

Toronto HPI

Ozel, Sinan

Introduction

Data: Home
Price Index
(HPI)

Problem
Statement:
Forecast the
HPI

Validation
Framework

Model
Framework:
Vector Au-
toRegressive
(VAR)

Forecasts &
Validation

Conclusions &
Future Work

Toronto Home Price Index

A Time Series Analysis

S. Ozel

AISC Time Series Discussion Group, 2021

Outline

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- Purpose: Forecast Home Price Index (HPI) in Toronto by neighborhood.
- Validation: MSE calculated for each time period & neighborhood.
- Benchmark: Moving average return.
- Code: <https://github.com/sinan-ozel/toronto-hpi>

Home Price Index (HPI)

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Home Price Index

- Based on the sold prices of residential real estate.
- Corrects for the estate's features to make it less volatile, compared to averages.
- <https://trreb.ca/index.php/market-news/mls-home-price-index/>

			2020-06-01	2020-07-01	2020-08-01	2020-09-01	2020-10-01	2020-11-01	2020-12-01	2021-01-01	2021-02-01	2021-03-01	2021-04-01
Area	Date	Type											
HPI	Milton	Apartment	287.6	289.8	290.9	287.8	288.9	288.7	NaN	292.4	298.8	306.6	320.2
		Composite	289.5	285.5	289.1	294.5	297.8	301.7	NaN	325.5	341.9	346.0	347.6
		Single-Family Attached	303.2	297.4	303.4	308.9	314.2	320.5	NaN	349.1	367.8	368.1	369.0
		Single-Family Detached	283.2	284.7	287.9	294.2	297.5	301.8	NaN	329.3	346.5	349.4	348.7
		Townhouse	291.9	302.8	309.3	319.3	317.3	319.9	NaN	324.5	344.2	362.5	362.2
Mississauga		Apartment	307.2	308.5	309.4	310.6	308.0	307.1	303.0	302.6	309.2	321.3	329.5
		Composite	287.4	291.1	294.3	296.0	295.8	296.2	296.9	301.5	313.8	327.0	332.6
		Single-Family Attached	275.3	280.0	285.2	288.0	290.1	292.4	295.7	302.7	320.1	333.3	336.5
		Single-Family Detached	273.5	278.5	282.9	285.8	287.3	288.8	292.3	300.0	316.3	330.2	334.9
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		Single-Family Detached	265.6	283.1	282.1	277.2	275.0	278.2	277.1	287.3	295.6	295.3	301.8
		Townhouse	279.9	279.1	281.8	277.0	282.5	282.2	279.0	266.5	272.5	273.2	284.8

Home Price Index (HPI)

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Granularity

- Area: Defined by the Toronto Region Real Estate Board (TRREB). (Toronto C10, Mississauga, Milton, etc...)
- Type: Housing type
- Date: Monthly, first of every month

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Panel Data

- Each panel is an Area x Type pair, i.e. each row in the below table.
- Each panel has either 103 or 69 data points (months)
- We can run multivariate analysis or multiple univariate analyses.

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Forecast HPI

- Come up with the best forecast of HPI possible.
- Refresh knowledge of time series models in the process.
- Present results to spark discussion.

Research Questions

- Can we beat a basic benchmark?
- Which approach will work best?
- Can we develop a better approach?

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Validation: Moving Window, Next Month Forecast MSE

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		Composite	287.4	291.1	294.3	296.0	295.8	296.2	296.9	301.5	313.8	327.0	332.6
		Single-Family Attached	275.3	280.0	285.2	288.0	290.1	292.4	295.7	302.7	320.1	333.3	336.5
		Single-Family Detached	273.5	278.5	282.9	285.8	287.3	288.8	292.3	300.0	316.3	330.2	334.9
		Townhouse	288.2	294.7	298.8	298.8	298.0	297.9	299.2	301.8	312.7	326.7	332.2
Toronto C10		Apartment	315.5	307.4	306.7	305.6	302.1	305.0	303.0	298.9	305.6	313.8	326.2
		Composite	299.4	298.5	297.8	295.6	292.7	295.7	294.0	293.3	300.5	306.1	317.0
		Single-Family Attached	254.0	271.8	272.2	266.5	262.9	269.3	269.4	279.0	287.9	288.8	292.2
		Single-Family Detached	265.6	283.1	282.1	277.2	275.0	278.2	277.1	287.3	295.6	295.3	301.8
		Townhouse	279.9	279.1	281.8	277.0	282.5	282.2	279.0	266.5	272.5	273.2	284.8

