

Observation of Three Resonant Structures in the Cross Section of $e^+e^- \rightarrow \pi^+\pi^-h_c$

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Using e^+e^- collision data collected with the BESIII detector operating at the Beijing electron positron collider, the cross section of $e^+e^- \rightarrow \pi^+\pi^-h_c$ is measured at 59 points with center-of-mass energy \sqrt{s} ranging from 4.009 to 4.950 GeV with a total integrated luminosity of 22.2 fb^{-1} . The cross section between 4.3 and 4.45 GeV exhibits a plateau-like shape and drops sharply around 4.5 GeV, which cannot be described by two resonances only. Three coherent Breit-Wigner functions are used to parametrize the \sqrt{s} -dependent cross section line shape. The masses and widths are determined to be $M_1 = (4223.6^{+3.6+2.6}_{-3.7-2.9}) \text{ MeV}/c^2$, $\Gamma_1 = (58.5^{+10.8+6.7}_{-11.4-6.5}) \text{ MeV}$, $M_2 = (4327.4^{+20.1+10.7}_{-18.8-9.3}) \text{ MeV}/c^2$, $\Gamma_2 = (244.1^{+34.0+24.2}_{-27.1-18.3}) \text{ MeV}$, and $M_3 = (4467.4^{+7.2+3.2}_{-5.4-2.7}) \text{ MeV}/c^2$, and $\Gamma_3 = (62.8^{+19.2+9.9}_{-14.4-7.0}) \text{ MeV}$. The first uncertainties are statistical and the second are systematic. The inclusion of the relatively narrower third component proves crucial for reproducing the drop at around 4.5 GeV. The statistical significance of the three-resonance assumption over the two-resonance assumption is greater than 5σ .

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The study of vector charmoniumlike states ($J^{PC} = 1^{--}$, known as Y states) has generated significant interest. The overpopulation of these Y states have led to exotic interpretations, including hybrid [1–5], tetraquark [6,7], molecule [8–11], and hadrocharmonium states [12,13], or kinematically induced peaks [14]. Meanwhile, the possibility that these states are excited charmonium states cannot be completely ruled out [15–17]. According to calculations based on an unquenched potential model, the $4S - 3D$ and $5S - 4D$ mixing charmonium states are predicted to lie between 4.2 and 4.5 GeV/ c^2 , with widths ranging from 30 to 80 MeV [16], the $\psi(4230)$, $\psi(4360)$, $\psi(4415)$, and $\psi(4500)$ are assigned to be these states. Precise measurement of their properties is essential to unraveling their nature.

Among the processes in which the Y states are observed, those containing h_c in the final state are particularly interesting. This is because transitions between vector charmonium states and h_c are expected to be suppressed due to heavy quark spin symmetry, so a strong coupling is indicative of an exotic internal structure, such as hybrid configurations [18,19]. The $e^+e^- \rightarrow \pi^+\pi^-h_c$ process was first observed by the CLEO Collaboration at a center-of-mass (c.m.) energy $\sqrt{s} = 4.17 \text{ GeV}$ [20]. Subsequently, the BESIII experiment studied the $e^+e^- \rightarrow \pi^+\pi^-h_c$ cross

section with \sqrt{s} ranging from 3.896 to 4.600 GeV and observed the $Y(4220)$ and $Y(4390)$ [21]. Figure 1 presents the resonance parameters of $Y(4220)$ and $Y(4390)$ alongside those obtained from other processes [22–31], based on the BESIII scan samples. In the $Y(4390)$ region, resonances observed in different processes show significant variation in mass and width. At higher energies, new vector structures around 4.75 GeV have been reported by BESIII in $e^+e^- \rightarrow K\bar{K}\eta/\psi$ [30,31] and $e^+e^- \rightarrow D_s^*D_s^*$ [32] processes. The decays of these higher Y states to h_c have not been investigated yet.

In this Letter, we report a measurement of the $e^+e^- \rightarrow \pi^+\pi^-h_c$ cross section at \sqrt{s} from 4.009 to 4.950 GeV. The data are collected with the BESIII detector [34] and include three sets: 19 energy points with large statistics [21] (referred to as XYZ-I), 25 energy points with lower statistics (referred to as XYZ-II), and 15 energy points, each with statistics of 8 pb^{-1} (referred to as R-scan). The integrated luminosity of these samples is 22.2 fb^{-1} , determined from large-angle Bhabha events with an uncertainty of 1% [35,36]. The c.m. energies for the XYZ-I and XYZ-II samples are determined from $e^+e^- \rightarrow \mu^+\mu^-$ or $e^+e^- \rightarrow \Lambda_c\bar{\Lambda}_c$ events [36–38], those for the R-scan samples are measured using multihadron final states.

