
Security of Cyberphysical Systems

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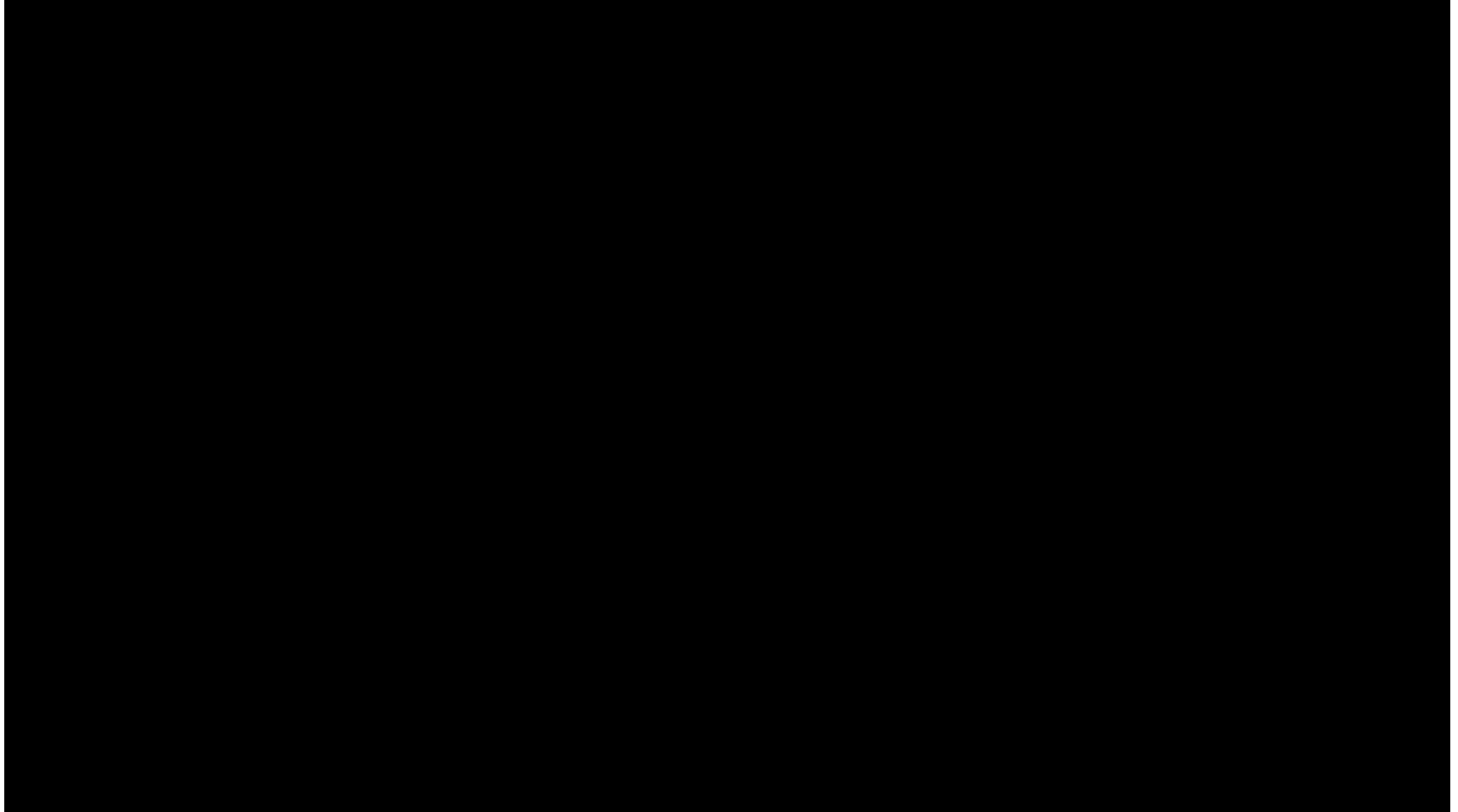
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Securing an automated transportation system



See the video “Tackling Autonomous Vehicle Cybersecurity Issues” at <https://cesg.tamu.edu/faculty/p-r-kumar/convergencelab/>

Cyber-physical systems

- ◆ Next generation of engineered systems in which computing, communication, and control technologies are tightly integrated
- ◆ Many societally important future applications
 - Smart grid
 - Automated transportation
 - Unmanned Air Vehicle Transportation System
 - Water treatment facilities
 - Telesurgery systems
 - ...
- ◆ Safety critical
 - Malfunctioning causes physical harm
- ◆ Critical infrastructure
 - Important to functioning of economy and society

Vulnerability of cyberphysical systems to attacks

- ◆ Hackers hitherto could tamper only with information or bits in cyber layer
- ◆ CPS tightly couples cyber and physical worlds
 - Actions in physical world taken based on information from cyber layer
- ◆ CPS, therefore, gives hacker ability to cause damage in physical world

Security of CPS

- ◆ As more systems are connected to the Internet and become more open, there are increasingly more vulnerabilities
- ◆ Can be more harmful than other violent attacks
- ◆ Next war may be “cyber” rather than “bombs”?
- ◆ Even after many decades we still cannot secure the Operating Systems
 - New patches every day
- ◆ We still cannot secure the Internet
- ◆ Interaction between bits and physical world is very complex
- ◆ How can we possibly secure CPSs?

Several attacks on critical infrastructure systems

- ◆ Several instances of attacks in the past
 - Maroochy-Shire sewage treatment plant
 - Davis-Besse nuclear power plant
 - Stuxnet
 - Ukraine power grid
 - Water filtering plant in Pennsylvania
 - Demonstrations of cyber attacks in automated cars
- ◆ Maroochy-Shire, Australia, 2003, attack on **sewage treatment** system, commands issued which led to a series of faults in the system
- ◆ Attack on computers controlling Davis-Besse **nuclear power plant** in Ohio, 2003, Slammer worm disabled the safety monitoring system
- ◆ Stuxnet worm, 2010, exploited Microsoft Windows vulnerability to subvert critical **computers controlling centrifuges** in Iran uranium enrichment facility
- ◆ Attacks on Supervisory Control and Data Acquisition system, **natural gas pipeline systems, trams, power utilities, and water systems**, etc.

Isn't network security enough for CPS security?