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4-month Training Sample Validation 1 Month After

		2020-06-01	2020-07-01	2020-08-01	2020-09-01	2020-10-01	2020-11-01	2020-12-01	2021-01-01	2021-02-01	2021-03-01	2021-04-01	
Area	Date Type												
HPI	Milton	Apartment	287.6	289.8	290.9	287.8	288.9	288.7	NaN	292.4	298.8	306.6	320.2
		Composite	289.5	285.5	289.1	294.5	297.8	301.7	NaN	325.5	341.9	346.0	347.6
		Single-Family Attached	303.2	297.4	303.4	308.9	314.2	320.5	NaN	349.1	367.8	368.1	369.0
		Single-Family Detached	283.2	284.7	287.9	294.2	297.5	301.8	NaN	329.3	346.5	349.4	348.7
		Townhouse	291.9	302.8	309.3	319.3	317.3	319.9	NaN	324.5	344.2	362.5	363.2
Mississauga		Apartment	307.2	308.5	309.4	310.6	308.0	307.1	303.0	302.6	309.2	321.3	329.5
		Composite	287.4	291.1	294.3	296.0	295.8	296.2	296.9	301.5	313.8	327.0	332.6
		Single-Family Attached	275.3	280.0	285.2	288.0	290.1	292.4	295.7	302.7	320.1	333.3	336.5
		Single-Family Detached	273.5	278.5	282.9	285.8	287.3	288.8	292.3	300.0	316.3	330.2	334.9
		Townhouse	288.2	294.7	298.8	298.8	298.0	297.9	299.2	301.8	312.7	326.7	332.2
Toronto C10		Apartment	315.5	307.4	306.7	305.6	302.1	305.0	303.0	298.9	305.6	313.8	326.2
		Composite	299.4	298.5	297.8	295.6	292.7	295.7	294.0	293.3	300.5	306.1	317.0
		Single-Family Attached	254.0	271.8	272.2	266.5	262.9	269.3	269.4	279.0	287.9	288.8	292.2
		Single-Family Detached	265.6	283.1	282.1	277.2	275.0	278.2	277.1	287.3	295.6	295.3	301.8
		Townhouse	279.9	279.1	281.8	277.0	282.5	282.2	279.0	266.5	272.5	273.2	284.8

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Ozel, Sinan

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4-month Training Sample Validation 1 Month After

	Date	2020-06-01	2020-07-01	2020-08-01	2020-09-01	2020-10-01	2020-11-01	2020-12-01	2021-01-01	2021-02-01	2021-03-01	2021-04-01	
Area	Type												
HPI	Milton	Apartment	287.6	289.8	290.9	287.8	288.9	288.7	NaN	292.4	298.8	306.6	320.2
		Composite	289.5	285.5	289.1	294.5	297.8	301.7	NaN	325.5	341.9	346.0	347.6
		Single-Family Attached	303.2	297.4	303.4	308.9	314.2	320.5	NaN	349.1	367.8	368.1	369.0
		Single-Family Detached	283.2	284.7	287.9	294.2	297.5	301.8	NaN	329.3	346.5	349.4	348.7
		Townhouse	291.9	302.8	309.3	319.3	317.3	319.9	NaN	324.5	344.2	362.5	363.2
Mississauga		Apartment	307.2	308.5	309.4	310.6	308.0	307.1	303.0	302.6	309.2	321.3	329.5
		Composite	287.4	291.1	294.3	296.0	295.8	296.2	296.9	301.5	313.8	327.0	332.6
		Single-Family Attached	275.3	280.0	285.2	288.0	290.1	292.4	295.7	302.7	320.1	333.3	336.5
		Single-Family Detached	273.5	278.5	282.9	285.8	287.3	288.8	292.3	300.0	316.3	330.2	334.9
		Townhouse	288.2	294.7	298.8	298.8	298.0	297.9	299.2	301.8	312.7	326.7	332.2
Toronto C10		Apartment	315.5	307.4	306.7	305.6	302.1	305.0	303.0	298.9	305.6	313.8	326.2
		Composite	299.4	298.5	297.8	295.6	292.7	295.7	294.0	293.3	300.5	306.1	317.0
		Single-Family Attached	254.0	271.8	272.2	266.5	262.9	269.3	269.4	279.0	287.9	288.8	292.2
		Single-Family Detached	265.6	283.1	282.1	277.2	275.0	278.2	277.1	287.3	295.6	295.3	301.8
		Townhouse	279.9	279.1	281.8	277.0	282.5	282.2	279.0	266.5	272.5	273.2	284.8