In this Letter, the h_c is reconstructed via its electric-dipole transition $h_c \rightarrow \gamma\eta_c$ with $\eta_c \rightarrow X_i$, where X_i signifies 16 exclusive hadronic final states: $p\bar{p}$, $2(\pi^+\pi^-)$, $2(K^+K^-)$, $\pi^+\pi^-K^+K^-$, $\pi^+\pi^-p\bar{p}$, $3(\pi^+\pi^-)$, $2(\pi^+\pi^-)K^+K^-$, $K_S^0K^\pm\pi^\mp$, $K_S^0K^\pm\pi^\mp\pi^+$, $K^+K^-\pi^0$, $p\bar{p}\pi^0$, $K^+K^-\eta$, $\pi^+\pi^-\eta$, $2(\pi^+\pi^-)\eta$, $\pi^+\pi^-\pi^0\pi^0$, and $2(\pi^+\pi^-\pi^0)$. The K_S^0 is reconstructed using its decay to $\pi^+\pi^-$, while π^0 and η are reconstructed through their $\gamma\gamma$ final state.

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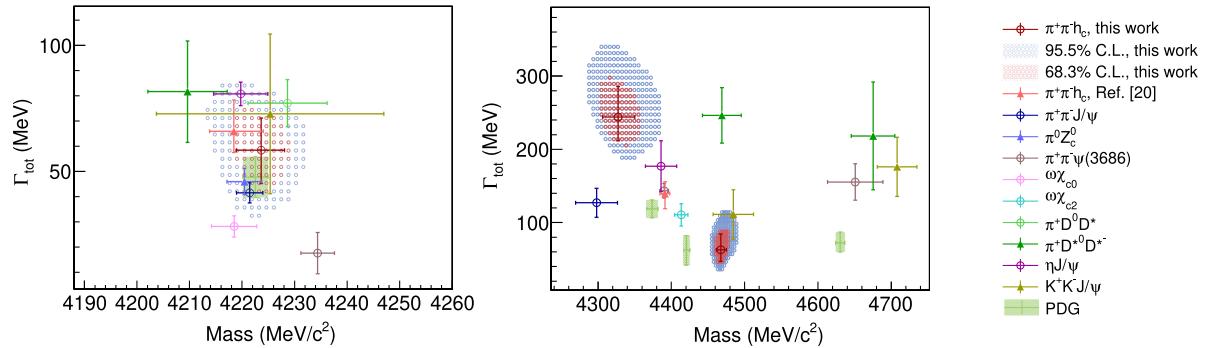


FIG. 1. Comparison of resonance parameters from hidden-charm or open-charm processes [21–31] (represented by dots with error bars in various colors), along with the parameters of $\psi(4230)$, $\psi(4360)$, $\psi(4415)$, and $\psi(4660)$ from PDG [33] (indicated by the green shaded square). The red and blue shaded regions represent the 68.3% and 95.5% C.L. regions determined in this Letter.

Monte Carlo (MC) samples are used to determine the detection efficiencies and to estimate the background contributions. They are produced with a GEANT4-based [39] simulation software package, which includes the geometric description of the BESIII detector and the detector response. The simulation models the beam energy spread and initial state radiation (ISR) in the e^+e^- annihilations with the generator KKMC [40]. The maximum energy of the ISR photon for the $e^+e^- \rightarrow \pi^+\pi^-h_c$ process corresponds to its kinematical threshold. The inclusive MC sample includes the production of open-charm processes, the ISR production of vector charmonium(-like) states, and the continuum processes. All particle decays are modeled with EVTGEN [41] using branching fractions either taken from Particle Data Group [33], when available, or otherwise estimated with LUNDCHARM [42]. Final state radiation from charged final state particles is incorporated using the PHOTOS package [43].

