

Assignment 2 COMP 302

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2. 1 Theorem: $\forall l1, l2 (rev_append\ l1\ l2 = rev_append'\ l1\ l2)$

Base case:

$$\begin{aligned} l1 &= [] \\ rev_append\ []\ l2 \\ \implies l2 & \qquad \text{by rev_append} \end{aligned}$$

$$\begin{aligned} rev_append'\ []\ l2 \\ \implies append\ rev([])\ l2 & \qquad \text{by rev_append'} \\ \implies append\ []\ l2 & \qquad \text{by rev} \\ \implies l2 & \qquad \text{by append} \end{aligned}$$

$l1 = [h::t]$

Induction hypothesis: $rev_append\ t\ l2 = rev_append'\ t\ l2$

Case 1 with $rev_append\ [h::t]\ l2$

$$\begin{aligned} rev_append\ [h::t]\ l2 \\ \implies rev_append\ t\ (h::l2) & \qquad \text{By rev_append} \\ \implies rev_append'\ t\ (h::l2) & \qquad \text{By induction hypothesis} \\ \implies append\ rev(t)\ (h::l2) & \qquad \text{By rev_append'} \end{aligned} \tag{1}$$

Case 1 with $rev_append'\ [h::t]\ l2$

$$\begin{aligned} rev_append'\ [h::t]\ l2 \\ \implies append\ rev([h::t])\ l2 & \qquad \text{By rev_append'} \\ \implies append\ rev(t)@[h]\ l2 & \qquad \text{By rev} \\ \implies rev(t)@[h]\ @l2 & \qquad \text{By append} \\ = rev(t)@[h]\ @l2 & \qquad \text{By associativity of append} \\ = rev(t)@(h::l2) \\ \implies append\ rev(t)\ (h::l2) & \qquad \text{by append} \end{aligned} \tag{2}$$

So we can see that $(1) = (2)$ therefore the induction holds.