,
Part[
                                       8 }
Part[
          2]
3]
4]
                     3,
                           6,
                                10
                                   }
             =
                           4,
Part
             =
                     1,
                                 8
                           9
                     5,
Part
             =
                           6,
Part[
                                 7
                                4,
LO }
7 }
                    1,
                           2,
Part<u></u>
          6]
             =
                                       8 }
Part[
Part[
                           9,
                                10
                           6,
          8]
             =
                                 _____
< Block Diagonal Solution Matrix >
               < Locations >
                 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0
                 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1
                      3 4 5 6 7 8 9 0
                 Machines
                 0000000000
                 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0
                                      1
                               3 6
< Parts >
                     4 8
                          5
                             9
              *
                        *
========
              * 1 1 1 1
                                         *
              *
           3
                 1
(
     2)
                      1 1
              *
                 1 1 1 1
     3)
           6
          ===
                 =
                   = =
                        =
                          =
                             =
               *
                                         *
                           1 1
(
           7
               *
                           1
                             1
     5)
                                       1
                                         *
           2
                                1
                                  1
                                       1
     6)
                                         *
               *
     7)
                                1
                                  1 1
               *
           8
     8)
                                1
                                  1
                        * *
               *
                 *
< Machine cells and Part families >
                             =.
2,
9,}
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
                    = {
= {
= {
                         1,
                          5,
                             6, 7, 10 }
       Family[ 1] = { 1, 3, 6 }
Family[ 2] = { 4, 7 }
Family[ 3] = { 2, 5, 8 }
Part
Part
Part
                          _____
< Summary of the performance measures >
No. of machines
                                                     = 10
No. of part types
No. of cells
                                                     = 8
= 3
Machine cell size
Total no. of 1's in the original MPIM: |A|
                                                       25
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
                                                        0.313
                                                        24
                                                        1
                                                     =
No. of voids
                                                     =
                                                        4
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                        96.00 %
                                                     = 91.90 %
Grouping efficacy (GF)
                                                     = 82.76 %
Machine utilization (MU)
                                                     = 85.71 %
                                                     = 0
No. of redundant machines (RMs)
______
```

DB_18_MiltenburgZhang(1991)_10x8.cfp

Problem(36) --> Data file name :

< Summary of the performance measures >

```
______
No. of machines
No. of part types
No. of cells
                                             = 17
= 20
                                             = 4
= 5
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                             = 78
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
                                             = 4
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                             = 15
                                               19
                                             = 94.87 %
                                             = 90.78 %
                                             = 79.57 %
Grouping efficacy (GF)
                                             = 83.15 %
Machine utilization (MU)
No. of redundant machines (RMs)
                                             = 0
_____
```

```
< Machines visited by parts: Process route numbers(PRN) >
                  2,
1}
Part[
                             6 }
Part[
         2]
3]
4]
Part[
Part[
                        4,
                   1,
                             7 }
                  6,
Part[
                             7 }
        6]
7]
8]
                  4,
Part[
           = {
= {
= {
Part[
Part[
                        6
        9] =
                  6,
                        7
Part[
Part[
Part[
                  3,
                        6 }
3 }
        107
       10] = {
11] = {
            =
                  2,
______
< Block Diagonal Solution Matrix >
             < Locations >
               0 0 0 0 0 0 0
               0 0 0 0 0 0
               1 2 3 4 5 6 7
             < Machines
               0 0 0 0 0 0
               0 0 0 0 0 0
            1 4 7 2 3 5 6
< Parts >
             * 1
          2
3
    1)
(
             * 1 1 1
                              *
    2)
         6
             *
                 1 1
    3)
             * 1
    4)
                   1
  ======= * = = = = = =
             *
                 1
                     1
             *
                   1
                            1
    6)
             *
                   1 1
                          1
    8)
                          1
                            1
             *
                              *
    9)
          9
         10
                            1
   10)
   11)
         11
             *
                        1
                      *
< Machine cells and Part families >
Machine Cell[ 1] = \{ 1, 4, 7 \}
Machine Cell[ 2] = \{ 2, 3, 5, 6 \}
______
      Family[ 1] = { 2, 3, 6, 7 }
Family[ 2] = { 1, 4, 5, 8, 9, 10, 11 }
< Summary of the performance measures >
                   _____
No. of machines
                                                = 7
No. of part types No. of cells
                                                = 11
                                                = 2
Machine cell
              size
                                                =
Total no. of 1's in the original MPIM : |A|
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                  20
                                                  20
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
""""" (MI)
                                                  24
                                                = 83.33 %
                                                = 69.59
                                                = 45.45 %
Machine utilization (MU)
                                                = 50.00 %
No. of redundant machines (RMs)
______
```

Problem(38) --> Data file name : DB_20_SeifoddiniHsu(1994)_7x11.cfp

```
Problem(39) --> Data file name : DB_21_Shargal(1995)_10x38.cfp
< Machines visited by parts: Process route numbers(PRN) >
                              2
Part[
Part[
           2]
3]
4]
                       3,
                              4
               =
                       4,
Part
               =
                              5
6
7
8
9
6
                       35,7,5,7,5,7,3,1,4,7,4,3,3,
Part
              =
Part[
           6]
7]
8]
Part
               =
Part
Part
               =
                                   10
                              4,
Part[
           9]
Part[
          10]
                              8
7
7
8
8
                                 =
Part
          11
               =
         12]
Part
               =
Part[
          13]
         14]
PartL
               =
                              8
7
5
3
5
4
7
7
9
5
7
Part
          15]
Part
         16]
               =
Part[
          17]
          18]
Part[
               =
Part
          19
               =
         20]
Part
               =
Part
          21]
                                 }
                       4,
5,
4,
         22]
                                     8 }
Part[
               =
                                `
}
Part[
         23]
24]
Part
               =
                                ,
}
          25]
                       4,
7,
2,
4,
                                     8 }
Part[
         26]
27]
                              8
9
7,
5
8
7,
Part[
               =
Part
               =
          28]
                                     8 }
Part
               =
                                '}
}
                       4,
7,
Part
          291
Part[
          30]
               =
Part[
                       4,
         31]
                                     8 }
                             7,
10 }
10 }
         32 🗍
                       6,
Part[
               =
                       6,
1,
Part[
          33]
                              2
7
                                     3 }
          34]
Part[
               =
                                 }
                       6,
3,
2,
Part[
          35]
36]
               =
                              4
                                    10 }
Part[
Part[
               =
                              3'}
5 }
          371
          38]
Part[
< Block Diagonal Solution Matrix >
                   < Locations
                                   0 0 0 0
                                      0 0 1
8 9 0
                 < Machines
                   0 0 0 0 0 0 0 0 0 0
                           0 0 0 0 0 0
                        0
                   0
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< Parts >
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                           5
                             7 8 1 9 6 0
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27
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37
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     28)
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     36)
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                                                1
     37<sup>)</sup>
                                             1
                  *
            35
< Machine cells and Part families >
Machine Cell[ 1] = { 2, 3 }
Machine Cell[ 2] = { 4, 5 }
Machine Cell[ 3] = { 7, 8 }
Machine Cell[ 4] = { 1, 9 }
Machine Cell\begin{bmatrix} 5 \end{bmatrix} = \{ 6, 10 \}
Part Family[ 1] = { 2, 4, 9, 15, 18, 20, 27, 34, 36, 37 } Part Family[ 2] = { 3, 8, 17, 19, 24, 29, 38 } Part Family[ 3] = { 5, 6, 10, 11, 12, 13, 14, 21, 22, 25, 26, 28, 30, 31 } Part Family[ 4] = { 1, 7, 16, 23 } Part Family[ 5] = { 32, 33, 35 }
< Summary of the performance measures >
______
No. of machines
                                                                  = 10
No. of part types
No. of cells
Machine cell size
                                                                  = 38
                                                                  = 5
= 3
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                                   = 0.221
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                                     26
                                                                     18
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                                                   = 44
                                                                  = 69.05 %
                                                                  = 83.88
                                                                  = 56.86 %
Machine utilization (MU)
                                                                  = 76.32 %
No. of redundant machines (RMs)
                                                                  = 0
      -----
```

```
Problem(40) --> Data file name : DB_22_Joines(1996)_20x35.cfp
< Machines visited by parts: Process route numbers(PRN) >
                                           8,
Part[
                                                17
Part
                             4,
           2]
3]
4]
                       2,
                                   13,
                                          14,
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              =
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                                    7,
                                           8,
Part
              =
                       1,
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17 }
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                                                19
                     11,
Part
              =
                       3,
                                    8,
Part[
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14 }
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                            12
PartL
                     11,
              =
                       2,
                             4,
Part
                                    9,
                             6,
                                          10,
           81
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Part
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19 }
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                                   15,
                            12,
Part[
           9]
                      11,
                                          16,
Part[
         10]
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                                   15,
                                          16,
Part
         11
              =
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4,
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Part
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Part[
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         35]
              =
< Block Diagonal Solution Matrix >
                < Locations >
                   0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
                   0\; 0\; 0\; 0\; 0\; 0\; 0\; 0\; 0\; 1\; 1\; 1\; 1\; 1\; 1\; 1\; 1\; 1\; 2\; 2
                        3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9 0
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                < Machines
                     0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
                                          1 0 0 0
7 5 6 9
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           30
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           32
                 *
    34)
           33
                 *
    35)
           35
< Machine cells and Part families >
______
Machine Cell[ 1] = { 2, 4, 13, 14, 18 }

Machine Cell[ 2] = { 1, 3, 7, 8, 17 }

Machine Cell[ 3] = { 5, 6, 9, 10, 20 }

Machine Cell[ 4] = { 11, 12, 15, 16, 19 }
Part Family[1] = { 2, 7, 10, 12, 13, 18, 24, 27, 31 } Part Family[2] = { 1, 3, 5, 15, 17, 20, 23, 25, 29 } Part Family[3] = { 8, 14, 16, 19, 22, 26, 34 } Part Family[4] = { 4, 6, 9, 11, 21, 28, 30, 32, 33, 35 }
< Summary of the performance measures >
______
No. of machines
                                                              = 20
No. of part types No. of cells
                                                              = 35
                                                              = 4
Machine cell size = 5
Total no. of 1's in the original MPIM : |A| = 136
Matrix density
Total no. of within-block 1's
                                                                134
No. of exceptional elements (EEs)
No. of voids
                                                              = 41
Sum of EEs and voids
Group Cability Index (GCI)
                                                              = 43
                                                              = 98.53 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                             = 88.10 %
= 75.71 %
= 76.57 %
No. of redundant machines (RMs)
                                                              = 0
```

=========