The event selection method is similar to the one used in Ref. [21]. However, the mass windows of π^0 , η , and η_c and the requirement of χ_{4C}^2 are re-optimized to enhance the signal-to-background ratio. For the $\eta_c \rightarrow \pi^+\pi^-\pi^0\pi^0$ and $\eta_c \rightarrow 2(\pi^+\pi^-\pi^0)$ modes, we further require $\chi_{4C}^2 < \chi_{4C,\pm\gamma}^2$, where χ_{4C}^2 is taken from a four-constraint (4C) kinematic fit of all selected final state particles with respect to the initial e^+e^- four momentum, and $\chi_{4C,\pm\gamma}^2$ is taken from the 4C kinematic fit that includes or excludes one photon. Figure 2 shows the invariant mass distribution of $\eta\eta_c$ ($M_{\eta\eta_c}$) in the η_c signal region for the sum of the 16 decay channels at $\sqrt{s} = 4.236$ GeV. A clear $h_c \rightarrow \eta\eta_c$ signal is observed. The background events are distributed linearly in the $M_{\eta\eta_c}$ distribution, in agreement with the analysis of the inclusive MC sample.

The $e^+e^- \rightarrow \pi^+\pi^-h_c$ signal events yield is determined by performing an unbinned maximum likelihood fit to the $M_{\eta\eta_c}$ spectrum. The signal contribution is modeled using the MC simulated shape, convolved with a Gaussian function, which accounts for the resolution difference between data and the MC simulation. The background

contribution is described by a linear function. For the XYZ-I data sample, a simultaneous fit to the 16 η_c decay modes is performed. The numbers of signal events in each mode are constrained according to the detection efficiencies and branching fractions. For the XYZ-II data sample, the $M_{\eta\eta_c}$ spectra summed over the 16 η_c decay modes are fitted (referred to as the summed fit). Additionally, the parameters of the Gaussian function are fixed to the average values obtained from the fits to the XYZ-I data sample. The consistency between the results from the simultaneous fit and the summed fit is confirmed with the XYZ-I data sample. For the R-scan data sample, the summed fit method is used, with the background shape fixed according to that obtained from the summed fit to the XYZ-I and XYZ-II data sample in the range $4.3 \text{ GeV} < \sqrt{s} < 4.8 \text{ GeV}$.

The Born cross section σ^{Born} is calculated via

$$\frac{N^{\text{obs}}}{\mathcal{L} \cdot (1 + \delta) \cdot (1/|1 - \Pi|^2) \cdot \mathcal{B}(h_c \rightarrow \gamma\eta_c) \cdot \sum_{i=1}^{16} \epsilon_i \mathcal{B}(\eta_c \rightarrow X_i)}, \quad (1)$$

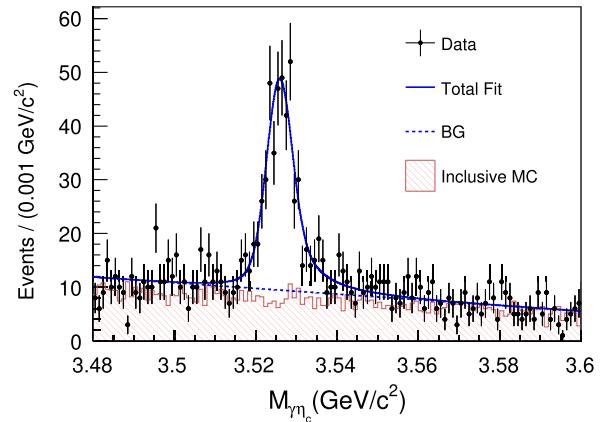


FIG. 2. The $M_{\eta\eta_c}$ distribution in the η_c signal region at $\sqrt{s} = 4.236$ GeV. Dots with error bars are the data, the solid curve is the best fit result, and the dashed curve represents the background contribution.

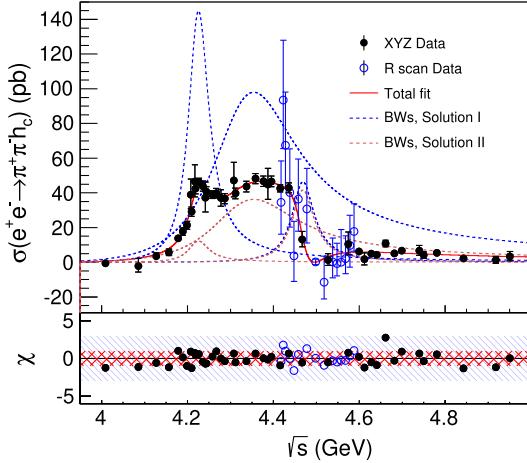


FIG. 3. Fit to the dressed cross section for the two solutions for $e^+e^- \rightarrow \pi^+\pi^-h_c$ with the baseline model (the red curve). The blue and red dashed curves are contributions from the three structures. The dots with error bars are the converged cross section. The bottom panel shows the χ values, in which the red and blue shadings represent ± 1 and ± 3 , respectively.