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Ozel, Sinan

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4-month Training Sample Validation 1 Month After

		2020-06-01	2020-07-01	2020-08-01	2020-09-01	2020-10-01	2020-11-01	2020-12-01	2021-01-01	2021-02-01	2021-03-01	2021-04-01	
Area	Date Type												
HPI	Milton	Apartment	287.6	289.8	290.9	287.8	288.9	288.7	NaN	292.4	298.8	306.6	320.2
		Composite	289.5	285.5	289.1	294.5	297.8	301.7	NaN	325.5	341.9	346.0	347.6
		Single-Family Attached	303.2	297.4	303.4	308.9	314.2	320.5	NaN	349.1	367.8	368.1	369.0
		Single-Family Detached	283.2	284.7	287.9	294.2	297.5	301.8	NaN	329.3	346.5	349.4	348.7
		Townhouse	291.9	302.8	309.3	319.3	317.3	319.9	NaN	324.5	344.2	362.5	363.2
	Mississauga	Apartment	307.2	308.5	309.4	310.6	308.0	307.1	303.0	302.6	309.2	321.3	329.5
		Composite	287.4	291.1	294.3	296.0	295.8	296.2	296.9	301.5	313.8	327.0	332.6
		Single-Family Attached	275.3	280.0	285.2	288.0	290.1	292.4	295.7	302.7	320.1	333.3	336.5
		Single-Family Detached	273.5	278.5	282.9	285.8	287.3	288.8	292.3	300.0	316.3	330.2	334.9
		Townhouse	288.2	294.7	298.8	298.8	298.0	297.9	299.2	301.8	312.7	326.7	332.2
	Toronto C10	Apartment	315.5	307.4	306.7	305.6	302.1	305.0	303.0	298.9	305.6	313.8	326.2
		Composite	299.4	298.5	297.8	295.6	292.7	295.7	294.0	293.3	300.5	306.1	317.0
		Single-Family Attached	254.0	271.8	272.2	266.5	262.9	269.3	269.4	279.0	287.9	288.8	292.2
		Single-Family Detached	265.6	283.1	282.1	277.2	275.0	278.2	277.1	287.3	295.6	295.3	301.8
		Townhouse	279.9	279.1	281.8	277.0	282.5	282.2	279.0	266.5	272.5	273.2	284.8

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4-month Training Sample Validation 1 Month After

		2020-06-01	2020-07-01	2020-08-01	2020-09-01	2020-10-01	2020-11-01	2020-12-01	2021-01-01	2021-02-01	2021-03-01	2021-04-01	
Area	Date Type												
HPI	Milton	Apartment	287.6	289.8	290.9	287.8	288.9	288.7	NaN	292.4	298.8	306.6	320.2
		Composite	289.5	285.5	289.1	294.5	297.8	301.7	NaN	325.5	341.9	346.0	347.6
		Single-Family Attached	303.2	297.4	303.4	308.9	314.2	320.5	NaN	349.1	367.8	368.1	369.0
		Single-Family Detached	283.2	284.7	287.9	294.2	297.5	301.8	NaN	329.3	346.5	349.4	348.7
		Townhouse	291.9	302.8	309.3	319.3	317.3	319.9	NaN	324.5	344.2	362.5	363.2
Mississauga		Apartment	307.2	308.5	309.4	310.6	308.0	307.1	303.0	302.6	309.2	321.3	329.5
		Composite	287.4	291.1	294.3	296.0	295.8	296.2	296.9	301.5	313.8	327.0	332.6
		Single-Family Attached	275.3	280.0	285.2	288.0	290.1	292.4	295.7	302.7	320.1	333.3	336.5
		Single-Family Detached	273.5	278.5	282.9	285.8	287.3	288.8	292.3	300.0	316.3	330.2	334.9
		Townhouse	288.2	294.7	298.8	298.8	298.0	297.9	299.2	301.8	312.7	326.7	332.2
Toronto C10		Apartment	315.5	307.4	306.7	305.6	302.1	305.0	303.0	298.9	305.6	313.8	326.2
		Composite	299.4	298.5	297.8	295.6	292.7	295.7	294.0	293.3	300.5	306.1	317.0
		Single-Family Attached	254.0	271.8	272.2	266.5	262.9	269.3	269.4	279.0	287.9	288.8	292.2
		Single-Family Detached	265.6	283.1	282.1	277.2	275.0	278.2	277.1	287.3	295.6	295.3	301.8
		Townhouse	279.9	279.1	281.8	277.0	282.5	282.2	279.0	266.5	272.5	273.2	284.8