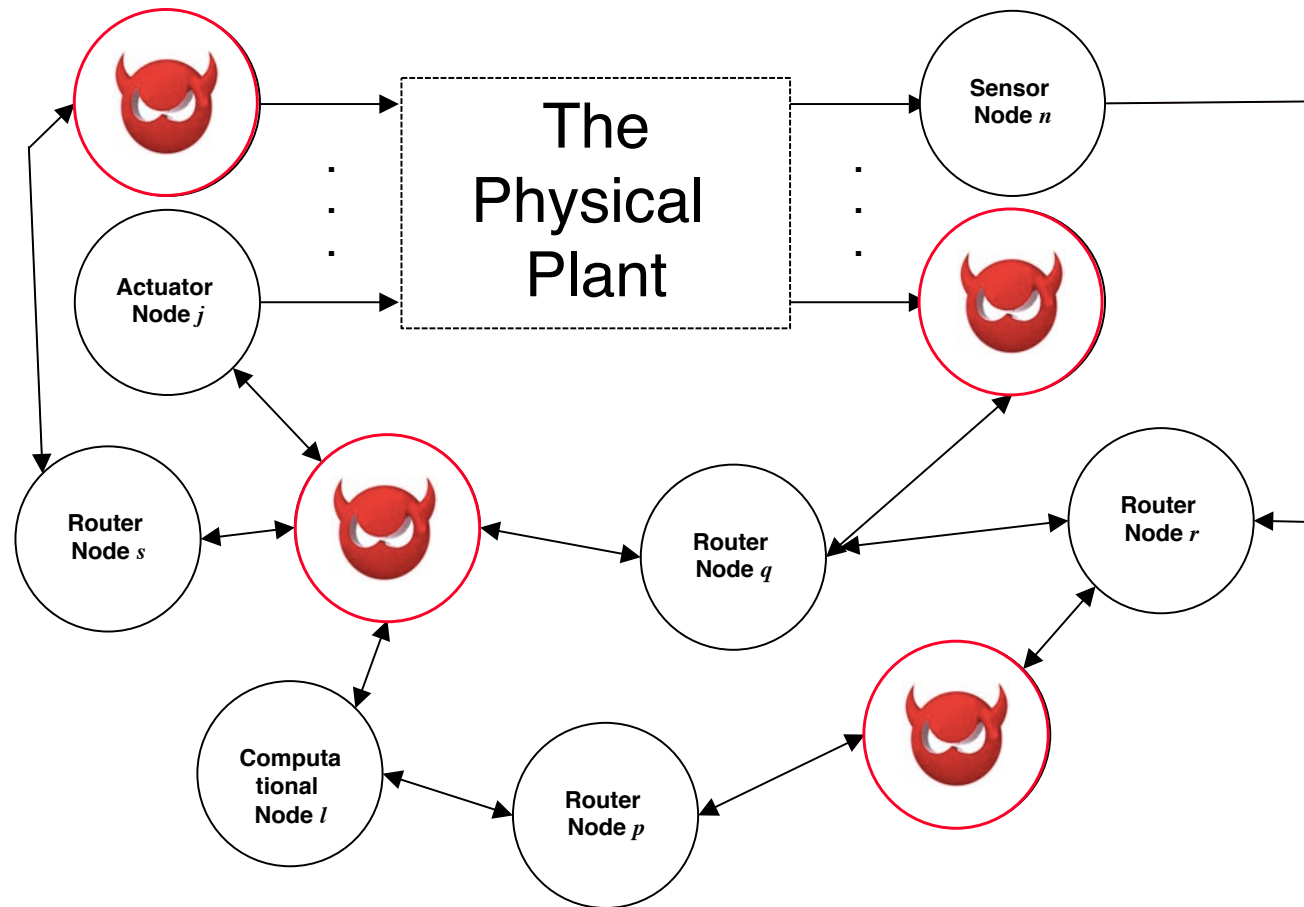
- ◆ Network and information security implemented through periodic patching.
 - CPS has a dynamic system in the loop, and may not admit controllers going online for patching
- ◆ Traditional notion of “Confidentiality, Integrity and Availability” in network and information security does not address real-time availability, which is critical for control system security
- ◆ Network or information security fundamentally cannot address physical layer attacks such as in Maroochy-Shire incident

Two-layer approach to CPS security

- ◆ Can think of CPS as consisting of two layers:
 - Cyber layer consisting routers, switches, relays, etc. providing communication backbone,
 - Physical layer consisting the plant, sensors and actuators, controllers which manipulate physical signals
- ◆ Cyber layer possibly secured using techniques such as cryptography
 - Therefore, network may possibly be abstracted as secure, reliable, delay-guaranteed bit pipes
- ◆ But how to secure the physical layer?

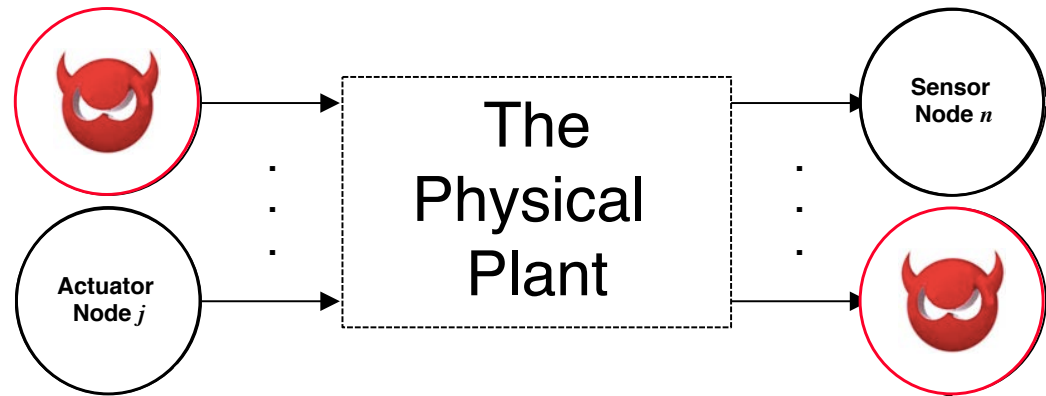
Abstraction of cyberphysical systems

- ◆ Overall system has
 - Physical plant
 - Actuators
 - Sensors
 - Routers
 - Computational nodes
 - Network
- ◆ But some of the routers, computation nodes, sensors, actuators may be **compromised**
- ◆ How do we secure the overall cyberphysical system?



