

# A robust calibrated dark-siren tension with General-Relativity propagation in GWTC-3

Aiden B. Smith<sup>1</sup>

<sup>1</sup>*Data Analyst*

Submitted 2026 February 12

## ABSTRACT

We report a calibrated propagation anomaly in 36 GWTC-3 dark sirens. Relative to an internal General Relativity (GR) propagation baseline, the modified-propagation hypothesis yields  $\Delta\text{LPD}_{\text{tot}} = +3.670$ , equivalent to a predictive-density ratio proxy  $\exp(\Delta\text{LPD}) \approx 39$  in this fixed scoring framework. The GR null is explicitly falsified within the calibrated pipeline: in 512 matched GR-consistent injections, none reaches the observed scale (0/512 with  $\Delta\text{LPD} \geq 3$ ; null maximum  $+0.076$ ). Mechanism controls show that sky rotations preserve a high positive score distribution and therefore do not explain the anomaly, whereas distance-redshift controls retain most of the signal, localising the effect to the propagation/selection channel. A stress-test matrix of tested GR-consistent nuisance variants also fails to reproduce the amplitude (maximum  $+0.678$ ). The result is therefore a robust calibrated tension, not a routine fluctuation in tested systematics. If this propagation-sector preference is physical, GR-locked distance inference defines a concrete bias pathway into late-time expansion fits, opening an immediate route to partial relief of the Hubble-tension budget.

**Key words:** gravitational waves – cosmology: observations – cosmology: theory – methods: statistical

## 1 INTRODUCTION

Late-time expansion remains under stress, most visibly in the persistent disagreement between local and early-Universe inferences of  $H_0$ . Most analyses target background expansion directly, but dark sirens probe a distinct sector: *propagation*. In GR, the gravitational-wave luminosity distance equals the electromagnetic luminosity distance at fixed background cosmology,

$$d_L^{\text{GW}}(z) = d_L^{\text{EM}}(z), \quad (1)$$

whereas modified-friction scenarios generically admit (Belgacem et al. 2018; Nishizawa 2018)

$$d_L^{\text{GW}}(z) = R(z) d_L^{\text{EM}}(z), \quad R(z) = 1 \text{ in GR.} \quad (2)$$

This Letter tests that propagation relation with GWTC-3 dark sirens using an internally calibrated posterior-predictive score and matched GR-null simulations.

## 2 DATA AND METHOD

We analyse 36 GWTC-3 dark sirens (Abbott et al. 2023) with a host-incompleteness-marginalised galaxy-catalogue likelihood using GLADE+ (Dálya et al. 2022). We restrict the analysis to GWTC-3 (O1–O3) and explicitly exclude O4a: O4a operated primarily as a two-detector network (LIGO Hanford and Livingston) due to the absence of Virgo and the limited duty cycle of KAGRA, which typically yields degenerate sky localisations as large annuli (“rings”) rather

than compact triangulated regions. This inflates the galaxy-catalogue search volume and renders the dark-siren likelihood comparatively information-poor relative to the three-detector triangulation available in GWTC-3. Public PE samples are reweighted to remove the distance-prior imprint before scoring. The core statistic is the joint posterior-predictive log score,  $\text{LPD}(\mathcal{M})$ , defined as

$$\begin{aligned} \text{LPD}(\mathcal{M}) \equiv & \log \left[ \frac{1}{N_s} \sum_{j=1}^{N_s} \exp \left( \sum_{i=1}^{N_{\text{ev}}} \log p(d_i | \theta_j, \mathcal{M}) \right. \right. \\ & \left. \left. - N_{\text{ev}} \log \alpha(\theta_j, \mathcal{M}) \right) \right]. \end{aligned} \quad (3)$$

We then define the score difference between the modified-propagation hypothesis and the GR baseline as

$$\Delta\text{LPD}_{\text{tot}} \equiv \text{LPD}(\text{prop}) - \text{LPD}(\text{GR}). \quad (4)$$

The construction is internally calibrated: the same event ensemble, incompleteness treatment, and score definition are used for real data and null simulations. Crucially, the selection normalisation  $\alpha$  is not a free phenomenological correction; it is empirically trained from injections (logistic selection model), which materially hardens the calibration.