```
< Machines visited by parts: Process route numbers(PRN) >
Part[
                          13,
                                22 }
Part[
                     3,
7,
          2]
3]
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                          20 }
             =
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8,
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17 }
                                      24 }
12,
18 }
Part
             =
                          14,
                           6,
                     5
Part
                                                   18 }
                                             15,
             =
Part[
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                          12,
                          10,
17 }
16 }
          6]
7]
Part
                     9
             =
                     9,
Part
                     4,
          81
Part
             =
                          21,
                                22 }
                    13,
Part[
          9]
Part[
                          5,
20 }
         10]
                     2,
                                11, 19 }
             =
                     3,
Part
         11
             =
        12]
Part
                    20
             =
                                19 }
19 }
20 }
22 }
Part
         13]
        14]
                     2,
3,
PartL
                          11,
             =
        15]
16]
                          12,
21,
Part
Part
                    13,
             =
                          13,
                                21,
                     1,
                                      22 }
Part[
         17]
                          9,
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                     8,
                                12,
                                             18 }
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Part[
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Part
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Part
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         34]
                          20 }
Part[
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Part[
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36]
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                                11 }
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                                11, 19 }
Part[
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         371
Part[
                     4,
                          16,
16 }
         38]
                                24 }
Part[
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                4
Part[
        39]
                     4,
             =
        40]
                     9,
                                17, 20 }
Part[
             =
                          10,
< Block Diagonal Solution Matrix >
               < Locations
                 2
                 \begin{smallmatrix}0&0&0&0&0&0&0&0&0&1&1&1&1&1&1&1\\1&2&3&4&5&6&7&8&9&0&1&2&3&4&5&6\end{smallmatrix}
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     18)
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     19)
            37
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     20)
            38
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     21)
                  *
                                       1
                                         1
            39
                  *
                  *
     22)
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     23)
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     24)
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     27)
            30
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     32)
            33
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     34)
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     37)
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            29
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1
     39)
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                  *
     40)
            40
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< Machine cells and Part families
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Machine Cell[ 1]
Machine Cell[ 2]
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                                    5,
                                        11, 19 }
                        =
                               3,
                                        }
                                    20
Machine Cell[3]
Machine Cell[4]
Machine Cell[5]
Machine Cell[6]
Machine Cell[7]
                               4,
                        = = = =
                                   16
                                   8, 12, 15,
13, 21, 22
14, 23, 24
10, 17 }
                                                   18 }
}
}
                               6,
1,
7,
                              9,
        Family[ 1]
Family[ 2]
Family[ 3]
Family[ 4]
Family[ 5]
Family[ 6]
Family[ 7]
                            { 10, 13, 14, 22, 35, 36 }
{ 2, 11, 12, 15, 23, 24, 31, 34 }
{ 8, 19, 21, 28, 37, 38, 39 }
{ 4, 5, 18, 26, 27, 30 }
{ 1, 9, 16, 17, 33 }
{ 3, 25, 32 }
{ 6, 7, 20, 29, 40 }
Part
                         =
Part
                        =
Part
                         =
Part
                         =
Part
                         =
Part
                         =
Part
< Summary of the performance measures >
No. of machines
No. of part types
No. of cells
                                                                 = 24
                                                                 = 40
                                                                 =
                                                                 = 5
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                                 = 119
                                                                    0.124
Matrix density
Total no. of within-block 1's
                                                                    112
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                                    19
                                                                    26
                                                                    94.12 %
grouping efficiency (GE)
                                                                 = 92.33
Grouping efficacy (GF)
                                                                             %
                                                                 = 81.16
Machine utilization (MU)
                                                                    85.50
No. of redundant machines (RMs)
_____
```

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*

```
< Machines visited by parts: Process route numbers(PRN) >
                                 13,
20 }
Part[
                                       22 }
Part[
                     2,
7,
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          2]
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< Block Diagonal Solution Matrix >
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               < Machines
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6 3 0 2 5 1 9 9 0 7 1
* * * * * * * * * * * *
                                                    2 2
                                                                    0
7
                                               1 3 *
                                                  2
                                                       0 0
                                                            1
                                                               1
5
*
                                                                 1
                                                                      1
                                                                           2
                 0
                                                       6
                                                          8
                                                                  8
                                                                            4
< Parts >
               * 1 1
                                                                               *
               *
                 1 1 1
          19
     2)
     3)
4)
          21
28
37
               *
                 1
                                                                               ÷
               * 1
                    1
               *
                                                                               *
     5)
                    1
               *
                 1 1
          38
     6)
                                                                            1
               *
     7)
          39
                 1 1
              *
                 =
     8)
           2
               *
                       1 1 1
               *
     9)
          11
                       1 1
   10)
          12
               *
                         1
          <del>1</del>5
               *
   11)
12)
                                                             1
                       1
               *
          23
                       1 1 1
                                           1
          24
               *
    13)
                         1
    14)
               *
                       1 1
          31
```

```
34 *
(
    15)
                            1 1
   ======= *
                                 _ _ _ _ _ _ _ _ _ _ _ _ _ _ _ _
                                     1 1
     16)
                                           1
    17)
            13
                                  1 1
                                           1
                  *
            14
                                        1 1
     18)
                                  1
            22
35
36
                                    1 1
1 1
1 1 1
                  *
    19)
                                  1
     20)
                                                          1
                                                                                   1
                  *
                                  1
                                                 1
     21)
                  *
                                              1
1
     22)
                  *
              6
                                                 1 1
                                                          1
((((
     23)
                  *
                                                    1
     24)
                  *
                                              1
                                                 1
            20
                  *
                                                 1 1
     25)
            29
            40
                  *
                                                 1 1
    26)
                               1
                  *
                                  1
     27)
                                                       1
                                                          1
                  *
                                                          9
                               1
                                                             1 1
     28)
                  *
     29)
                                                                                1
            16
                  *
                                                       1
     30)
             17
                                                              1
                  * 1
            33
                                                       1
                                                          1
     31)
                  * =
     32)
33)
                  *
                               1
                                     1
                                                                   1
                                                                      1 1 1
              5
                                                                      1
1
1
     34)
35)
                                                                         1 \overline{1} \overline{1}
            18
                                              1
                                                                         1
1
            26
                  *
                                                                                1
                  *
            27
                                  1
                                                                   1
                                                                            1
                                                                               1
     36)
                  *
                                                                      1
     37)
            30
            ====
              3
                  *
     38)
     39)
                                                                                            1
1
            25
                                                                                      1
            32
                  *
                                                                                         1
    40)
< Machine cells and Part families >
_____
Machine Cell[ 1] = { 4, 16 }

Machine Cell[ 2] = { 3, 20 }

Machine Cell[ 3] = { 2, 5, 11, 19 }

Machine Cell[ 4] = { 9, 10, 17 }

Machine Cell[ 5] = { 1, 13, 21, 22 }

Machine Cell[ 6] = { 6, 8, 12, 15, 1

Machine Cell[ 7] = { 7, 14, 23, 24 }
        Family[ 1] = { 8, 19, 21, 28, 37, 38, 39 }
Family[ 2] = { 2, 11, 12, 15, 23, 24, 31, 34 }
Family[ 3] = { 10, 13, 14, 22, 35, 36 }
Family[ 4] = { 6, 7, 20, 29, 40 }
Family[ 5] = { 1, 9, 16, 17, 33 }
Family[ 6] = { 4, 5, 18, 26, 27, 30 }
Family[ 7] = { 3, 25, 32 }
Part
Part
Part
Part
Part
Part
Part
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
                                                                   = 24
                                                                   = 40
                                                                   = 7
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                                   = 121
                                                                   = 0.126
Matrix density
Total no. of within-block 1's
                                                                   = 101
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                                   = 20
                                                                      30
                                                                       50
                                                                      83.47 %
grouping efficiency (GE)
                                                                   = 87.34
Grouping efficacy (GF)
                                                                   = 66.89 %
Machine utilization (MU)
                                                                      77.10
No. of redundant machines (RMs)
______
```

```
DB_25_SeifoddiniDjassemi(1996)_Version_3_7x11.cfp
< Machines visited by parts: Process route numbers(PRN) >
______
          1]
2]
3]
4]
Part[
                     2,
                              }
                            3
Part[
-+[
                            3577357
Part
                     1,
                                  6 }
             =
                              }
                     4,
Part[
          5]
6]
7]
                     4,
PartL
             =
Part
Part
                     1
                                  6 }
              =
                     ā,
                              }
          8
Part[
         9]
10]
                            3
7
Part[
                     2,
             =
Part[
Part[
                     4,
                            5,
                     1,
                                  6 }
         11]
             =
< Block Diagonal Solution Matrix >
               < Locations >
                  0 0 0 0 0 0
                  0 0 0 0 0 0
                       3 4 5 6 7
               < Machines
                            >
                  0 0 0 0 0 0
                  0
                    0 0 0 0 0 0
                    5 6 2 3 4
< Parts >
               * *
               * 1 1 1
                                   *
           3
     1)
(
                 *
                                   *
     2)
               *
     3)
                                   *
          11
               *
    ======
                 = = = = = =
               *
                                   *
                         1 1
((((
               *
     5)
           2
                         1 1
           6
               *
                         1 1
     6)
           8
                            1
               *
                                   *
     8)
           9
                         1 1
               *
                              =
                                 1
                                   *
     9)
           4
               *
                              1
                              1
    10)
           5
               *
                                   *
          10
                              1
                                 1
< Machine cells and Part families >
                         1, 5, 6
2, 3 }
Machine Cell[ 1] = {
Machine Cell[ 2] = {
Machine Cell[ 3] = {
                                  6
                          3, 7,
1, 2,
4, 5,
      Family[ 1] = { 3,
Family[ 2] = { 1,
Family[ 3] = { 4,
Part
                                  11 }
                                  6, 8
10 }
Part
                                         9 }
Part
< Summary of the performance measures >
No. of machines
                                                       = 7
No. of part types No. of cells
                                                       = 11
                                                         3
                                                       =
Machine cell
                size
Total no. of 1's in the original MPIM : |A|
                                                          25
                                                       = 0.325
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                       =
                                                          24
                                                          1
                                                       =
                                                          1
Sum of EEs and voids
Group Cability Index (GCI) grouping efficiency (GE) Grouping efficacy (GF)
                                                         96.00 %
                                                       = 97.04
                                                       = 92.31 %
                                                       = 96.00 %
Machine utilization (MU)
                                                       = 0
No. of redundant machines (RMs)
```

Problem(43) --> Data file name :

