```
Problem(70) --> Data Tite name : DC_OI_Burbluge(1973)_30x89.CTp
```

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< Machines visited by parts: Process route numbers(PRN) >
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              34
    _____ * * * * * * * * * * * * * *
< Machine cells and Part families >
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Machine Cell[ 1] = { 3, 4, 7, 9, 11, 14, 15, 16, 17, 19, 20, 21, 22, 24, 25, 26, 27, 28, 29, 30 }
Machine Cell[ 2] = { 1, 2, 5, 6, 8, 10, 12, 13, 18, 23 }
Part Family[1] = { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 19, 20, 21, 22, 23, 24, 25, 27, 28, 29, 30, 31, 32, 33, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89 }
Part Family[2] = { 18, 26, 34 }
```

< Summary of the performance measures >

```
No. of machines = 30

No. of part types = 89

No. of cells = 2

Machine cell size = 20

Total no. of 1's in the original MPIM: |A| = 302

Matrix density = 0.113

Total no. of within-block 1's = 284

No. of exceptional elements (EEs) = 18

No. of voids = 1466

Sum of EEs and voids = 1484

Group Cability Index (GCI) = 94.04 %

grouping efficiency (GE) = 57.14 %

Grouping efficacy (GF) = 16.06 %

Machine utilization (MU) = 16.23 %

No. of redundant machines (RMs) = 7
```

< Machine cells and Part families >

Machine Cell[1] = { 13, 19, 26, 27, 29, 37, 38, 43, 47, 50, 51, 52, 54, 62, 67, 69, 71, 77 } Machine Cell[2] = { 3, 5, 6, 7, 9, 10, 11, 12, 14, 23, 28, 30, 31, 34, 36, 41, 42, 46, 55, 56, 57, 58, 63, 65, 66, 68, 72, 73, 75, 78 } Machine Cell[3] = { 1, 2, 4, 8, 15, 16, 17, 18, 20, 21, 22, 24, 25, 32, 33, 35, 39, 40, 44, 45, 48,

```
< Machines visited by parts: Process route numbers(PRN) >
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Part[
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Part[
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7]
                   1,
1 }
            =
Part[
                        _____
< Block Diagonal Solution Matrix >
              < Locations >
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                0 0 0 0 0
                1 2 3 4 5
                Machines >
                0 0 0 0 0
                0
                  0 0 0 0
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< Parts >
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                     1 1 1 *
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                1
          6
                       1 1
                  * *
< Machine cells and Part families >
______
Machine Cell[ 1] = \{ 1, 4 \}
Machine Cell[ 2] = \{ 2, 3, 5 \}
      Family[ 1] = \{ 1, 7 \}
Family[ 2] = \{ 2, 3, 4, 5, 6 \}
Part
Part
< Summary of the performance measures >
_____
No. of machines
No. of part types
No. of cells
Machine cell size
                                                  = 7
                                                   =
               size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                   = 0.571
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                     15
                                                     4
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                                     9
                                                  = 75.00 %
= 73.85 %
                                                  = 62.50
Machine utilization (MU)
                                                  = 78.95 %
No. of redundant machines (RMs)
                                                  = 0
```

Problem(72) --> Data file name : DC_03_WaghodekarSahu(1984)_5x7.cfp

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< Machines visited by parts: Process route numbers(PRN) >
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< Block Diagonal Solution Matrix >
             < Locations >
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< Machine cells and Part families >
______
Machine Cell[ 1] = { 1, 2, 4 Machine Cell[ 2] = { 3, 5 }
Part Family[ 1] = { 1, 2, 3, 5, 6, 8, 11, 12, 13, 14, 16, 17 } Part Family[ 2] = { 4, 7, 9, 10, 15, 18 }
______
< Summary of the performance measures >
_____
No. of machines
No. of part types
No. of cells
                                                = 5
                                                = 18
= 2
Machine cell size
Total no. of 1's in the original MPIM : |A| = 46
```

Problem(73) --> Data file name : DC_04_Seifoddini(1989)_5x18.cfp

```
      Matrix density
      = 0.511

      Total no. of within-block 1's
      = 41

      No. of exceptional elements (EEs)
      = 5

      No. of voids
      = 7

      Sum of EEs and voids
      = 12

      Group Cability Index (GCI)
      = 89.13 %

      grouping efficiency (GE)
      = 86.76 %

      Grouping efficacy (GF)
      = 77.36 %

      Machine utilization (MU)
      = 85.42 %

      No. of redundant machines (RMs)
      = 0
```

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```
Machine Cell[ 2] = { 6, 8, 9 }
Machine Cell[ 3] = { 10, 14 }
Machine Cell[ 4] = { 2, 3, 11 }
Machine Cell[ 5] = { 1, 12, 13 }
______
Part Family[ 1] = { 2, 3, 17, 19, 20, 22 }
Part Family[ 2] = { 1, 6, 10, 11, 12, 14, 15, 16 }
Part Family[ 3] = { 13, 23 }
Part Family[ 4] = { 4, 5, 21 }
Part Family[ 5] = { 7, 8, 9, 18 }
< Summary of the performance measures >
_____
No. of machines
No. of part types
No. of cells
                                                                        = 14
                                                                        = 23
= 5
Machine cell size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                                        = 3
                                                                        = 0.18
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                                           16
                                                                        = 23
```

No. of redundant machines (RMs) = 0

grouping efficiency (GE)

Grouping efficacy (GF)
Machine utilization (MU)

= 87.93 %

= 86.69 %

= 68.92 % = 76.12 %

Problem(75) --> Data file name : DC_06_Stanfel(1985)_14x24.cfp < Machines visited by parts: Process route numbers(PRN) > 4, 7 } Part[Part[4, 2] 3] 5, 7 = 2, 10, 11,} 3, Part = 11 } 3 Part = 9 8, Part[13 } 7, 6] 7] 1, Part[= Part 12, 13 } 81 3 8, 8 } `} Part 12 13 = 9] 6, 9, Part[14 } 10] 6 Part[= Part 11 = 6, 14 Part 12 6, 8 9 } = 9, } Part[13] 14 6, 14] 8 } Part = 8 8, የ} 6, 9, Part 15] 14 } 16] Part 6 = 4, 7 } Part[13 18] Part[= Part 19 = 4 5, 11 } 8 } 20] 4, 7 } Part = Part 21] 3, 22] 6, Part[= Part[4, 5, 11 } 23] 13 } = 24] 10, Partl = < Block Diagonal Solution Matrix > < Locations Machines 0 1 0 1 1 * * 0 0 0 0 0 1 0 5 7 6 8 9 4 3 * * * * * * * 1 2 * 0 2 * 1 3 * 1 0 < Parts > 4 * * * 1 1 1 * 2 17 * 1 2) 1 1 3) * 1 1 1 * * 4) 19 1 * $\overline{1}$ 1 1 * 20 * * 6) 23 1 1 1 * = * ==== = = = = = = = = 1 1 * 8) * 1 1 1 1 * 9) 10 1 1 10) * 1 * 11 1 12 11) 1 1 1 * * 12) 13 1 1 * * 14 1 13) 1 1 14) 15 * 1 * 1 1 16 * 15) 1 22 * 1 1 * 16) * * * 1 1 1 * (17) 4 1 1 18) 21 24 * 19) * 1 1 * * = * 1 1 * 20) 6 21) 22) * 1 1 1 1 8 * 1 1 * * * (23) 18 1 * * 24) 1 1 1 1

< Machine cells and Part families >

* * *

*

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```
_____
Machine Cell[ 1] = { 4, 5, 7 }
Machine Cell[ 2] = { 6, 8, 9, 14 }
Machine Cell[ 3] = { 3, 11 }
Machine Cell[ 4] = { 1, 12, 13 }
Machine Cell[ 5] = { 2, 10 }
______
Part Family[ 1] = { 1, 2, 17, 19, 20, 23 }

Part Family[ 2] = { 5, 9, 10, 11, 12, 13, 14, 15, 16, 22 }

Part Family[ 3] = { 4, 21, 24 }

Part Family[ 4] = { 6, 7, 8, 18 }

Part Family[ 5] = { 3 }
_____
< Summary of the performance measures >
_____
No. of machines
                                                       = 14
No. of part types No. of cells
                                                       = 24
Machine cell size
Total no. of 1's in the original MPIM : |A| = 61
                                                       = 0.182
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                       = 6
                                                       = 23
Sum of EEs and voids
                                                       = 29
Group Cability Index (GCI) grouping efficiency (GE)
                                                       = 90.16 %
                                                       = 84.09 %
Grouping efficacy (GF)
                                                       = 65.48 %
                                                       = 70.51 %
Machine utilization (MU)
```

No. of redundant machines (RMs)

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19

24)

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```
< Machine cells and Part families >
                                                 -----
Machine Cell[ 1] = { 1, 2, 6, 8 }

Machine Cell[ 2] = { 5, 7 }

Machine Cell[ 3] = { 10, 11, 12, 16 }

Machine Cell[ 4] = { 9, 13 } --> Residual Cell

Machine Cell[ 5] = { 14, 15 }

Machine Cell[ 6] = { 3, 4 }
______
Part Family[ 1] = { 1, 3, 7, 8, 10, 13, 15, 18, 22, 23 } Part Family[ 2] = { 21 } Part Family[ 3] = { 2, 9, 11, 14, 17, 20, 24 } Part Family[ 4] --> Empty Part family Part Family[ 5] = { 4, 5, 6, 12 } Part Family[ 6] = { 16, 19 }
_____
< Summary of the performance measures >
______
No. of machines
                                                             = 16
No. of part types No. of cells
                                                              = 24
                                                              = 6
Machine cell size = 4
Total no. of 1's in the original MPIM : |A| = 86
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                                31
                                                              = 27
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                                              = 58
                                                              = 63.95 %
                                                             = 78.40
                                                             = 48.67 %
Machine utilization (MU)
                                                             = 67.07 %
                                                             = 3
No. of redundant machines (RMs)
```

```
< Machines visited by parts: Process route numbers(PRN) >
                       2,
Part[
                               3 }
Part[
                       4,
           2]
3]
4]
                                     8,
                                           11,
                                                  12 }
               =
                       5,
Part
               =
                             13
                              2,
9,
                       1,
                                             7,
                                                   8,
                                                         12 }
Part
               =
                                    15<sup>'</sup>}
Part[
                       5,
           6]
7]
                                    14,
7,
                             10,
                                           16 }
PartL
               =
                              4,
                                           8,
16 }
11 }
                       1,
                                                  11,
Part
                                                         12,
                                                                16 }
                       5,
1,
                                    14,
           81
                             10,
Part
               =
                              4,
                                     8,
Part[
           9]
                       2,
5,
Part[
          10]
                             13<sup>'</sup>}
               =
                             10,
Part
          11
               =
                                    11,
                                           14
                       1,
Part
         12]
                              7,
                                     8,
                                           11,
                                                  12 }
               =
                       3,
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Part[
          13]
                       <u>5</u>,
                                    14,
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PartL
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Part
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Part
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Part[
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Part[
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Part
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Part[
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Part[
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Part[
         30]
                                           11,
< Block Diagonal Solution Matrix >
                 < Locations
                   Locations > 0 0 0 0 0 0 0 0 0 0 0 0 0
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                                                  1 2
                                                     1
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                 < Machines
                   0 0 1 1 0 1 1 1 0 0 0
                      0
                                                       1 0 1
< Parts >
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           20
< Machine cells and Part families >
_____
Machine Cell[ 1] = { 1, 4, 7, 8, 11, 12 }
Machine Cell[ 2] = { 5, 10, 14, 16 }
Machine Cell[ 3] = { 3, 6, 9, 15 }
Machine Cell[ 4] = { 2, 13 }
Part Family[ 1] = { 2, 4, 7, 9, 12, 18, 19, 22, 30 } Part Family[ 2] = { 3, 6, 8, 11, 14, 15, 17, 21, 24, 26 } Part Family[ 3] = { 5, 23, 25, 27, 28, 29 } Part Family[ 4] = { 1, 10, 13, 16, 20 }
< Summary of the performance measures >
______
No. of machines
                                                             = 16
No. of part types No. of cells
                                                             = 30
                                                             = 4
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                             = 116
Matrix density
Total no. of within-block 1's
                                                             = 0.242
                                                             = 97
No. of exceptional elements (EEs)
                                                             = 19
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                             = 31
                                                                50
                                                             = 83.62 %
                                                             = 85.19 %
                                                             = 65.99 %
= 75.78 %
Grouping efficacy (GF)
```

= 0

Machine utilization (MU)

No. of redundant machines (RMs)

35

36

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< Machine cells and Part families >
Machine Cell[ 1] = { 3, 6, 7, 10, 14 } Machine Cell[ 2] = { 4, 5, 8, 11, 15 } Machine Cell[ 3] = { 1, 2, 9, 16 } Machine Cell[ 4] = { 12, 13 }
43 }
Part Family[ 3] = { 2, 4, 10, 18, 28, 32, 37, 38, 40, 42 } 
Part Family[ 4] = { 11, 22, 24, 30 }
< Summary of the performance measures >
______
No. of machines
                                                         = 16
No. of part types
No. of cells
                                                         = 43
                                                         = 4
Machine cell
                 size
                                                         = 5
Total no. of 1's in the original MPIM : |A| = 126
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                         = 100
                                                         = \overline{26}
                                                         = 93
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                                         = 119
                                                         = 79.37 %
= 73.28 %
                                                         = 45.66 %
Machine utilization (MU)
No. of redundant machines (RMs)
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    43)
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< Machine cells and Part families >
Machine Cell[1] = { 1, 3, 14 }
Machine Cell[2] = { 4, 5, 8, 15 }
Machine Cell[3] = { 11, 12, 13 }
Machine Cell[4] = { 7, 10 }
Machine Cell[5] = { 2, 6, 9, 16 }
Part Family[ 1] = { 17, 34, 35, 36 }
Part Family[ 2] = { 5, 8, 9, 14, 15, 16, 19, 21, 23, 29, 31, 33, 41, 43 }
Part Family[ 3] = { 3, 11, 20, 22, 24, 27, 30 }
Part Family[ 4] = { 1, 13, 25, 26, 39 }
Part Family[ 5] = { 2, 4, 6, 7, 10, 12, 18, 28, 32, 37, 38, 40, 42 }
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
                                                              = 16
                                                              = 43
                                                              = 5
Machine cell size
                                                               = 4
Total no. of 1's in the original MPIM : |A|
                                                              = 126
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
                                                               = 30
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                                 55
85
                                                                 76.19 %
grouping efficiency (GE)
                                                              = 78.99 %
Grouping efficacy (GF)
                                                              = 53.04 %
Machine utilization (MU)
                                                              = 63.58 %
No. of redundant machines (RMs)
                                                              = 1
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                                                 ======== * * * * * * * * * * * * *
< Machine cells and Part families >
Machine Cell[ 1] = { 3, 14 }
Machine Cell[ 2] = { 4, 5, 8, 15 }
Machine Cell[ 3] = { 7, 10 }
Machine Cell[ 4] = { 11, 12 }
Machine Cell[ 5] = { 2, 6, 9, 16 }
Machine Cell[ 6] = { 1, 13 } --> Residual cell
______
Part Family[ 1] = { 17, 34, 35, 36 }
Part Family[ 2] = { 5, 8, 9, 11, 12, 14, 15, 16, 19, 20, 21, 23, 29, 31, 33,
41, 43 }
Part Family[ 3] = { 1, 13, 25, 26 }
Part Family[ 4] = { 3, 22, 24, 27, 30 }
Part Family[ 5] = { 2, 4, 6, 7, 10, 18, 28, 32, 37, 38, 39, 40, 42 }
Part Family[ 6] --> Empty Part family
< Summary of the performance measures >
_____
No. of machines
No. of part types
No. of cells
                                                             = 16
                                                             = 43
                                                             = 6
Machine cell size = 4
Total no. of 1's in the original MPIM : |A| = 126
Matrix density
Total no. of within-block 1's
                                                             = 0.183
                                                             = 32
No. of exceptional elements (EEs)
= 52
                                                             = 74.60 %
grouping efficiency (GE)
                                                             = 79.24
Grouping efficacy (GF)
                                                             = 52.81 %
```

Machine utilization (MU) = 64.38 % No. of redundant machines (RMs) = 2

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< Machine cells and Part families >
                                                                                                                                                   _____
Machine Cell[ 1] = { 3, 4, 5, 6, 7 }
Machine Cell[ 2] = { 11, 12, 13, 14, 15 }
Machine Cell[ 3] = { 8, 9 }
Machine Cell[ 4] = { 1, 2 }
Machine Cell[ 5] = { 10, 18 } --> Residuation Resid
                                                                                                                            --> Residual cell
Part Family[ 1] = { 2, 5, 6, 8, 9, 10, 11, 12, 15, 16, 17 } 

