

Homework 1

Question 1. Please read chapters 0 and 1 of Chartrand et al. and write a couple sentences about a topic/example/concept that you found difficult or interesting and why?

Question 2. Let P, Q and R be statements. Determine whether the following is true.

$$P \oplus (Q \oplus R) \equiv (P \oplus Q) \oplus R. \quad \text{Use a truth table.}$$

Question 3. Let P, Q and R be statements. Determine whether the following is true.

$$P \vee (Q \oplus R) \equiv (P \vee Q) \oplus (P \vee R). \quad \text{Use a truth table.}$$

Question 4. For an integer n , consider the open sentences

$$P(n) : n(n+1)(2n+1)/6 \text{ is even.} \quad Q(n) : (n+1)^2(n+2)^2/4 \text{ is even.}$$

Determine whether the biconditionals $P(1) \iff Q(1)$ and $P(2) \iff Q(2)$ are true or false.

Question 5. For statements P and Q , determine whether the compound statement

$$(P \wedge (\sim Q)) \Rightarrow (P \vee Q)$$

is a tautology, a contradiction or neither.

Question 6. Each of the following statements is an implication $P \Rightarrow Q$. For each statement, indicate what P and Q are.

- (a) I'm going to my class reunion only if I lose weight.
- (b) To win a free \$20 gift certificate, I must spend \$100 at the store.
- (c) To win the game, it is necessary that we score a touchdown.
- (d) It is necessary to do research to be promoted to professor.
- (e) I'll get an A on this exam if I'm lucky.
- (f) All I need is a B on the final exam to get an A in the course.