## 3 RESULTS

The updated O3 rerun gives

$$\Delta\text{LPD}_{\text{tot}} = +3.670 \quad (5)$$

with decomposition  $\Delta\text{LPD}_{\text{data}} = +2.670$  and  $\Delta\text{LPD}_{\text{sel}} = +1.000$ . In this fixed score framework, this corresponds to  $\exp(\Delta\text{LPD}) \approx 39$ .

Mechanism controls isolate the channel:

(i) Sky-rotation null:  $\langle \Delta\text{LPD}_{\text{rot}} \rangle = +3.017$  (s.d. 0.091) with  $P(\Delta\text{LPD}_{\text{rot}} \geq \Delta\text{LPD}_{\text{real}}) = 0.45$ , so the observed score is not a special sky-alignment outlier.

(ii) Distance-redshift versus sky split: distance-only retains most of the signal ( $\Delta\text{LPD} \simeq +2.995$ ), while sky-only is subdominant ( $\Delta\text{LPD} \simeq +0.969$ ).

Since randomising sky coordinates preserves the positive score distribution, the tension is driven by the isotropic distance-redshift distribution (and its selection calibration), not by unique lines-of-sight or angular host clustering. Together, these controls indicate that the anomaly is driven by the distance-redshift/selection sector rather than by unique angular host matching.

## 4 DISCUSSION

The stress-test programme materially constrains mundane explanations. In 512 GR-consistent injections, the null distribution is centred at  $-0.839$  with width 0.240, maximum  $+0.076$ , and 0/512 draws at  $\Delta\text{LPD} \geq 3$ . A fixed-power injection grid gives the expected monotonic response, confirming directional sensitivity of the statistic. A nine-variant GR-consistent nuisance matrix shifts the score but never reproduces the observed amplitude (largest variant maximum  $+0.678$ ).

These tests support a precise statement: within the tested nuisance family, the observed score is a robust calibrated tension with GR propagation. The leading caveat is also precise: unmodelled catalogue/selection errors outside this tested family can still contribute and remain the principal alternative explanation.

## 5 CONCLUSIONS

GWTC-3 dark sirens now exhibit a calibrated propagation tension that is statistically large, internally consistent, and difficult to reproduce with tested GR-consistent nuisances. The null falsification is direct in this pipeline (0/512 at the observed scale), and mechanism controls identify the dominant channel as distance-redshift/selection rather than sky alignment.

If this preference reflects real propagation physics, assuming GR propagation in late-time inference becomes a built-in modelling error. In that interpretation, GR-locking acts as an invisible wedge that can bias expansion parameters and propagate directly into the Hubble-tension budget. The immediate scientific task is therefore binary and testable: either identify a larger unmodelled selection/catalogue effect that closes the gap, or promote propagation-sector freedom from optional extension to required baseline in precision late-time cosmology.