where N^{obs} , \mathcal{L} , $(1 + \delta)$, and $(1/|1 - \Pi|^2)$ are the signal yields, the integrated luminosity, the ISR correction factor, and the vacuum polarization correction factor, respectively. For the i th η_c decay mode, ϵ_i represents the detection efficiency, and $\mathcal{B}(\eta_c \rightarrow X_i)$ denotes the branching fraction. The branching fractions of $h_c \rightarrow \gamma\eta_c$ and the η_c decays are taken from previous BESIII measurements [44,45]. The cross section is obtained through an iterative procedure, since both the ISR factor and the detection efficiency depend on the cross section line shape [46]. The procedure adopts the dressed cross section as its input, which is the product of the Born cross section and the vacuum polarization correction factor. The dressed cross sections are shown in Fig. 3 and summarized in the Supplemental Material [47], together with all the inputs used in the calculation.

The \sqrt{s} -dependent dressed cross section is fitted using a maximum likelihood method to investigate the vector resonance structures. The best fit is achieved with a model incorporating three coherent Breit-Wigner (BW) functions (the baseline model), which is written as

$$|BW_1(\sqrt{s}) + e^{i\phi_2}BW_2(\sqrt{s}) + e^{i\phi_3}BW_3(\sqrt{s})|^2. \quad (2)$$

Here, BW_k with $k = 1, 2$, or 3 is used to describe the resonance, defined as

$$\frac{M_k}{\sqrt{s}} \cdot \frac{\sqrt{12\pi(\Gamma_{ee}\mathcal{B}(R_k \rightarrow \pi^+\pi^-h_c))_k\Gamma_k}}{s - M_k^2 + iM_k\Gamma_k} \cdot \sqrt{\frac{PS(\sqrt{s})}{PS(M_k)}}. \quad (3)$$

In the fit, the mass M_k , the total width Γ_k , the product of the electromagnetic width and the branching fraction

$[\Gamma_{ee}\mathcal{B}(R_k \rightarrow \pi^+\pi^-h_c)]_k$, and the relative phase ϕ_k are free parameters.

In the baseline model, four solutions with two sets of parameters are found in accordance with expectations [48]. The fit results are shown in Fig. 3, and the resonance parameters are listed in Table I. The mass versus width plots for the three resonance structures, along with the 68.3% and 95.5% confidence level (CL) contours are shown in Fig. 1, together with the resonance parameters of vector charmonium(-like) states observed in other processes. The parameters of the first resonance are consistent with those reported for $Y(4220)$ by BESIII. However, the mass and width of the second resonance [$M = (4327.4^{+20.1}_{-18.8}) \text{ MeV}/c^2$, $\Gamma_{\text{tot}} = (244.1^{+34.0}_{-27.1}) \text{ MeV}$] are found to be 60 MeV/c^2 lower and 100 MeV wider compared to the reported values for $Y(4390)$ from previous study of the same process [$M = (4391.6 \pm 6.3 \pm 1.0) \text{ MeV}/c^2$, $\Gamma_{\text{tot}} = (139.5 \pm 16.1 \pm 0.6) \text{ MeV}$] [21,47]. This discrepancy arises from the inclusion of a third resonance in this Letter. The model using two coherent BW functions cannot describe the dip in the cross section at $\sqrt{s} = 4.498 \text{ GeV}$ [47]. The fit quality is calculated to be $\chi^2/\text{ndf} = 77.9/66$ in the two-resonance fit and $41.9/70$ when the third resonance is added. Result of the two-resonance fit is shown in Supplemental Material [47]. The statistical significance of the third resonance is 5.4σ , estimated by utilizing the changes in likelihood values [$\delta(-2 \ln L) = 38.8$] and the number of degrees of freedom [$\delta(\text{ndf}) = 4$].