Abstraction of security problem

- ◆ Some sensors, actuators may be compromised
- ◆ If information from a sensor is compromised, we say sensor is compromised
- ◆ It does not matter whether sensor is compromised or its information is compromised downstream

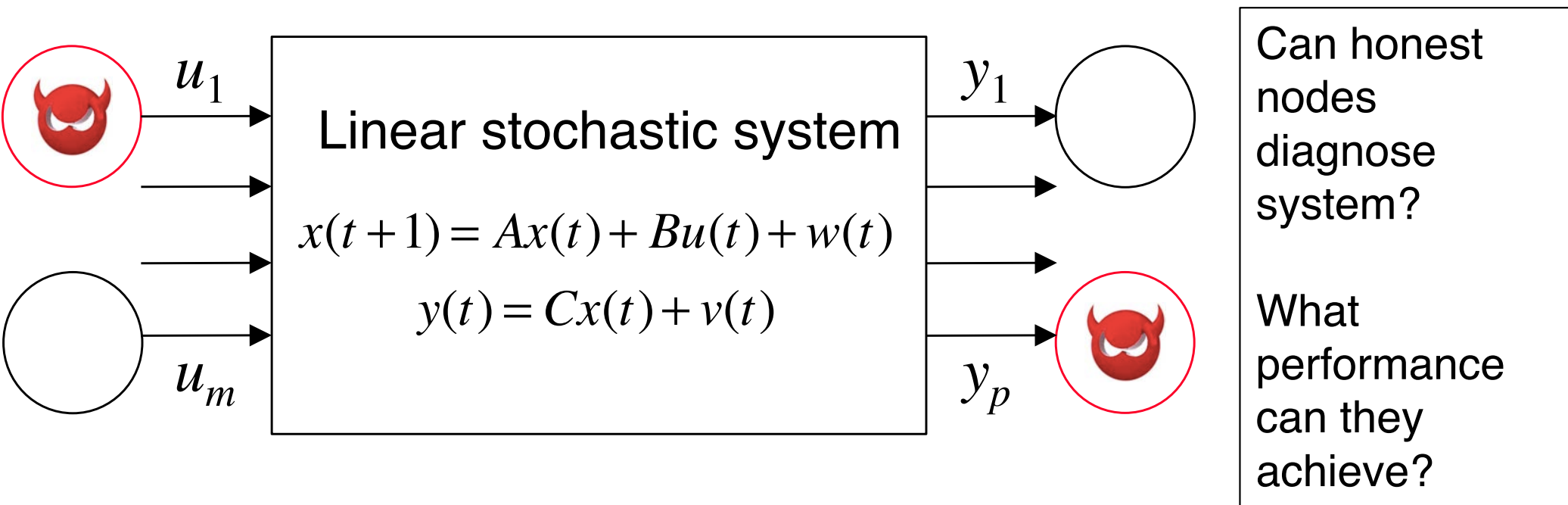


How do we secure the overall cyberphysical system when some sensors and actuators may be compromised?



Towards a **paranoid** theory of linear stochastic systems

Let's start with linear stochastic systems



- ◆ Physical plant modeled as linear stochastic system
 - Most common practical design
- ◆ Some actuators/sensors malicious
- ◆ Malicious actuators/sensors can collude
- ◆ Honest actuators/sensors don't know which nodes malicious

Linear systems theory in a more innocent age

- ◆ Linear system $x(t+1) = Ax(t) + Bu(t)$
- ◆ When is system controllable (Kalman)?

$$x(n) = A^n x(0) + Bu(n-1) + ABu(n-2) + \dots + A^{n-1}Bu(0)$$

$$x(n) - A^n x(0) = [B, AB, A^2 B, \dots, A^{n-1} B] \begin{bmatrix} u(n-1) \\ u(n-2) \\ \vdots \\ u(0) \end{bmatrix}$$

- ◆ Controllable subspace = $\text{Span}[B, AB, \dots, A^{n-1} B]$
- ◆ System is **stabilizable** if unstable modes of A are in controllable subspace

Linear systems theory in a more innocent age

◆ Linear system $x(t+1) = Ax(t)$
 $y(t) = Cx(t)$

◆ When is system state observable from outputs?

$$\begin{bmatrix} y(0) \\ y(1) \\ \vdots \\ y(n-1) \end{bmatrix} = \begin{bmatrix} C \\ CA \\ \vdots \\ CA^{n-1} \end{bmatrix} x(0)$$

◆ Unobservable subspace = Null Space of $\begin{bmatrix} C \\ CA \\ \vdots \\ CA^{n-1} \end{bmatrix}$

◆ System is **detectable** if unstable modes are observable

But what if some actuators or sensors are **malicious**?

$$\begin{bmatrix} x_1(t+1) \\ x_2(t+1) \\ \vdots \\ x_n(t+1) \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{n1} & a_{n2} & \dots & a_{nn} \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \\ \vdots \\ x_n(t) \end{bmatrix} + \begin{bmatrix} b_{11} & b_{12} & \dots & b_{1m} \\ b_{21} & b_{22} & \dots & b_{2m} \\ \dots & \dots & \dots & \dots \\ b_{n1} & b_{n2} & \dots & b_{nm} \end{bmatrix} \begin{bmatrix} u_1(t) \\ u_2(t) \\ \vdots \\ u_m(t) \end{bmatrix}$$

$$\begin{bmatrix} y_1(t) \\ y_2(t) \\ \vdots \\ y_p(t+1) \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & \dots & c_{1n} \\ c_{21} & c_{22} & \dots & c_{2n} \\ \dots & \dots & \dots & \dots \\ c_{p1} & c_{p2} & \dots & c_{pn} \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \\ \vdots \\ x_n(t) \end{bmatrix}$$

- ◆ Some of the u_i 's and y_j 's may be malicious
- ◆ What harm can malicious sensors/actuators cause without the honest sensors/actuators knowledge?