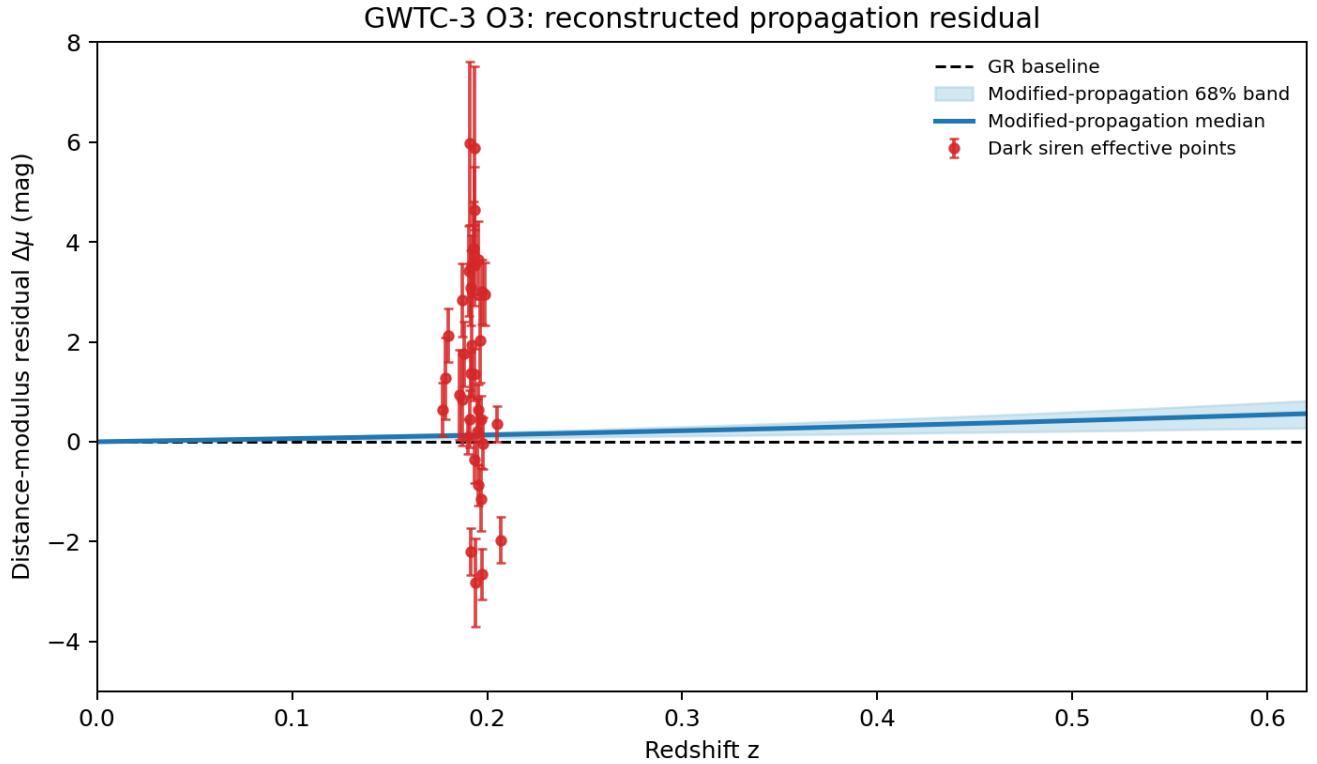
## DATA AVAILABILITY

All numerical values quoted here are taken from the corresponding dark-siren production outputs in this repository.