Part Family[ 2] = { 1, 7, 13, 14, 18, 19, 21, 22 } 

Part Family[ 3] = { 3, 20, 24 } 

Part Family[ 4] = { 23 } 

Part Family[ 5] --> Empty Part family 

Part Family[ 6] = { 4 }
 ______
 < Summary of the performance measures >
 ______
 No. of machines
                                                                                                                                                                                  = 18
No. of part types No. of cells
                                                                                                                                                                                   = 24
                                                                                                                                                                                   = 6
Machine cell size = 5
Total no. of 1's in the original MPIM : |A| = 88
 Matrix density
 Total no. of within-block 1's
                                                                                                                                                                                   = 64
No. of exceptional elements (EEs)
No. of voids
                                                                                                                                                                                   = 41
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                                                                                                                                                                   = 65
                                                                                                                                                                                  = 72.73 %
= 76.81 %
                                                                                                                                                                                  = 49.61 %
 Machine utilization (MU)
                                                                                                                                                                                   = 60.95 %
                                                                                                                                                                                  = 2
 No. of redundant machines (RMs)
 _____
```

```
< Machines visited by parts: Process route numbers(PRN) >
Part[
                               18,
                                     20 }
Part
         2]
3]
                    2,
                         13 }
             =
                                     15,
12,
16,
Part
                          3,
                                           20 }
                          8,
                               11,
                                           17
                                                 20 }
Part
            =
                               15,
Part[
                         11,
                                      7,
                          4,
         6]
                    1,
2,
2,
                                6,
                                                  9 }
                                            8
Part
             =
Part
                          6,
                                           18
Part
         81
                          3
                               15,
                                     18,
                                           20
                                7,
                                            9,
Part[
         91
                          4,
                                      8,
                          4,
                                8,
        10]
                    2,
                                     10,
                                           13,
                                                 19
Part[
             =
                    2,
1,
? }
Part
        11
             =
                          3,
                               10,
                                     12,
                                           13,
                                                 16
        12]
                   12
Part
             =
                          2,
                                3,
                                      5,
                                           10,
                                                 11,
                                                       13,
Part[
        13]
                                                             14 }
                                Ž,
                                      8,
                                            9,
                    3,
2,
        14]
                          6,
                                                11,
17 }
                                                       12,
                                                             14,
                                                                  16, 17, 19 }
Partl
             =
                                           11,
                                8,
                                     10,
        15]
Part
                          Ì,
                                      9,
                                                 Ī5,
                                                             17,
        16]
                                           13,
                                                       16,
                                                                   18 }
Part
                               13,
                                     14<sup>1</sup>
Part[
        171
                          7,
                                8,
        18]
                    3,
                                     11,
                                           12,
                                                13,
20 }
Part[
             =
                                                       14 }
Part
        19
             =
                          9,
                               10,
                                     11,
                                           14.
                                8 }
        20]
                    2,
Part[
            =
< Block Diagonal Solution Matrix >
              < Locations >
                 1 1
2 3
                                                      1
7
                                                 1
5
                                                    1
                                               1
                                               4
              < Machines
                 0
                  0 1 1 1 1 2 0 0 0 0 0 5 0 1 3 4 0 1 4 6 7 9
                                           0 1 1 0
9 6 7 3
                                                    1 0
                 0
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< Parts >
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                     1
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              * 1
         15
                  1 1 1
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              * 1
     9)
         17
                          1 1
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   10)
         18
                          1
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    11)
          19
              *
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              * 1
   12)
         20
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   13)
                                        1
           6
              *
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   14)
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   15)
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              *
           9
                                 1 1
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   16)
                                        1 1
         14
                            1
                                      1 1 1
                                             111111
   17)
              *
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                                 1
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   18)
         16
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   19)
         12
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                _ _ _ _ _ _ _ _ _ _ _ _ _
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              *
                                                                *
              * 1
                               1
    20)
    * * * *
                                          * * * *
< Machine cells and Part families
Machine Cell[ 1] = \{ 2, 5, 10, 11, 13, 14, 20 \}
Machine Cell[ 1] = { 1, 4, 6, 7, 9, 16, 17 }
Machine Cell[ 3] = { 3, 12 }
Machine Cell[ 4] = { 8, 19 } --> Residual Communication  
Machine Cell[ 5] = { 15, 18 }
                                    --> Residual cell
Part Family[1] = { 2, 3, 4, 5, 10, 11, 13, 15, 17, 18, 19, 20 }
```

Problem(80) --> Data file name : DC_11_MosierTaube(1985b)_20x20.cfp

< Summary of the performance measures >

```
______
No. of machines
                                                    = 20
                                                   = 20
= 5
= 7
No. of part types
No. of cells
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                    = 111
Matrix density
                                                    = 0.278
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                    = 62
                                                    = 49
                                                    = 68
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                                    = 117
                                                   = 55.86 %
= 64.77 %
= 34.64 %
                                                    = 47.69 %
Machine utilization (MU)
No. of redundant machines (RMs)
                                                    = 3
_____
```

```
Machine Cell[ 2] = { 1, 3, 5, 6, 12, 13, 17 } Machine Cell[ 3] = { 2, 16 } Machine Cell[ 4] = { 18, 19 } --> Residual cell Machine Cell[ 5] = { 4, 8, 9, 11, 14, 15, 20 }
______
Part Family[ 1] = { 6, 7, 8, 9, 17 }
Part Family[ 2] = { 1, 2, 4, 10, 11, 15, 18, 20 }
Part Family[ 3] = { 5, 13, 14 }
Part Family[ 4] --> Empty Part family
Part Family[ 5] = { 3, 12, 16, 19, 21, 22, 23 }
< Summary of the performance measures >
_____
No. of machines
No. of part types
No. of cells
                                                                         = 20
                                                                         = 23
Machine cell size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                                         = 0.246
Total no. of within-block 1's
                                                                          = 71
No. of exceptional elements (EES)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                                         = 42
                                                                            50
                                                                         = 92
                                                                         = 62.83 %
                                                                         = 73.14 %
= 43.56 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                                         = 58.68 %
```

= 3

No. of redundant machines (RMs)

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32

18)

19)

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23)
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    24)
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                        1
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          22
26
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    27)
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                *
    28)
                        1
    29)
                *
          10
                *
    30)
                                        1
                                                       1 1 1 1
           12
                        1
    31)
          13
                *
                                                     1
                                                       1 1 1 1
                * 1
                                        1
    32)
           18
                                                     1
    33)
                *
           24
                  1
                        1
                                                       1 1 1 1
    34)
           27
                *
    35)
           31
                     1 1
                                                     1
                                                             1 1
======== * = = = = = = =
< Machine cells and Part families >
______
Machine Cell[ 1] = { 1, 3, 7, 8, 17 }
Machine Cell[ 2] = { 11, 12, 15, 16, 19 }
Machine Cell[ 3] = { 6, 10, 20 }
Machine Cell[ 4] = { 2, 4, 13, 14, 18 }
Machine Cell[ 5] = { 5, 9 } --> Residual Cell
Part Family[ 1] = { 1, 3, 5, 15, 17, 20, 23, 25, 29, 34, 35 } 

Part Family[ 2] = { 4, 6, 9, 11, 21, 28, 30, 32, 33 } 

Part Family[ 3] = { 8, 14, 16, 19, 22, 26 } 

Part Family[ 4] = { 2, 7, 10, 12, 13, 18, 24, 27, 31 }
       Family [ 5] --> Empty Part family
< Summary of the performance measures >
No. of machines
No. of part types
No. of cells
                                                          = 20
                                                          = 35
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                          = 0.213
Matrix density
Total no. of within-block 1's
                                                            112
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                          = 37
                                                             51
                                                             88
                                                            75.17 %
grouping efficiency (GE)
                                                          = 80.91 %
                                                          = 56.00 %
Grouping efficacy (GF)
Machine utilization (MU)
                                                          = 68.71 %
No. of redundant machines (RMs)
                                                          = 2
______
```

```
Problem(83) --> Data file name : DC_14_ChandraRaja(1989)_5_24x40.cfp
< Machines visited by parts: Process route numbers(PRN) >
                                21,
                          15,
Part[
                    13,
                                      22 }
Part
                                24 }
23,
15,
12,
          2]
3]
4]
                     3,
                          20,
             =
                          21,
                                      24 }
18 }
Part
             =
                    14,
                     8,
                          12,
Part
             =
                          8,
Part[
                                            18 }
                    9
17
         6]
7]
                          10 }
Part[
             =
Part
                     4,
          81
                          16 }
21 }
Part
             =
         9]
Part[
                     1,
                          6,
Part[
         10]
                     5,
                                11,
20 }
                                      21 }
             =
                          18,
Part
         11
             =
                     4,
                     3,
                                13,
                           5,
Part
         12
                                      20 }
             =
                                19,
                          11,
                                      23 }
Part[
         13]
                                5,
20 }
        14]
                           2,
                                                  19 }
                     1,
                                            15,
                                      14,
Partl
             =
                     3,
                          11,
Part
         15]
                                21,
17,
18 }
20 }
17 }
                          14,
                                      22 }
22 }
Part
        16]
                    13,
             =
                          13,
                     1,
Part[
         177
         18]
                     6,
                          12,
Part[
             =
                     4,
                          16,
Part
         19]
             =
        20]
                    10,
                          12,
Part
             =
Part[
         21]
                     4,
                          16<sup>'</sup>}
                           5,
                                11,
20 }
12 }
20 }
                     2,
        22]
Part[
             =
                                      12 }
                     3,
                          11,
Part[
        23]
             =
                     3,
7,
                          10,
Part
         24]
             =
                          14,
Part[
         25]
                           8,
                     6,
                                10,
                                      15,
19 }
         26]
                                            16 }
Part[
             =
                   12,
4 }
                          15,
Part
             =
                                18.
         281
Part
             =
Part
         291
                     9
                          17 }
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1 }
                     6,
                                18,
                                      22 }
Part[
         30]
             =
Part[
                    17,
        31]
                          20
             =
                           7,
2,
                                      23,
21 }
         32]
                     1,
                                16,
                                            24 }
Part
             =
                                9,
20 }
                     1,
         33]
Part[
                     3,
                           8,
         34]
Part[
             =
                                ī3,
                                      16,
19 }
Part[
         35]
36]
                     5,
2,
                          11,
                                            19 }
             =
                           5,
                                16,
Part
             =
Part[
         371
                    15,
                          16
                     4,
         38]
Part[
             =
                           6
Part[
                     8,
         391
                           9
             =
                           9,
         40]
                                19 }
Part[
             =
< Block Diagonal Solution Matrix >
               < Locations
                 0 0
                                                                     2
                 1
7
                                                      1
                                                           1
                                                              1
                                                                2
                                                                   2
                 Machines
                 0
                                                           0
                                                             0
                                                                0
                                                                  0
                                       1 0 0
7 2 5
* * *
                                                   2
                   1 0 2 0 2 0 1 0
2 3 0 1 1 4 6 9
* * * * * * * * *
                                                         1
                                                           2
                                                              0
                                                                0
                                                                   1
5
                                              1
                                                 1
                                                      2
                                                                     1
                                                                       0
                 1
                                                                          1
                                               1
                                                 9
                                                      4
                                                              6
                                                                8
                                                                     8
                                                                          4
< Parts >
                 0
         ====
          20
              * 1 1
                                       1
     1)
               *
     2)
                 1 1 1
(
          24
              *
                      =
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     3)
                      1
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          11
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          12
15
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                      1
                         1
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                                                         1
     5)
    6)
7)
               *
                      1
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                         1
               *
                                               \bar{1}
          23
                      1
                         1
     8)
          31
              *
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              *
          34
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     9)
                      1 1
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33

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15)
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              21
              28
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     16)
              37
                                                 1
                                                                                              1
                     *
     17)
              38
                                             1
                     *
    =======
                                                =
                     *
     18)
                        1
                                                    1
     19)
                     *
                                                        1
                     *
                                                    1
     20)
              29
                                                        1
                     *
              39
                                                    1
     21)
                                                                                          1
                                          1
                                                                                       1
     22)
              10
                                                              1 1
     23)
                     *
              13
                                                                  1 1
     24)
              14
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              22
35
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     27)
              36
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                3
                                          1
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     28)
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     29)
              32
                                                 1
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                1
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     30)
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     31)
              16
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     32)
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     35)
              18
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     36)
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     39)
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                                                                                                        1
              40
                                                                                                     1
< Machine cells and Part families
                                    10, 12
3, 20
1, 21
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
                                           12 }
                             =
                             =
                             =
Machine Cell[
Machine Cell[
Machine Cell[
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                                    4, 16
                                    9,
                        5]
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                                         17
                                   9, 1,
2, 5, 11,
23, 24 }
13, 22 }
6, 8, 15
7, 14 }
                        6]
                                               11, 19 }
                             =
                             =
Machine Cell[ 8]
Machine Cell[ 9]
Machine Cell[10]
                             =
                             =
                                               15, 18 }
                             =
          Family[
Family[
Family[
Family[
                                    20, 24 }
                        1]
2]
Part
                                    20, 24 }
2, 11, 12, 15, 23, 31, 34 }
9, 33 }
8, 19, 21, 28, 37, 38 }
6, 7, 29, 39 }
10, 13, 14, 22, 35, 36 }
3, 32 }
1, 16, 17 }
4, 5, 18, 26, 27, 30 }
Part
                             =
                        3]
Part
                             =
Part
                             =
          Family[ 5]
Family[ 6]
Family[ 7]
Family[ 8]
Family[ 9]
Part
                             =
Part
                             =
Part
                             =
Part
                             =
                                         5,
                                    4,
Part
                                              18, 26, 27, 30 }
                                    25,
                                          40 }
          Family[10]
Part
< Summary of the performance measures >
No. of machines
No. of part types
                                                                            = 24
                                                                            = 40
No. of cells
                                                                             = 10
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                                            = 131
                                                                            = 0.136
Matrix density
Total no. of within-block 1's
                                                                             = 80
No. of exceptional elements (EEs)
                                                                             = 51
```

*

*

```
No. of voids = 24
Sum of EEs and voids = 75
Group Cability Index (GCI) = 61.07 %
grouping efficiency (GE) = 85.48 %
Grouping efficacy (GF) = 51.61 %
Machine utilization (MU) = 76.92 %
No. of redundant machines (RMS) = 0
```

```
Problem(84) --> Data file name : DC_15_ChandraRaja(1989)_6_24x40.cfp
< Machines visited by parts: Process route numbers(PRN) >
                                21,
                          15,
Part[
                    13,
                                       22 }
Part[
                                24 }
24 }
18 }
          2]
3]
4]
                          20,
23,
                     3,
             =
                    21,
Part
             =
                          12,
                     8,
Part
             =
                           8,
                                 15,
                                       18 }
Part[
                    9
17
          6]
7]
                          10 }
Part[
             =
Part
                     4,
          81
                          16 }
Part
             =
                          10,
                                 19,
          9]
                     1,
Part[
                                       21 }
Part[
         10]
                     5,
                           6,
                                 11,
                                       21 }
20 }
             =
                          14,
                                 18,
Part
         11
             =
                     4,
                                  9,
                     3,
2,
                           5,
7,
                                       13,
23 }
Part
         12
                                             20,
                                                   23 }
             =
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Part[
         13]
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3,
                                15,
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         14]
                                       19 }
PartL
             =
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Part
         15]
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                     8,
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                                 14,
Part
         16]
                                       22 }
             =
                                 17
Part[
         17]
                     1,
                          13,
         18]
                     6,
                          12,
                                 18
Part[
             =
                          16,
                     1,
Part
         19
             =
                                 20
         20]
                    10,
                                 17
Part
             =
                          12,
Part[
         21]
                     4,
                          16<sup>'</sup>}
                     2,
                           5,
                                11,
20 }
12 }
20 }
         22]
Part[
             =
                                       12 }
                     3,
                          11,
Part[
         23]
             =
                     3,
7,
                          10,
         24]
Part
             =
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         25]
Part[
                           8,
         26]
27]
                     6,
                                10,
                                       15,
19 }
                                             16 }
Part[
             =
                          15,
7
17
                    12,
                                 18,
Part
             =
                     4
         28
Part
             =
Part
         291
                           8,
                                18,
20 }
                     6,
Part[
         30]
             =
                                       22 }
Part[
                          17,
         31]
                     1,
             =
         32]
                          16,
                                 23,
                                       24 }
21 }
24 }
Part
             =
                                9,
20,
19 }
                           2,
         33]
Part[
                     3,
                           8,
         34]
Part[
             =
Part[
         35]
36]
                     5,
2,
                          13,
             =
Part
             =
Part[
                    15,
                          16
             =
                     4,
         38]
                                  8
                           6,
Part[
             =
                           9,
Part[
                     8,
         391
                                 16
             =
                           9,
         40]
                                 19
Part[
             =
< Block Diagonal Solution Matrix >
               < Locations
                 0 0
                                                                    2
1
                                                                      2
                 1 1
3 4
                                                    1
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2, 11, 12, 15, 23, 25,
5, 26, 30, 37, 38, 39 }
7, 9, 17, 20, 29, 31 }
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         Family[10]
Part
< Summary of the performance measures >
No. of machines
No. of part types
                                                                      = 24
                                                                      = 40
No. of cells
                                                                      = 10
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                                      = 3
                                                                      = 131
                                                                      = 0.136
Matrix density
Total no. of within-block 1's
                                                                      = 73
No. of exceptional elements (EEs)
                                                                      = 58
```

*

```
No. of voids = 30
Sum of EEs and voids = 88
Group Cability Index (GCI) = 55.73 %
grouping efficiency (GE) = 82.05 %
Grouping efficacy (GF) = 45.34 %
Machine utilization (MU) = 70.87 %
No. of redundant machines (RMS) = 0
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13, 14, 27, 37, 40 }
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          Family[10]
Part
< Summary of the performance measures >
No. of machines
No. of part types
                                                                            = 24
                                                                            = 40
No. of cells
                                                                            = 10
Machine cell size
Total no. of 1's in the original MPIM :
                                                                            = 3
                                                                            = 131
                                                                            = 0.136
Matrix density
Total no. of within-block 1's
                                                                            = 70
No. of exceptional elements (EEs)
                                                                            = 61
```

*

```
No. of voids = 32
Sum of EEs and voids = 93
Group Cability Index (GCI) = 53.44 %
grouping efficiency (GE) = 80.76 %
Grouping efficacy (GF) = 42.94 %
Machine utilization (MU) = 68.63 %
No. of redundant machines (RMS) = 0
```