Innocent age concerns vs New age concerns

- ◆ **Nature** causes stability/instability
- ◆ **Malicious** agents cause harm
- ◆ **Stability** of benign systems
- ◆ **Security** of malicious systems
- ◆ **Stabilizability/Detectability** of benign systems
- ◆ **Securability** of malicious systems

Passive guarantees based on system structure

The **securable** and **unsecurable** subspaces for deterministic systems

- ◆ What states can the malicious sensors/actuators drive the system to without the honest sensors/actuators finding out?
- ◆ The **unsecurable subspace** V is the set of states that the malicious sensors and actuators can keep indistinguishable from the 0 state
- ◆ The **securable subspace** is V^\perp

The **unsecurable states** of deterministic systems

- ◆ Suppose $x(t+1) = Ax(t) + B_m u_m(t)$

$$y_h(t) = \begin{bmatrix} x_1(t) \\ \vdots \\ x_H(t) \end{bmatrix} = C_h x(t)$$

- ◆ Then $x(0)$ can be made indistinguishable from 0 if for some $u_m(0), u_m(1), \dots, u_m(t), \dots$

$$C_h x(0) = 0$$

$$C_h (Ax(0) + B_m u_m(0)) = 0$$

$$\vdots$$

$$C_h (A^t x(0) + A^{t-1} B_m u_m(0) + \dots + B_m u_m(t-1)) = 0$$

Characterization of **Unsecurable** and **Securable** subspaces

- ◆ **Unsecurable subspace** is the maximal subspace V such that for all v in V

$$C_h v = 0$$

There exists u such that $Av + B_m u \in V$

- ◆ **Securable subspace** is V^\perp

Stochastic systems

Malicious sensors and actuators in linear stochastic system

- ◆ Consider a linear stochastic system

$$x(t+1) = Ax(t) + Bu^g(z^t) + B_m u_m(t) + w(t+1)$$

$$y(t) = x(t)$$

- ◆ w is white noise of variance Σ
- ◆ Honest sensors measure y_1, y_2, \dots, y_H
- ◆ Malicious sensors measure $y_{H+1}, y_{H+2}, \dots, y_p$
- ◆ Sensor measurements reported are $z(t)$, where $z_i(t) = x_i(t)$ for $i = 0, 1, \dots, H$
- ◆ But for the malicious sensor's $z_i(t)$ need not equal $x_i(t)$ for $i = H+1, H+2, \dots, p$
- ◆ And malicious actuators may apply $u_m(t)$ different from 0

What performance can be guaranteed for a linear stochastic system?

- ◆ Honest sensors conduct Test to detect if there is any malicious activity:

$$\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{t=0}^{T-1} \left(z(t+1) - Az(t) + Bu^g(z^t) \right) \left(z(t+1) - Az(t) + Bu^g(z^t) \right)^T = \Sigma$$

- ◆ To remain undetected malicious sensors/actuators must pass Test

- ◆ **Theorem:** Then the error in the reported state error in the securable subspace V^\perp is guaranteed to be of zero power

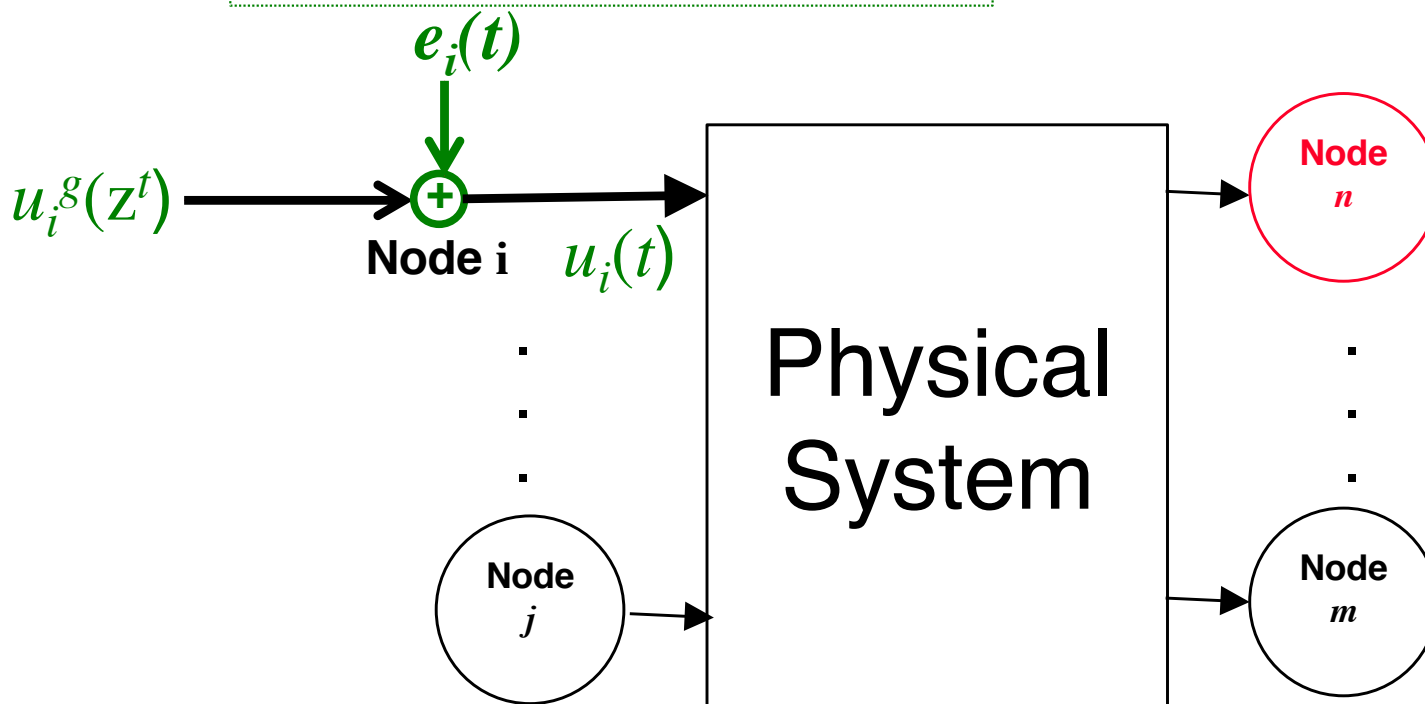
$$\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{t=0}^{T-1} \left\| \tilde{x}(t)_{V^\perp} \right\|^2 = 0$$

where $\tilde{x}(t)_{V^\perp} := \text{Projection of } (z(t) - x(t)) \text{ on } V^\perp$

Can we do better?

Dynamic watermarking

Random noise $e_i(t)$ is privately added to the signal



- ◆ Actuator node superimposes a private excitation whose realization is unknown to other nodes

Why does it help?