```
DB_26_SeifoddiniDjassemi(1996)_Version_4_7x11.cfp
< Machines visited by parts: Process route numbers(PRN) >
______
          1]
2]
3]
4]
Part[
Part[
Part[
                     2,
                              }
                            4
                            3577357
Part
                      1,
                                  6 }
             =
                              }
                     4,
Part[
          5]
6]
7]
                     1,
PartL
             =
Part
                      1
Part
                                  6 }
              =
                              `}
          8]
                     4,
Part[
                           3,
7 }
         9]
10]
                     2,
Part[
                                  6 }
             =
Part[
Part[
                     4,
                            5,
                      1,
                                  6 }
         11]
             =
< Block Diagonal Solution Matrix >
               < Locations >
                  0000000
                  0 0 0 0 0 0
                       3 4 5 6 7
               < Machines >
                  0 0 0 0 0 0
                  0
                    0 0 0 0 0 0
                    5 6 2 3 4
< Parts >
               * *
               * 1 1 1
                                   *
           3
(((
                 1
1
           5
7
               *
     2)
                                 1
               *
                    1
                                    *
               * 1 1 1
     4)
          11
               * = = = =
                                   *
               *
                                    *
                         1
(
     5)
           1
                              1
               *
                                   *
           2
                         1 1
     6)
           6
                         1 1
               *
                                   *
     8)
           9
                       1 1 1
               *
                              = =
                                 1
                              1
                                   *
     9)
           4
               *
    10)
           8
               *
                                   *
          10
                               1
                                 1
< Machine cells and Part families >
                         1, 5, 6
2, 3 }
4. 7 }
Machine Cell[ 1] = {
Machine Cell[ 2] = {
Machine Cell[ 3] = {
                                  6
                                  7,
      Family[ 1]
Family[ 2]
Family[ 3]
                    = { 3,
= { 1,
= { 4,
                          3,
                              5,
2,
Part
                                      11 }
                          1,
                                  6, 9
10 }
Part
Part
< Summary of the performance measures >
No. of machines
                                                        = 7
No. of part types No. of cells
                                                        = 11
                                                          3
                                                        =
Machine cell
                size
Total no. of 1's in the original MPIM : |A|
                                                          26
                                                          0.338
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                          23
3
                                                        =
                                                        =
                                                          3
Sum of EEs and voids
                                                        = 6
                                                       = 88.46 %
= 91.29 %
= 79.31 %
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                                        = 88.46 %
Machine utilization (MU)
No. of redundant machines (RMs)
                                                        = 0
```

Problem(44) --> Data file name :

```
DB_27_SeifoddiniDjassemi(1996)_Version_5_7x11.cfp
< Machines visited by parts: Process route numbers(PRN) >
______
          1]
2]
3]
4]
Part[
                     2,
                              }
                            3
Part[
-+[
                            3
5
4
                     1,
3,
Part
                                  6 }
             =
                              ,
}
}
Part[
          5]
6]
7]
                     4,
                            7
PartL
             =
                      3,
                            4
Part
                            5
7
                      1
Part
                                  6 }
              =
                              }
          8
                     4,
Part[
         9]
10]
                     2,
                            3
7
Part[
              =
Part[
Part[
                     4,
                            5,
                      1,
                                  6 }
         11]
             =
< Block Diagonal Solution Matrix >
               < Locations >
                  0 0 0 0 0 0
                  0 0 0 0 0 0
                       3 4 5 6 7
               < Machines
                            >
                  0 0 0 0 0 0
                  0
                    0 0 0 0 0 0
                    5 6 2 3 4
< Parts >
               * *
               * 1 1 1
                                    *
           3
     1)
(
                 *
                                    *
     2)
               *
     3)
                                    *
          11
               * = = = = =
    ======
               *
                                    *
                         1 1
((((
               *
     5)
           2
                         1 1
               *
                            1
                              1
                                    *
     6)
           6
                            1
                              1
               *
                                    *
     8)
           9
                         1 1
               *
                              =
                              1
                                 1
                                    *
     9)
           5
               *
           8
    10)
                                   *
               *
          10
                               1
                                 1
< Machine cells and Part families >
                          1, 5, 6
2, 3 }
4, 7 }
Machine Cell[ 1] = {
Machine Cell[ 2] = {
Machine Cell[ 3] = {
                                  6
      Family[ 1] = { 3,
Family[ 2] = { 1,
Family[ 3] = { 5,
                          3,
                              7,
2,
Part
                                  11 }
                          1,
                                  4, 6
10 }
Part
                                      6,
                                          9 }
Part
< Summary of the performance measures >
No. of machines
                                                        = 7
No. of part types No. of cells
                                                        = 11
                                                          3
                                                        =
Machine cell
                size
Total no. of 1's in the original MPIM : |A|
                                                          25
                                                          0.325
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                          23
2
2
                                                        =
                                                        =
Sum of EEs and voids
Group Cability Index (GCI) grouping efficiency (GE) Grouping efficacy (GF)
                                                          92.00 %
                                                        = 94.08
                                                        = 85.19 %
                                                        = 92.00 %
Machine utilization (MU)
                                                          0
No. of redundant machines (RMs)
```

Problem(45) --> Data file name :

```
Problem(46) --> Data file name : DB_28_PaRkinLi(1997)_6x7.cfp
< Machines visited by parts: Process route numbers(PRN) >
                   1,
Part[
                              6
                                 }
Part[
         2]
3]
4]
5]
                   1,
4,
                         3,
                              5
            =
Part[
Part[
            =
                              3
5
                   1,
            =
Part[
                   2,
                         3,
                   4,
                         6<sup>'</sup>}
3 }
Part[
         6]
7]
            =
Part[
                           _____
< Block Diagonal Solution Matrix >
              < Locations >
                0 0 0 0 0 0
                0 0 0 0 0
                1 2 3 4 5 6
               Machines >
                0 0 0 0 0
                0
                  0 0 0 0 0
             2
* *
                  3 4 6 1 5
< Parts >
             * 1 1
          4
    1)
             * 1 1
    2)
                             *
(
             * 1 1
          7
                             *
    3)
             * = =
             *
    4)
          1
                    1 1 1
             *
                             *
    5)
          3
                    1
(
             *
                    1 1
                             *
    6)
          6
                             *
             *
               = = = = =
< Machine cells and Part families >
Machine Cell[ 1] = \{2,
Machine Cell[ 2] = { 4, Machine Cell[ 3] = { 1,
                           6 }
5 }
      Family[ 1] = { 4,
Family[ 2] = { 1,
Family[ 3] = { 2 }
Part
                           3,
Part
Part
                             ______
< Summary of the performance measures >
No. of machines
No. of part types
                                                 = 6
= 7
No. of cells
                                                  = 3
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                  =
                                                    17
Matrix density
                                                    0.405
Total no. of within-block 1's
                                                    13
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
                                                  =
                                                    4
                                                    1
                                                    5
                                                  =
Group Cability Index (GCI)
                                                    76.47 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                 = 89.29
= 72.22
                                                          %
                                                  = 92.86 %
                                                  = 0
No. of redundant machines (RMs)
______
```

```
< Machines visited by parts: Process route numbers(PRN) >
                          15,
Part[
                    13,
                                 21, 22 }
Part[
                          20'}
23,
          2]
3]
4]
                     3,
             =
                                 24 }
Part
             =
                    14,
                          12,
                                 15,
                                       18 }
                     8
Part
             =
                                 12,
                     6,
                                       15,
                                             18 }
Part[
                     9,
9,
          6]
7]
PartL
                          10 }
             =
                          10,
16 }
                                 17 }
Part
          81
                     4,
Part
             =
                     1,
                          13,
                                 21 }
Part[
          9]
                          5,
20 }
20 }
Part[
         10]
                     2,
3,
2,
2,
                                 11, 18 }
             =
Part
         11
             =
         12]
Part
             =
                          11,
                                 19 }
Part[
         13]
                          5,
20 }
        14]
                                 19 }
PartL
             =
Part
         15]
                                21,
22,}
         16]
                     1,
Part
                          13,
             =
                                       22 }
                          13,
                     1,
Part[
         17]
                          12,
16 }
17 }
         18]
                     6,
                                 15,
                                       18 }
Part[
             =
                     4,
Part
         19]
             =
         20]
                    10,
Part
             =
                     4,
2,
3,
                          16
Part
         21]
         22]
                                       19 }
Part[
             =
                                 11,
                          20 }
20 }
        23]
24]
Part[
             =
                     3,
7,
Part
             =
                          14,
                                 23 }
Part[
         25]
                                 15,
                           8,
         26]
27]
                     6
                                       18 }
Part[
             =
                    6,
3 }
Part[
                           8,
                                       15,
             =
                                             18 }
        281
Part[
             =
Part[
                     9,
         291
                          17 }
                           8,
                                12,
                                       18,
Part[
         30]
                                             22 }
< Block Diagonal Solution Matrix >
               < Locations
                 1 5
                                                                    2
1
                    0 0 0 0 0 0 0 0 1
                                          1
1
                                             1 2
                                                1 3
                                                  14
                                                       16
                                                          1
7
                                                            18
                                                               19
                                                                 2
                      3 4 5 6 7 8 9 0
               < Machines
                 0 0
                                                                    0
                    2 0 0 1 1 1 0 1 2 2 0 0 6 8 2 5 8 1 3 1 2 4
                                                       1
7
                                                          0
                                               1 0 1
                                                            0
                                                               1
                                                                 1
                                                                    0
                                                                       1
                                                                         2
                                                                            2
                                                  9 0
< Parts >
                                               6
                                                            5
                                                               1 9
                    1
               *
                 1
                 1
          11
12
15
               *
                    1
1
                 1
                                                                               *
               *
                 \overline{1}
     4)
               *
                    \overline{1}
     5)
          23
                 1
               *
          24
                 1
     6)
               * 1
              * =
                    =
                      ______
                         1 1
1 1
                              1 1
1 1
     8)
               *
           5
                         1
     9)
   10)
          18
               *
                       1
                            1 1 1
                                                                               *
          26
27
               *
                                                                               *
   11)
                       1
                         1
                              1 1
                      \overline{1}
                        \overline{1}
                           \begin{array}{ccc} 1 & \bar{1} \\ 1 & \end{array}
   12)
               *
                                                                               ÷
                                 1
   13)
          30
                                 1
                                           1
               *
                              =
                         = =
          ===
                                      = = =
                                     1 1 1
1 1
1 1 1
               *
           1
                              1
                                                                               *
   14)
                                   1
1
   15)
           9
               *
                                                                               *
               *
          16
   16)
   17)
          17
               *
                                   1 1
                                           1
                                                                               *
               *
               *
                                             1
   18)
           8
                                                1
   19)
                                             1
                                                1
          19
          21
               ÷
                                             1 1
                                                                               *
   20)
               *
               *
   21)
           6
                                                   1 1
```

```
22)
                                                                          1 1 1
     23)
               20
                                                                             1 1
                                                                          1
      24)
               29
======
              ====
                      *
     25)
               10
                                                1
                                                                                     1 1 1
     26)
               13
                                                                                     1
                                                                                            1 1
                                                                                        1 1
1 1 1
                                                                                     \overline{1}
      27)
               14
               22
                      *
     28)
                     *
                      *
     29)
                 3
                                                                                                        1 1 1
      30)
< Machine cells and Part families >
Machine Cell[ 1] = { 3, 20 }
Machine Cell[ 2] = { 6, 8, 12, 15, 18 }
Machine Cell[ 3] = { 1, 13, 21, 22 }
Machine Cell[ 4] = { 4, 16 }
Machine Cell[ 5] = { 9, 10, 17 }
Machine Cell[ 6] = { 2, 5, 11, 19 }
Machine Cell[ 7] = { 7, 14, 23, 24 }
Part Family[ 1] = { 2, 11, 12, 15, 23, 24, 28 } Part Family[ 2] = { 4, 5, 18, 26, 27, 30 } Part Family[ 3] = { 1, 9, 16, 17 } Part Family[ 4] = { 8, 19, 21 } Part Family[ 5] = { 6, 7, 20, 29 } Part Family[ 6] = { 10, 13, 14, 22 } Part Family[ 7] = { 3, 25 }
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
                                                                                 = 24
                                                                                 = 30
Machine cell size = 5
Total no. of 1's in the original MPIM : |A| = 89
= 0.
Matrix density
                                                                                 = 0.124
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                                                 = 3
                                                                                     16
                                                                                    19
                                                                                 = 96.63 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                                                 = 91.91 %
= 81.90 %
                                                                                 = 84.31 %
No. of redundant machines (RMs)
```