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4-month Training Sample Validation 1 Quarter After

		2020-06-01	2020-07-01	2020-08-01	2020-09-01	2020-10-01	2020-11-01	2020-12-01	2021-01-01	2021-02-01	2021-03-01	2021-04-01
Area	Date Type											
HPI	Milton	287.6	289.8	290.9	287.8	288.9	288.7	NaN	292.4	298.8	306.6	320.2
	Composite	289.5	285.5	289.1	294.5	297.8	301.7	NaN	325.5	341.9	346.0	347.6
	Single-Family Attached	303.2	297.4	303.4	308.9	314.2	320.5	NaN	349.1	367.8	368.1	369.0
	Single-Family Detached	283.2	284.7	287.9	294.2	297.5	301.8	NaN	329.3	346.5	349.4	348.7
	Townhouse	291.9	302.8	309.3	319.3	317.3	319.9	NaN	324.5	344.2	362.5	363.2
	Mississauga	307.2	308.5	309.4	310.6	308.0	307.1	303.0	302.6	309.2	321.3	329.5
	Composite	287.4	291.1	294.3	296.0	295.8	296.2	296.9	301.5	313.8	327.0	332.6
	Single-Family Attached	275.3	280.0	285.2	288.0	290.1	292.4	295.7	302.7	320.1	333.3	336.5
	Single-Family Detached	273.5	278.5	282.9	285.8	287.3	288.8	292.3	300.0	316.3	330.2	334.9
	Townhouse	288.2	294.7	298.8	298.8	298.0	297.9	299.2	301.8	312.7	326.7	332.2
Toronto C10	Apartment	315.5	307.4	306.7	305.6	302.1	305.0	303.0	298.9	305.6	313.8	326.2
	Composite	299.4	298.5	297.8	295.6	292.7	295.7	294.0	293.3	300.5	306.1	317.0
	Single-Family Attached	254.0	271.8	272.2	266.5	262.9	269.3	269.4	279.0	287.9	288.8	292.2
	Single-Family Detached	265.6	283.1	282.1	277.2	275.0	278.2	277.1	287.3	295.6	295.3	301.8
	Townhouse	279.9	279.1	281.8	277.0	282.5	282.2	279.0	266.5	272.5	273.2	284.8

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4-month Training Sample Validation 1 Quarter After