- ◆ Private excitation $e_i(t)$ appears in transformed returned signals from sensors at time $t+1$
- ◆ Measurement reported by sensor at time $t+1$ has to contain suitably transformed contribution of $e_i(t)$
- ◆ So actuator can check if private excitation comes back properly from sensors
- ◆ Checks if the reported measurements have the appropriately correlations with $e_i(t)$ reported
- ◆ This provides powerful guarantees against general attacks on sensors – not just replay attack

Illustration on simple first order SISO system

- ◆ SISO system: $x(t+1) = ax(t) + bu(t) + w(t+1)$
 $w(t) \sim N(0, \sigma_w^2)$, i.i.d.
- ◆ Dynamic watermarking $u(t) = u^g(t) + e(t)$ with $e(t) \sim N(0, \sigma_e^2)$, i.i.d.
- ◆ Two tests are conducted by actuator

$$\lim_{T} \frac{1}{T} \sum_{t=0}^{T-1} \left(z(t+1) - az(t) - bu^g(t) - be(t) \right)^2 \stackrel{?}{=} \sigma_w^2$$

$$\lim_{T} \frac{1}{T} \sum_{t=0}^{T-1} \left(z(t+1) - az(t) - bu^g(t) \right)^2 \stackrel{?}{=} b^2 \sigma_e^2 + \sigma_w^2$$

- ◆ If either test fails, then there is malicious sensor information
 - System goes into safety mode
 - Halted, checked, rebooted, manual operation, etc

Guarantee provided by Dynamic Watermarking

◆ Theorem

$$\lim \frac{1}{T} \sum_{t=0}^{T-1} v^2(t) = 0$$

◆ Where $v(t+1) := z(t+1) - az(t) - bu^g(t) - be(t) = w(t+1)$

◆ Interpretation:

$$z(t+1) - az(t) - bu^g(t) - be(t) = w(t+1) + v(t+1)$$

◆ So reported sensor measurements can distort actual noise $w(t)$ only by zero power signal $v(t)$

Proof - 1

- ◆ From the first test $\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=1}^T (v[k] + w[k])^2 = \sigma_w^2$
- ◆ Hence $\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=1}^T v^2[k] + 2v[k]w[k] + w^2[k] = \sigma_w^2$
- ◆ So $\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=1}^T v^2[k] + \lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=1}^T 2v[k]w[k] = 0$
- ◆ From the second test $\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=1}^T (v[k] + be[k-1] + w[k])^2 = b^2 \sigma_e^2 + \sigma_w^2$
- ◆ So $\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=1}^T (v[k] + w[k])^2 + \lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=1}^T b^2 e^2[k-1]$
 $+ \lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=1}^T 2be[k-1](v[k] + w[k]) = b^2 \sigma_e^2 + \sigma_w^2$

Proof - 2

- ◆ Since e has variance σ^2 : $\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=1}^T e[k-1](v[k] + w[k]) = 0$
- ◆ Since $e(t-1)$ and $w(t)$ are independent: $\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=1}^T e[k-1]v[k] = 0$
- ◆ Define the σ -algebra $\mathcal{S}_k := \sigma(x^k, z^k, e^{k-2})$
- ◆ And $\hat{w}[k] := E[w[k] | \mathcal{S}_k]$
- ◆ Since $w[k] = x[k] - ax[k-1] - bg_{k-1}(z^{k-1}) - be[k-1]$
- ◆ We have the Markov Chain: $(x^{k-2}, e^{k-2}) \rightarrow (x[k-1], x[k], z^k) \rightarrow w[k]$

Proof - 3

◆ So

$$\hat{w}[k] := E[w[k] | \sigma(e^{k-2}, x^{k-2}, x[k-1], x[k], z^k)] = E[w[k] | \sigma(x[k-1], x[k], z^k)]$$

◆ Since $x[k] - ax[k-1] - bg_{k-1}(z^{k-1}) = be[k-1] + w[k]$ is i.i.d. Gaussian

◆ The estimate $\hat{w}[k] = \frac{\sigma_w^2}{b^2\sigma_e^2 + \sigma_w^2}(be[k-1] + w[k]) = \beta(be[k-1] + w[k])$

◆ Note $\beta := \frac{\sigma_w^2}{b^2\sigma_e^2 + \sigma_w^2} < 1$

◆ Let $\tilde{w}[k] := w[k] - \hat{w}[k]$

◆ Then. $(\tilde{w}[k-1], \mathcal{S}_k)$ Is a martingale

Proof - 4

- ◆ Also $v[k] \in \mathcal{S}_k$, in fact $v[k] \in \sigma(x^k, z^k)$
- ◆ By Martingale Stability Theorem $\sum_{k=1}^T v[k] \tilde{w}[k] = o(\sum_{k=1}^T v^2[k]) + O(1)$
- ◆ Now $\sum_{k=1}^T v[k] w[k] = \sum_{k=1}^T v[k] (\hat{w}[k] + \tilde{w}[k])$
$$= \sum_{k=1}^T v[k] \hat{w}[k] + o(\sum_{k=1}^T v^2[k]) + O(1)$$
- ◆ So $\sum_{k=1}^T v[k] w[k] = \beta b \sum_{k=1}^T v[k] e[k-1] + \beta \sum_{k=1}^T v[k] w[k] + o(\sum_{k=1}^T v^2[k]) + O(1)$
- ◆ Hence $\sum_{k=1}^T v[k] w[k] = \frac{\beta b}{1-\beta} \sum_{k=1}^T v[k] e[k-1] + o(\sum_{k=1}^T v^2[k]) + O(1)$

Proof - 5

- ◆ Now $\sum_{k=1}^T v[k]e[k-1] = o(T)$
- ◆ So it follows that $\sum_{k=1}^T v[k]w[k] = o\left(\sum_{k=1}^T v^2[k]\right) + o(T) + O(1)$
- ◆ So $\sum_{k=1}^T v^2[k] + \sum_{k=1}^T 2v[k]w[k] = (1 + o(1))\left(\sum_{k=1}^T v^2[k]\right) + o(T)$
- ◆ Taking limits and dividing by T gives the result

Comments

- ◆ Surprising complexity of proof
- ◆ Difficult to handle general non-Gaussian case

Stability consequences of Dynamic Watermarking

- ◆ **Theorem:**
- ◆ Suppose $|a| < 1$, i.e., system is open-loop stable,
- ◆ Then distortion $d[t] := z[t] - x[t]$ is zero power: $\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=0}^{T-1} d^2[k] = 0$
- ◆ Mean-square performance is same as reported performance $\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=0}^{T-1} x^2[k] = \lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=0}^{T-1} z^2[k]$
- ◆ Suppose $u^g(t) = fx(t)$ with $|a + bf| < 1$
- ◆ Then mean square performance is optimal $\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{k=0}^{T-1} x^2[k] = \frac{\sigma_w^2 + b^2 \sigma_e^2}{1 - |a + bf|^2}$