```
< Machines visited by parts: Process route numbers(PRN) >
                            6 }
Part[
                     3,
Part[
                     2,
2,
          2]
3]
4]
                            5,
                                       10 }
10 }
                                  8
             =
                                 8,
9,
                           5,
7,
Part
Part
             =
                                  4,
                                        6,
Part[
                                              8 }
          6]
7]
                           9
Part[
             =
                              }
Part
                                 10 }
          81
Part
                          10
             =
                           3,
Part[
          9]
                                        8 }
                     ī,
7
        10]
                           3,
Part[
                                  6 }
             =
Part[
Part[
         11]
         12]
                     2,
                            5,
                                  8 }
             =
< Block Diagonal Solution Matrix >
               < Locations >
                 0 0 0 0 0 0 0 0 0 0
                 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0
                                       1
                      3 4 5 6 7 8 9 0
               < Machines
                            >
                 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0
                   0 0 1 0 0 0 0 0 0
                    5 8 0 1 3 6 4
< Parts >
               * *
               * 1 1 1 1
                                           *
2)
3)
               *
                 1
                   1 1 1
                                           *
                   ī
               *
                 1
                                           *
                         1
               * 1
     4)
           8
                         1
               * \overline{1} 1 1
     5)
          12
    ======
                 = = = = = = =
               *
           1
                              1 1
                                           *
     6)
(
           5
                      1
                            1 1 1 1
               *
                                           *
           9
                            1 1 1
          10
               *
     9)
                            1 1 1
                                          *
                                     1
                                        1
                                   1
    10)
                                          *
               *
    11)
           6
                                      1
                                       1
                                     1
               *
                                           *
    12)
          11
              * * * * * * * *
< Machine cells and Part families >
Machine Cell[ 1] = { 2, Machine Cell[ 2] = { 1, Machine Cell[ 3] = { 4,
                                  8,
6 }
9 }
       Family[ 1] = {
Family[ 2] = {
Family[ 3] = {
                         2,
1,
                              3,
5,
Part
                                         12 }
                                  9,
                                      10
Part
                              6,
                                  11 }
Part
< Summary of the performance measures >
______
No. of machines
                                                       = 10
No. of part types No. of cells
                                                       =
                                                         12
                                                         3
                                                       =
Machine cell size
Total no. of 1's in the original MPIM: |A|
                                                         36
Matrix density
                                                         0.3
Total no. of within-block 1's No. of exceptional elements (EEs)
                                                          33
                                                         3
No. of voids
                                                         8
Sum of EEs and voids
                                                         11
Group Cability Index (GCI) grouping efficiency (GE)
                                                       = 91.67
                                                       = 88.35 %
= 75.00 %
Grouping efficacy (GF)
                                                       = 80.49 %
Machine utilization (MU)
```

Problem(48) --> Data file name : DB_30_NairNarendran(1998)_Table_1_10x12.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
Part[
                                3 }
Part[
         2]
3]
4]
                    1,
                          2
4
             =
                            }
                    3,
Part
             =
aı [[
Part[
p⁻
                          4
            =
Part[
                          6,
                                7 }
                    3,
                          5,
                                6,
Part[
         6]
7]
             =
Part[
                                            _____
< Block Diagonal Solution Matrix >
              < Locations
                 0 0 0 0 0 0
                 0 0 0 0 0 0
                 1 2 3 4 5 6 7
                Machines > 0 0 0 0 0 0
                 0
                   0 0 0 0 0
                     3 4 5 6 7
                1
< Parts >
                   2
              *
              * 1 1 1
           1
     1)
              * 1 1
     2)
           2
              * = = = = = =
========
              *
                      1
                        1
              *
     4)
           4
                     1 1
              *
                                 *
           5
              *
                          1
     5)
                            1 1
                             1
1
*
                               1
1
*
     6)
           6
              *
                          1
                        1 1
              *
           7
     7)
              *
                 * *
< Machine cells and Part families >
Machine Cell[ 1] = \{ 1, 2 \}
                               }
Machine Cell[ 2] = {
Machine Cell[ 3] = {
                         3,
                             4
                         5, 6, 7 }
       Family[ 1] = {
                         1, 2
Part
       Family[2] = \{3, 4\}
Family[3] = \{5, 6\}
                            4 }
Part
Part
< Summary of the performance measures >
No. of machines
No. of part types
                                                     = 7
= 7
                                                     = 3
= 3
No. of cells
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                       20
Matrix density
                                                       0.408
Total no. of within-block 1's
                                                       17
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
                                                       3
                                                     =
                                                       0
                                                       3
                                                     =
Group Cability Index (GCI)
                                                       85.00 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                     = 95.31 %
= 85.00 %
                                                     = 100.00%
No. of redundant machines (RMs)
                                                     = 0
______
```

Problem(49) --> Data file name : DB_31_NairNarendran(1998)_Example_3_7x7.cfp

*

1 1

1

1

19)

20)

12

*

*

* * * * * * *

< Summary of the performance measures >

```
No. of machines = 8
No. of part types = 20
No. of cells = 3
Machine cell size = 4
Total no. of 1's in the original MPIM : |A| = 61
Matrix density = 0.381
Total no. of within-block 1's = 52
No. of exceptional elements (EEs) = 9
No. of voids = 0
Sum of EEs and voids = 9
Group Cability Index (GCI) = 85.25 %
grouping efficiency (GE) = 95.83 %
Grouping efficacy (GF) = 85.25 %
Machine utilization (MU) = 100.00%
No. of redundant machines (RMS) = 0
```

```
< Machines visited by parts: Process route numbers(PRN) >
                                  3,
Part[
                                               6 }
                                         9,
Part
                                  8,
          2]
3]
4]
                     6,
                                              14 }
              =
                                       9,
10 }
                     6,
Part
                                  8,
                                              10,
                                                    15 }
                            8,
                                 9,
12
Part
             =
                     9
                           11,
Part[
                           12,
12,
12,
                    11,
                                 13 }
13 }
13 }
                                 13
PartL
          6]
              =
                    11,
Part
          81
                    11,
Part
             =
                                 12,
                     5,
                                       13 }
          91
                           11,
Part[
                    10,
                                       18, 19, 20 }
Part[
         10] = {
                                 17,
                           16,
< Block Diagonal Solution Matrix >
               1 5
                                                          1
                                                        1
               < Machines
                  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
                                                          1
7
                    0 0 0 1 1 1 0 1 1 1 0 0 0 0
                                                        1
                                                             1
                                   5 1 2 3 1 2
< Parts >
                    7
                      8 9 0 4 5
                                                     4
========
               *
                 1
                    1
                      1
                         1
     1)
                              1
(
(
               * 1
                    1 1 1 1
     2)
           3
               *
     3)
           4
                    1 1 1 1
               * = = =
                         = = = = = =
                                        =
                                      1
1
                                        1
1 1
               *
           5
                         1
     5)
           6
               *
     6)
                                      1
                                        1 1
                                      1
     7)
                                        1 1
     8)
           9
               *
                                    1 1
                                        1 1
          ===
               *
     9)
                 1
                                              1 1 1 1
(
                         = =
                                                        =
    10)
          10
               *
                            *
< Machine cells and Part families >
Machine Cell[ 1] = { 6, 7, 8, 9, 10, 14, 15 }

Machine Cell[ 2] = { 5, 11, 12, 13 }

Machine Cell[ 3] = { 1, 2, 3, 4 }

Machine Cell[ 4] = { 16, 17, 18, 19, 20 }
       Family[ 1] = { 2, 3
Family[ 2] = { 5, 6
Family[ 3] = { 1 }
Family[ 4] = { 10 }
                          2, 3, 4 }
5, 6, 7, 8, 9 }
1 }
Part
Part
Part
Part
< Summary of the performance measures >
No. of machines
                                                        = 20
No. of part types
                                                        = 10
                                                          4
7
No. of cells
                                                        =
Machine cell
                 size
Total no. of 1's in the original MPIM : |A|
                                                          42
                                                        = 0.21
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                          39
                                                          11
Sum of EEs and voids
                                                          14
                                                          92.86 %
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                                        = 88.00
                                                        = 73.58 %
Machine utilization (MU)
                                                        = 78.00 %
No. of redundant machines (RMs)
                                                          0
```