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< Machine cells and Part families >
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Machine Cell[ 1] = { 1, 2, 4, 5, 7, 8, 10, 13, 14, 16, 19, 22 } Machine Cell[ 2] = { 6, 11, 15, 17, 20, 21, 23, 24, 25, 26, 27 } Machine Cell[ 3] = { 3, 12 } --> Residual cell Machine Cell[ 4] = { 9, 18 } --> Residual cell
______
Part Family[1] = { 1, 2, 3, 4, 5, 7, 8, 9, 10, 12, 13, 14, 16, 18, 19, 22 } Part Family[2] = { 6, 11, 15, 17, 20, 21, 23, 24, 25, 26, 27 } Part Family[3] --> Empty Part family Part Family[4] --> Empty Part family
______
< Summary of the performance measures >
            _____
                                          = 27
No. of machines
No. of part types
No. of cells
                                           = 27
Machine cell size
Total no. of 1's in the original MPIM : |A| = 219
Matrix density
Total no. of within-block 1's No. of exceptional elements (EEs)
                                           = 46
No. of voids
                                           = 140
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                           = 186
                                           = 79.00 %
= 72.11 %
                                           = 48.19 %
Machine utilization (MU)
                                           = 55.27 %
No. of redundant machines (RMs)
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      35)
               11
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               32
      36)
      37)
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                       *
      38)
                 9
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      39)
               10
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1
               44
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      42)
               45
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               33
                                  1
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      43)
                      * 1
      44)
               34
                                                                                                                               1
                      * 1
                                                                                                                                  *
      45)
               35
                                                                                                                           1
                                                                                                                               1
      46)
               46
                       *
< Machine cells and Part families
                                      3, 4, 5, 18 }
1, 2 }
11, 12, 13, 24
8, 9, 10, 15 }
7, 27 }
21, 22 }
19 20 }
Machine Cell[ 1]
Machine Cell[ 2]
                               =
Machine Cell[ 3]
Machine Cell[ 4]
Machine Cell[ 5]
Machine Cell[ 6]
                               =
                                                     13, 24 }
                               =
                               =
                               =
Machine Cell[ 0] - { 21, 22 }

Machine Cell[ 7] = { 19, 20 }

Machine Cell[ 8] = { 23, 26 }

Machine Cell[ 9] = { 16, 17 }

Machine Cell[10] = { 14, 28 }

Machine Cell[11] = { 6, 25 }
                                                          --> Residual cell
                               ====
          Family[ 1]
Family[ 2]
Family[ 3]
Family[ 4]
Family[ 5]
Family[ 6]
Family[ 7]
Family[ 8]
                               = { 14, 17, 18, 19, 20, 21, 22, 23, 25, 28, 29, 30, 31, 37 }
= { 38 }
Part
Part
                              = { 36 }

= { 27, 39, 40, 41, 42, 43 }

= { 1, 2, 3, 4, 5, 6, 7, 12, 13, 15, 16, 24 }

= { 26 }

= { 11, 32 }

= { 8, 9, 10, 36 }

--> Empty Part family
Part
Part
Part
Part
Part
Part
```

```
______
No. of machines
                                              = 28
No. of part types
No. of cells
                                               = 46
                                               = 11
Machine cell size = 4
Total no. of 1's in the original MPIM : |A| = 211
Matrix density
                                               = 0.164
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                               = 115
= 96
                                               = 41
Sum of EEs and voids
                                               = 137
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                               = 54.50 %
                                              = 82.62 %
= 45.63 %
Machine utilization (MU)
                                              = 73.72 %
No. of redundant machines (RMs)
                                              = 3
______
```

```
< Machines visited by parts: Process route numbers(PRN) >
                                           _____
                         19,
Part[
                               20,
                                     29,
                                           30 }
Part[
         2]
3]
4]
                   10,
                         23 }
             =
                    9,
                         19,
Part
             =
                               20,
                                     29,
                                           30 }
                   14,
5,
                         25
14
Part
            =
Part[
         6]
7]
                    6
PartL
                         16
             =
                         17
27,
Part
                    4,
         81
                    8,
                               28 }
Part
             =
                         29'}
                    8,
Part[
         9]
                        25
11,
12 }
Part[
        10]
                    1,
2,
2,
9,
                                     22 }
                               21,
             =
                         12
3
Part
        11
             =
                                           21, 22, 23 }
Part
        12]
                               10,
                                     12,
             =
                         29
Part[
        13]
                    8,
        14]
                         18
PartL
             =
                         27 }
17,
15 }
                    4,
Part
        15]
        16]
Part
                               18,
                                     26 }
             =
Part[
        17]
                   2,
12 }
        18]
                         12,
                               13,
                                     14 }
Part[
             =
Part
        19]
             =
        20]
                   10
Part
            =
                               20,
Part
        21]
                    9
                         19,
                                     29,
                                           30 }
        22]
                   19,
                         20,
Part[
            =
                        10,
Part[
        23]
24]
                    3,
                               12,
                                     22,
                                           23 }
             =
                    4,
                         12
Part
            =
        25]
                         13
Part[
                         14 }
17,
16 }
        26]
27]
                    6,
7,
Part[
             =
                               18,
Part
             =
                                     26 }
                    4,
                         16
        281
Part
            =
Part
        291
                    8,
                         28
                   19,
                         29
Part[
        30]
            =
Part[
                    1,
                         3,
                               21,
                                     22,
                                           23 }
22 }
        31]
             =
                                     21,
21 }
        32 🗍
                    1,
                          2,
                                3,
Part[
            =
                          2,
                    1,
                               11,
        33]
                       2,
7,
28 }
7,
15
Part[
                    5,
        34]
                                     26 }
Part[
             =
                               18,
Part[
        35]
36]
                    4,
            =
                    5,
                               17,
                                     26 }
Part
            =
Part[
        371
                   14,
        38]
        38] = {
39] = {
40] = {
41] = {
                   13,
Part[
                                3,
                         2,
Part[
                    1,
                                     10, 11, 12, 22, 23 }
22 }
                               21,
11 }
                    3,
                         12,
Part[
                         2,
Part[
                                   _____
< Block Diagonal Solution Matrix >
              < Locations >
                                                                       \begin{smallmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 2 & 2 & 2 & 2 & 2 & 2 & 3 \end{smallmatrix}
                0
2
1
                                                                  0
2
2
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2
3
                1 5
                                                    1 1
6 7
                                                              2
                                                                          2 5
                                                                               2
                                                         1
                                                           1
                                                         8
                                                              ō
              < Machines >
                                                                         0
2
1
                0
2
6
                                                                0 2 3
                                                              0
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                                                                     0
                                                                       0
                                                                            0
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                                                              10
                  1 2 *
                     0 2 0 1 0 2 0 1
9 9 5 5 8 8 6 6
* * * * * * * * *
                                     1 1
6 3
                                             1 2 3 0 1
9 0 0 7 7
                                                         18
                                                                   0
1
                                                                     0
                                                                       1
1
                                                                            2
                                                                                 2
7
                                                                                      2 5
                                           2
                                                                               0
                                                                                   1
                                          4
                                                                               4
                2
< Parts >
              *
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==
              *
                1
     1)
         11
                   1
(((
    2)
3)
              *
                1
                  1
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         18
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              *
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                   1
              *
     4)
         24
                   1
             * = = = = = = = = = = = = =
          9
              *
                               1
     5)
                       1
                     1 1
         13
    6)
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         17
              *
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    8)
          8
              *
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    9)
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                               1
                                                         1
   10)
         14
         29
              *
                               1 1
                                                                                        *
   11)
```

Problem(88) --> Data file name : DC_19_KumarVannelli(1987)_30x41.cfp

```
(
      12)
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               35
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                                                      1
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      13)
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      14)
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      16)
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      18)
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      19)
                                    1
              21
22
      20)
                      *
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                      *
      21)
                                                                    1
      22)
               30
                      *
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1
                      *
      23)
                7
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                      *
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      24)
               16
      25)
                      *
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               27
                      *
               34
      26)
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                      *
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      27)
               36
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                     *
      28)
                2
                      *
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      29)
                      *
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      30)
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      31)
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      32)
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      33)
                      *
               31
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               33
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                      *
      36)
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      37)
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                     * 1
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      38)
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      39)
              15
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========
                     *
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      40)
               37
      41)
                     ^{*} ^{1}
< Machine cells and Part families >
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
                             = {
= {
= {
                                     2, 12
                                     9,
                                           29
                                     5, 15
Machine Cell[ 3] = { 5, 15 }
Machine Cell[ 4] = { 8, 28 }
Machine Cell[ 5] = { 6, 16 }
Machine Cell[ 6] = { 13, 24 }
Machine Cell[ 7] = { 19, 20, 30 }
Machine Cell[ 8] = { 7, 17, 18, 26 }
Machine Cell[ 9] = { 10, 23 }
Machine Cell[10] = { 1, 3, 11, 21, 22 }
Machine Cell[11] = { 4, 27 }
Machine Cell[12] = { 14, 25 }
                             = { 11, 18, 19, 24 }
= { 9, 13 }
= { 5, 17 }
= { 8, 14, 29, 35 }
= { 6, 26, 28 }
= { 25, 38 }
= { 1, 3, 21, 22, 30 }
= { 7, 16, 27, 34, 36 }
= { 2, 20, 23 }
= { 10, 12, 31, 32, 33, 39, 40, 41 }
= { 15 }
= { 4, 37 }
_____
          Family[ 1]
Family[ 2]
Family[ 3]
Family[ 4]
Family[ 5]
Family[ 6]
Family[ 7]
Family[ 8]
Family[ 9]
Family[10]
Part
           Family[11] =
Part
           Family[12]
Part
```

```
No. of machines
                                                                             = 30
No. of part types
No. of cells
Machine cell size
                                                                             = 41
= 12
= 5
Total no. of 1's in the original MPIM : |A| = 128
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                                             = 0.104
= 90
                                                                             = 38
                                                                             = 31
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                                                             = 69
                                                                             = 70.31 %
= 85.48 %
= 56.60 %
Machine utilization (MU)
                                                                             = 74.38 %
No. of redundant machines (RMs)
                                                                             = 0
```

```
Problem(89) --> Data file name : DC_20_Stanfel(1985)_Figure_5_30x50.cfp
< Machines visited by parts: Process route numbers(PRN) >
Part[
                                          11,
                                                13 }
Part[
                                    9 }
12 }
11 }
13 }
                    2,
2,
3,
         2]
3]
4]
                          3,
                                5
            =
                          5,
7,
Part
            =
                                9
                               10,
Part
            =
                    1,
                          6,
                                8,
Part[
                               9,
                                    10,
         6]
7]
                    1,
                          3,
                                          13 }
PartL
            =
                              8,
12,}
7,
                          5,
                    4,
                                    10,
                                                12 }
Part
                                          11,
                    1,
2,
                          3,
         81
Part
            =
                          6,
                                    10,
Part[
         9]
                                          13 }
Part[
        10]
                    5,
                         10
            =
                    3,
7,
6,
Part
        11
            =
                          5
                               10 }
                          8
        12]
Part
            =
                         7,
                                8
Part[
        13]
                          8,
        14]
                    6,
                               12
Partl
            =
                    6,
                          8,
                               12
Part
        15]
                          8,
                               1\bar{2}
Part
        16]
                    6,
            =
                    2,
                         9,
Part[
        17]
                              13
                         4,
        18]
                    1,
                              10,
                                    11 }
            =
Part[
                         16'}
                   14,
Part
        19]
            =
        20]
                   14,
                         15,
                              17 }
Part
            =
                   14,
Part
        21]
                         16
                   15,
        22]
                         16
Part[
            =
        23]
24]
                   14,
Part[
                         16
                              17 }
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                           '}
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15,
                   15,
Part
            =
                   14,
        25]
Part[
                               17 }
        26]
27]
                   14,
                         16
Part[
            =
                   15,
Part
            =
                         16
                         <u>1</u>9,
        281
                   18
                               20
Part
            =
Part
        291
                   19,
                         20,
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                   18,
                         21,
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Part[
        30]
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        32 🗍
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        33]
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Part[
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21
22
                   18,
                         19,
        34]
Part[
            =
Part[
        35]
36]
                   20,
                         22,
20,
            =
                   18,
Part
            =
                         20,
Part
        37
                   18
            =
                              23
29
                   19,
        38]
Part[
            =
                         21,
        39]
                   24,
                         28,
Part[
                                    30 }
            =
                   27,
25,
        40]
                         29,
                               30
Part[
            =
                         27,
        41]
                               29
Part[
            =
                        25,
28 }
27,
28,
        42]
                   24,
                               30
Part[
            =
        43]
44]
Part[
            =
                   26
                   24,
25,
                              30 }
29 }
Part
            =
        451
Part
            =
                   26,
27,
                         30
        46]
Part[
            =
Part[
        471
                         28
            =
                         29,
        48]
                   24,
                               30
Part[
            =
                   25,
                         26,
        491
                               27 }
Part「
            =
                         29'}
        50] = {
                   25,
Part[
______
< Block Diagonal Solution Matrix >
              < Locations
                0 0
                                                             2
                                                                2
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7
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                                                        18
                  0 0 0 0 0 0 0
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                                               1
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                                               4
                     3 4 5 6
                                 8 9 0
                1
                  2
              < Machines
                  0
1
1
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2
0
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2
4
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2
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5
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2
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5
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7
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                0
< Parts >
                6
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1 *

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1

1

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*

*

12 13

14

15

1) 2) 3)

4)

5)

1 1

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1 1 1 1

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      6)
             16
                   * 1 1 1
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      7)
             19
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((((
             21
22
      8)
                                 1
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                   *
      9)
                                    1
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1
             23
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    10)
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    11)
             26
                                 1
    ====
            ===
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             29
                   *
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     12)
             31
                   *
    13)
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1
1
             33
    14)
                   *
    15)
             38
                   *
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1 1
16)
             40
                   *
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     17)
             41
                                                 \frac{1}{1}
    18)
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             45
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     19)
             49
                   *
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    20)
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    21)
22)
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    23)
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    25)
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             43
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     27)
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                   *
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    28)
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    29)
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7
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             18
    31)
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     32)
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             32
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             34
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             35
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     36)
    37)
38)
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1
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                   *
             36
             37
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             39
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    40)
             42
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    41)
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3
17
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    43)
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45)
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     46)
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    47)
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             25
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    48)
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    49)
             27
                                                                                                                           *
                                                                                                                    1
     50)
                         * * * *
```

< Machine cells and Part families >