More general results

- ◆ Results extend to

- ◆ ARMAX Systems used in process control:

$$y[t] = -\sum_{k=1}^p a_k y[t-k] + \sum_{k=0}^h b_k u[t-l-k] + \sum_{k=0}^r c_k w[t-k]$$

- ◆ MIMO partially observed Gaussian systems

$$\mathbf{x}[t+1] = A\mathbf{x}[t] + Bu[t] + \mathbf{w}[t+1]$$

$$y[t+1] = C\mathbf{x}[t+1] + n[t+1]$$

- ◆ Some non-Gaussian systems

Example

- ◆ System: $y(t+1) + 0.7y(t) - 0.2y(t-1) = u(t) + 0.5u(t-1) + w(t)$

$$w(t) \sim N(0,1), \text{ i.i.d.}$$

- ◆ Actuator applies $u(t) = -0.7z(t) - 0.2z(t-1) - 0.5u(t-1) + e(t)$

$$e(t) \sim N(0,1), \text{ i.i.d.}$$

- ◆ Closed-loop system:

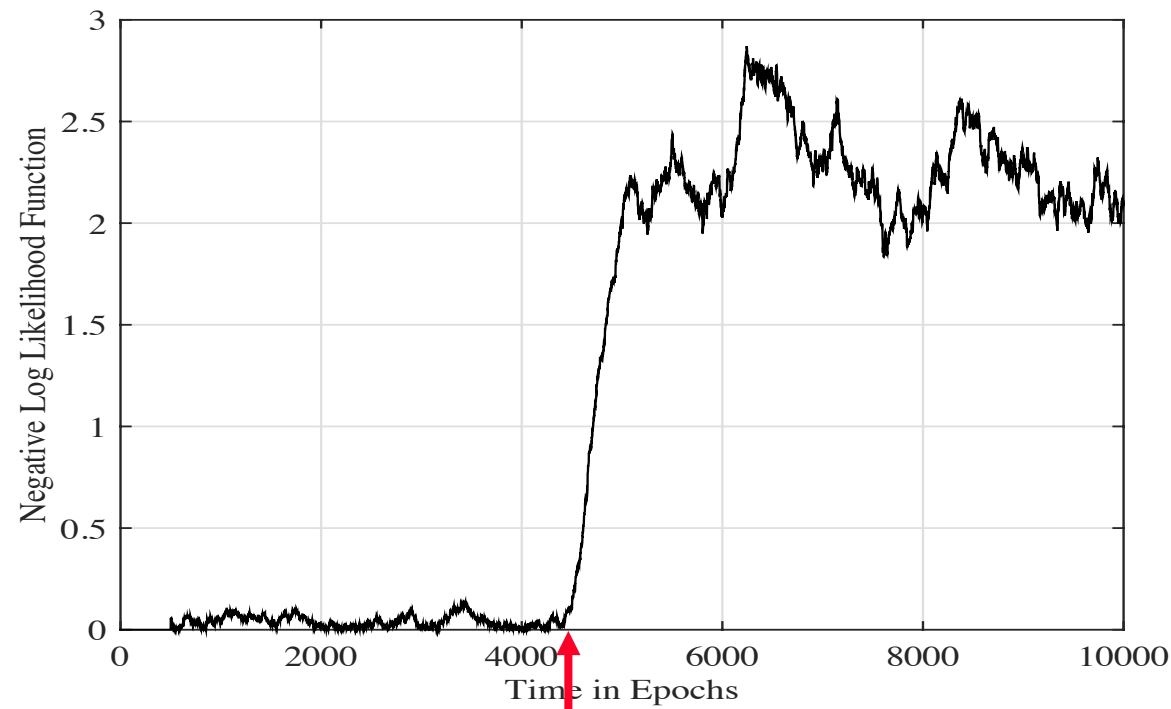
$$y[t+1] = 0.7(y[t] - z[t]) + 0.3(y[t-1] - z[t-1]) + e[t] + w[t+1]$$

- ◆ Sensor estimates process noise by

$$\hat{w}[t+1] := \frac{1}{2}(y[t+1] - 0.7(y[t] - z[t]) - 0.3(y[t-1] - z[t-1]))$$