Problem(51) --> Data file name : DB_33_Sandbothe(1998)_20x10.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
Part[
                       2,
                                     6
Part[
                       4,
                                    7,
           2]
3]
4]
                              5,
7,
5,
                                           8 }
              =
                                       ,
}
}
Part
              =
                       1,
                                     8
                                     6
Part
              =
Part[
                                     6
          6]
                       4,
Part[
                                    6,
                                           7 }
              =
                              5
3
7
                                `}
Part[
Part[
           7]
8]
                       1,
                                     8 }
              =
                              3
Part[
           91
                                    4,
         10]
                       1,
                              2,
                                           7,
              = {
                                                  8 }
Part[
< Block Diagonal Solution Matrix >
                < Locations > 0 0 0 0 0 0 0
                   0 0 0 0 0 0 0 0
                   1 2 3 4 5 6 7
                                     8
                < Machines
                   0 0 0 0 0 0 0 0
                     0 0 0 0 0 0 0
                   0
                     3
< Parts >
                   2
                       1 7 8
                                  5
                *
========
                *
                   1
                                      1
                                        *
                     1
(
            5
7
                *
     2)
                  1
                     1
                                      1
                * 1
                                         *
     3)
                     1
            9
                *
                   1 1
     4)
                *
                     = = = = =
                *
                        1 1 1
            3
     5)
                *
     6)
            8
                        1 1 1
(
                * 1
           10
                        1 1 1 1
     7)
                *
                          = = = = =
                *
     8)
            2
                           1 1 1 1
                *
                                1 1 1
                                        *
     9)
                                   1
                                     1
    10)
            6
               < Machine cells and Part families >
Machine Cell[ 1] = { 2, Machine Cell[ 2] = { 1, Machine Cell[ 3] = { 4,
                                3 }
7, 8 }
5, 6 }
       Family[ 1] = { 1,
Family[ 2] = { 3,
Family[ 3] = { 2,
                                5,
Part
Part
                                    6 }
Part
< Summary of the performance measures >
No. of machines
                                                           = 8
No. of part types
No. of cells
                                                              10
                                                           =
                                                              3
                                                            =
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                              32
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
                                                              0.4
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                              1
                                                              78.13 %
                                                              91.60
                                                           = 75.76 %
Grouping efficacy (GF)
Machine utilization (MU)
                                                           = 96.15 %
                                                           = 0
No. of redundant machines (RMs)
```

Problem(52) --> Data file name : DB_34_NairNarendran(1999)_8x10.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                       2,
                                    7
Part[
                             3,
4,
5 }
Part[
                       3,
                                    8
          2]
3]
4]
5]
              =
                      1,
Part
              =
                             5,
Part
              =
Part[
                                    8
          6]
7]
8]
                      2,
Part[
                             5
              =
Part[
Part[
                               '}
                             6
                             5,
                                    7
              =
Part[
          91
                                    8
                      2,
                             3,
                                    7,
                                          8 }
         10] = {
Part[
< Block Diagonal Solution Matrix >
                < Locations > 0 0 0 0 0 0 0
                  0 0 0 0 0 0 0 0
                  1 2 3 4 5 6 7 8
                < Machines
                  0 0 0 0 0 0 0 0
                     0 0 0 0 0 0 0
                  0
                     Š
< Parts >
                  2
                       7
                          3 4 8 1 6
               *
                       *
========
                *
                  1
                                        *
                     1
(
                  1
                     į
                *
     2)
            4
                       1
                *
                                        *
     3)
                  1
                     1 1
     4)
            8
                *
                  1 1 1
                *
                  1
     5)
          10
                        1 1
                                1
                *
                  = = = = = = =
     ======
                *
     6)
                          1 1 1
                *
            5
     7)
                          1 1 1
                *
     8)
            9
                          1 1 1
           ===
                  _ _ _ _ _
               *
                                       *
            3
     9)
                                    1
                *
    10)
                                     1
               * * * * * * *
< Machine cells and Part families >
Machine Cell[ 1] = { 2, Machine Cell[ 2] = { 3, Machine Cell[ 3] = { 1,
                           2,
                               5,
                           3,
       Family[ 1] = Family[ 2] = Family[ 3] =
                     = {
= {
= {
                           1,
2,
3,
                                    6, 8, 10 }
9 }
Part
Part
Part
< Summary of the performance measures >
No. of machines
                                                          = 8
No. of part types
No. of cells
                                                          =
                                                            10
                                                             3
                                                          =
Machine cell size
                                                            29
Total no. of 1's in the original MPIM : |A|
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
                                                             0.362
No. of voids
                                                             1
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                             93.10 %
                                                            96.29 %
Grouping efficacy (GF)
                                                          = 90.00 %
Machine utilization (MU)
                                                          = 96.43 %
No. of redundant machines (RMs)
                                                          = 0
```

Problem(53) --> Data file name : DB_35_IslamSarker(2000)_8x10.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                                -----
Part[
Part[
Part[
Part[
         2] = {
3] = {
4] = {
5] = {
                   1,
                         4
                           3,
                         5
                         4
2
3
Part[
         6]
7]
8]
Part[
                   1,
                               5 }
            = {
= {
= {
Part[
Part[
                         4
                   1,
                         3
                               5 }
         9] =
Part[
                         4
                         3,<sup>3</sup>,5,3
Part[
Part[
                   1,
                               5 }
        107
        10] = {
11] = {
            =
                   3,
______
< Block Diagonal Solution Matrix >
              < Locations >
                0 0 0 0 0
                0 0 0 0 0
                1 2 3 4 5
              < Machines >
                0 0 0 0 0
                0 0 0 0 0
             1 2 4 3 5
< Parts >
             * 1 1
          1
2
* 1
     2)
          4
              *
                  1 1
     3)
             * 1 1
                           *
             * 1
                    1
             *
                           *
    6)
          9
                  1 1
  ======== * = = = = *
             *
                       1 1
             * 1
                      1 1
    8)
          6
             * 1
    9)
          8
             * 1
         10
                       1 1
   10)
              *
   11)
         11
             * * * *
< Machine cells and Part families >
Machine Cell[ 1] = { 1, 2, 4 Machine Cell[ 2] = { 3, 5 }
______
      Family[ 1] = { 1, 2, 4, 5, 7, 9 }
Family[ 2] = { 3, 6, 8, 10, 11 }
< Summary of the performance measures >
No. of machines
                                                  = 5
No. of part types No. of cells
                                                  = 11
                                                  = 2
= 3
Machine cell
               size
                                                  =
Total no. of 1's in the original MPIM : |A|
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                    6
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
""""" (MI)
                                                  = 88.00 %
                                                  = 83.73
                                                  = 70.97 %
Machine utilization (MU)
                                                  = 78.57 %
No. of redundant machines (RMs)
                                                  = 0
______
```

Problem(54) --> Data file name : DB_36_Won(2000)_5x11.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                            }
Part[
                          6
Part[
         2]
3]
4]
                    1,
                          2
             =
                                4 }
6 }
                          3,
Part
Part
            =
                            ,
}
}
                          5
Part[
         6]
Part[
                          4
            =
Part[
Part[
                          6
         81
                    3
                    3,
                          4 }
Part[
         9]
Part
                    1,
                          3, ´
4 }
        107
                                5 }
             =
        10] = {
11] = {
                    3,
Part[
______
< Block Diagonal Solution Matrix >
              < Locations >
                0 0 0 0 0
                0 0 0 0 0
                1 2 3 4 5 6
              < Machines
                0 0 0 0 0 0
                0 0 0 0 0
                3 4 5 6 1 2
< Parts >
              * *
              * 1 1
                            1
              *
                               *
     2)
          4
                   1
              *
                               *
          6
                   1
                          1
     3)
              * 1
                               *
          8
              * 1
          9
                  1
              * 1 1
     6)
         11
             * = = = = = *
    ======
              *
                     1 1
              * 1
     8)
         10
                     1
                          1
             * = = =
                       = = = *
    9)
          2
5
7
              *
                          1 1 *
                            1 *
    10)
              *
                            1
  11) 7 * 1
======= * * * * * *
< Machine cells and Part families >
Machine Cell[ 1] = \{ 3, 4 \}
Machine Cell\begin{bmatrix} 2 \end{bmatrix} = \{5, 6\}
Machine Cell\begin{bmatrix} 3 \end{bmatrix} = \{1, 2\}
                         5,
Part Family[ 1] = { 3, 4, Part Family[ 2] = { 1, 10 Part Family[ 3] = { 2, 5,
                                6, 8, 9, 11 }
                            10
< Summary of the performance measures >
_____
No. of machines
No. of part types
                                                    = 6
                                                    = 11
No. of cells
                                                    = 3
Machine cell size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                      0.364
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
                                                      16
                                                      8
                                                      6
                                                      14
Group Cability Index (GCI)
                                                    = 66.67 %
                                                    = 77.27
= 53.33
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                    = 72.73 %
No. of redundant machines (RMs)
                                                    = 0
______
```

Problem(55) --> Data file name : DB_37_BrownSumichrast(2001)_6x11.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                   2,
                         4
                           }
Part[
Part[
                   3,
                         7
         2]
3]
4]
5]
            =
                   1,
                         6,
Part
            =
                               8 }
                           '}
                         3
Part
            =
                         4,
Part[
                                     6 }
                               5,
         6]
Part<u></u>
                   1,
                         8
            =
Part[
Part[
                   6 }
         8]
                         5 }
            =
                         _____
< Block Diagonal Solution Matrix >
              < Locations >
                0 0 0 0 0 0 0
                0 0 0 0 0 0 0 0
                1 2
                    3 4 5 6 7 8
               Machines
                00000000
                0 0 0 0 0 0 0 0
                  6 8 2
< Parts >
                1
                         4
                           5
              *
                *
                    *
========
             * 1 1 1
     1)
          3
                                  *
             * 1
                                  *
(
          6
    2)
                    1
             *
                                  *
    3)
                  1
         ===
               =
                  =
                    =
                      = = =
              *
                                  *
          1
     4)
                       1 1
              *
                                  *
          4
                       1
     5)
                              1
                                  *
     6)
          5
              *
                       1
                         1
                           1
              *
          8
                         1
                           1
    7)
                                  *
              *
              *
    8)
          2
(
                              1
                                1
               * * *
                      * *
             *
< Machine cells and Part families >
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
                   =
                   =
      Family[ 1] = { 3, Family[ 2] = { 1, Family[ 3] = { 2}}
                           6,
Part
                           4,
Part
Part
                        _____
< Summary of the performance measures >
No. of machines
                                                  = 8
No. of part types
No. of cells
                                                    8
                                                  =
                                                  =
Machine cell size
                                                     3
                                                    18
Total no. of 1's in the original MPIM: |A|
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
                                                    0.281
                                                     16
                                                    7
                                                  =
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                     9
                                                  =
                                                     88.89 %
                                                    82.34 %
Grouping efficacy (GF)
                                                  = 64.00 %
                                                  = 69.57 %
Machine utilization (MU)
No. of redundant machines (RMs)
                                                  = 0
______
```

Problem(56) --> Data file name : DB_38_SarkerKhan(2001)_8x8.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                                    9
31,
36 }
                         21,
Part[
                               14,
         2]
3]
                   19,
Part[
                         10,
                                           26 }
             =
                   15,
                               28,
Part
             =
                         11,
                               32,
17,
         4]
Part[
                    3,
                         21,
Part[
         5]
                         16,
                                           13, 23,
                                                      29 }
         6]
7]
8]
                         20,
25,
17,
                               11,
22,
27,
                                     18 ]
12,
Part
            =
                                           14,
35 }
                   19
                                                 33,
Part[
             =
                                                       31 }
Part
            =
                                                       30 }
         9]
                         16,
                                6,
                                                35,
Part[
             =
                                           13,
                                     12<sup>'</sup>}
28<sup>'</sup>}
Part[
        10]
             =
                   34,
                         24,
                                5,
        11]
                         20,
Part[
Part[
        12]
13]
                                     33,<sup>2</sup>
24 }
                               22,
             =
                         10,
                                           31 }
                         34,
                                4,
Parti
            =
                         15,
                               11,
                                     18 }
        147
Part[
             =
                                                 8, 13, 23, 35, 29 }
                                     17,
                                           27,
Part[
        15]
            =
                    1,
                         16,
                                6,
< Block Diagonal Solution Matrix >
              2 2 2 2
0 1 2 3
                                                                       2
                                                                              2
                                                                            2
                                                                                2
8
                                                                                     3
                                                           0 0 0 0 0 0 0 0 0
                0
                                                                                   0 0
                                                                                        0
                                                                                          00000
                1 3 2 4
                                                                    1 1 1 0 4 9
                                                                            2
                                                                                 2
                                                                                   3
                                                                                      3
                                                                                        0 0 3 4
                                                                                          0 0
4 9
                                                                              2 5
                                                                                                    3
< Parts >
                       111111
    1)
2)
                     1
           8
                1
                            1
(
(
          9
              *
                \bar{1} 1 \bar{1} 1
                                                                                                      *
              *
     4)
         15
                1 1 1 1 1 1 1 1 1
                                        1
                                                      3
                                               1 1
     5)
    6)
7)
                                               1
                                                    1
                                                      1
           6
                                                  1
              *
         11
                                           1
                                                       1 1
     8)
         14
              *
                                             1
                                               1
                                                 1 1
              *
                                               =
                                                  =
                                                                                                 1
              *
                                                              1 1 1
                                                                                                      *
(
    9)
         10
                                                             =
                                                                =
                                                                  =
                                                                     1 1 1
          2
7
                                                                                 1 1
   10)
                                                                       1 1 1 1
                                                                                   *
                                                                1
   11)
                                                                     1
                                                                                                      *
   12)
         12
              *
                                                                            1 1
              *
                                                                                                      *
                                                                            = = = = =
                                                                                        1
1
                                                                                            1 1
          1
   13)
                                                                                                    1
                                                                                                    1 *
                                                                                          1
    14)
           4
                                                                                            1
                                                                                                 1
         13
                                                                                           1
             * * * * * * * * * *
< Machine cells and Part families >
Machine Cell[ 1] = { 1, 6, 8, 13, 16, 17, 23, 27, 29, 30, 35 } Machine Cell[ 2] = { 2, 7, 11, 15, 18, 20, 28, 36 } Machine Cell[ 3] = { 5, 12, 34 } Machine Cell[ 4] = { 10, 14, 19, 22, 25, 26, 31, 33 } Machine Cell[ 5] = { 3, 4, 9, 21, 24, 32 }
      Family[ 1] = { 5, 8, 9, 1
Family[ 2] = { 3, 6, 11,
Family[ 3] = { 10 }
Family[ 4] = { 2, 7, 12 }
Family[ 5] = { 1, 4, 13 }
                            8, 9, 15 }
6, 11, 14 }
Part
Part
Part
Part
Part
                                   -----
< Summary of the performance measures >
No. of machines
No. of part types
No. of cells
                                                    = 15
                                                    =\overline{5}
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                    = 11
Matrix density
                                                     = 0.144
Total no. of within-block 1's No. of exceptional elements (EEs)
                                                      75
                                                    = 3
No. of voids
                                                    = 46
```