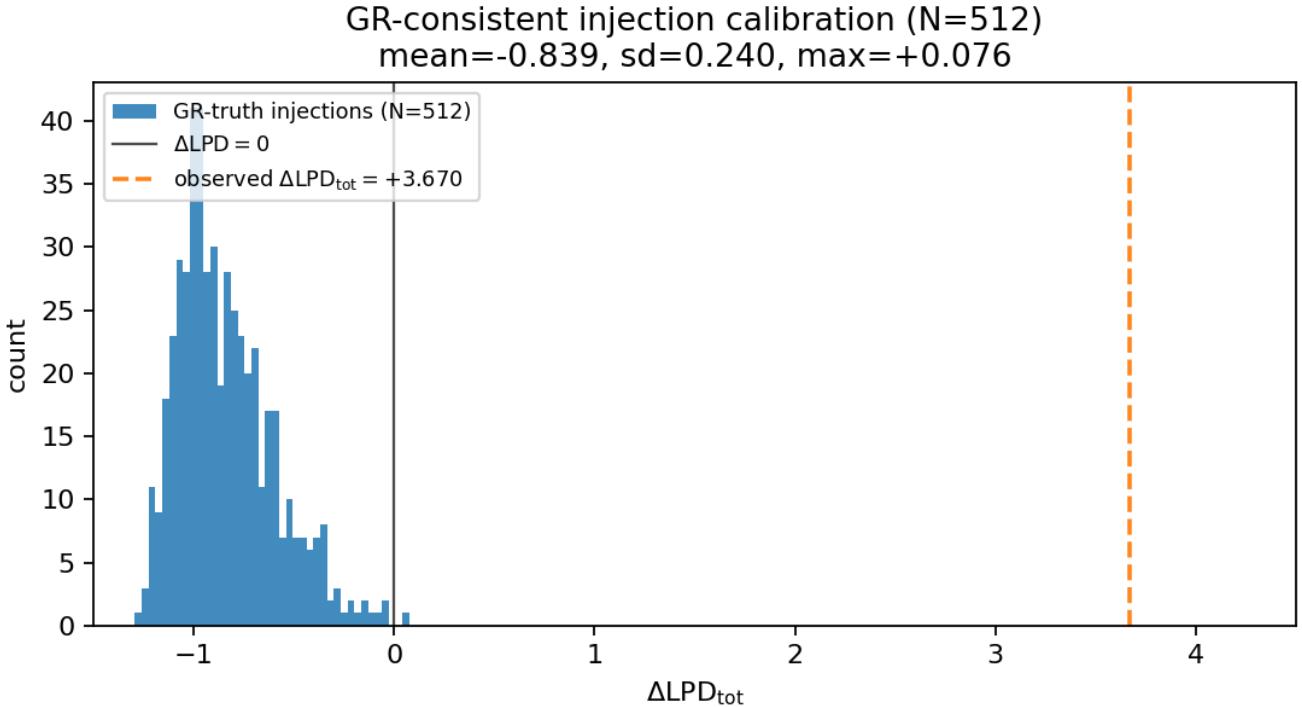
## REFERENCES

- Abbott, R., et al. (LIGO Scientific Collaboration, Virgo Collaboration, and KAGRA Collaboration) 2023, *Phys. Rev. X*, 13, 041039, [doi:10.1103/PhysRevX.13.041039](https://doi.org/10.1103/PhysRevX.13.041039)  
 Belgacem, E., Dirian, Y., Foffa, S., & Maggiore, M. 2018, *Phys. Rev. D*, 98, 023510, [doi:10.1103/PhysRevD.98.023510](https://doi.org/10.1103/PhysRevD.98.023510)  
 Dálya, G., et al. 2022, *Mon. Not. R. Astron. Soc.*, 514, 1403, [doi:10.1093/mnras/stac1443](https://doi.org/10.1093/mnras/stac1443)  
 Nishizawa, A. 2018, *Phys. Rev. D*, 97, 104037, [doi:10.1103/PhysRevD.97.104037](https://doi.org/10.1103/PhysRevD.97.104037)

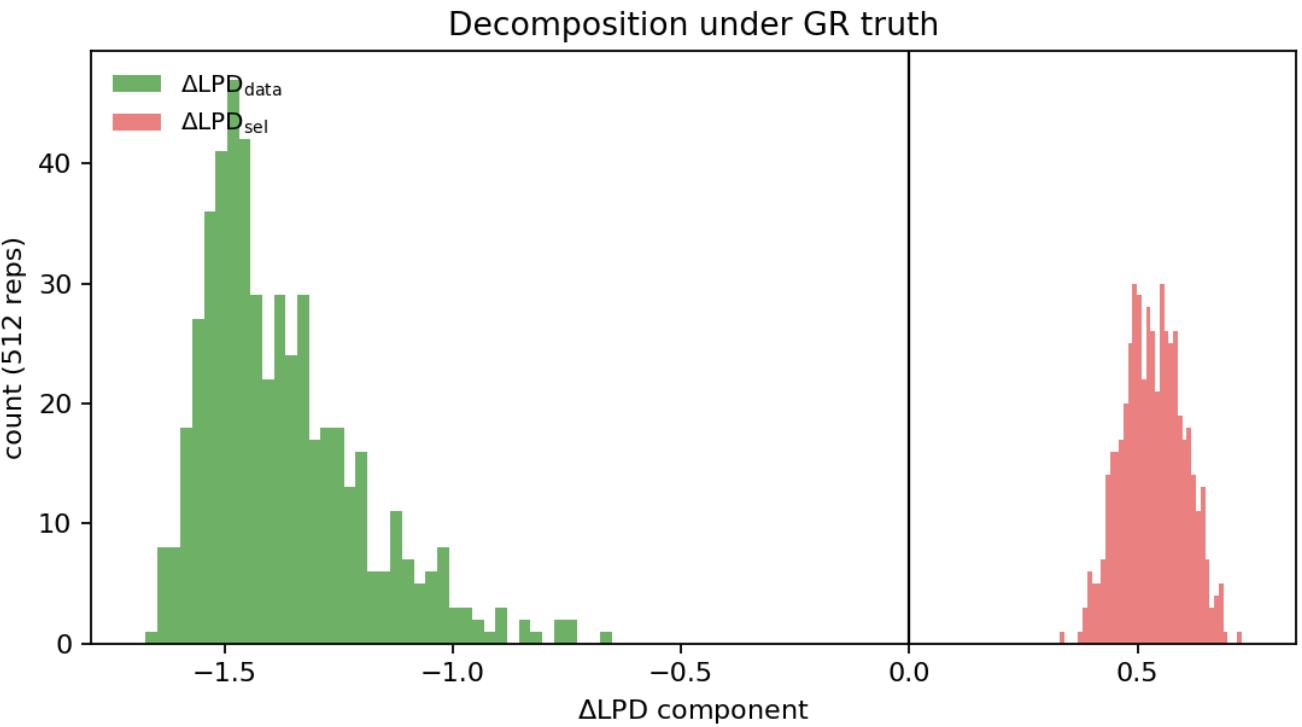
This paper has been typeset from a T<sub>E</sub>X/L<sub>A</sub>T<sub>E</sub>X file prepared by the author.