		2020-06-01	2020-07-01	2020-08-01	2020-09-01	2020-10-01	2020-11-01	2020-12-01	2021-01-01	2021-02-01	2021-03-01	2021-04-01	
Area	Date Type												
HPI	Milton	Apartment	287.6	289.8	290.9	287.8	288.9	288.7	NaN	292.4	298.8	306.6	320.2
		Composite	289.5	285.5	289.1	294.5	297.8	301.7	NaN	325.5	341.9	346.0	347.6
		Single-Family Attached	303.2	297.4	303.4	308.9	314.2	320.5	NaN	349.1	367.8	368.1	369.0
		Single-Family Detached	283.2	284.7	287.9	294.2	297.5	301.8	NaN	329.3	346.5	349.4	348.7
		Townhouse	291.9	302.8	309.3	319.3	317.3	319.9	NaN	324.5	344.2	362.5	363.2
Mississauga		Apartment	307.2	308.5	309.4	310.6	308.0	307.1	303.0	302.6	309.2	321.3	329.5
		Composite	287.4	291.1	294.3	296.0	295.8	296.2	296.9	301.5	313.8	327.0	332.6
		Single-Family Attached	275.3	280.0	285.2	288.0	290.1	292.4	295.7	302.7	320.1	333.3	336.5
		Single-Family Detached	273.5	278.5	282.9	285.8	287.3	288.8	292.3	300.0	316.3	330.2	334.9
		Townhouse	288.2	294.7	298.8	298.8	298.0	297.9	299.2	301.8	312.7	326.7	332.2
Toronto C10		Apartment	315.5	307.4	306.7	305.6	302.1	305.0	303.0	298.9	305.6	313.8	326.2
		Composite	299.4	298.5	297.8	295.6	292.7	295.7	294.0	293.3	300.5	306.1	317.0
		Single-Family Attached	254.0	271.8	272.2	266.5	262.9	269.3	269.4	279.0	287.9	288.8	292.2
		Single-Family Detached	265.6	283.1	282.1	277.2	275.0	278.2	277.1	287.3	295.6	295.3	301.8
		Townhouse	279.9	279.1	281.8	277.0	282.5	282.2	279.0	266.5	272.5	273.2	284.8

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Framework:
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4-month Training Sample Validation 1 Quarter After

		2020-06-01	2020-07-01	2020-08-01	2020-09-01	2020-10-01	2020-11-01	2020-12-01	2021-01-01	2021-02-01	2021-03-01	2021-04-01
Area	Date Type											
HPI Milton	Apartment	287.6	289.8	290.9	287.8	288.9	288.7	NaN	292.4	298.8	306.6	320.2
	Composite	289.5	285.5	289.1	294.5	297.8	301.7	NaN	325.5	341.9	346.0	347.6
	Single-Family Attached	303.2	297.4	303.4	308.9	314.2	320.5	NaN	349.1	367.8	368.1	369.0
	Single-Family Detached	283.2	284.7	287.9	294.2	297.5	301.8	NaN	329.3	346.5	349.4	348.7
	Townhouse	291.9	302.8	309.3	319.3	317.3	319.9	NaN	324.5	344.2	362.5	363.2
Mississauga	Apartment	307.2	308.5	309.4	310.6	308.0	307.1	303.0	302.6	309.2	321.3	329.5
	Composite	287.4	291.1	294.3	296.0	295.8	296.2	296.9	301.5	313.8	327.0	332.6
	Single-Family Attached	275.3	280.0	285.2	288.0	290.1	292.4	295.7	302.7	320.1	333.3	336.5
	Single-Family Detached	273.5	278.5	282.9	285.8	287.3	288.8	292.3	300.0	316.3	330.2	334.9
	Townhouse	288.2	294.7	298.8	298.8	298.0	297.9	299.2	301.8	312.7	326.7	332.2
Toronto C10	Apartment	315.5	307.4	306.7	305.6	302.1	305.0	303.0	298.9	305.6	313.8	326.2
	Composite	299.4	298.5	297.8	295.6	292.7	295.7	294.0	293.3	300.5	306.1	317.0
	Single-Family Attached	254.0	271.8	272.2	266.5	262.9	269.3	269.4	279.0	287.9	288.8	292.2
	Single-Family Detached	265.6	283.1	282.1	277.2	275.0	278.2	277.1	287.3	295.6	295.3	301.8
	Townhouse	279.9	279.1	281.8	277.0	282.5	282.2	279.0	266.5	272.5	273.2	284.8

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Ozel, Sinan

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Framework:
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4-month Training Sample Validation 1 Quarter After