Problem(57) --> Data file name : DB_39_SeifoddiniDjassemi(2001)_Figure_5_36x15.cfp

```
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
No. of redundant machines (RMS)
                                                                                                                                                                                                                = 49
= 96.15 %
= 80.63 %
= 60.48 %
= 61.98 %
= 0
```

```
Problem(58) --> Data file name : DB_40_MalakootiYang(2002)_10x15.cfp
< Machines visited by parts: Process route numbers(PRN) >
                                         8 }
7,
Part
            2]
3]
4]
                                 6,
                                                9
Part[
                                                   }
                =
                          6,
                                         4,
                                                        9 }
Part
                =
                                                8,
                                           '}
                                 8,
Part[
                          4,
                                         9
Part[
            5]
6]
7]
8]
                =
                          2,
                                10
                          6,
                                 3,
6,
                                                8,
                                         4
3
3
Part
                                                        9 }
                =
Part[
                          1,
                =
                          5,
Part[
                                10,
                =
            9]
                                 5,
                                       10
Part[
                =
Part[
           10]
                =
                                 5,
                                       10
           11]
Part[
                                 6,
          12]
13]
Part[
Part[
                          ī,
2,
                                 6,
5,
                =
                                       10,
                =
                                 à,
                          3,
          147
                   {
                                         8
Part[
                =
                          2,
Part[
          15]
                =
                                 5,
                                       10
< Block Diagonal Solution Matrix >
                  < Locations >
   0 0 0 0 0 0 0 0 0 0
                     0 0 0 0 0 0 0 0 0 0 1
1 2 3 4 5 6 7 8 9 0
                     Machines
                     0 0 0 0 0 0 0 0 0 0
                     0 0 0 0 0 1 0 0 0 0 1 6 7 2 5 0 3 4 8 9 * * * * * * * * * * *
< Parts >
                    1 1 1
1 1
1 1 1
1 1 1
                  *
      1)
2)
                                                1
                  *
(
(
            11
                  *
                                                   *
            12
                  *
      4)
                                                1
                           ===
                     = =
                                                =
             5
                  *
      5)
                              1
      6)
7)
                                 1
                                    1 1
             8
             9
                  *
                                 1
                                    1
                              1 1 1
1 1 1
1 1 1
1 1 1
                                    1
1 1
      8)
            10
                  *
      9)
                  *
            13
    10)
            15
                  *
                              = =
                                    =
                  *
    11)
             1
                                       1 1 1
                  *
    12)
             3
                        1
                                       1
                                          1
                                             1
1
1
                                                   *
    13)
             4
                  *
                                          1
                                                1
                                                1
1
*
                                          1
1
*
    14)
             6
                  *
                        1
                                       1
                                                   *
                                       \frac{1}{*}
    15)
            14
< Machine cells and Part families >
Machine Cell[ 1] = { 1, 6, 7 }
Machine Cell[ 2] = { 2, 5, 10
Machine Cell[ 3] = { 3, 4, 8,
                                         10 }
Part Family[1] = {
Part Family[2] = {
Part Family[3] = {
                                    7, 11, 12 }
8, 9, 10, 13,
3, 4, 6, 14 }
                               2,
< Summary of the performance measures >
No. of machines
No. of part types
No. of cells
                                                                     10
                                                                     15
                                                                     3
                                                                  =
Machine cell
                   size
Total no. of 1's in the original MPIM: |A|
Matrix density
Total no. of within-block 1's
                                                                     45
No. of exceptional elements (EEs)
No. of voids
                                                                      5
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                                  = 12
                                                                     86.54 %
                                                                  = 91.50 %
= 78.95 %
Grouping efficacy (GF)
Machine utilization (MU)
                                                                  = 90.00 %
No. of redundant machines (RMs)
```

= 0

```
< Machines visited by parts: Process route numbers(PRN) >
                                    3,
                                            5,
7
Part
                                                    7 }
             2]
3]
4]
                            3,
2,
                                    4,
Part[
                  =
                                    6
4
Part
                  =
Part[
                  =
                            3,
             5]
6]
7]
Part[
                  =
                            1,
                                       }
                                    5
6
3
7
Part
                  =
Part[
                                            5,
                                                    7 }
                  =
             .
8]
Part[
                  =
< Block Diagonal Solution Matrix >
                    < Locations > 0 0 0 0 0 0
                       0 0 0 0 0 0 0 0 1 2 3 4 5 6 7
                       Machines
                          000000
                       0 0 0 0 0 0 0 0
1 3 5 4 7 2 6
* * * * * * *
< Parts >
===
      ======
                    *
                       1
       1)
               1
                         1
                             1
                                    1
       2)
3)
                    *
                       1
1
               5
7
(
                    *
                         1\overline{1}
                                    1
                    *
                       =
                          =
                             =
                                    =
                    *
                          1
       4)
               2
                                 1 1
                                 \bar{1}
       5)
                          1
                                 1
      6)
               8
                                   1
                    *
                                          =
1
1
                                              *
                    *
                                       1
               3
                                              *
       8)
               6
                   *
                                       1
                    *
                       * * * * *
< Machine cells and Part families >
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
                               {/{/{/{/
                                       3,
7 }
6 }
                                  1,
                                  4,
                           =
                           = {
= {
= {
Part Family[1] = Part Family[2] = Part Family[3] =
                                       5,
4,
6 }
                                  1, 5
2, 4
3, 6
< Summary of the performance measures >
No. of machines
                                                                        = 7
No. of part types
                                                                          8
                                                                          3
No. of cells
                                                                        =
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                                          21
                                                                           0.375
Matrix density
Total no. of within-block 1's
                                                                           17
No. of exceptional elements (EES)
No. of voids
Sum of EES and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
No. of redundant machines (PMS)
                                                                           4
                                                                           2
                                                                           6
                                                                          80.95 %
                                                                        = 89.33 %
= 73.91 %
                                                                        = 89.47 %
No. of redundant machines (RMs)
```

Problem(59) --> Data file name : DB_41_ZolphagariLiang(2002)_7x8.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                                          3,
Part
                                                  9,
                                                        10 }
                                  9,
5,
            2]
3]
4]
                                         10 }
Part[
                           1,
                 =
                           4,
                                                  LO }
9 }
                                          9,
                                                 10
Part
                 =
Part[
                 =
                           6,
                                          8,
            5]
6]
7]
Part[
                 =
                                   8
                                     }
                                   3
                                          9,
                                                 10 }
Part
                 =
                           4,
Part[
                 =
                                  5,
7,
             .
81
                           4,
                                         10 }
Part
                 =
                                                  9 }
Part
             d.
                 =
                           6,
                                          8,
                                   8'}
Part[
           10]
                 =
                           7,
< Block Diagonal Solution Matrix >
                   < Locations > 0 0 0 0 0 0 0 0
                      \begin{smallmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 0 \end{smallmatrix}
                     Machines
                      1 3 4 9 0
< Parts >
                      6
*
                        7
*
                            8
                                               2
                      1
      1)
2)
                   *
                        1
                                         1
                                                     *
                            1
                            1
1
              5
                   *
                         1
                                                     *
      3)
              9
                   *
                      1\overline{1}
                                         1
      4)
                   *
            10
                         1 1
                         =
                   *
                                         \begin{smallmatrix}1&1&1\\1&1\end{smallmatrix}
                               1
                                  1
      6)
7)
                               1
                   *
                                      1
                                         1 1
                                                     *
      8)
                   *
                                                      *
                               1
                                  1
                                         1 1
              6
                                      1
                                         1
                                            1
     10)
              8
                                      1
                                                  1
                      =
                            =
*
                         =
                   *
< Machine cells and Part families >
Machine Cell[ 1] = { 6, Machine Cell[ 2] = { 1, Machine Cell[ 3] = { 2,
                                     7, 8 }
3, 4,
5 } -
                                          4, 9, 10 }
} --> Residual cell
       Family[ 1] = { 4, 5, 9, 10 }

Family[ 2] = { 1, 2, 3, 6, 7, 8 ]