```
Machine Cell[ 1] = { 6, 8, 12 }
Machine Cell[ 2] = { 14, 16 }
Machine Cell[ 3] = { 19, 21, 23 }
Machine Cell[ 4] = { 25, 27, 29 }
Machine Cell[ 5] = { 1, 3, 10 }
Machine Cell[ 6] = { 26, 28 }
Machine Cell[ 7] = { 4, 5, 11 }
Machine Cell[ 8] = { 18, 20, 22 }
Machine Cell[ 9] = { 24, 30 }
Machine Cell[10] = { 2, 9 }
Machine Cell[11] = { 15, 17 }
```

```
Machine Cell[12] = \{ 7, 13 \}
Part Family[ 1] = { 5, 12, 13, 14, 15, 16 }

Part Family[ 2] = { 19, 21, 22, 23, 26 }

Part Family[ 3] = { 29, 31, 33, 38 }

Part Family[ 4] = { 40, 41, 45, 49, 50 }

Part Family[ 5] = { 4, 6, 8, 10, 11 }

Part Family[ 6] = { 43, 46, 47 }

Part Family[ 7] = { 1, 7, 18 }

Part Family[ 8] = { 28, 30, 32, 34, 35, 36, 37 }

Part Family[ 9] = { 39, 42, 44, 48 }

Part Family[10] = { 2, 3, 17 }

Part Family[11] = { 20, 24, 25, 27 }

Part Family[12] = { 9 }
                                                                    _____
_____
< Summary of the performance measures >
______
No. of machines
No. of part types
No. of cells
                                                                                    = 30
                                                                                    = 50
                                                                                    = 12
Machine cell size = 5
Total no. of 1's in the original MPIM : |A| = 154
= 0.10
Matrix density
                                                                                    = 0.103
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
                                                                                    = 49
                                                                                    = 25
                                                                                    = 74
```

No. of redundant machines (RMs) ______

grouping efficiency (GE) Grouping efficacy (GF) Machine utilization (MU)

= 68.18 %

= 88.60 % = 58.66 % = 80.77 %

```
Problem(90) --> Data file name : DC_21_Stanfel(1985)_Figure_6_30x50.cfp
< Machines visited by parts: Process route numbers(PRN) >
                          8,
                               19,
Part[
                    3,
                                     25 }
Part
                               10,
13 }
25 }
         2]
3]
4]
                    5,
                          6,
                                     13 }
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23 }
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                   17,
                         18,
Part[
                                     21 }
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Part
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```

< Machine cells and Part families >

```
Machine Cell[ 1] = { 5, 13 }
Machine Cell[ 2] = { 10, 19 }
Machine Cell[ 3] = { 23, 26 }
Machine Cell[ 4] = { 7, 17, 18, 20, 21 }
Machine Cell[ 5] = { 12, 29 }
Machine Cell[ 6] = { 16, 30 }
Machine Cell[ 7] = { 22, 24, 27 }
Machine Cell[ 8] = { 3, 8, 25 }
Machine Cell[ 9] = { 1, 9, 11 }
Machine Cell[ 10] = { 2, 4, 6, 14 }
Machine Cell[ 11] = { 15, 28 }
```

```
Part Family[ 1] = { 2, 3, 11 }
Part Family[ 2] = { 37, 46, 47, 50 }
Part Family[ 3] = { 31, 34 }
Part Family[ 4] = { 5, 6, 7, 12, 26, 27, 28, 29, 30 }
Part Family[ 5] = { 23, 24, 25, 44 }
Part Family[ 6] = { 35, 39 }
Part Family[ 7] = { 13, 15 }
Part Family[ 8] = { 1, 4, 16, 33, 42, 45 }
Part Family[ 9] = { 8, 9, 21, 36, 41, 43, 49 }
Part Family[10] = { 17, 19, 20, 22, 32, 38, 48 }
Part Family[11] = { 10, 14, 18, 40 }
 ______
< Summary of the performance measures >
 ______
```

```
No. of machines
                                                      = 30
No. of part types No. of cells
                                                       = 50
                                                       = 11
Machine cell size = 5
Total no. of 1's in the original MPIM : |A| = 167
Matrix density
                                                       = 0.111
Total no. of within-block 1's
                                                       = 101
No. of exceptional elements (EEs)
No. of voids
                                                       = 66
                                                       = 55
Sum of EEs and voids
                                                       = 121
Group Cability Index (GCI)
                                                       = 60.48 %
grouping efficiency (GE)
Grouping efficacy (GF)
                                                      = 79.92 %
= 45.50 %
Machine utilization (MU)
                                                       = 64.74 %
No. of redundant machines (RMs)
                                                       = 0
```

< Machines visited by parts: Process route numbers(PRN) >

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28 }
Part[
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                      20, 26 }
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    34)
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    35)
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    41)
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36
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    43)
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72
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    60)
            74
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            75
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    62)
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    63)
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64)
            14
                  *
            32
47
    65)
                  *
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    66)
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                  *
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            53
    67)
                  *
    68)
            66
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                  *
    69)
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                  *
    70)
            82
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            70
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    72)
            18
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73)
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    74)
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            24
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    76)
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            45
48
59
67
    77)
78)
79)
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1
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    80)
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    81)
82)
83)
            71
81
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            83
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    84)
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35
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    85)
    86)
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            78
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    87)
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1
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1
            ===
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                                     1
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(
            86
    88)
            ===
            34
(
    89)
                                                                                                                   1
(
    90)
            26
                  * * *
```

```
Machine Cell[ 4] = { 13, 29 }
Machine Cell[ 5] = { 2, 14 }
Machine Cell[ 6] = { 10, 23 }
Machine Cell[ 7] = { 3, 15, 22, 30 }
Machine Cell[ 8] = { 6, 20 }
Machine Cell[ 9] = { 12, 16 }
Machine Cell[10] = { 1, 9 }
Machine Cell[11] = { 5, 18 }
                                                              _____
Part Family[ 1] = { 8, 15, 21, 22, 30, 40, 51, 52, 56, 62, 63, 64, 65, 68, 73, 76, 77, 79, 87, 88, 89, 90 } Part Family[ 2] = { 1, 2, 3, 4, 5, 6, 7, 10, 11, 12, 13, 16, 19, 23, 25, 27, 28, 29, 31, 33, 36, 37, 38, 41, 42, 43, 46, 49, 50, 54, 55, 57, 58, 60, 61, 69, 72, 74, 75, 84 }
28, 29, 31, 33, 36, 37, 38, 41, 42, 43, 46, 49, 50, 54, 55, 57, 58, 67, 72, 74, 75, 84 }

Part Family[ 3] = { 39 }

Part Family[ 4] = { 14, 32, 47, 53, 66, 80, 82 }

Part Family[ 5] = { 70 }

Part Family[ 6] = { 18 }

Part Family[ 7] = { 9, 20, 24, 44, 45, 48, 59, 67, 71, 81, 83, 85 }

Part Family[ 8] = { 17, 35, 78 }

Part Family[ 9] = { 86 }

Part Family[10] = { 34 }

Part Family[11] = { 26 }
______
< Summary of the performance measures >
_____
No. of machines
                                                                               = 30
No. of part types No. of cells
                                                                                      = 90
                                                                                      = 11
Machine cell size = 6
Total no. of 1's in the original MPIM : |A| = 302
Matrix density
Total no. of within-block 1's
                                                                                      = 192
No. of exceptional elements (EEs)
No. of voids
                                                                                      = 110
                                                                                      = 198
Sum of EEs and voids
                                                                                       = 308
Group Cability Index (GCI)
                                                                                      = 63.58 %
= 72.23 %
= 38.40 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                                                      = 49.23 %
No. of redundant machines (RMs)
                                                                                      = 5
```

```
< Machines visited by parts: Process route numbers(PRN) >
                                  8,
Part[
Part[
                                        4,
                     1,
          2]
3]
4]
                           2,
                                  6,
                                                    7 }
9 }
Part[
+[
                                       7,
9 }
                                  4,
                                              8,
                     1,
                           4,
                                        9
7,
Part
                                              9 }
9 }
Part[
                           6,
                                10,
                                 7,
          6]
7]
8]
                                        8,
9 }
Part[
             = {
= {
= {
                     6,
                          10,
Part[
Part[
                           4,
                                  8,
                                  2,
6,
                     3,
3,
                           5,
                                        6,
                                                    8,
9<sup>'</sup>}
                                                           9 }
                                              8,
Part[
          9]
                         5,
6,
12,}
7,
Part[
         10]
                     3,
             =
Part[
Part[
         11
                     6,
                                12 }
7,
10 }
        12]
                    11,
             =
Part[
                    11,
                          10,
7,
                                       12 }
         13]
        14]
15]
16]
                    11,
Part[
             =
                          10'}
12',
7',
7',
7'}
Part[
Part[
                    11,
        15] = {
16] = {
17] = {
                    11,
                                12 }
10 }
                    11,
Part[
        18] = {
19] = {
Part[
Part[
                     6,
                    10,
______
< Block Diagonal Solution Matrix >
               < Locations >
                 0 0 0 0 0 0 0 0 0 0 0
                 0 0 0 0 0 0 0 0 0 1 1 1
                 1 2 3 4 5 6 7 8 9 0 1 2
               < Machines
                 0 0 0 0 0 0 0 0 0 0 0 0
                 0 0 0 0 0 0 0 1 1 1 0 0
                 1 4 6 8 9 3 7 0 1 2 2 5
< Parts >
              * *
               * 1 1
                         1 1
* 1 1 1 1
                                                *
               * 1 1
           3
                         1 1
                                1
     3)
              * 1 1
                           \overline{1}
                                                *
                                1
               * 1
           5
                      1
                                1 1
                   \begin{array}{c} \bar{1} \ 1 \ \bar{1} \\ 1 \ 1 \ 1 \ 1 \end{array}
               *
                                                *
           6
                   8)
              *
                                          1 1
     9)
           9
              *
                                                *
   10)
          10
                   1 1 1 1
         ==== * = = = = = = = = =
   11)
          11
               *
                                        1
   12)
13)
                                        1
          13
               *
                                1 1 1 1
                                                *
               *
   14)
          14
                                1 1 1
   15)
          15
               *
                                   1 1
   16)
          16
                                     1 1
               *
    17)
          17
    18)
          18
                                1 1
                      1
          19
              *
                                1 1
   19)
< Machine cells and Part families >
Machine Cell[ 1] = { 1, 4, 6, 8, 9 }
Machine Cell[ 2] = { 3, 7, 10, 11, 12 }
Machine Cell[ 3] = { 2, 5 } --> Residual cell
                          _____
Part Family[ 1] = { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 }
Part Family[ 2] = { 11, 12, 13, 14, 15, 16, 17, 18, 19 }
Part Family[ 3] --> Empty Part family
< Summary of the performance measures >
______
```

Problem(92) --> Data file name : DC_23_DeWitte(1980)_12x19.cfp

```
No. of machines = 12
No. of part types = 19
No. of cells = 3
Machine cell size = 5
Total no. of 1's in the original MPIM : |A| = 75
Matrix density = 0.329
Total no. of within-block 1's = 58
No. of exceptional elements (EEs) = 17
No. of voids = 37
Sum of EEs and voids = 54
Group Cability Index (GCI) = 77.33 %
grouping efficiency (GE) = 74.14 %
Grouping efficacy (GF) = 51.79 %
Machine utilization (MU) = 61.05 %
No. of redundant machines (RMs) = 3
```

```
< Machines visited by parts: Process route numbers(PRN) >
                                                12 }
Part[
Part[
           2]
3]
4]
                      5,
                             9,
                                  10,
                                         13,
14,}
                                                15
              =
                                   6,
Part
                       1,
                             3,
                             4,
                                         ī3,
                                               14 }
15 }
12 }
                                    6,
Part
              =
                                         ī3,
                             9,
                       8,
                                  10,
Part[
          6]
                                   7,
                      2,
2,
                             6,
                                         11,
12,}
PartL
              =
Part[
Part[
                             6,
                                   4,
                             3,
                                          6,
           81
                      1,
                                                11,
                                                      14 }
              =
                                    6,
Part[
           91
                                         14
                      8,
                             9,
                                  10,
                                         13,
         10] = {
                                                15 }
Part[
< Block Diagonal Solution Matrix >
                < Locations > 0 0 0 0 0 0 0 0 0 0 0 0 0
                                               1 1
2 3
                   0 0 0 0 0 0 0 0 0 1 1
                   1 2 3 4 5 6 7 8 9 0 1
                < Machines
                   0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
                     0 0 0 1 0 0 0 1 1
                                             1 0 0
                                                     1
                                                       1
< Parts >
                     3 4 6 4 5 8 9 0 3 5
========
                *
                  1
                     1
                          1
(
                * 1
                        1 1 1
     2)
            4
                                          1
                * 1 1 1 1 1
                                                          *
     3)
            8
            9
                *
                     1 1 1 1
     4)
                *
                     = = = =
                *
                                     1 1 1 1
            2
                                1
                *
     6)
                                  1 1 1 1 1
(
          10
                                  1 1 1 1 1
     8)
            1
                          1
                                                1 1
                                                     1
                *
     9)
                          1
                                                1
                                                  1
                                                     1 1
            6
    10)
               * 1
*****
< Machine cells and Part families >
                          1,
Machine Cell[ 1] = { 1, 3, 4, 6, 14 }
Machine Cell[ 2] = { 5, 8, 9, 10, 13, 15 }
Machine Cell[ 3] = { 2, 7, 11, 12 }
       Family[ 1] = { 3, Family[ 2] = { 2, Family[ 3] = { 1,
Part
Part
Part
< Summary of the performance measures >
No. of machines
                                                          = 15
No. of part types
No. of cells
                                                          =
                                                            10
                                                             3
                                                          =
Machine cell size
                                                            6
Total no. of 1's in the original MPIM : |A|
                                                            48
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
                                                             0.32
                                                             43
                                                             5
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                             12
                                                             89.58 %
                                                            90.50
Grouping efficacy (GF)
                                                          = 78.18 %
Machine utilization (MU)
                                                          = 86.00 %
```

= 0

No. of redundant machines (RMs)

Problem(93) --> Data file name : DC_24_ChanMilner(1982)_Figure_3a_15x10.cfp

```
< Machines visited by parts: Process route numbers(PRN) >
                                        10 }
10 }
10 }
Part[
Part[
                            4,
                                   5,
          2]
3]
4]
                      1,
              =
                            4,
                                  5,
11 }
                      1,
7,
2,
Part
              =
                            9,
Part
              =
                                   6,
                                          8,
Part[
                                               10 }
          6]
7]
                      3,
5,
2,
                                   8
Part[
              =
                           10 }
Part
          81
                                  10 }
Part
                            6,
              =
                            8,
                                        11 }
Part[
          9]
                                   9,
         10]
                      8
                           11 }
Part[
              =
Part
         11
              =
                      1,
                             2
                                        10 }
                      2,
3,
7,
                                         8,
                             3
                                   6,
         12]
                                               10 }
Part
              =
                               }
Part[
         13]
                             8
                            8,
                                   9 }
         14]
PartL
              =
                                        10 }
10 }
11 }
                            4,
                                   5,
5,
Part
         15]
                      1,
7,
                            4,
         16]
Part
              =
                                   9,
                            8,
Part[
         17]
                                   9,
         18]
                            8,
                                        10,
Part[
              =
                                               11 }
                                   6,
         19
Part
              =
                             3,
                      1,
         20]
                                   5
Part
              =
Part[
                            4,
         21]
                                   5
                                   5 }
Part[
         22]
                      1,
< Block Diagonal Solution Matrix >
                < Locations
                  Locations > 0 0 0 0 0 0 0 0 0
                  0 0 0 0 0 0 0 0 0 1
                                            1
                  1 2 3 4 5 6 7 8 9 0 1
                < Machines
                  0 0 0 0 0 0 0 0 0 0 0
                  0
                    0
                       0
                          1 0 0 0 1 0 0 0
                       5 0 7 8 9 1 2
< Parts >
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          11
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     5)
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                  1
                    1 1 1
          15
               * 1 1 1 1
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22
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            9
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    14)
          10
                               1
                *
                                               *
          13
                               1
                                          1
    15)
          14
17
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                                  1
                *
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    16)
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    17)
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    18)
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                                               *
                                            1
    20)
            8
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                                       1
                *
                                         1 1
                                               *
    21)
          12
                               1
                                       1
                          1
               *
                               1
                                       1
          19
                                          1
    22)
               * * * * * *
                                 * *
< Machine cells and Part families >
Machine Cell[ 1] = { 1, 4, 5, 10 }
Machine Cell[ 2] = { 7, 8, 9, 11 }
Machine Cell[ 3] = { 2, 3, 6 }
                               4,
Part Family[1] = { 1, 2, 3, 7, 11, 15, 16, 20, 21, 22 }
```

Problem(94) --> Data file name : DC_25_Seifoddini(1989)_11x22.cfp