		2020-06-01	2020-07-01	2020-08-01	2020-09-01	2020-10-01	2020-11-01	2020-12-01	2021-01-01	2021-02-01	2021-03-01	2021-04-01	
Area	Date Type												
HPI	Milton	Apartment	287.6	289.8	290.9	287.8	288.9	288.7	NaN	292.4	298.8	306.6	320.2
		Composite	289.5	285.5	289.1	294.5	297.8	301.7	NaN	325.5	341.9	346.0	347.6
		Single-Family Attached	303.2	297.4	303.4	308.9	314.2	320.5	NaN	349.1	367.8	368.1	369.0
		Single-Family Detached	283.2	284.7	287.9	294.2	297.5	301.8	NaN	329.3	346.5	349.4	348.7
		Townhouse	291.9	302.8	309.3	319.3	317.3	319.9	NaN	324.5	344.2	362.5	363.2
Mississauga		Apartment	307.2	308.5	309.4	310.6	308.0	307.1	303.0	302.6	309.2	321.3	329.5
		Composite	287.4	291.1	294.3	296.0	295.8	296.2	296.9	301.5	313.8	327.0	332.6
		Single-Family Attached	275.3	280.0	285.2	288.0	290.1	292.4	295.7	302.7	320.1	333.3	336.5
		Single-Family Detached	273.5	278.5	282.9	285.8	287.3	288.8	292.3	300.0	316.3	330.2	334.9
		Townhouse	288.2	294.7	298.8	298.8	298.0	297.9	299.2	301.8	312.7	326.7	332.2
Toronto C10		Apartment	315.5	307.4	306.7	305.6	302.1	305.0	303.0	298.9	305.6	313.8	326.2
		Composite	299.4	298.5	297.8	295.6	292.7	295.7	294.0	293.3	300.5	306.1	317.0
		Single-Family Attached	254.0	271.8	272.2	266.5	262.9	269.3	269.4	279.0	287.9	288.8	292.2
		Single-Family Detached	265.6	283.1	282.1	277.2	275.0	278.2	277.1	287.3	295.6	295.3	301.8
		Townhouse	279.9	279.1	281.8	277.0	282.5	282.2	279.0	266.5	272.5	273.2	284.8

AR(2) \longrightarrow 2-panel VAR(2)

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AR(2) Model

I start with the AR(2) model.

$$Y_t = \beta_0 + \beta_1 Y_{t-1} + \beta_2 Y_{t-2} + \epsilon_t$$

AR(2) \longrightarrow 2-panel VAR(2)

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AR(2) Model on One Panel

I added the subscript 1 to show that this is one panel.

$$Y_{1,t} = \beta_0 + \beta_{1,1} Y_{1,t-1} + \beta_{1,2} Y_{1,t-2} + \epsilon_t$$

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AR(2) Model on One Panel

Now I added two more terms from another panel.

$$Y_{1,t} = \beta_0 + \beta_{1,1} Y_{1,t-1} + \beta_{1,2} Y_{1,t-2} + \beta_{2,1} Y_{2,t-1} + \beta_{2,2} Y_{2,t-2} + \epsilon_t$$

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VAR(2) Model on Two Panels

Finally, I do the same for Panel 2.

$$Y_{1,t} = \beta_0 + \beta_{11,1} Y_{1,t-1} + \beta_{11,2} Y_{1,t-2} + \beta_{12,1} Y_{2,t-1} + \beta_{12,2} Y_{2,t-2} + \epsilon_{1,t}$$

$$Y_{2,t} = \beta_0 + \beta_{21,1} Y_{1,t-1} + \beta_{21,2} Y_{1,t-2} + \beta_{22,1} Y_{2,t-1} + \beta_{22,2} Y_{2,t-2} + \epsilon_{2,t}$$

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Why VAR Models?

- Why not: we have additional data, so why not use it?
- Explanatory power: Impulse Response Functions (IRF)
- Granger Causality

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Stationarity: Dickey-Fuller & Differencing

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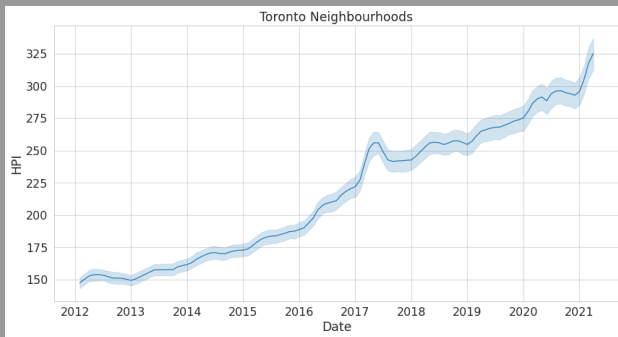
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Are the panels stationary?

- Visually, it is clear that the panels are not stationary.
- For each panel, I run the Augmented Dickey-Fuller test
- I reject non-stationarity for over 99% of the panels.