Family[ 3] --> Empty Part family
                                 4,
Part
Part
Part
< Summary of the performance measures >
No. of machines
No. of part types
No. of cells
                                                                     = 10
                                                                        10
                                                                     =
                                                                        3
                                                                     =
Machine cell
                    size
Total no. of 1's in the original MPIM : |A|
Matrix density
Total no. of within-block 1's
                                                                        0.33
                                                                        28
No. of exceptional elements (EEs)
No. of voids
                                                                        14
Sum of EEs and voids
                                                                        19
                                                                     = 84.85 %
= 79.02 %
= 59.57 %
Group Cability Index (GCI) grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                                     = 66.67 %
No. of redundant machines (RMs)
                                                                     = 2
```

Problem(60) --> Data file name : DB_42_Mahdavi(2007)_Example_2_10x10.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
Part
                                13
                                    }
            2]
3]
4]
                                                 9,
                                         8
Part[
                                 4
                                                       12 }
                 =
                          2,
2,
                                               8,
15 }
                                                        9,
                                                              12 }
                                  3,
Part
                =
                                         4,
                                        13,
7,
7,
Part[
                                 3,
Part[
            5]
6]
7]
8]
                 =
                                 6,
                                               11,
                                                       15 }
                               6,
13
13
4,
                                                              15 }
                                               10,
                                                       11,
Part
                =
Parti
                 =
                          3,
2,
Part
                =
                                        8,
                                                 9,
Part[
                 =
                                                       12 }
           10]
                                10,
                                        14
Part[
                 =
Part[
           11]
                                        14
           12]
13]
                                               14 }
9,
                          ĺ,
2,
                                        10,
                                 8,
Part
                =
                                         8,
7,
                                 4,
                                                      12 }
Parti
                =
                          5,
                                 6,
                                               11,
14 }
           14]
                                                       12,
                                                              15 }
Part[
                 =
                    {
{
Part[
           15]
                =
                          1,
                                10,
                                        11,
< Block Diagonal Solution Matrix >
                  Machines
                      0 0 0 0 0 0 0 0 0 0 0 0 0 0
                     0 1 0 1 1 0 0 0
3 3 1 0 4 5 6 7
* * * * * * * *
                                             1 1 0
1 5 2
* * *
                                                      0 0 0
4 8 9
                                                                1
< Parts >
                     1 1
1 1
1 1
1 1
1 1
1 1
      1)
2)
3)
                  *
((((
                  *
              4
                                                 1 1
                  *
              8
                  *
      4)
                  *
      5)
            11
                                 1
                              = =
1 1
1 1
1 1
                           =
1
                        =
            10
      6)
                  *
)
(
                            1
      8)
            15
                  *
                            1
                                              1
                     = =
                           =
                              =
                                 =
                                          = = =
                                    1
1
                                       1
1
                                          1
1
                                             1
1
      9)
              5
                  *
                                                 1
1
     10)
              6
                  *
    11)
            14
                                    1
                                       1 1 1 1
                                                                1
                                                       1
1
1
                                                         1
1
1
     12)
                  *
                                                            1
1
1
*
                                                    \overline{1}
     13)
              3
                  *
                     1
                                                                1
1
1
     14)
                  *
              9
                                                          1
     15)
            13
                                                    1
                                                       1
< Machine cells and Part families
Machine Cell[ 1] =
Machine Cell[ 2] =
Machine Cell[ 3] =
Machine Cell[ 4] =
                               3,
1,
5,
2,
                                    13 }
                             ~~~~
                                    10, 14 }
6, 7, 11, 15 }
4, 8, 9, 12 }
                                   4,

4, 7, 8,

12, 15 }

5, 14 }

9, 13 }
         Family[ 1] = Family[ 2] = Family[ 3] = Family[ 4] =
                         = {
= {
= {
= {
                               1, 4,
10, 12
5, 6,
2, 3,
                                             8, 11 }
L5 }
Part
Part
Part
< Summary of the performance measures >
                      -----
No. of machines
                                                                   = 15
No. of part types
No. of cells
                                                                      15
                                                                      4
Machine cell size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                                   = 62
                                                                      0.276
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GCI)
                                                                      54
                                                                      8
                                                                      0
                                                                   = 87.10 %
grouping efficiency (GE)
                                                                   = 97.66 %
```

Problem(61) --> Data file name : DB_43_YangYang(2008)_Figure_6b_15x15.cfp

Grouping efficacy (GF) = 87.10 %
Machine utilization (MU) = 100.00%
No. of redundant machines (RMs) = 0

```
< Machines visited by parts: Process route numbers(PRN) >
Part
                                13
                                    }
            2]
3]
4]
                                                 9 }
Part[
                                  4
                                         8
                 =
                                         5,
5 }
                          2,
2,
                                  4,
                                                 8,
                                                         9,
                                                              12 }
Part
                =
                                        15
Part[
                                13,
                          5,
5,
3,
Part[
            5]
6]
7]
8]
                                        11,
                                               15 }
                                6
13
13
4
                                               10,
                                                       15 }
Part
                =
Parti
                 =
                          3,
2,
Part
                =
                                         9,
             9
Part
                 =
                                               12 }
                                10,
                                        14'}
Part[
           10
                 =
Part[
           11]
                                14
           12]
13]
                                  8,
8,
7,
                                               14 }
12 }
                                        10,
Part
                =
                                         9,
                          ā,
Part
                =
                                        11,
                          6,
                                               12,
                                                       15 }
Part[
           147
                 =
                    {
{
                                        14 }
Part[
           15]
                =
                          1,
                                11,
< Block Diagonal Solution Matrix >
                  < Locations > 0 0 0 0 0 0 0 0 0 0 0 0 0
                     Machines
                      0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
                     0 0 0 0 1 0 1 0 0 0 0 0 2 4 8 9 2 3 3 5 6 7 * * * * * * * * * * * *
                                                   1 1 *
                                                       1 0 1
5 1 0
* * *
                                                                1
< Parts >
                  *
                     1
                        1
1
1
                              \begin{array}{c} 1\\1\\1\\1\end{array}
      1)
2)
                           1
                     1
1
                  *
              3
                           1
                                           1
(
(
              9
                  *
                  *
                        \bar{1} 1 \bar{1} \bar{1}
      4)
            13
                                    =
1
                     =
                        =
                           =
                              =
                                  =
                                       1
1
      5)
              1
      6)
7)
                                     1
              8
                  *
                                     1
                                       1
      8)
             11
                  *
                                     1
                  *
                                    =
      9)
                  *
                     1
                                        1
                                                       1
1
     10)
              5
                                                 1
                                                    1
                                           1
                                              1
    11)
              6
                                                 1
                                                       1
                                                             1
     12)
             14
                                  1
                                              1
                                                 1
                                                    1
                                                       1
                  *
                                                             1
1
             10
                  *
                                                          1
                                                                1
                                                                   *
     13)
     14<sup>)</sup>
                                                          1
1
*
                            1
             12
     15)
            15
< Machine cells and Part families
                               2, 4,
3, 13
5, 6,
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
Machine Cell[ 4]
                                         8, 9, 12 }
                          =
                             ~~~~
                         =
                          =
                                              11, 15 }
                                5, 6, 7, 11
1, 10, 14 }
                          =
         Family[ 1] = Family[ 2] = Family[ 3] = Family[ 4] =
                         = {
= {
= {
= {
                                    3, 9
7, 8
5, 6
                                2,
1,
4,
10,
                                         9,
                                              13
11
Part
                                         8,
Part
Part
                                         6,
                                            15 }
< Summary of the performance measures >
                       No. of machines
                                                                   = 15
No. of part types
No. of cells
                                                                      15
                                                                      4
Machine cell size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                                      53
                                                                   =
                                                                      0.236
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GCI)
                                                                      45
                                                                      8
                                                                      12
                                                                      20
                                                                   = 84.91 %
grouping efficiency (GE)
                                                                   = 87.09 %
```

Problem(62) --> Data file name : DB_44_YangYang(2008)_Figure_6d_15x15.cfp

Grouping efficacy (GF) = 69.23 %
Machine utilization (MU) = 78.95 %
No. of redundant machines (RMs) = 0

```
< Machines visited by parts: Process route numbers(PRN) >
Part
                                      6 }
           2]
3]
4]
                        1,
3,
                               4,
Part[
                                      6
                                             8 }
               =
                                      9
Part
               =
                               4,
                        3,
7,
                                      9
Part[
                               4,
Part[
           5]
6]
7]
8]
               =
                              10,
                                     11
                               5
Part
               =
Parti
               =
                               4
Part
               =
                               4
Part
               =
          10
Part
               =
                               4
                                     3,
6,
7,
1 }
9 }
                                      6,
                                             8
9
Part[
          12
13
                        4,
7,
Part
               =
                                     11
Part
               =
                        3,
4
2
7
          14]
Part[
               =
          15
Part|
               =
          16]
17]
Part[
Part
                                 }
                               8
7
Part
                        4,
          19]
               =
Part[
                      < Block Diagonal Solution Matrix >
                 < Locations > 0 0 0 0 0 0 0 0 0
                    0 0 0
0 0 0
2 6 8
* * *
                   Machines
                   0 0 0 0 0 0 0 0 0
0 0 0 0 0 0 1 1 0
3 4 5 9 7 0 1 1
* * * * * * * * *
< Parts >
                                                   *
                   1 1
1 1
      1)
2)
3)
                            1
1 1 1
             6
                 *
                      1
                   11111
     5)
6)
7)
8)
9)
                 *
                      1
1
1
                 *
           12
14
                 *
                         1 1 1
                   1
                 *
           15
                      1
           18
19
                 *
    10)
                       1
                 *
    11)
                      1
                 *
                               =
1
1
                   = =
                            =
                                  1 1
1 1
            5
                 *
    12)
    13)
           13
                               1
    14)
           17
                 *
    15)
                 *
                      1
                                          1
                                             1
1
                 *
                      1
                                                   *
    16)
                                               1
1
           10
                 *
                      \bar{1}
                                          1
                                                   *
    17<sup>)</sup>
                      1
    18)
           11
                                        1
                                             1
                                          1
    19)
           16
< Machine cells and Part families >
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
                       = {
= {
= {
                             3, 4, 5, 9 }
7, 10, 11 }
1, 2, 6, 8 }
       Family[ 1] = {
Family[ 2] = {
Family[ 3] = {
                             3, 4, 6, 7, 8
5, 13, 17 }
1, 2, 10, 11,
                                               8, 9, 12, 14, 15, 18, 19 }
Part
Part
                                                 16 }
Part
< Summary of the performance measures >
No. of machines
                                                              = 11
No. of part types
No. of cells
Machine cell size
                                                                 19
                                                              = 3
= 4
Total no. of 1's in the original MPIM: |A|
                                                                 50
Matrix density
                                                              = 0.239
Total no. of within-block 1's
```

Problem(63) --> Data file name : DB_45_FengPheng(2011)_Matrix_3_11x19.cfp

```
No. of exceptional elements (EEs) = 7
No. of voids = 30
Sum of EEs and voids = 37
Group Cability Index (GCI) = 86.00 %
grouping efficiency (GE) = 76.88 %
Grouping efficacy (GF) = 53.75 %
Machine utilization (MU) = 58.90 %
No. of redundant machines (RMs) = 0
```

```
< Machine cells and Part families
Machine Cell[ 1] = { 1, 5, 9, 12 }

Machine Cell[ 2] = { 4, 7, 10, 13

Machine Cell[ 3] = { 8, 14, 15 }

Machine Cell[ 4] = { 2, 3, 6, 11 }
                                               5, 9, 12 }
7, 10, 13 }
14, 15 }
                                                                    -----
```