```
Part Family[2] = { 4, 6, 9, 10, 13, 14, 17, 18 }
Part Family[3] = { 5, 8, 12, 19 }
```

```
_____
No. of machines
No. of part types
No. of cells
                                                         = 11
= 22
= 3
Machine cell size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                         = 4
                                                         = 78
                                                          = 0.322
Total no. of within-block 1's
                                                          = 68
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
arouning officiency (GCI)
                                                         = 10
                                                           16
                                                         = 26
                                                         = 87.18 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                         = 87.31 %
= 72.34 %
                                                         = 80.95 %
No. of redundant machines (RMs)
_____
```

```
______
No. of machines
No. of part types
No. of cells
                                               = 20
= 20
                                               = 4
= 7
Machine cell size
Total no. of 1's in the original MPIM : |A|
Matrix density
Total no. of within-block 1's
                                                = 0.198
                                               = 68
No. of exceptional elements (EEs)
                                                = 11
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                               = 40
                                                 51
                                               = 86.08 %
                                               = 79.60 %
                                               = 57.14 %
Grouping efficacy (GF)
Machine utilization (MU)
No. of redundant machines (RMs)
                                               = 62.96 %
                                               = 0
_____
```

```
Part[
                      10,
                             14 }
Part
                              4,
           2]
3]
                                   15,
13,
                                          16,
14 }
15 }
                       1,
              =
                                                 17 }
                             10,
Part
                       3,
                                   Ī4,
                       5,
                              6,
Part
              =
                                          15,
9 }
                                     4,
                              3,
Part[
                       1,
                                                 17 }
                                    4,
           6]
7]
                              3,
                       1,
Part[
              =
                             10,
                                   11'}
Part
                       9
                       3,
3,
                                          15,
                              4,
                                                 17 }
17 }
Part
           81
                              4,
                                          15,
Part[
           91
                       3,
2,
                              8,
         10]
                                     9,
                                                 11,
                                          10,
                                                        12,
                                                               14,
                                                                      15 }
Part[
              =
                             15'}
Part
         11
              =
                              4,
                                   15,
                       1,
         12
                                                 17 }
Part
                                          16,
              =
                       4,
7,
                              9,
                                   10,
Part[
         13]
                                          11 }
         14]
                              9
Part
                                }
              =
                                   10,
Part
         15
                       3
2
3
                              4
                                          15,
                                                 17 }
         16]
                             15
Part
              =
                             4,
                                   10
11,
16 }
                                   10,
                                          15,
18 }
Part
                                                 17 }
                       9
7
                            10,
         18]
Part[
              =
                              9,
Part
         19
              =
         20]
                       2,
                             14,
Part
              =
Part[
                       9
                             11,
                                    18 }
                              7,
                                    9,
                       4,
                                          11
PartL
         22]
              =
Part[
                       3,
         23]
                              8,
                                     9
                                          15
              =
                       3,
                                   14,
         24]
Partl
                             13,
```

```
< Block Diagonal Solution Matrix >
```

< Locations

```
\begin{smallmatrix}0&0&0&0&0&0&0&0&0&1&1&1&1&1&1&1\\1&2&3&4&5&6&7&8&9&0&1&2&3&4&5&6\end{smallmatrix}
               Machines
                1 0
7 6
* *
                                                08
                    1 1 0 0 0 0 1
1 8 1 2 3 4 0
* * * * * * *
                                    1 1
4 5
                                             1
2
*
                0
                                                  1
                  0
                        1 2
                    1 8
                                                  6
< Parts >
             *
                  1 1
                                  1
                                                         *
*
                                1 1
    2)
         13
                  1 1
                                                         *
    3)
             * 1 1
         14
    4)
         18
                  1 1 1
                                  1
             * 1 1
                                                         *
         19
                                                  1
             *
                                                         *
         21
                  1 1 1
    6)
    7)
         22
             *
                1 1 1
                                1
               = = = =
             *
                                  1 1
                                                         *
    8)
    9)
                         1
                                1
                                       1 1
                                                  1
   10)
             *
                                  1
                                    1
                                                       1
                                                         *
                              1
          4
                                    1
                                       1
                                                     1
   11)
                                           1
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   12)
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   16)
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   18)
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   20)
         16
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                              1 1 1
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   21)
         17
   22)
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   23)
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```

< Machine cells and Part families >

```
-----
Machine Cell[ 1] = { 7, 9, 11, 18 }
Machine Cell[ 2] = { 1, 2, 3, 4, 10, 14, 15, 17 }
Machine Cell[ 3] = { 6, 12 } --> Residual cell
Machine Cell[ 4] = { 8, 16 } --> Residual cell
Machine Cell[ 5] = { 5, 13 } --> Residual cell
______
Part Family[ 1] = \{ 7, 13, 14, 18, 19, 21, 22 \}
Part Family[ 2] = \{ 1, 2, 3, 4, 5, 6, 8, 9, 10, 11, 12, 15, 16, 17, 20, 23, 24 \}
Part Family[3] --> Empty Part family Part Family[4] --> Empty Part family Part Family[5] --> Empty Part family
_____
< Summary of the performance measures >
______
No. of machines
                                                        = 18
No. of part types No. of cells
                                                        = 24
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                        = 95
Matrix density
Total no. of within-block 1's
                                                        = 73
No. of exceptional elements (EEs)
                                                        = 22
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                        = 91
                                                        = 113
                                                        = 76.84 %
                                                        = 68.15 %
                                                        = 39.25 %
Grouping efficacy (GF)
Machine utilization (MU)
                                                        = 44.51 %
No. of redundant machines (RMs)
                                                        = 6
```

```
< Machines visited by parts: Process route numbers(PRN) >
                             8 }
Part[
Part[
                      9,
           2]
3]
4]
                            10,
                                   11 }
12 }
              =
                            10
11,
8 }
                      9,
Part
              =
                       4,
Part
              =
Part[
                      11
          6]
7]
                       1,
2,
Part[
                             6 }
              =
                                   12 }
                             9,
Part
                             Ž,
           81
Part
                                           6 }
              =
                            11,
                     10,
Part[
          9]
Part[
         10]
                            11 }
                     10,
              =
                             9,
Part
         11
                                    5
Part
         12]
                       1,
                             3
              =
                                   6,
10 }
10 }
11 }
                             4,
Part[
                       3,
                                           8 }
         13]
         14]
                       4,
                             8,
PartL
              =
Part[
         15]
16]
                       5,
                             6,
                             5,
Part
              =
                            10,
Part[
         171
Part[
Part[
                       1,
                            5,
12,}
                                           7 }
         187
                                    6,
              =
                       9,
         197
< Block Diagonal Solution Matrix >
                < Locations >
                   0 0 0 0 0 0 0 0 0 0 0 0
                   0 0 0 0 0 0 0 0 0 1 1 1
                   1 2 3 4 5 6 7 8 9 0 1 2
                < Machines
                   0 0 0 0 0 0 0 0 0 0 0 0
                     0 0 1 1 1 0 0 0 0 0 0
                     8 9 0 1 2 1 5 6
                   4
                                          7
< Parts >
                * *
                *
     1)
            1
                  1
                     1
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     2)
            4
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           13
                * 1 1
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     3)
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           14
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                                     =
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< Machine cells and Part families >
Machine Cell[ 1] = { 4, 8 }
Machine Cell[ 2] = { 9, 10, 11, 12 }
Machine Cell[ 3] = { 1, 5, 6, 7 }
Machine Cell[ 4] = { 2, 3 } --> Residual cell
      Family[ 1] = { 1, 4, 13, 14, 16 }

Family[ 2] = { 2, 3, 5, 7, 9, 10, 11, 17, 19 }

Family[ 3] = { 6, 8, 12, 15, 18 }
Part
Part
Part
Part Family[ 4] --> Empty Part family
                                         _____
```

Problem(97) --> Data file name : DC_28_MoonChi(1992)_12x19.cfp

```
______
No. of machines
                                                              = 12
No. of part types = 19
No. of cells = 4
Machine cell size = 4
Total no. of 1's in the original MPIM : |A| = 53
Matrix density
                                                                = 0.232
Total no. of within-block 1's
                                                               = 43
No. of exceptional elements (EEs)
No. of voids
                                                               = 10
                                                               = 23
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                               = 33
                                                               = 81.13 %
= 79.49 %
= 56.58 %
                                                               = 65.15 %
No. of redundant machines (RMs)
                                                               = 2
```

```
< Machines visited by parts: Process route numbers(PRN) >
                                               10 }
10 }
10 }
                                         9,
                          3,
Part[
Part[
                                         9,
                                 4,
            2]
3]
4]
                          3,
                                      9,
9,
11 }
5,
7
                =
                          3,
6,
Part
                =
                                  4,
                                 8,
2,
Part
                =
Part[
                                                 7,
                                                       10 }
                                 6,
            6]
7]
8]
                          2,
Part[
                =
Part[
Part[
                          4,
                                 9,
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                                 5,
7,
                          1,
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                =
                          6,
7,
                                               11 }
Part[
            9]
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Part[
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Part[
Part[
           11
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                                 3,
2,
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                                        10 }
                          1,
2,
                                                7,
           12]
                                         5,
                                                        9,
                                                            10 }
                =
Part[
           13]
          14]
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16]
                          6,
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Part[
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Part[
Part[
                          3,
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                =
                                               11 }
11 }
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9 }
                                         8,
Part[
           17]
          18]
19]
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Part[
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Part[
Part[
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                                         5
                                 3,
                                         4,
          20]
                          1,
                =
< Block Diagonal Solution Matrix >
                  < Locations >
                     0 0 0 0 0 0 0 0 0 0 0
                     \begin{smallmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 \\ 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 0 & 1 \end{smallmatrix}
                                          8 \ 9 \ 0 \ \overline{1}
                  < Machines
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                     < Parts >
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            19
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                  * * * * * *
< Machine cells and Part families >
         -----
Machine Cell[ 1] = { 3, 4, Machine Cell[ 2] = { 6, 7, Machine Cell[ 3] = { 1, 2,
                                         9, 10 }
8, 11 }
                                         8,
5 }
Part Family[ 1] = { 1, 2, 3, 7, 11, 15, 16, 20 }
Part Family[ 2] = { 4, 6, 9, 10, 13, 14, 17, 18 }
Part Family[ 3] = { 5, 8, 12, 19 }
```

Problem(98) --> Data file name : DC_29_Sule(1994)_11x20.cfp

```
No. of machines = 11
No. of part types = 20
No. of cells = 3
Machine cell size = 5
Total no. of 1's in the original MPIM : |A| = 71
Matrix density = 0.323
Total no. of within-block 1's = 60
No. of exceptional elements (EEs) = 11
No. of voids = 16
Sum of EEs and voids = 27
Group Cability Index (GCI) = 84.51 %
grouping efficiency (GE) = 85.65 %
Grouping efficacy (GF) = 68.97 %
Machine utilization (MU) = 78.95 %
No. of redundant machines (RMs) = 0
```

 $\begin{smallmatrix}0&0&0&0&0&0&0&0&0&1&1&1&1&1&1&1\\1&2&3&4&5&6&7&8&9&0&1&2&3&4&5&6\end{smallmatrix}$

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43
       41)
       42)
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       48)
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                  49
       49)
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      50)
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57
58
59
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                          *
      60)
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                  60
```

```
< Machine cells and Part families >
                                                       ______
Machine Cell[ 1] = { 9, 10, 11, 12 }

Machine Cell[ 2] = { 1, 2, 3, 4 }

Machine Cell[ 3] = { 5, 6, 7, 8 }

Machine Cell[ 4] = { 13, 14, 15, 16 }

Machine Cell[ 5] = { 17, 18, 19, 20 }
Part Family[ 1] = { 23, 24, 25, 26, 27, 28, 29, 30, 32, 33, 34, 35, 42 } Part Family[ 2] = { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 31, 36 } Part Family[ 3] = { 13, 14, 15, 16, 17, 18, 19, 21, 22 } Part Family[ 4] = { 37, 38, 39, 40, 41, 43, 44, 45, 46, 47, 48 } Part Family[ 5] = { 20, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60 }
_____
< Summary of the performance measures >
______
No. of machines
                                                                = 20
No. of part types No. of cells
                                                                = 60
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                                = 155
Matrix density
Total no. of within-block 1's
                                                                = 0.129
                                                                = 128
No. of exceptional elements (EEs)
                                                                = 27
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                                = 112
                                                                = 139
                                                                = 82.58 %
                                                                = 75.26 %
                                                                = 47.94 %
Grouping efficacy (GF)
                                                                = 53.33 %
Machine utilization (MU)
                                                                = 0
No. of redundant machines (RMs)
______
```

```
< Machines visited by parts: Process route numbers(PRN) >
                       4 }
Part[
Part[
           2]
3]
4]
                       3,
              =
                              4
                                 }
                                     4,
                                           8,
8)
                              3,
3,
                       1,
                                                   9 }
Part
              =
                                     4,
9 }
                       2,
Part
              =
Part[
                              3,
                       9
2,
1
           6]
7]
PartL
                         }
              =
                                     7 }
                              6,
Part
           81
Part
              =
                       4,
                              9 }
Part[
           9]
                       1,
Part[
         10]
                              2,
                                       }
}
              =
                              6,
                                     9
Part
         11
              =
                                     7,
         12]
                       1,
Part
                              3,
                                            8 }
              =
                                     4
Part[
         13]
                              3,
                       9<sup>'</sup>5, 1, 2,
         14]
PartL
              =
                              6
Part
         15]
                                }
                              7,
6
                                     9 }
Part
         16]
              =
                                `
}
}
Part[
         17]
         18]
                       1,
                              8
2
9
Part[
              =
Part
         19
              =
                       1,
6
2,
1,
         20]
Part
              =
Part[
         21]
                              3
         22]
                                     8 }
Part[
              =
                                '}
         23]
Part
                              8
                              3,
7,
                       1,
                                     7
8
         24]
Part
                                       }
              =
Part[
                              7,
3,
                       2,
         26]
27]
                                     8
Part[
              =
Part[
                                     6,
              =
                                                   8 }
                       1,
                              Š,
         281
                                     <u>6</u>,
Part[
              =
                                     7 }
8 }
Part[
                              5,
         291
Part[
         30]
< Block Diagonal Solution Matrix >
                < Locations
                   Locations > 0 0 0 0 0 0 0 0
                     0 0 0 0 0 0 0 0
                   0
                   1 2 3 4 5 6 7 8 9
                < Machines
                   000000000
                                   0 0 0
                     0
                        0 0 0 0
< Parts >
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                                   3
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    18)
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23)
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           18
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1

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22

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1

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24)
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25
26
    25)
26)
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    27)
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          27
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    28)
              *
    29)
          28
                         1 1 1
                                  1
              *
    30)
          29
                                  1
======== * * * * *
< Machine cells and Part families >
Machine Cell[ 1] = { 4, 9 }
Machine Cell[ 2] = { 2, 5, 6 }
Machine Cell[ 3] = { 1, 3, 7, 8 }
Part Family[ 1] = { 1, 2, 6, 9, 14 }
Part Family[ 2] = { 7, 11, 15, 17, 19, 21, 30 }
Part Family[ 3] = { 3, 4, 5, 8, 10, 12, 13, 16, 18, 20, 22, 23, 24, 25, 26, 27,
28, 29 }
______
< Summary of the performance measures >
______
No. of machines
                                                   = 9
No. of part types No. of cells
                                                      = 30
                                                      = 3
Machine cell size = 4
Total no. of 1's in the original MPIM : |A| = 79
Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
                                                      = 58
                                                      = 21
                                                      = 45
Sum of EEs and voids
                                                      = 66
Group Cability Index (GCI)
                                                      = 73.42 %
grouping efficiency (GE)
Grouping efficacy (GF)
                                                      = 71.87 %
= 46.77 %
Machine utilization (MU)
                                                      = 56.31 %
No. of redundant machines (RMs)
                                                      = 0
```