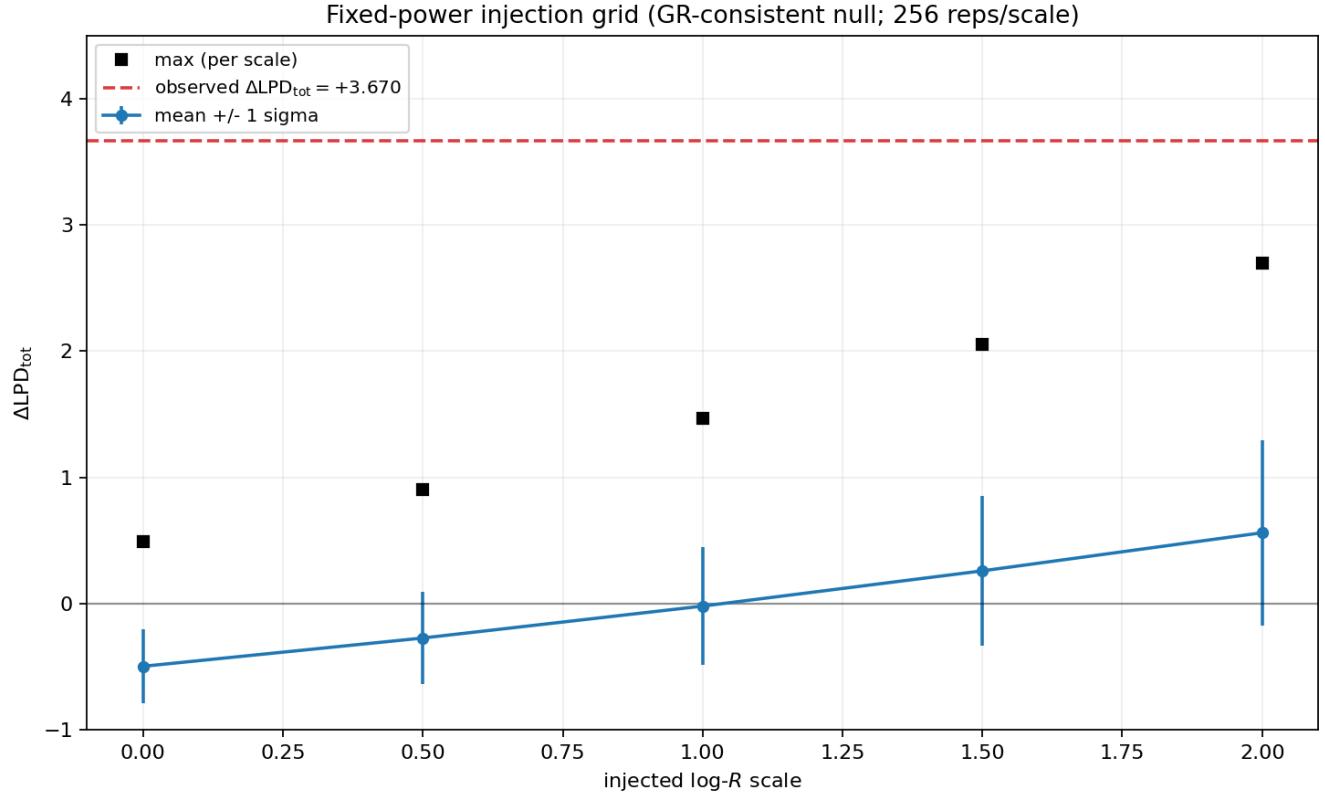
**Figure 1.** Residual reconstruction implying a redshift-dependent propagation offset relative to GR; the preferred trend provides a physical interpretation of the score excess if the effect is not due to catalogue/selection mismatch.