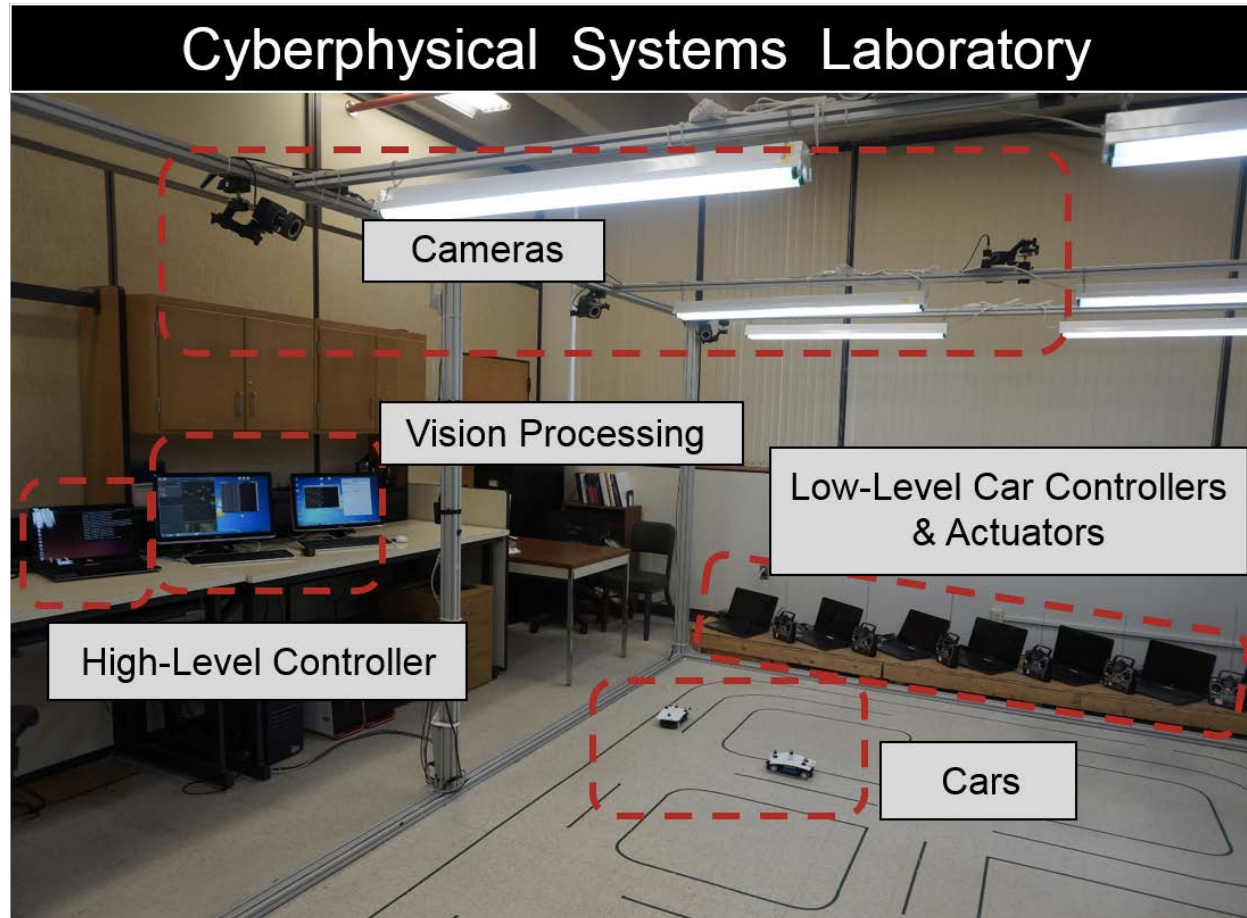
Example

- ◆ Simulates a fake system with a fake noise $n(t) - \hat{w}(t)$
 $n(t) \sim N(0,1)$, i.i.d.
- ◆ Reports output of fake simulated system
- ◆ In absence of watermarking, actuator would not suspect any malicious measurements
- ◆ Sensor attack begins at time 4500



Attack initiated

Test of autonomous transportation system in CPS lab



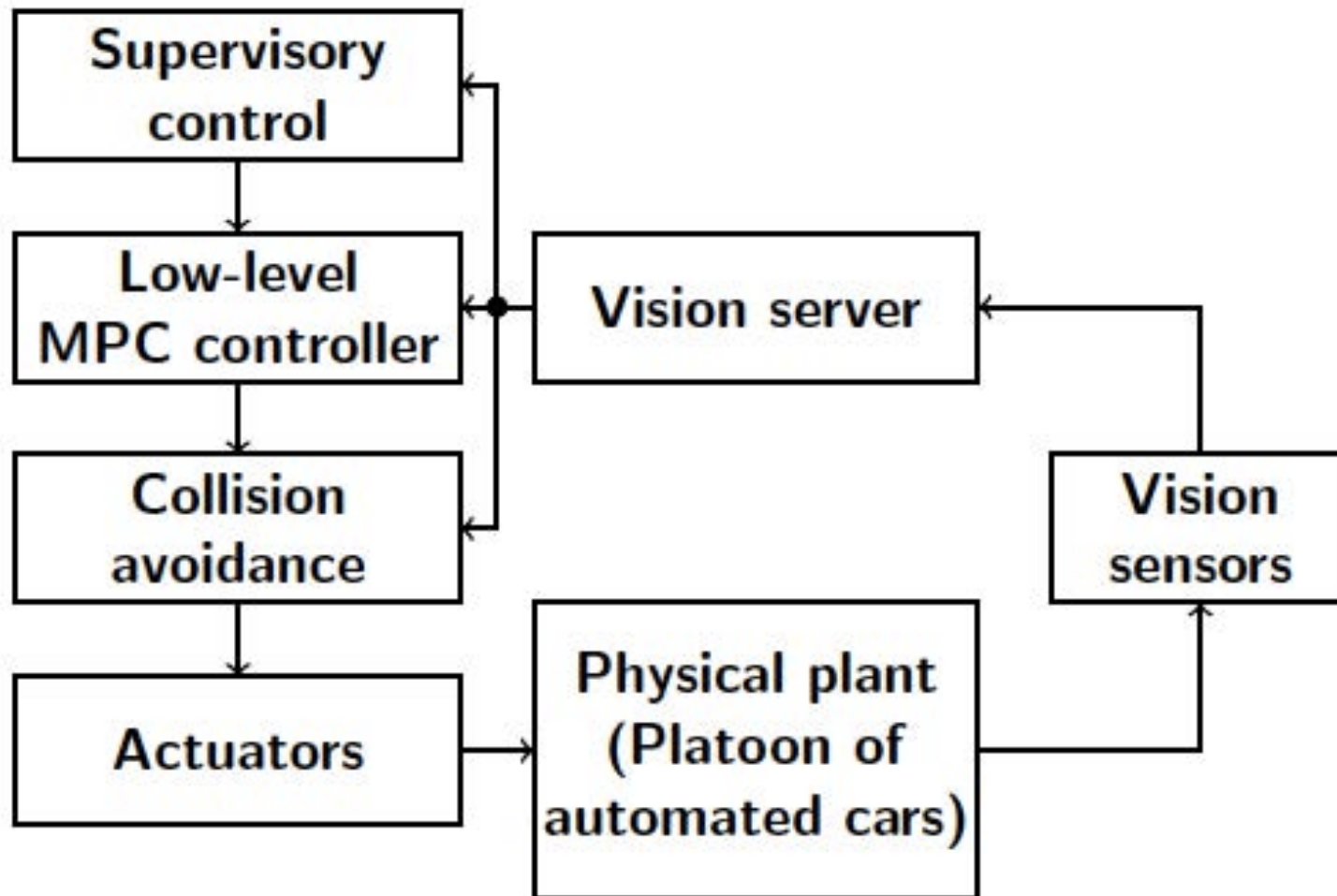
Automated vehicles are vulnerable to cyber attacks

- ◆ Hackers have demonstrated remote hijack of a Jeep's digital systems over the Internet
 - Resulted in the car manufacturer recalling over a million units to patch identified security vulnerabilities
- ◆ Automated cars use various sensors
 - Ultrasound sensor to determine distance of close objects
 - mm-wave radar to map road immediately ahead
- ◆ These sensors can be jammed.
Researchers from Zhejiang University have demonstrated such sensor attacks
- ◆ Several other demonstrations reported recently

Attacks on cars

- ◆ Car hacking is the future and sooner or later you'll be hit
 - <https://www.theguardian.com/technology/2016/aug/28/car-hacking-future-self-driving-security>
- ◆ Critical reasons for crashes investigated in the national motor vehicle crash causation survey
 - <https://crashstats.nhtsa.dot.gov/Api/Public/ViewPublication/812115>
- ◆ Hackers Remotely Kill a Jeep On the Highway- With Me in it”
 - <https://www.wired.com/2015/07/hackers-remotely-kill-jeep-highway/>
- ◆ Feature of daily news ...