```
< Machines visited by parts: Process route numbers(PRN) >
Part[
                                  8,
                                        9 }
Part
                                 4,
          2]
3]
4]
                     1,
                           2,
2,
                                        6,
                                              7,
7,
             =
                                       6
4,
9 }
                                 3,
7,
7,
                                                          9 }
Part
                                                    8,
                           4,
                     1,
Part
             =
                                        9,
                           6,
                                             10 }
Part[
          6]
7]
                     6,
                                  8
                                       10
Part[
             =
                     4,
                           6,
Part
                     2,
2,
                           3,
3,
                                 4,
          81
Part
                                              6 }
          9]
                                 4,
Part[
                                                    8 }
                           4,
                                8,
12 }
         10]
                     3
7
                                       12 }
Part[
             =
                          11,
Part
         11
                                ī1,
         12]
                          10,
                                       12 }
Part
             =
                          10,
Part[
         13]
                                11 }
         14]
                     9,
7,
                          10,
                                11 }
PartL
             =
Part[
                          10,
                                11,
         15]
             =
                                       12 }
                                10'}
         16]
Partl
< Block Diagonal Solution Matrix >
               < Locations
                 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0
                 < Machines
                 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0
                   0 0 0 0 1 1
4 8 9 7 0 1
* * * * * *
                                  1 0 0 0 0
2 2 3 5 6
* * * * *
                 0
< Parts >
               * 1 1 1 1
               * 1 1 1
           2
     2)
                           1
                                     1
                                             1
               *
     3)
                 1
                   1 1 1 1
                                     1 1
               * 1
                   1
           4
                         1 1
               * 1
                                               *
                         1 1 1
                                             1
                                               *
                    1 1
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     6)
                    1 1
          10
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                 = =
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                                               *
           6
                      1
                           1 1
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     9)
          11
                           1
                                1 1
    10)
          12
               *
                           1 1 1 1
                                                *
    11)
          13
                           1
                              1 1
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                                                *
    12)
          14
                              1 1
               *
(
          15
                           1
                             1 1 1
    13)
    14)
          16
               *
                           1 1
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                           =
                                               *
               *
                    1
                                     1 1 1 1
    15)
    16)
                    1
                      1
                                     1
                                        1
                                          1
                      *
                          *
                 *
< Machine cells and Part families >
Machine Cell[ 1] = { 1, 4, 8, 9 }
Machine Cell[ 2] = { 7, 10, 11, 13
Machine Cell[ 3] = { 2, 3, 5, 6 }
      Family[ 1] = { 1, 2, 3
Family[ 2] = { 6, 11,
Family[ 3] = { 8, 9 }
                                   3, 4, 5, 7, 10 }
12, 13, 14, 15, 16 }
                              2, 3,
Part
Part
Part
                             -----
< Summary of the performance measures >
______
                                                       = 12
No. of machines
No. of part types No. of cells
                                                       = 16
                                                         3
Machine cell size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                       = 0.359
```

Problem(101) --> Data file name : DC_32_LeeGarcia(1996)_12x16.cfp

```
Total no. of within-block 1's = 48

No. of exceptional elements (EEs) = 21

No. of voids = 16

Sum of EEs and voids = 37

Group Cability Index (GCI) = 69.57 %

grouping efficiency (GE) = 79.30 %

Grouping efficacy (GF) = 56.47 %

Machine utilization (MU) = 75.00 %

No. of redundant machines (RMs) = 0
```

```
< Machines visited by parts: Process route numbers(PRN) >
Part[
                            13,
20 }
                                   21,
          1]
2]
3]
4]
                       1,
3,
7,
                                         22 }
Part
                            14,
8,
                                   23,
                                          24 }
Part
              =
                                   12,
15,
17,
17,
19,
                                          15,
18 }
Part[
                                                18 }
                             8,
          5]
6]
7]
                       6,
PartL
              =
                       9,
                            10,
Part
Part
                      10,
                            12,
                                          22 }
              =
                            Ī6,
           8]
Part[
                       4,
         9]
[10]
Part[
                       1,
2,
3,
2,
2,
1,
                             5,
                                   13,
                                          21,
                                                22,
19 }
                                                       24 }
              =
                             5,
                                   _9′,
20′}
                                          11,
Part
              =
                             8,
Part
         11\overline{]}
              =
Part[
         12]
                            20
                             5,
         13]
                                   11,
                                          17,
12,
Part[
              =
                            5,
20 }
                                   11,
Part
         14]
         15]
Part
              =
                                   22 }
22 }
                            21,
Part[
         16]
                            13,
                       1,
         17]
                                  2<sub>4</sub>
11,
16 }
Part[
              =
                             8,
                       6,
                                          12,
                                                15,
Part
         18]
              =
                                                       18 }
                             7,
                       4,
9,
         19]
Part
              =
                            10,
Part
         20]
                                   17,
                                          22 }
                       4,
2,
3,
7,
6,
                            16 }
Part[
         21]
              =
Part[
         22]
23]
                             5,
7,
                                   11,
20 }
                                          19,
                                                20 }
              =
Part
              =
                            20 }
Part[
         24]
                                   14,
12,
11,
16 }
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                                         23,
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12,
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18
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27]
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Part[
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Part
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                                                       18 }
Part
              =
Part
                             4,
         281
                       1,
                       9,
                            10,
         29]
Part[
              =
Part[
                       8,
                            12,
20 }
         30]
              =
                       3,
7,
1,
3,
2,
         31]
Part[
              =
                                   23,
                                          24 }
22 }
Part[
         32]
                            14,
                                   21,
20 }
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         33]
Part[
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35]
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Part
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Part[
                                   11,
         361
                                          13,
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                       4,
Part[
         37]
              =
                            16 }
Part[
         38]
39]
                       4,
                            16
              =
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                            16
Part[
         40]
                                  17 }
Part[
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                                          _____
< Block Diagonal Solution Matrix >
                < Locations >
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     5)
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           38
                  1
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           11
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          12
15
                *
    10)
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    12)
           23
                                           1
           24
                *
    13)
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14)
            31
                 *
                  *
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    15)
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            34
                  *
    16)
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     17)
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                                    1 1 1 1
1 1 1 1
1 1 1 1
    18)
            18
                                  1
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            26
27
     19)
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    26)
27)
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1
            13
                  *
            14
                                        1
            22
35
     28)
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     29)
                  *
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     30)
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                  * =
     31)
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     32)
33)
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     34)
            29
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            40
                                                                            1 1
     35)
     36)
                                                                                     1 1 1
                  *
              9
     37)
     38)
                  *
            16
                                                                                         1 1
     39)
            17
                  *
                                                                                     1
                                                                                           1
            33
     40)
< Machine cells and Part families >
Machine Cell[ 1] = {
                                4, 16
Machine Cell[ 1] = { 4, 10 }
Machine Cell[ 2] = { 3, 20 }
Machine Cell[ 3] = { 6, 8, 12, 15, 18 }
Machine Cell[ 4] = { 7, 14, 23, 24 }
Machine Cell[ 5] = { 2, 5, 11, 19 }
Machine Cell[ 6] = { 9, 10, 17 }
Machine Cell[ 7] = { 1, 13, 21, 22 }
        Family[ 1] = { 8, 19, 21, 28, 37, 38, 39 }
Family[ 2] = { 2, 11, 12, 15, 23, 24, 31, 3
Family[ 3] = { 4, 5, 18, 26, 27, 30 }
Family[ 4] = { 3, 25, 32 }
Family[ 5] = { 10, 13, 14, 22, 35, 36 }
Family[ 6] = { 6, 7, 20, 29, 40 }
Family[ 7] = { 1, 9, 16, 17, 33 }
Part
Part
                                                                   31, 34 }
Part
Part
Part
Part
Part
< Summary of the performance measures >
_____
No. of machines
No. of part types
                                                                   = 24
No. of cells
Machine cell size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                                     0.149
Total no. of within-block 1's
                                                                   = 124
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
                                                                      19
                                                                      26
Group Cability Index (GCI)
                                                                   = 86.71 %
grouping efficiency (GE)
                                                                   = 96.18
Grouping efficacy (GF)
Machine utilization (MU)
                                                                   = 82.67
                                                                   = 94.66 %
No. of redundant machines (RMs)
                                                                   = 0
```

```
< Machines visited by parts: Process route numbers(PRN) >
Part[
                                                22 }
20 }
23,
15 }
18 }
                                         13,
            1]
2]
3]
4]
                          1,
7,
5,
                                         11,
Part
                                  3,
                                        11,
14,
12,
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17 }
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Part
                                  8,
                                                        24 }
                =
Part[
                                  6,
            5]
6]
7]
                          8
                                 12,
PartL
                 =
                                 10,
                          9
Part
                          9,
4,
Part
                                 14,
                 =
                                        17 }
22 }
            8]
                                 16,
Part[
                         13,
2,
3,
           9]
[10]
                                 21,
Part[
                 =
                                -<u>-</u>,
20
Part
                 =
                                         11,
                                                17,
                                                        19 }
Part
           11\overline{]}
                 =
Part[
                         20
           12]
                                  5,
           13]
                          2,
32,
18,
49,
12,
33,
                                         19 }
Part[
                 =
                                11,
12,
13,
                                                19 }
20 }
22 }
                                         ī4,
Part
           14]
                                         ī8,
           15]
Part
                 =
                                        21,
Part[
           16]
                                                19,
                                         13,
                                 12,
                                                        21,
18 }
           17]
Part[
                 =
                                                                22 }
                                 9,
Part
           18
                 =
                                         12.
                                                15.
           \overline{19}
                                 16
Part
                 =
Part
           20]
                                 10
                                 4
Part[
           21]
                 =
                                        19,
           22]
23]
                                 11,
                                                20 }
Part
                 =
                                 20,
Part
                 =
                                 20'}
Part[
           24]
                                        23,
12,
12,
16 }
                                                24
18
                         11,
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           25]
Part[
                 =
           26]
27]
                          6,
6,
                                  8,
Part
                 =
                                  8,
                                                15,
                                                        18 }
Part
                 =
                                  4,
Part
                          3,
           281
                                        17,
                          9,
6,
                                10,
           29]
                                                24 }
Part[
                 =
                                10
11,
20 }
Part[
                                         12,
                                                13,
           30]
                 =
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                                                                18 }
                          3,
6,
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7,
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Part
                 =
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11,
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           32]
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           34]
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5,
Part
                 =
                                                12 }
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                 =
Part
           361
                                         11,
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                =
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Part[
           37]
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Part[
           38]
39]
                          4,
                                16,
16}
                                        22,
                 =
                                                24 }
                          4,
                 =
Part[
Part[
           40]
                                        17,
                                10,
                                                20 }
< Block Diagonal Solution Matrix >
                   < Locations >
                     0
2
0
                                                                                    0
2
1
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2
2
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                   < Machines
                     0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 1 1 1 1 0 1 2 2 4 6 6 8 2 5 8 7 4 3 4
                                                           0
2
0
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2
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< Parts >
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3)
            19
21
28
37
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7)
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            38
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            39
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                                  1 1
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                            1
      9)
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                               1
                   *
    10)
            18
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            26
27
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    11)
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                                     \begin{array}{ccc} 1 & \overline{1} \\ 1 & 1 \end{array}
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     12)
                            1
            30
                   *
                            1
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     13)
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*
     14)
                3
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              25
32
     15)
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     16)
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                                                                  1
      18)
                                                               1
              12
15
      19<sup>)</sup>
                     *
                                                               1
                                                                  1
      20)
                                      1
              23
24
                                                               1
1
     21)
22)
23)
                     *
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                                                                                1
              31
                                                                  1
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     24)
              34
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    =======
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      27)
              16
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     28)
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              17
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     29)
              33
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      30)
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1
      31)
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     32)
33)
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              20
              29
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                                                           1
      34)
              40
                     *
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                     *
      35)
              10
     36)
              13
                                                                                              1
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                     *
      37)
              14
                                                    1
                                                                                                         1
              22
35
                     *
                                                                                                     1
      38)
                                                                  1
                     *
                                      1
      39)
                                      1
      40)
              36
< Machine cells and Part families >
                                    4, 16 }
6, 8, 12, 15, 18 }
7, 14, 23, 24 }
3, 20 }
1, 13, 21, 22 }
Machine Cell[ 1] =
Machine Cell[ 2] = { 6, 8, 12, 15, 3
Machine Cell[ 3] = { 7, 14, 23, 24 ]
Machine Cell[ 4] = { 3, 20 }
Machine Cell[ 5] = { 1, 13, 21, 22 ]
Machine Cell[ 6] = { 9, 10, 17 }
Machine Cell[ 7] = { 2, 5, 11, 19 }
                            = { 8, 19, 21, 28, 37, 38, 39 }
= { 4, 5, 18, 26, 27, 30 }
= { 3, 25, 32 }
= { 2, 11, 12, 15, 23, 24, 31,
= { 1, 9, 16, 17, 33 }
= { 6, 7, 20, 29, 40 }
= { 10, 13, 14, 22, 35, 36 }
          Family[ 1]
Part
          Family[ 1]
Family[ 2]
Family[ 3]
Family[ 4]
Family[ 6]
Family[ 7]
Part
Part
                                                                     24, 31, 34 }
Part
Part
Part
          Family[ 7]
Part
< Summary of the performance measures >
_____
No. of machines
No. of part types
                                                                             = 24
                                                                               40
                                                                             =
No. of cells
Machine cell size
Total no. of 1's in the original MPIM : |A|
Matrix density
                                                                                0.147
Total no. of within-block 1's
                                                                             = 111
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
                                                                                30
                                                                                20
                                                                                50
Group Cability Index (GCI)
                                                                               78.72 %
                                                                            = 90.56 %
= 68.94 %
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
                                                                             = 84.73 %
No. of redundant machines (RMs)
```

```
< Machines visited by parts: Process route numbers(PRN) >
                                    20,
                                          24,
                              11,
                                                31 }
Part[
                    9,
                                    25,
27,
         2]
                        13,
                                          30
35
Part[
                              18,
            =
         3]
Part
            =
                        10,
                              14,
                                               31 }
28 }
19 }
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                               -9,
         4]
                                    20,
                                          24,
Part[
                         3,
                                    22,
15,
                                          26,
17,
30,
Part[
         5]
            =
                   12,
                              16,
         6]
7]
8]
                        5,
13,
                              10,
Part
            =
                              18,
26 }
                                    21,
                  11,
Part[
            =
                                         29,
'3'}
Part
            =
                        16,
                                    15,
         9]
                                                34 }
Part[
            =
                              12,
                                    23,
27 }
Part[
        10]
            =
                    4,
                        11,
                              18,
        11]
                              19,
Part[
                                               30,
33 }
24 }
                               9,
                                    21,
16,
                                          24,
23,
17,
Part[
        12]
13]
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            =
                                                     32 }
                              1Ž,
Parti
            =
                              10,
                                    14,
                         6,
Part[
        147
            =
                    5,
                                                     26,
                                                           28, 34 }
Part[
        15]
            =
                         7,
                              12,
                                    13,
                                          15,
                                               16,
< Block Diagonal Solution Matrix >
              2 2 6 7
                0 0 0
                                                                                      0
                  1
7
                                                                                 2
                                                                               1
                                                                                    3
                                                                                      2 5
                0 0 1 1 1 2 2 2
                                                                                        2
                                                                                          0
< Parts >
              *
                1
    1)
2)
          2
                     1
                            1
                                 1
                                     1
                                                 1
                       1 1
                                   1
                                                                                      1
              *
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              *
    4)
                     1 1 1
                              1
                                   1
                                       1
              *
                              \bar{1} 1 \bar{1}
                  1
                                       1
                                                                   1
    5)
         12
                                            1
                       = = = = = = =
                                              = = = = = = =
                                                   1 1 1 1 1 1
                                                        1
                                                            1
    8)
          9
              *
                                            1 1
                                                   1
    9)
              *
                                                 1 1
         13
                                          1
                                                        1
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   10)
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                                                   \overline{1} 1 1
         15
                                                            1 1 1
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   11)
                                            1
                                                                        1 1
                                                                                 1 1
   12)
          6
                                            1
                                                      1
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                                                                             1 1
                                                                           1
                                                                      \begin{smallmatrix}&&&1\\1&1&1\end{smallmatrix}
         11
              *
   14)
         14
              *
                                                                            1
              *
                = =
                                = =
                                                                      = = =
                                                                            =
        10 *
                                                                                           1 1 1
   15)
                     1
                         1
* * * * *
                                                                     *
< Machine cells and Part families >
Machine Cell[ 1] = { 2, 9, 11, 13, 18, 20, 21, 24, 30, 31, 32 } Machine Cell[ 2] = { 3, 5, 7, 8, 12, 15, 16, 22, 26, 28, 34 } Machine Cell[ 3] = { 1, 6, 10, 14, 17, 19, 27, 35 } Machine Cell[ 4] = { 25, 29 } --> Residual cell Machine Cell[ 5] = { 4, 23, 33 }
            _____
     Family[ 1] = { 1, 2, 4, 7, 12 }

