# Comparison between Adam variants

Here we compare different variations and implementations of Adam:

- 1. Adam The default Adam implementation included in Tensorflow 2.x.
- 2. my Adam My custom implementation of the same Adam algorithm using the Tensorflow API.
- 3. cAdam My proposed variant "centered Adam" using  $m_t$  as the estimate of  $\mathbb{E}[g_t]$ .
- 4. cAdam hat My proposed variant "centered Adam" using  $\hat{m}_t$  as the estimate of  $\mathbb{E}[g_t]$ .

#### best and worst values regarding training time

parameter name	best values						
training time	53.155	53.89	56.399	56.989	57.293		
neurons per layer	(50, 10)	(50, 10)	(50, 10)	(50, 10)	(50, 10)		
activation functions	ReLU	ReLU	ReLU	ReLU	ReLU		
last activation function	sigmoid	softmax	softmax	sigmoid	sigmoid		
loss function	cat-cross	cat-cross	cat-cross	cat-cross	cat-cross		
training data percentage	1.0	1.0	1.0	1.0	1.0		
number of epochs	50	50	50	50	50		
batch size	100	100	100	100	100		
optimizer	Adam	Adam	my Adam	cAdam	my Adam		
learning rate	0.001	0.001	0.001	0.001	0.001		
$\varepsilon$	$10^{-7}$	$10^{-7}$	$10^{-7}$	$10^{-7}$	$10^{-7}$		

**Table 0.1:** best settings regarding *training time* for the MNIST dataset

parameter name	worst values					
training time	56.989	57.293	58.796	59.013	59.761	
neurons per layer	(50, 10)	(50, 10)	(50, 10)	(50, 10)	(50, 10)	
activation functions	ReLU	ReLU	ReLU	ReLU	ReLU	
last activation function	sigmoid	sigmoid	softmax	softmax	sigmoid	
loss function	cat-cross	cat-cross	cat-cross	cat-cross	cat-cross	
training data percentage	1.0	1.0	1.0	1.0	1.0	
number of epochs	50	50	50	50	50	
batch size	100	100	100	100	100	
optimizer	cAdam	my Adam	cAdam	c adam hat	c adam hat	
learning rate	0.001	0.001	0.001	0.001	0.001	
$\varepsilon$	$10^{-7}$	$10^{-7}$	$10^{-7}$	$10^{-7}$	$10^{-7}$	

Table 0.2: worst settings regarding training time for the MNIST dataset

### parameter influence on training time

parameter name	parameter values		win ratios in %		avg. differences in s		best value
last activation	softmax	sigmoid	50.0	50.0	0.635	0.41	sigmoid
optimizer	Adam   my Adam	cAdam cAdam hat	100.0 0	0 0	0   3.324	4.37 5.864	Adam

Table 0.3: parameter influence regarding training time for the MNIST dataset

## best and worst values regarding accuracy

parameter name	best values					
test accuracy	0.96826	0.96692	0.96828	0.9686		
final validation accuracy	0.96788	0.96418	0.96795	0.96622		
training time	57.293	56.399	53.155	53.89		
neurons per layer	(50, 10)	(50, 10)	(50, 10)	(50, 10)		
activation functions	ReLU	ReLU	ReLU	ReLU		
last activation function	sigmoid	softmax	sigmoid	softmax		
loss function	cat-cross	cat-cross	cat-cross	cat-cross		
training data percentage	1.0	1.0	1.0	1.0		
number of epochs	50	50	50	50		
batch size	100	100	100	100		
optimizer	my Adam	my Adam	Adam	Adam		
learning rate	0.001	0.001	0.001	0.001		
$\varepsilon$	$10^{-7}$	$10^{-7}$	$10^{-7}$	$10^{-7}$		

Table 0.4: best settings regarding test accuracy for the MNIST dataset

parameter name	worst values					
test accuracy	0.96826	0.96788	0.96692	0.4184	0.18496	
final validation accuracy	0.96788	0.96762	0.96418	0.41733	0.18395	
training time	57.293	58.796	56.399	59.013	59.761	
neurons per layer	(50, 10)	(50, 10)	(50, 10)	(50, 10)	(50, 10)	
activation functions	ReLU	ReLU	ReLU	ReLU	ReLU	
last activation function	sigmoid	softmax	softmax	softmax	sigmoid	
loss function	cat-cross	cat-cross	cat-cross	cat-cross	cat-cross	
training data percentage	1.0	1.0	1.0	1.0	1.0	
number of epochs	50	50	50	50	50	
batch size	100	100	100	100	100	
optimizer	my Adam	cAdam	my Adam	c adam hat	c adam hat	
learning rate	0.001	0.001	0.001	0.001	0.001	
$\varepsilon$	$10^{-7}$	$10^{-7}$	$10^{-7}$	$10^{-7}$	$10^{-7}$	

Table 0.5: worst settings regarding test accuracy for the MNIST dataset

## parameter influence on accuracy

parameter name	parameter values		win ratios in %		avg. differences		best value
last activation	softmax	sigmoid	50.0	50.0	0.0	0.058	softmax
optimizer	Adam   my Adam	cAdam cAdam hat	50.0 0	50.0 0	0.0   0.001	0.0 0.667	Adam

 Table 0.6: parameter influence regarding test accuracy for the MNIST dataset