Several parametrization models are tested. Adding one resonance with free parameters or a phase space term [$PS(\sqrt{s})/s^n$] to the baseline model slightly improves the fit quality. The statistical significance of this fourth resonance (or phase space term) is 0.7σ (0.1σ), where $PS(\sqrt{s})$ is the three-body phase space factor. The model used in Ref. [14] is also tested, yielding a nonconvergent fit. The cross section is then updated using the baseline model as input cross section line shape and iterated until convergence.

Systematic uncertainties in the cross section measurement come mainly from the integrated luminosity, the statistical uncertainties of the c.m. energy for the R-scan data sample, the input cross section line shape, the branching fractions, the detection efficiency, and the determination of N^{obs} . The uncertainty of the integrated luminosity is 1% [35,36]. The effect from the statistical uncertainties of the c.m. energy for the R-scan data sample is estimated by shifting \sqrt{s} by $\pm 1 \text{ MeV}$. The uncertainty from the parametrization of the cross section line shape is estimated by adding a phase space term to Eq. (2). The difference is 1%, and is taken as the uncertainty. The uncertainty of the cross section is reflected by the uncertainty of the parameters in the formula used to describe the cross section line shape. This is estimated by sampling these parameters according to the covariance matrix and recalculating the ISR factor, and the standard deviation of

TABLE I. The fit results from the baseline model. The first uncertainty is statistical and second systematic. The numbers in brackets are from the second solution with equal fit quality.

Parameter	R_1	R_2	R_3
M (MeV/ c^2)	$4223.6^{+3.6+2.6}_{-3.7-2.9}$	$4327.4^{+20.1+10.7}_{-18.8-9.3}$	$4467.4^{+7.2+3.2}_{-5.4-2.7}$
Γ (MeV)	$58.5^{+10.8+6.7}_{-11.4-6.5}$	$244.1^{+34.0+24.2}_{-27.1-18.3}$	$62.8^{+19.2+9.9}_{-14.4-7.0}$
$\Gamma_{ee} \cdot \mathcal{B}(R \rightarrow \pi^+ \pi^- h_c)$ (eV)	$10.2^{+1.2+1.4}_{-1.5-1.4} (0.9^{+0.4+0.3}_{-0.4-0.2})$	$29.1^{+5.7+4.4}_{-3.9-3.4} (10.8^{+2.5+1.9}_{-1.8-1.5})$	$3.9^{+3.5+1.7}_{-1.7-0.5} (3.5^{+3.0+1.5}_{-1.6-0.7})$
ϕ (rad)	...	$3.6^{+0.1+0.1}_{-0.1-0.1} (0.7^{+0.3+0.2}_{-0.3-0.2})$	$0.7^{+0.3+0.1}_{-0.3-0.2} (-2.2^{+0.3+0.2}_{-0.3-0.1})$

the resultant distribution is taken as the systematic uncertainty. The combined branching fractions $\mathcal{B}(h_c \rightarrow \gamma \eta_c) \cdot \mathcal{B}(\eta_c \rightarrow X_i)$ are taken from Ref. [44], updated with the latest measurement of $\psi(3686) \rightarrow \pi^0 h_c$ from BESIII [45], giving an uncertainty of 9.7%.

The uncertainty related to the detection efficiency contains the tracking efficiency, photon reconstruction, K_S^0 reconstruction, π^0/η mass window, η_c mass window, χ^2_{4C} requirement, and intermediate states in πh_c and $\pi^+ \pi^-$ system. The first four terms are not added in this Letter since they are included in the branching fraction of η_c . The uncertainties of the two additional pion tracks accompanying the h_c are also included (1% per track). The uncertainties from the mass, width [33], and line shape of η_c [49] used in MC simulations are estimated by varying them within uncertainties or adding the missing terms and check the difference in detection efficiencies, which are 1.1% for the η_c parameters and 0.2% for the line shape. The uncertainty from the applied requirement on the χ^2_{4C} value is estimated by correcting the helix parameter of charged particles to match the resolution in data [50]. The uncertainty from the requirement of $\chi^2_{4C} < \chi^2_{4C,\pm\gamma}$ is estimated by removing this requirement and repeating the analysis. The systematic uncertainties for the two aforementioned terms are 2.1% and 2.3%, respectively. The uncertainty from the intermediate states in πh_c and $\pi^+ \pi^-$ system is estimated by reweighting the MC simulation using a Dalitz plot obtained from data, and is 8.0%, 12.5%, and 3.5% for data the samples at $\sqrt{s} = 4.189$ GeV, $\sqrt{s} = 4.199$ GeV, and the other c.m. energies.