Family[ 2] = { 5, 8, 9, 13, 15 }

Family[ 3] = { 3, 6, 11, 14 }

Family[ 4] --> Empty Part family

Family[ 5] = { 10 }
Part
Part
Part
Part
Part
                  -----
< Summary of the performance measures >
No. of machines
No. of part types
No. of cells
                                                   = 15
                                                     5
Machine cell size Total no. of 1's in the original MPIM : |A|
                                                   = 11
Matrix density
                                                   = 0.164
Total no. of within-block 1's No. of exceptional elements (EEs)
                                                   = 70
                                                   = 16
No. of voids
```

Problem(104) --> Data file name : DC_35_SeifoddiniDjassemi(1996)_35x15.cfp

```
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
No. of redundant machines (RMS)
                                                                                                                                                                                                                = 91
= 81.40 %
= 72.03 %
= 43.48 %
= 48.28 %
= 2
```

```
< Machines visited by parts: Process route numbers(PRN) >
Part
                                    }
                         4,
1,
            2]
3]
4]
                                              10 }
                                        9,
Part[
                =
Part
                =
Part[
                                                        8, 10 }
                                 7,
2,
2,
Part[
            5]
6]
7]
8]
                                       10 }
                                               6,
९)
                                        3,
7,
7,
Part
                                                        7 }
                =
                         1,
Part[
                =
                                                8,
                                 6
                                                      10 }
                          1,
Part
                =
            9]
                                   `}
Part[
                =
                                 8
                                       10
Part[
           10]
                =
                                 8,
Part[
                                 6,
           12]
                =
                                       10
Part
< Block Diagonal Solution Matrix >
                  < Locations > 0 0 0 0 0 0 0 0
                     0 0 0 0 0 0 0 0 0 0 1
1 2 3 4 5 6 7 8 9 0
                  < Machines´>
                     0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0
                     0 0
                           0
                              0
                                 100000
                           7 8 0 4
< Parts >
                  *
                     1 1
1
1 1
                  *
                              1 1 1
                                                1
      2)
3)
                  *
             5
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             6
                           1
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1
      4)
      5)
6)
                  *
              8
            10
                  *
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      7)
8)
                  *
                     1
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            11
                              1
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                                 1
            12
                              =
                                 = =
      9)
                                    1
                                       1
     10)
                  *
                                 1 1 1 1
                  *
     11)
                                    1
             9
                  *
                    * * * *
    12)
                                 *
< Machine cells and Part families >
Machine Cell[ 1] = { 1, 6, 7, 8, 10 } Machine Cell[ 2] = { 4, 5, 9 } Machine Cell[ 3] = { 2, 3 }
       Family[ 1] = { 4, 5, 6, 7, 8, 10, 11, 12 }

Family[ 2] = { 1, 2, 3 }

Family[ 3] = { 9 }
Part
Part
< Summary of the performance measures >
No. of machines
                                                                  = 10
No. of part types
No. of cells
                                                                     12
                                                                  = 3 = 5
Machine cell size
Total no. of 1's in the original MPIM : |A|
                                                                     41
Matrix density
                                                                     0.342
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
                                                                     17
                                                                  =
                                                                  = 24
= 82.93 %
= 78.26 %
= 58.62 %
Machine utilization (MU)
                                                                  =
                                                                     66.67 %
No. of redundant machines (RMs)
                                                                  = 1
```

DC_36_Viswanathan(1996)_10x12.cfp

Problem(105) --> Data file name :

```
< Parts >
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1
1
1
                              1
1
                                  1 1
1 1
       1)
2)
3)
                 9
                                      1
                                                      1
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                       *
               12
17
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                       *
        4)
                              1
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                                  1 1
        5)
                20
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1
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                 2
                                              1
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        6)
        7)
                                          1 1
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                                                                                     1
        8)
                 6
                       *
                                                  1 1
                                                                                                1 1
(
                11
                       *
                                              1
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      10)
                19
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                                          1 1 1 1
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1
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                 5
      11)
                                                              1
                                                                     1
                                                                         1
      12)
                 8
                               1
                                                                 1
                       *
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      13)
                13
                                                                     1
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      14)
                16
                       *
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                 3
      15)
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                10
      16)
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      17)
                14
                           1
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      18)
                18
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      19)
                                                                                                    \frac{1}{*}
                       *
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      20)
                15
< Machine cells and Part families
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
Machine Cell[ 4]
Machine Cell[ 5]
                                        1, 9, 12, 18 }
2, 3, 5, 11, 14
4, 6, 7, 13, 15
8, 10, 19, 20 }
16, 17 }
                                    ~~~~~~
                                =
                               =
                                =
                                =
           Family[
Family[
Family[
Family[
Family[
                                             9, 12, 17, 20 }
4, 6, 11, 19 }
8, 13, 16 }
10, 14, 18 }
                                        1,
Part
                           1]
2]
3]
4]
5]
                                    =
                                        2,
5,
                                =
Part
                                =
Part
                                        3,
7,
Part
                                =
```

< Summary of the performance measures >

```
No. of machines = 20
No. of part types = 5
No. of cells = 5
Machine cell size = 5
Total no. of 1's in the original MPIM : |A| = 79
Matrix density = 0.198
Total no. of within-block 1's = 63
No. of exceptional elements (EEs) = 16
No. of voids = 22
Sum of EEs and voids = 38
Group Cability Index (GCI) = 79.75 %
grouping efficiency (GE) = 84.52 %
Grouping efficacy (GF) = 62.38 %
Machine utilization (MU) = 74.12 %
No. of redundant machines (RMS) = 0
```

Problem(107) --> Data file name : < Machines visited by parts: Process route numbers(PRN) > 16, 25 } 10, 7, 2, Part 18, 22 } 2] 3] 4] ī7, Part[= 3, 12, 20'} Part = 11, $\overline{23}$ ' Part[= Part[5] 6] 7] 8] = 12, 18 } 23 } 18 12, 16, 7, Part = 10, 19 } 4, 16, 18 } Parti = 5, 3, 16, Part = ¹20, ²⁵, } 9 25 } Part = 11, 10] Part = 8, 9, 21['] 3, 11, Part[8, 12 13 17, 20 } 1, 3, Part = 24, 25 } Part = 3, 2, 14] 20 } Part[11, = 5, 16, 18 } 10, 15] 5, 19 } Part| = 16, 18 } 22 } 10 } 16] 17] 4, 7, Part 10, Part Ī5, 18 Part = 8, 23 8, 19] 20] 21] 22] 23] Part[= 9, '} Part = 9 10 } Part[= 9, 19 } 17 } Part 3, 8, 5, 5, 16, Part 16 15, 12, 24] Part = 25] 6, 21 } Part = ặ, 26] 27] 28] 29] 15, 22 = 23 } Part Part = 12, 21, 10 } 21 } Part| 8, 9, 6, 7, Part = 301 16, 18 } Part 31] 32] 33] 5, 17, 19'} = Part 14, 20, 15, 25 22 } Part = 13, 25 } 24 } 21, Part[= 11, 23, 34] Part = 12, Part 6, 2, 12, 11, 23 } 22 } 36] = 1, Part 37] Part = Part[38] 39] 9, 8 = `} 12 6, Part = 21 } Part[40] = 15, < Block Diagonal Solution Matrix > < Locations > Machines 0 2 5 * 0 0 0 0 0 0 1 0 0 1 1 0 8 9 0 4 7 6 8 3 * * * * * * * * 1 2 1 0 * * 1 3 * 1 4 * 1 2 * 2 3 * 2 4 * 0 5 * 1 9 < Parts > 1 1 1 1) 2) 3) 4) 5) 10 * 1 1 1 1 1 1 11 1 1 19 * 1 21 22 28 * 1 * 1 1 1 1 6) 1 * 7) 38 1 1 1 * = = 1 1 1 1 1 8) 1 **9**) 57 1 1 1 1 10) 1 1 * $\overline{1}$ $\overline{1}$ 11) 12) 16 17 1 1 * 1 1 * 1 13) 24 30 * 1111 14)

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25
27
29
35
       23)
24)
       25)
                   40
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1 1 1 1
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1 1 1
       26)
27)
       28)
                   36
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       29)
                   32
                                                                                                                          1
1
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1
1
        30)
       32)
33)
                   20
26
                                                                                                                          1
                                              1
                                                                                  1
                   34
37
       34)
                                                                                                                          1
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        35)
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        36)
                   39
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1
1
*
        37)
                                                                                                                                        1
1
1
1
*
       38)
39)
                  15
23
                                                                                                    1
       40)
                   31
 < Machine cells and Part families
Machine Cell[ 1]
Machine Cell[ 2]
Machine Cell[ 3]
Machine Cell[ 4]
Machine Cell[ 5]
Machine Cell[ 6]
Machine Cell[ 7]
Machine Cell[ 8]
                                              8, 9, 10 }
4, 7, 16, 18 }
3, 11, 20 }
6, 15, 21, 22 }
1, 2, 17, 25 }
13, 14 }
12, 23, 24 }
5, 19 }
                                     Family[
Family[
Family[
Family[
Family[
Family[
Family[
Family[
Family[
                                     | | | | | | | | |
                                               10, 11, 19, 21, 22, 28, 38 }
1, 5, 7, 16, 17, 24, 30 }
3, 9, 13, 14, 33 }
18, 25, 27, 29, 35, 40 }
2, 12, 36 }
32 }
                                1]
2]
3]
4]
5]
6]
7]
 Part
 Part
 Part
 Part
 Part
                                               4, 6, 20, 26, 34, 37, 39 }
8, 15, 23, 31 }
 Part
 Part
 < Summary of the performance measures >
 No. of machines
                                                                                                    = 25
No. of machines
No. of cells
No. of cells
Machine cell size
Total no. of 1's in the original MPIM: |A|
                                                                                                    =
                                                                                                       40
                                                                                                    = 8
                                                                                                    = 4
                                                                                                        132
Matrix density
                                                                                                       0.132
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                                                                        32
                                                                                                    =
                                                                                                        31
                                                                                                   = 63
= 75.76 %
= 86.33 %
= 61.35 %
 Grouping efficacy (GF)
Machine utilization (MU)
                                                                                                       76.34 %
No. of redundant machines (RMs)
                                                                                                    = 0
```

1

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1)
2)
3)
4)
5)
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         8
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1
1
       14
                   1
             *
       15
                   1
                                         1
             *
                         1
1
1
       20
                   1
 6)
                   1
1
             *
                1
1
       27
                                                  1
             *
 8)
       32
                                        1
             *
                =
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                      =
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             *
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 9)
         1
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                                         1 1 1
10)
         5
                                   1
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             *
11)
         6
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                                        1
                                                  1
12)
13)
                                                                       *
         9
             *
                                1
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                                           1
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       10
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                            1
                                   1
                               1
1
       11
12
                            1
1
                                              1
1
             *
                                                                       *
14)
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                                            1
15)
                                   1
                                                              1
       18
21
23
             *
                                                                       *
16)
                                   1
                                      1
             *
                                     1
                                                                       *
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                                        1
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                                                                       *
             *
                                            1 1
18)
                             1 1
19)
       24
             *
                                1
                                  1
                                         1
                                           1 1
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1
                                        1
20)
       30
             *
                                                  1
             *
                                                                       *
21)
       31
                          1
                                                  1
                            1
                               1
                                         1
                                           1 1
22)
       34
             *
                                                 *
23)
         4
             *
24)
       16
             *
                                                                       *
25)
             *
       17
                                                  1 1 1 1
```

```
19
28
29
       26)
27)
28)
 (
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1
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1 1
1 1
                                                                                      1
1
1
                      2
                                                                                                          1
1
1
        30)
31)
                    13
22
25
                                                                                  1
                             *
        32)
                                  1
                                                                                  1
1
1
        33)
                    26
                             *
                                  1
                                                                                                              1
1
1
*
                    33
35
                                                                                      1
                             *
        35)
                             *
                                  1
 < Machine cells and Part families
Machine Cell[ 1] = { 3, 8, 16, 18 }
Machine Cell[ 2] = { 2, 4, 6, 9, 10, 12, 13, 15 }
Machine Cell[ 3] = { 1, 5, 11 }
Machine Cell[ 4] = { 7, 14, 17 }
             Family[ 1] = { 3, 7, 8, 14, 15, 20, 27, 32 }
Family[ 2] = { 1, 5, 6, 9, 10, 11, 12, 18, 21, 23, 24, 30, 31, 34 }
Family[ 3] = { 4, 16, 17, 19, 28, 29 }
Family[ 4] = { 2, 13, 22, 25, 26, 33, 35 }
 Part
 Part
 < Summary of the performance measures >
 No. of machines
                                                                                                          = 18
No. of part types
No. of cells
                                                                                                         = 35
= 4
= 8
Machine cell size
Total no. of 1's in the original MPIM : |A|
Total no. of 1's in the original in Matrix density
Total no. of within-block 1's
No. of exceptional elements (EEs)
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
Grouping efficacy (GF)
Machine utilization (MU)
No. of redundant machines (RMs)
                                                                                                        = 0.4
= 121
= 30
= 62
= 92
80
                                                                                                              0.24
                                                                                                          = 80.13 %
                                                                                                         = 79.70 %
= 56.81 %
= 66.12 %
 No. of redundant machines (RMs)
                                                                                                          = 0
```

```
Problem(109) --> Data file name : DC_40_SeifoddiniDjassemi(2001)_Figure_6_36x15.cfp
< Machines visited by parts: Process route numbers(PRN) >
                          21,
Part[
                                                  12 }
                   19,
          2]
3]
                                14,
15,
32,
17,
2,
22,
27,
                                      31,
Part[
                          10,
                                            26 }
             =
                                            28,
                                                  36 }
10 }
Part
             =
                    16,
                           8,
                                      11,
          4]
                          21,
                                            25,
Part[
                     3,
                                       4,
Part[
          5]
                          16,
                                            13,
                                                  23,
                                                        29 }
                                                  18 }
33,
14 }
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          6]
7]
8]
                          16,
25,
17,
                                      20,
Part
             =
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Part[
                                                         31 }
             =
                                            35,
Part
             =
                                            13,
          9]
                                       8,
                                                         30 }
                                 6,
Part[
             =
                          16,
                                                  35,
                                            12'}
28 }
Part[
         10]
             =
                    34,
                          24,
                                 5,
                                      19,
         11]
                     8,
                                20,
Part[
                                      15,
Part[
                                25,
9,
                                      10,
                                            22,
                                                  33,
24'}
        12]
13]
                          20,
                   16,
                                                        31 }
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3 }
                                      34,
Parti
                     6,
7,
             =
                          15,
                                      18,
        147
                                11,
             =
Part[
                                            27,
                                                    8,
                                                       13, 23, 35, 29 }
Part[
        15]
             =
                     1,
                          16,
                                 6,
                                      17,
< Block Diagonal Solution Matrix >
               < Locations >
                 2 2 6 7
                                                                                   2
                 0 0
                                                                                           0
                 2 2 3 0
0 8 6 5
                                                                                               2
                                                                                             0
                                                                                                  3 0
< Parts >
                        1\ 1\ 1\ 1\ 1\ 1
     1)
2)
                      1
           8
                 1
                             1
                                  1
                                                    1
(
(
           9
              *
                 1
                   1\ \bar{1}\ 1
                                                                                                          *
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     4)
          15
                 1 1 1 1 1 1 1 1 1
                                          1
                 _ _ _ _ _ _ _ _ _ _ _ _
                                            1
     5)
           1
                                            1
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                                                                  1
                                                                                             1
     6)
7)
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           4
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     8)
               *
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     9)
               *
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                                                           1 1 1
                                                                                                          *
          12
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1 1
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           3
    10)
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    11)
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    12)
          11
                      1
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              *
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                                                                                                          *
    14)
                                                 1
                                                                                           1
          10
              *
                                                                                                          *
    15)
          13
                   1
                        1
=
< Machine cells and Part families >
Machine Cell[ 1] = { 1, 6, 8, 13, 16, 17, 23, 27, 29, 30, 35 } Machine Cell[ 2] = { 3, 10, 12, 14, 19, 21, 22, 25, 31, 32, 33 } Machine Cell[ 3] = { 2, 7, 11, 15, 18, 20, 28, 36 } Machine Cell[ 4] = { 5, 9, 24, 34 } Machine Cell[ 5] = { 4, 26 } --> Residual Cell
      Family[ 1] = { 5, 8, 9, 15 }