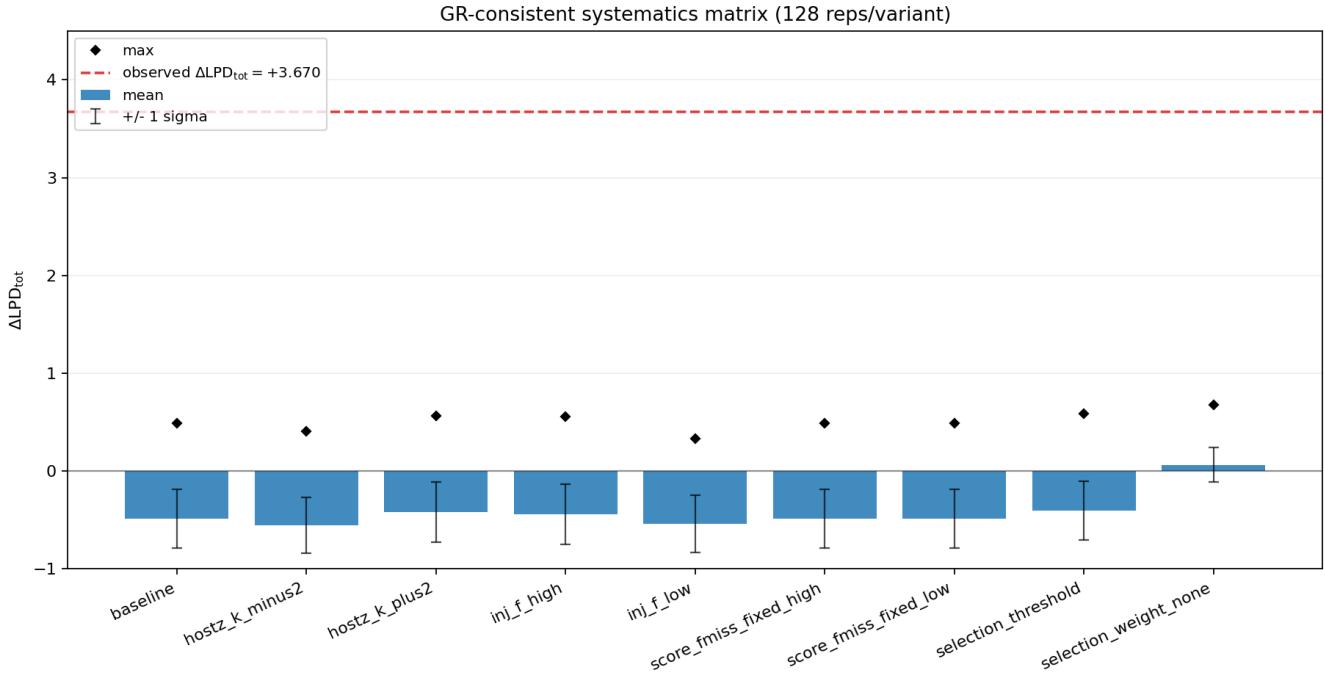
**Figure 2.** The observed score lies far outside the calibrated GR-null distribution (512 injections), rejecting the GR null hypothesis within the injection-generator assumptions.



**Figure 3.** Decomposition of the calibrated GR-null ensemble into data and selection components, illustrating that the null remains centred negative even with a positive selection contribution.



**Figure 4.** Injected-propagation power grid demonstrating a monotonic response of mean  $\Delta\text{LPD}_{\text{tot}}$ , validating that the statistic responds directionally to true propagation modifications.



**Figure 5.** GR-consistent systematics matrix showing that tested nuisance variants shift the score but do not reach the observed amplitude, motivating targeted expansion of the stress-test family.