The uncertainties in the determination of N^{obs} are estimated by varying the fit conditions and observing the resulting changes in the cross section results. Uncertainties from the fixed parameters in the fit, including the mass resolution difference between data and MC simulation for XYZ-II and R-scan data sample, as well as the background shape for R-scan data sample, are estimated by adjusting each parameter by 1 standard deviation. To access the uncertainty from the background shape, the linear function is replaced with a second order Chebyshev function, the impact on the results is negligible. The uncertainty from the fit range is tested by modifying the nominal fit range by ± 5 and ± 10 MeV/ c^2 and examining the uncorrelated

uncertainty as outlined in [51,52], which is found negligible. The total systematic uncertainty in the $e^+ e^- \rightarrow \pi^+ \pi^- h_c$ cross section measurement, listed in Supplemental Material [47], is determined by assuming these sources as independent.

The systematic uncertainties for the parameters of the resonance structures are summarized in Table II. They primarily arise from the systematic and statistical uncertainties of the c.m. energy, the beam energy spread, the systematic uncertainty of the cross section, and the choice of the parametrization model. The impact of the systematic uncertainty in the c.m. energy measurement is 0.6 MeV [36–38] and only affects the mass measurements. The effect from the statistical uncertainty in c.m. energy measurement for the R-scan data sample is estimated by randomly modifying the corresponding \sqrt{s} values according to a Gaussian function with mean 0 and standard deviation 1 MeV, and reevaluating the resonance parameters.

The uncertainties from cross section measurement are divided into two classes. “Cross section I” relates to the uncorrelated terms, including the mass resolution difference between data and MC simulation, fixed background shape for the R-scan sample, ISR factor, and uncorrelated systematic uncertainty terms in the detection efficiency (the requirement of $\chi^2_{4C} < \chi^2_{4C,\pm\gamma}$ and the intermediate states in $\pi \pi h_c$ system). They are considered by adding these terms to the statistical uncertainty. The systematic uncertainty for each parameter is calculated with $\sqrt{\delta_{w/o}^2 - \delta_{w/o}^2}$, where δ_w and $\delta_{w/o}$ are the uncertainties with and without the systematic terms included. “Cross section II” represents the correlated terms common to all data samples, estimated to be 10.2%. The uncertainty from the parametrization model is estimated by adding a phase space term to the baseline model. The cross section is obtained through an iterative procedure, since both the ISR factor and the detection efficiency depend on the cross section line shape [46]. The systematic uncertainty due to iteration stability is the maximum difference (1.0%) across all energy points between the final two iterations. The uncertainty from the beam energy spread is estimated by convolving a Gaussian function (with the standard deviation provided by the beam energy measurement system [53]) to the fit formula.

TABLE II. The systematic uncertainty in the measurement of resonance parameters of the Y states. The numbers in brackets indicate uncertainty of the second solution. Syst. and stat. refer to systematic and statistical uncertainties of the c.m. energy measurement, respectively.

Sources	R_1			R_2			R_3				
	M (MeV/ c^2)	Γ_{tot} (MeV)	$\Gamma_{ee} \cdot \mathcal{B}$ (%)	M (MeV/ c^2)	Γ_{tot} (MeV)	$\Gamma_{ee} \cdot \mathcal{B}$ (%)	ϕ (rad)	M (MeV/ c^2)	Γ_{tot} (MeV)	$\Gamma_{ee} \cdot \mathcal{B}$ (%)	ϕ (rad)
c.m. energy (syst.)	0.6	0.6	0.6
c.m. energy (stat.)	0.0	0.1	0.0 (0.3)	0.1	0.4	0.2 (0.2)	0.0 (0.0)	0.1	0.3	0.8 (0.6)	0.0 (0.0)
Cross section I	+2.5 -2.8	+6.4 -6.1	+8.1 (28.2) -8.0 (17.9)	+10.6 -9.1	+20.2 -13.1	+10.3 (11.1) -5.7 (4.3)	+0.1 (0.2) -0.1 (0.2)	+2.9 -2.4	+8.9 -6.1	+37.8 (38.4) -4.5 (14.6)	+0.1 (0.2) -0.2 (0.1)
Cross section II	10.2	10.2	10.2	...
Parametrization	0.4	1.8	3.2 (9.4)	1.1	12.3	0.7 (8.6)	0.0 (0.0)	0.8	2.4	3.9 (4.9)	0.1 (0.0)
Energy spread	+0.4 -0.3	+1.1 -1.3	+0.8 (3.3) -1.8 (3.4)	+0.7 -1.1	+5.1 -3.5	+4.0 (4.7) -1.1 (1.8)	+0.0 (0.0) -0.0 (0.0)	+0.9 -0.7	+3.6 -2.3	+19.3 (17.7) -1.7 (1.2)	+0.0 (0.0) -0.0 (0.0)
Total	+2.6 -2.9	+6.7 -6.5	+13.5 (31.6) -13.5 (22.9)	+10.7 -9.3	+24.2 -18.3	+15.1 (18.0) -11.8 (14.2)	+0.1 (0.2) -0.1 (0.2)	+3.2 -2.7	+9.9 -7.0	+43.8 (43.8) -12.0 (18.6)	+0.1 (0.2) -0.2 (0.1)