* * * * * * * * *

1

*

1

* 25

```
Part Family[ 1] = { 1, 5, 16, 20, 23 }
Part Family[ 2] = { 9, 10, 11, 12, 15, 18, 22 }
Part Family[ 3] = { 3, 6, 7, 14, 17, 21, 24 }
Part Family[ 4] = { 2, 4, 8, 13, 19, 25 }
 < Summary of the performance measures >
 ______
No. of machines
No. of part types
No. of cells
Machine cell size
Total no. of 1's in the original MPIM: |A|
                                                                                                                      = 15
= 25
= 4
= 4
= 76
Total no. of 1's in the original Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficiency (GF)
Machine utilization (MU)
No of redundant machines (RMS)
                                                                                                                      = 9
= 26
                                                                                                                      = 35
= 88.16 %
                                                                                                                      = 84.43 %
= 65.69 %
= 72.04 %
```

= 0

No. of redundant machines (RMs)

*

*

*

*

*

*

10

13 21

15 *

20

1

1

1 1

1

18) 19)

20)

21)

22) 23) 24)

25)

26)

*

*

*

*

*

*

*

*

1 1 1

1

1 1 1

1 1 1 1 1 1

1

1

1

1 1 1

1

1

1 1

1 1

1 1

=

```
30
      27)
                                                                                                                                                            1 1 1
                                                                                                                                                                              1
1
1
        28)
                      8
                             *
        29)
                             *
                     18
        30)
                             * 1
                    23
 < Machine cells and Part families >
Machine Cell[ 1] = { 1, 5, 8, 18, 27 }

Machine Cell[ 2] = { 4, 6, 7, 25 }

Machine Cell[ 3] = { 14, 19, 22 }

Machine Cell[ 4] = { 2, 9, 10, 29 }

Machine Cell[ 5] = { 13, 15, 20, 28 }

Machine Cell[ 6] = { 3, 12, 16, 17, 21 }

Machine Cell[ 7] = { 11, 24, 26 }

Machine Cell[ 8] = { 23, 30 }
Part Family[ 1] = { 2, 9, 14, 17 }
Part Family[ 2] = { 1, 6, 24, 25, 27 }
Part Family[ 3] = { 4, 26, 28 }
Part Family[ 4] = { 3, 5, 16 }
Part Family[ 5] = { 11, 12, 19, 22, 29 }
Part Family[ 6] = { 7, 10, 13, 21 }
Part Family[ 7] = { 15, 20, 30 }
Part Family[ 8] = { 8, 18, 23 }
 ______
 < Summary of the performance measures >
 ______
 No. of machines
                                                                                                           = 30
 No. of part types
No. of cells
                                                                                                           = 30
                                                                                                           = 8
= 5
 Machine cell size
 Total no. of 1's in the original MPIM : |A|
                                                                                                           = 103
Matrix density
Total no. of 1's in the original in
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
No. of redundant machines (RMS)
                                                                                                           = 0.114
= 92
                                                                                                           = 11
                                                                                                            = 24
                                                                                                                35
                                                                                                           = 89.32 %
= 88.95 %
= 72.44 %
= 79.31 %
```

= 0

No. of redundant machines (RMs)

* *

```
< Machines visited by parts: Process route numbers(PRN) >
                               7,
6 }
9 }
10 }
Part[
                                      11 }
Part[
                           Ž,
          2]
3]
4]
5]
                     1,
             =
                     2,
Part[
Part[
                           6,
             =
                           5
7
             =
Part[
                           4,
                    3,
Part[
         6]
7]
             =
                                11
Part[
                                10
                                      _____
< Block Diagonal Solution Matrix >
               < Locations
                 0 0 0 0 0 0 0 0 0 0
                 00000000011
                 1\ 2\ 3\ 4\ 5\ 6\ 7\ 8\ 9\ 0\ 1
                 Machines >
                 00000000000
                 00000010001
              1 2 6 9 3 7 1 4 5 8 0
< Parts >
              * 1 1 1
           2
     1)
              *
     2)
           3
                   1 1 1
(
* 1
                           1 1 1
(
     4)
               *
           5
                           1 1
              *
                                            *
     5)
           6
                           1
                                1 1
                 _ _ _ _ _ _ _ _ _ _ _
               *
                                  1
                                    1
                                         į
               *
                                     \frac{1}{*}
                                       1
                 * * * * * * *
< Machine cells and Part families >
Machine Cell[1] = \{1, 2, 6,
Machine Cell[ 2] = { 3, Machine Cell[ 3] = { 4,
                             7, 11 }
5, 8, 10 }
       Family[ 1] = { 2, 3 }
Family[ 2] = { 1, 5,
Family[ 3] = { 4, 7 }
Part
Part
                                 6 }
Part
< Summary of the performance measures >
No. of machines
No. of part types
                                                     = 11
= 7
No. of cells
                                                      = 3
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                        21
Matrix density
                                                        0.273
Total no. of within-block 1's
                                                        19
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
                                                      =
                                                        2
                                                        6
                                                        8
Group Cability Index (GCI)
                                                        90.48 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                     = 86.08
= 70.37
                                                      = 76.00 %
No. of redundant machines (RMs)
                                                      = 0
```

Problem(66) --> Data file name : DB_48_Noktehdan(2016)_Table_1_11x7.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                              5,
6}
Part[
                                    6 }
Part[
         2] =
3] =
4] =
5] =
                        4,
                   2,
Part[
Part[
                   1,
                        3,
                              5,
                                    6 }
                                '}
                              o 4, 6 } }
                              6
Part[
                                         6 }
         6]
Part[
                   1,
            =
Part[
Part[
         8]
            =
                             _____
< Block Diagonal Solution Matrix >
             < Locations >
               0 0 0 0 0
                0 0 0 0 0
                1 2 3 4 5 6
              < Machines >
                0 0 0 0 0
               0 0 0 0 0
< Parts >
* 1
                    1 1
((((
             * 1 1 1 1
          3
    2)
             * 1
                    1 1 1 1
             * 1
                    1 1
          6
             * \overline{1} 1
                             *
                      1
             * = = = = =
             *
                      1
             *
                      \bar{1} \ \bar{1} \ \bar{1} \ *
          4
             *
                      1 1 1 *
     8)
          8
======== * * * *
< Machine cells and Part families >
Machine Cell[ 1] = \{ 1, 3, 5, 6 \}
Machine Cell[ 2] = \{ 2, 4 \}
      Family[ 1] = { 1, 3, 5, Family[ 2] = { 2, 4, 8 }
Part
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
                                                 = 6
                                                   8
                                                 =
                                                 =
Machine cell size Total no. of 1's in the original MPIM : |A|
Matrix density
Total no. of within-block 1's
                                                   22
No. of exceptional elements (EEs)
                                                 = 6
No. of checkers.

No. of voids

Sum of EEs and voids

Group Cability Index (GCI)
                                                   4
                                                   10
                                                 = 78.57 %
                                                 = 78.67
= 68.75
grouping efficiency (GE)
Grouping efficacy (GF)
                                                 = 84.62
Machine utilization (MU)
No. of redundant machines (RMs)
______
```

Problem(67) --> Data file name : DB_49_Noktehdan(2016)_Table_7_6x8.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                         4
Part[
                    1,
                           }
Part[
                   3,
1,
                           }
                         6
         2]
3]
4]
5]
            =
Part
            =
                   2,
                           }
                         5
4
Part
            =
Part[
         6]
                   2,
Part[
                         5
                           }
            =
                   3,
Part[
Part[
                         5
                               6 }
                           `}
         8]
                   1,
                         2
            =
                         _____
< Block Diagonal Solution Matrix >
              < Locations >
                0 0 0 0 0
                0 0 0 0 0
                1 2
                    3 4 5 6
              < Machines
                0 0 0 0 0
                0 0 0 0 0
                       5
*
< Parts >
                  4
                         3 6
             * *
========
              *
                1
                  1
                              *
              *
     2)
          3
                1
(
(
             *
     3)
                1
                  1
              *
     4)
          8
                1
                     1
             *
                    =
          4
              *
                     1 1
     5)
              *
                              *
    6)
          6
                     1 1
    ======
                =
                  = =
                      = = =
              *
                              *
                         1 1
              *
    8)
                       1 1 1
               * * *
             *
                      *
< Machine cells and Part families >
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
                   =
                            5
                   =
      Family[ 1] = { 1, 3,
Family[ 2] = { 4, 6 }
Family[ 3] = { 2, 7 }
Part
                               5, 8 }
Part
Part
                           _____
< Summary of the performance measures >
No. of machines
                                                   = 6
No. of part types
No. of cells
                                                  = 8
= 3
                                                     2
Machine cell size
Total no. of 1's in the original MPIM: |A|
                                                    16
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
                                                     0.333
                                                     14
                                                     2
                                                   =
                                                     2
No. of voids
                                                   =
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                   =
                                                     87.50 %
                                                    90.63 %
                                                   =
Grouping efficacy (GF)
                                                   = 77.78 %
                                                  = 87.50 %
Machine utilization (MU)
No. of redundant machines (RMs)
                                                  = 0
______
```

Problem(68) --> Data file name : DB_50_Won(2024)_6x8.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                              }
}
                            2
Part[
Part[
                     1,
                            2
2
          2]
3]
4]
5]
              =
Part
              =
                      1,
                                  3 }
                              }
                            4
                      3,
Part
             =
                            4
Part[
                     Ì,
          6]
Part[
                            4
                              }
             =
Part[
Part[
                      4,
                            5
                                  6 }
          8]
                            6
              =
                                        _____
< Block Diagonal Solution Matrix >
               < Locations >
                  0 0 0 0 0
                  0 0 0 0 0
                  1 2
                       3 4 5 6
                 Machines
                  0 0 0 0 0
                    0 0 0 0 0
                  0
< Parts >
                         4
                            5
               *
                  *
========
               * 1
                    1
                                 *
               *
           2
                 1
                    1
(
     2)
               *
           3
     3)
                 1 1 1
               *
           ===
                 =
                    =
                       = =
               *
                                 *
                       1 1
     4)
               *
                       1
           5
                         1
     5)
               *
     6)
           6
                       1
                         1
    ====
          ===
                 = =
                      =
                         = = =
               *
                                 *
                         1 1 1
               *
           8
     8)
                            1 1
                 * * * *
                            *
               *
< Machine cells and Part families >
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
                           1,
                     =
                           3,
                     =
                          1, 2,
4, 5,
7, 8 }
       Family[ 1] = {
Family[ 2] = {
Family[ 3] = {
Part
                                  6
Part
Part
< Summary of the performance measures >
No. of machines
                                                        = 6
No. of part types
No. of cells
                                                          8
                                                        =
                                                        =
                                                           2
Machine cell size
Total no. of 1's in the original MPIM: |A|
                                                          18
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
                                                           0.375
                                                           16
                                                           2
                                                        =
No. of voids
                                                        =
                                                           0
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                           88.89 %
                                                           96.88 %
                                                        =
Grouping efficacy (GF)
                                                        = 88.89 %
Machine utilization (MU)
                                                        = 100.00\%
                                                        = 0
No. of redundant machines (RMs)
```

Problem(69) --> Data file name : DB_51_AskinStandridge(1993)_6x8.cfp