Stationarity: Dickey-Fuller & Differencing

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Differencing & Percent Changes

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Differencing

$$\Delta Y_t = Y_t - Y_{t-1}$$

Percent Changes, i.e. "Returns"

$$r_t = \frac{Y_t - Y_{t-1}}{Y_{t-1}} \approx \log Y_t - \log Y_{t-1}$$

Justification for Percent Changes

- Easier to interpret
- Easier to discuss with stakeholders and laypeople
- Normalizes the amount of change to each period.

Differencing & Percent Changes

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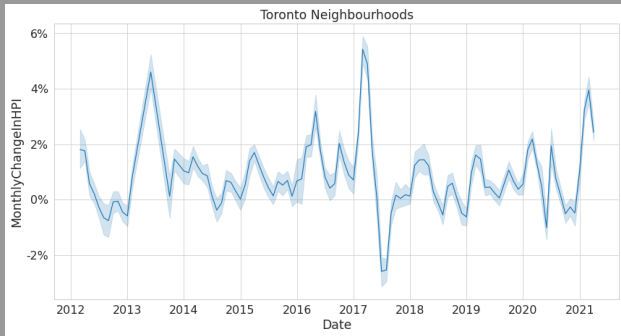
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- KPSS test could have been a better option.

Monthly Percent Changes: i.e "Returns"

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A Good Example

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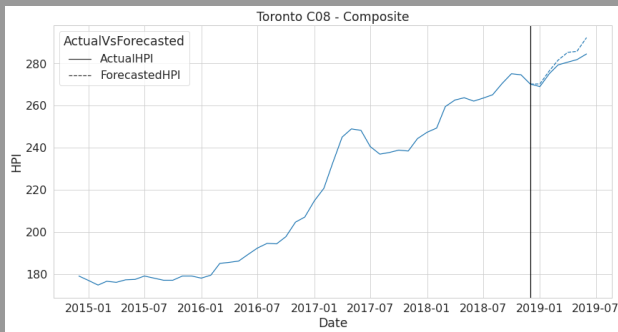
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Too Good An Example (To Be True)

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Looks good, but...

- This only works this well when trained from 2014 Dec to 2018 Dec & validated against 2019 Jan to 2019 Jun.
- ... hence my justification for the "rolling window" validation.
- If we modelled on the right date (July 2019), we would "believe" in our model, but only by mistake.

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A Simple Benchmark

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"Return" Moving Average

- Obtain the return.
- Calculate the moving average over the rolling window.
- Use this return to forecast the next month.
- Use exponential growth formula to obtain a forecast for n months into the future.

Average "Return"

$$r_t = \frac{Y_t - Y_{t-1}}{Y_{t-1}}$$

1-month forecast

$$\hat{r}_{t+1} = \sum_{t-T}^t r_t / T$$

n -month forecast

$$\hat{r}_{t+n} = (1 + \hat{r}_{t+1})^n - 1$$

A Simple Benchmark

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MSE: Benchmark vs VAR model

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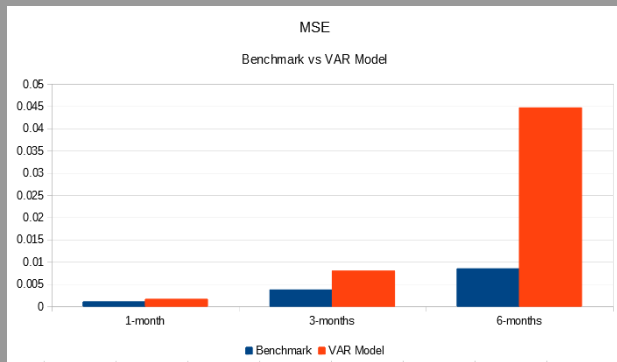
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	1-month	3-months	6-months
Benchmark	0.001016761439712	0.00366345390135	0.008432082243063
VAR Model	0.001587714029696	0.007939166535112	0.044613766619586

Conclusions & Final Thoughts

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- VAR still not great for forecasting
- Exogenous data might improve: monthly inflation rate & mortgage rates.
- VAR for explainability: IRF

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I would like to repeat the work with the following sets of models:

- ARMA and derivative models (ARIMA, ARIMAX, etc...)
- VECM
- ARCH & GARCH models
- LSTM networks
- Idea: A bootstrapping of VAR models with different sets of neighbourhoods and years.