In summary, we measure the $e^+e^- \rightarrow \pi^+\pi^- h_c$ cross section at 59 energy points from $\sqrt{s} = 4.009$ to 4.951 GeV. The cross section between 4.3 and 4.45 GeV exhibits a plateau-like shape and has a dip at 4.5 GeV. The best description of the cross section line shape is achieved by the coherent sum of three BW functions. The significance of the third resonance is larger than 5σ . No obvious resonance structure is observed at around $\psi(4660)$, which is in tension with the theoretical prediction in a hidden charm P -wave tetraquark model [54].

The mass and width of the first resonance are consistent with the $\psi(4230)$ [33] and the observation in a previous Letter of the same process [21]. The mass of the second resonance is consistent with the $\psi(4360)$ [33], but the obtained width is about 100 MeV broader. It is noteworthy that the mass of the second resonance is much closer to the resonance observed in $e^+e^- \rightarrow \pi^+\pi^- J/\psi$ [22], with respect to the previous Letter [21]. The parameters of the third resonance are consistent with the $\psi(4500)$ found in K^+K^-J/ψ [30,31], whereas the mass is 40 MeV higher than the $\psi(4415)$.

The model proposed in Ref. [14] cannot describe the cross section line shape, where the structure around 4.39 GeV is attributed to the interference between $\psi(4160)$ and $\psi(4415)$. Subsequent studies predict two pairs of $S - D$ mixing vector charmonium states [16]. The masses of R_1 and R_2 align with the $4S - 3D$ mixing model; however, the width of R_2 significantly exceeds the predicted limit of $\Gamma_2 \leq 80$ MeV. While R_3 could be one of the $5S - 4D$ states, its expected partner is not seen. Additionally, the mass of R_2 and R_3 are also close to that of $\psi(3D)$, yet the large width of R_2 is incompatible with the model [15,17]. Notably, the mass and width of R_3 are consistent with a hybrid state prediction [4].

Reference [55] suggests $\mathcal{O}(10^2)$ eV $\lesssim \Gamma_{ee}^{Y(4260)} \lesssim \mathcal{O}(10^3)$ eV. Assuming $\Gamma_{ee}^{R_1, R_2} \in (10^2, 10^3)$ eV, we determine $\Gamma_{\pi^+\pi^- h_c}^{R_1} \in (0.05, 0.5)$ MeV or (0.6, 6.0) MeV and

$\Gamma_{\pi^+\pi^- h_c}^{R_2} \in (2.6, 26.4)$ MeV or (7.1, 71.0) MeV for the two solutions. $\Gamma_{\pi^+\pi^- h_c}^{R_1}$ lies within the upper limit $\Gamma_{\pi^+\pi^- h_c}^{\psi(4230)} < 1.26$ MeV set by a molecular model calculation [8]. The $\Gamma_{\pi^+\pi^- h_c}^{R_1}$ is smaller than hybrid configuration predictions, which are $\Gamma_{h_c + l.h.}^{\psi(4230)} = 17(15)$ and $\Gamma_{h_c + l.h.}^{\psi(4360)} = 14(12)$ MeV, where $l.h.$ stands for light hadrons [5]. However, the model cannot be excluded due to large uncertainties of the theoretical result.

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Data availability—The data that support the findings of this Letter are openly available [57].

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