Family[ 2] = { 1, 2, 4, 7, 12 }

Family[ 3] = { 3, 6, 11, 14 }

Family[ 4] = { 10, 13 }

Family[ 5] --> Empty Part family
Part
Part
Part
Part
Part
                  ._____
< Summary of the performance measures >
No. of machines
No. of part types
No. of cells
                                                      = 15
                                                      =\overline{5}
Machine cell size Total no. of 1's in the original MPIM : |A|
                                                      = 11
Matrix density
                                                      = 0.174
Total no. of within-block 1's No. of exceptional elements (EEs)
                                                      = 77
                                                      = 17
```

= 62

No. of voids

```
Sum of EEs and voids = 79
Group Cability Index (GCI) = 81.91 %
grouping efficiency (GE) = 75.58 %
Grouping efficacy (GF) = 49.36 %
Machine utilization (MU) = 55.40 %
No. of redundant machines (RMs) = 2
```

```
< Machines visited by parts: Process route numbers(PRN) >
                                    13 }
Part[
                              11,
                               9,
Part
                                    10,
13 }
14 }
13 }
         2]
3]
4]
                    6,
                          8,
                                                14 }
             =
                                          12,
                          7,
Part
                    5,
                              11,
                    6,
                              10,
                          9,
Part
            =
                          3,
                              11,
Part[
         6]
                    2,
                          4,
                                    14 }
                              12,
Part[
             =
                         3,
                                    11,
Part
                              10,
                                          13 }
                    Ž,
2,
         81
Part
                        13
                          4,
Part[
         9]
                                    14 }
                         4,
Part
        10]
                    2,
                               7 }
            =
Part[
Part[
                                5,
                          3,
                                     7 }
        11]
                    1,
        12]
                                 '}
                                9
                    2,
                          6,
            =
Part[
                               5,
                                     7,
9 }
                          3,
        13]
                                           8 }
        14] = {
Part
< Block Diagonal Solution Matrix >
              < Locations > 0 0 0 0 0 0 0 0 0 0 0 0
                < Machines
                5 7 1 3 2 4 6 9 0 4
< Parts >
             * *
              *
                     1
                       1 1
                            1
2)
3)
                     \bar{1} \bar{1} \bar{1}
                            1
              * 1 1
                                                 *
          7
              *
     4)
                1 1
                          1 1
                                        1
              *
     5)
                1 1 1 1
         11
              * 1 1 1 1
     6)
         13
                                            1
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     8)
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                                 1
                                          1
     9)
                                                 *
   10)
         10
              *
                       1
                              1 1
              *
   11)
         14
                              1 1 1 1
              *
                                   1 1 1 1 1 1 *
   12)
          2
              *
                                                 *
   13)
                                   1 1 1 1
   14)
              *
(
                              1
         12
                                   1 1
======== *
                = = = = = = =
< Machine cells and Part families >
                                                   ______
Machine Cell[ 1] = { 1, 3, 5, 7, 11, 13 }
Machine Cell[ 2] = { 2, 4 }
Machine Cell[ 3] = { 6, 9, 10, 14 }
Machine Cell[ 4] = { 8, 12 } --> Residual cell
                               =======
      Family[ 1] = { 1, 3, 5, 7, 11, 1 Family[ 2] = { 6, 8, 9, 10, 14 } Family[ 3] = { 2, 4, 12 } Family[ 4] --> Empty Part family
                               5, 7, 11, 13 }
Part
Part
Part
Part
< Summary of the performance measures >
______
No. of machines
                                                   = 14
No. of part types
                                                   = 14
No. of cells
                                                   = 4
Machine cell
Total no. of 1's in the original MPIM : |A| = 56
Matrix density
Total no. of within-block 1's
                                                     43
```

Problem(110) --> Data file name : DC_41_Li(2003)_14x14.cfp

```
No. of exceptional elements (EEs) = 13
No. of voids = 15
Sum of EEs and voids = 28
Group Cability Index (GCI) = 76.79 %
grouping efficiency (GE) = 82.36 %
Grouping efficacy (GF) = 60.56 %
Machine utilization (MU) = 74.14 %
No. of redundant machines (RMs) = 2
```

= =

25)

26) 27)

28)

29)

10

20 21

3 *

12

*

=

=

1

*

11 *

1 1

1

1

```
( 30) 19 * 1
 < Machine cells and Part families >
Machine Cell[ 1] = { 7, 8, 9, 10, 11, 12, 13, 16, 18, 20, 21, 26, 31 } Machine Cell[ 2] = { 1, 3, 4, 5, 15, 19, 24, 32, 33, 34, 35, 36, 37 } Machine Cell[ 3] = { 14, 17, 22, 29, 30 } Machine Cell[ 4] = { 2, 6, 23, 25, 27, 28 }
Part Family[ 1] = { 1, 2, 7, 8, 13, 14, 15, 22, 23, 24 } Part Family[ 2] = { 4, 5, 6, 9, 11, 16, 17, 18, 25, 26, 27, 28, 29, 30 } Part Family[ 3] = { 10, 20, 21 } Part Family[ 4] = { 3, 12, 19 }
 < Summary of the performance measures >
 ______
No. of machines = 37

No. of part types = 30

No. of cells = 4

Machine cell size = 13

Total no. of 1's in the original MPIM : |A| = 107

Matrix density = 0.0964

Total no. of within-block 1's = 94

No. of exceptional elements (EES) = 13

No. of voids = 251

Sum of EEs and voids = 264

Group Cability Index (GCI) = 87.85 %

grouping efficiency (GE) = 62.77 %

Grouping efficacy (GF) = 26.26 %

Machine utilization (MU) = 27.25 %

No. of redundant machines (RMS) = 0
 No. of machines
                                                                                                              = 37
                                                                                                              = 13
= 251
= 264
= 87.85 %
= 62.77 %
= 26.26 %
= 27.25 %
```

= 0

No. of redundant machines (RMs)

```
< Machines visited by parts: Process route numbers(PRN) >
Part[
                    24,
                          26,
                                  3
Part
                    24,
          2]
3]
                          26,
25,
26,
                                16
             =
                                      12,
27,
17,
                    26,
Part
             =
                                  5
                                             10 }
                                19,
                    20,
                                             11,
Part
                                                     4 }
             =
                                             28'}
15 }
                                 4,
                    22,
Part[
                          10,
                           7,
          6]
7]
                     1,
                                       21,
16 }
                                14,
Part[
             =
                                 3,
                    24,
                          26,
Part
                           7,
                                14,
                                             15,
11 }
12 }
                     1,
          81
                                       21,
                                                    9,
                                                         27 }
Part
             =
                           9,
                    25,
                                12,
          9]
                                       23,
Part[
                                       5
5,
1 }
                                 9,
Part[
         10]
                    21,
                          25,
             =
                                27,
                    19,
                          23,
                                       11
Part
         11
             =
                                       22,
                                             10,
Part
         12]
                    26,
                          16,
                                18,
                                                          17 }
             =
                                       16,
                                             18,
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                     6,
                          26,
                                 3,
Part[
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        14]
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Part
         15]
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                                       13,
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                     8,
Part
        16]
             =
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                    21,
                                16,
Part[
         17]
                                                          12,
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        18]
                                 9,
                                        5,
                                             17 }
11 }
                    21,
                          13,
Part[
             =
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                    15,
25,
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Part
         19
             =
                                23,
                                             22,
        20]
                          12,
                                       18,
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                                                   10,
Part
             =
                                26,
Part[
         21]
                    21,
                          24,
                                             16<sup>'</sup>}
                                 ì,
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                    24,
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                                       16 }
Part[
             =
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                                       22,
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22 }
Part[
         23]
                                                                28 }
                                      5,
16}
                                  9,
                                                   19,
         24]
                          25,
Part
                                             12,
             =
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                          26,
                    24,
Part[
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5,
2,
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27 }
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23,
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Part
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                    14,
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                                14,
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Part[
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Part[
                     2,
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17,
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         31]
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Part[
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                                       21,
             =
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        35]
                    15,
                          18,
                                  4,
Part[
             =
< Block Diagonal Solution Matrix >
               < Locations >
                 2 2 2 2 3
                 0\; 0\; 0\; 0\; 0\; 0\; 0\; 0\; 0\; 1\; 1\; 1\; 1\; 1\; 1\; 1\; 1\; 1\; 2\; 2
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                      3 4 5 6 7 8 9 0 1 2 3 4 5 6 7
                                                            8 9 0
                 1 2
               < Machines
                    0 2 3
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     21)
22)
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             18
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     26)
27)
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27
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     30)
             12
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             20
                   *
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     31)
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             23
                                            1
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1 1
     32)
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                                            1
     33)
             29
                            1
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                   *
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1
*
             32
                                                                                              1
                                                                                                 1
     34)
                                                                  1
                                                                                            1
                   *
                                                                                            1
                                                                                                  1
< Machine cells and Part families
______
Machine Cell[ 1] = { 1, 7, 14, 15, 21 }
Machine Cell[ 2] = { 3, 16, 24, 26 }
Machine Cell[ 3] = { 2, 6, 8, 13, 20 }
Machine Cell[ 4] = { 5, 9, 12, 25 }
Machine Cell[ 5] = { 11, 19, 23, 27 }
Machine Cell[ 6] = { 4, 10, 17, 18, 22, 28 }
_____
         Family[ 1]
Family[ 2]
Family[ 3]
Family[ 4]
Family[ 5]
Family[ 6]
                         = { 6, 8, 14, 15, 30, 34 }

= { 1, 2, 7, 13, 21, 22, 25, 31 }

= { 16, 26, 28 }

= { 3, 9, 10, 17, 18, 24 }

= { 4, 11, 19, 27, 33 }

= { 5, 12, 20, 23, 29, 32, 35 }
Part
Part
Part
Part
Part
Part
< Summary of the performance measures >
_____
No. of machines
                                                                        28
No. of part types
No. of cells
                                                                        35
                                                                     =
                                                                     =
                                                                        6
Machine cell size
                                                                        6
                                                                        195
Total no. of 1's in the original MPIM : |A|
Matrix density
Total no. of within-block 1's
                                                                        0.199
No. of exceptional elements (EEs)
                                                                        51
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                                        19
                                                                        70
                                                                     =
                                                                        73.85 %
                                                                     = 91.05
Grouping efficacy (GF)
                                                                     = 67.29 %
Machine utilization (MU)
                                                                     = 88.34
```

= 0

No. of redundant machines (RMs)

*

```
< Machines visited by parts: Process route numbers(PRN) >
                               5,
Part[
                                     7 }
Part[
                         2,
         2]
3]
4]
                   1,
                               6,
6 }
                                     7,
                                          10 }
            =
                         5,
2,
3,
Part
            =
                                           6,
8 }
Part
                                                 8,
                                                       9 }
            =
                  12,
7,
2,
                               4,
Part[
                                     6,
         6]
7]
                         8
Part[
            =
                         3,
                                       }
Part
                         2,
2,
                                     7
5,
                   1,
                               6,
         81
Part
                                           9,
                               4,
                                                10 }
Part[
         9]
                   1,
2,
                                           8,
9 }
Part[
        10]
                         2,
                               6,
                                                 9,
                                                     10 }
            =
                                     5,
8 }
                         3,
                               4,
Part
        11
                    1,
                         3,
2,
7,
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                               7,
        12]
Part
            =
                               4,
Part[
                                                       9 }
        13]
                                                 8,
        14]
15]
16]
                                     9,
                               8,
                                          10<sup>'</sup>}
6 }
                   6,
PartL
            =
Part[
Part[
                   1,
                               4,
                                     5,
                    3,
                               9
            =
Part[
                                           8 }
                 ______
< Block Diagonal Solution Matrix >
              < Locations >
                0000000001
                1 2 3 4 5 6 7 8 9 0
              < Machines >
                0 0 0 0 0 0 0 0 0 0
                  0 0 0 0 0 0 0
                  5 9 1 2 6 7 8 3 0
             4
* *
< Parts >
              *
                1
          1
                  1
                       1
                              1
((
    1)
              *
     2)
          9
                1 1 1 1 1
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                                     1
              * 1 1 1
     3)
         11
              * 1
                                       *
     4)
         16
                    1
                                   1
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          3
              * 1
                     1 1 1 1
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              * 1
    8)
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    9)
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              *
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   10)
                         1 1
                                   1
                  1
              *
                                       *
   11)
                       1 1 1 1
                                     1 *
              *
   12)
         10
                     1 1 1 1 1 1
                       12
13
   13)
              *
                                       *
   14)
15)
                1
         14
              *
                     1
                            1 1 1
                                     1 *
         15
   16)
                1 1
                       1 1 1
             *
                       1 1 1
                                1 1
                                       *
   17)
< Machine cells and Part families >
Machine Cell[ 1] = { 4, 5, 9 }
Machine Cell[ 2] = { 1, 2, 6, 7, 8 }
Machine Cell[ 3] = { 3, 10 } --> Residual cell
      Family[ 1] = { 1, 9, 11, 16 }
Family[ 2] = { 2, 3, 4, 5, 6, 7, 8, 10, 12, 13, 14, 15, 17 }
Family[ 3] --> Empty Part family
Part
Part
Part
< Summary of the performance measures >
______
No. of machines
                                                   = 10
No. of part types
                                                   = 17
No. of cells
                                                   = 3
= 5
Machine cell size
```

Problem(113) --> Data file name : DC_44_Arkat(2011)_10x17.cfp

```
Total no. of 1's in the original MPIM: |A| = 80

Matrix density = 0.471

Total no. of within-block 1's = 53

No. of exceptional elements (EEs) = 27

No. of voids = 24

Sum of EEs and voids = 51

Group Cability Index (GCI) = 66.25 %

grouping efficiency (GE) = 69.90 %

Grouping efficacy (GF) = 50.96 %

Machine utilization (MU) = 68.83 %

No. of redundant machines (RMs) = 2
```

```
*
                                                                                            *
                           1
                                                   1
                                                                              1
                                                                                            *
                       1
                              1 1 1
       2)
               9
                    *
                               1
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                       1 1 \overline{1} \overline{1}
             10
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             11
                           1
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                    *
                           1 1
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             14
      6)
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                    *
             17
                       1 1
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      8)
             16
                                            1 1
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             18
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      9)
                                         1
                                            \begin{bmatrix} \bar{1} & \bar{1} & \bar{1} \\ 1 & 1 \end{bmatrix}
     10)
             19
                    *
                                         1
                                                             1
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                                                          1
             20
                                                                                     1
     11)
                    *
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     16)
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     17)
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    18)
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     19)
             13
                                                                                         1
     20)
                    *
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                                                                                            *
                                                                                  1
< Machine cells and Part families
         Family[ 1] = { 7, 8, 9, 10, 11, 14, 17 }
Family[ 2] = { 16, 18, 19, 20 }
Family[ 3] = { 2, 3, 4, 5, 6 }
```

Machine Cell[1] = { 6, 7, 8, 9, 14 }
Machine Cell[2] = { 16, 17, 18, 19, 20 }
Machine Cell[3] = { 2, 3, 5, 10, 11 }
Machine Cell[4] = { 1, 4, 12, 13, 15 } Part

< Summary of the performance measures >

```
______
No. of machines
No. of part types
No. of cells
                                                 = 20
= 20
                                                 = 4
= 5
Machine cell size
                                                 = 87
Total no. of 1's in the original MPIM : |A|
Matrix density
Total no. of within-block 1's
                                                 = 58
No. of exceptional elements (EEs)
                                                 = 29
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                                 = 42
                                                   71
                                                = 66.67 %
= 74.17 %
                                                 = 44.96 %
Grouping efficacy (GF)
Machine utilization (MU)
No. of redundant machines (RMs)
                                                 = 58.00 %
                                                 = 0
_____
```

< Summary of the performance measures >

```
______
No. of machines
No. of part types
No. of cells
                                              = 20
= 20
                                              = 4
Machine cell size
                                              = 5
Total no. of 1's in the original MPIM : |A|
                                              = 176
Matrix density
Total no. of within-block 1's
                                              = 81
No. of exceptional elements (EEs)
                                              = 95
No. of voids
Sum of EEs and voids
Group Cability Index (GCI)
grouping efficiency (GE)
                                              = 19
                                              = 114
                                             = 46.02 %
= 74.67 %
                                              = 41.54 %
Grouping efficacy (GF)
                                              = 81.00 %
Machine utilization (MU)
No. of redundant machines (RMs)
                                              = 0
_____
```