Testbed architecture



System model for automatic vehicles

- ◆ Plant model for vehicle i given by its kinematic equations

$$x_i[t+1] = x_i[t] + h \cos(\theta_i[t])v_i[t] + h \cos(\theta_i[t])w_{ix}[t]$$

$$y_i[t+1] = y_i[t] + h \sin(\theta_i[t])v_i[t] + h \sin(\theta_i[t])w_{iy}[t]$$

$$\theta_i[t+1] = \theta_i[t] + h\omega_i[t] + hw_{i\theta}[t]$$

- ◆ h is the sampling period (100ms)
- ◆ $v_i[t]$ a control input, denoting speed
- ◆ $\omega_i[t]$ a control input, denoting angular
- ◆ $w_{ix}[t]$, $w_{iy}[t]$, $w_{i\theta}[t]$ all $N(0,2)$, i.i.d.
- ◆ Non-linear system

Watermarked system's performance in absence of attack

◆ Watermarked system

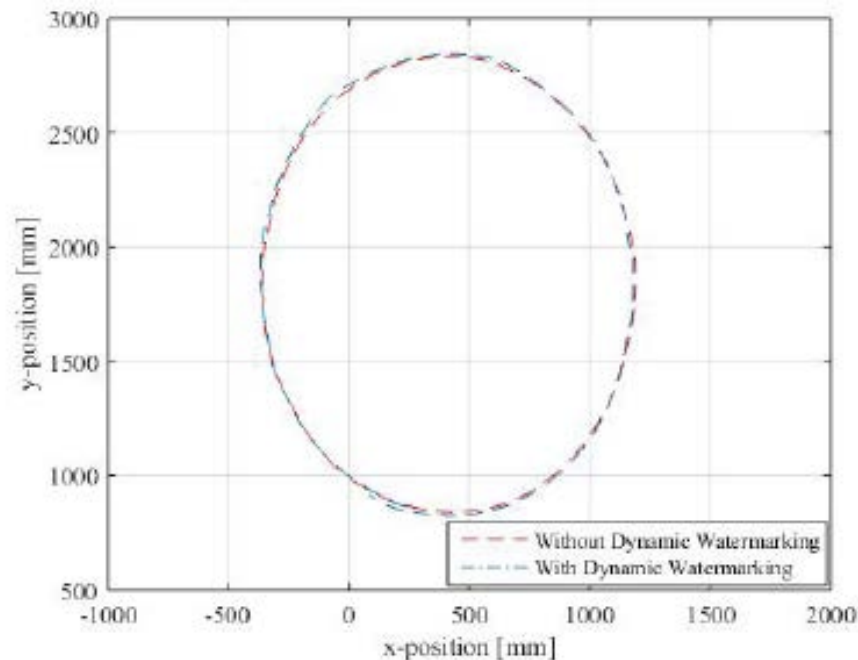
$$x_i[t+1] = x_i[t] + h \cos(\theta_i[t]) u_i^g(\mathbf{z}_1^t, \mathbf{z}_2^t) + h \cos(\theta_i[t]) e_{iv}[t] + h \cos(\theta_i[t]) w_{ix}[t]$$

$$y_i[t+1] = y_i[t] + h \sin(\theta_i[t]) u_i^g(\mathbf{z}_1^t, \mathbf{z}_2^t) + h \sin(\theta_i[t]) e_{iv}[t] + h \sin(\theta_i[t]) w_{iy}[t]$$

$$\theta_i[t+1] = \theta_i[t] + h \omega_i[t] + h e_{i\theta}[t] + h w_{i\theta}[t]$$

◆ Performance with and without watermarking

◆ Watermarks do not result in any added penalty on performance



Sensor attack

- ◆ Sensor attack

$$z_{2x}[t_A] = x_2[t_A] + \tau, \text{ where } \tau = \text{bias}$$

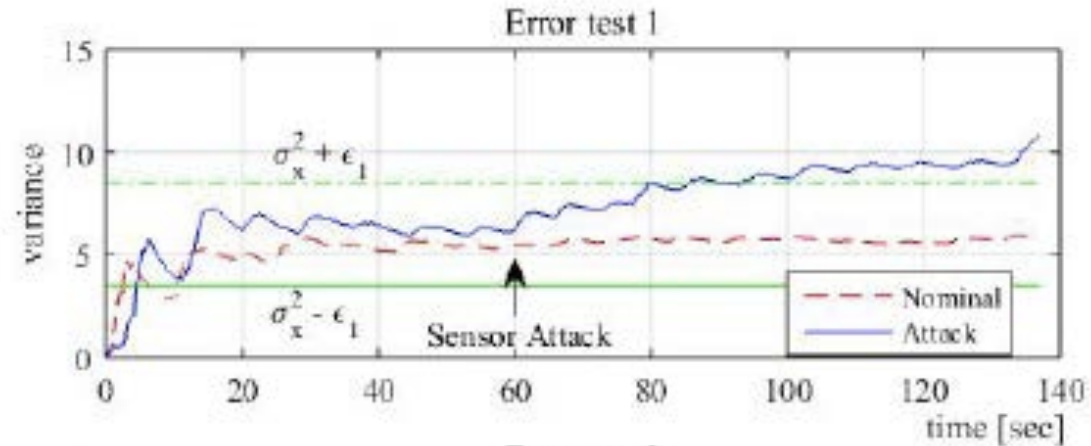
$$z_{2x}[t+1] = z_{2x}[t] + h \cos(\theta_2[t]) u_2^g(\mathbf{z}_1^t, \mathbf{z}_2^t) + \cos(\theta_2[t]) n[t]$$

$$n[t] \sim \mathcal{N}(0, \sigma_x^2)$$

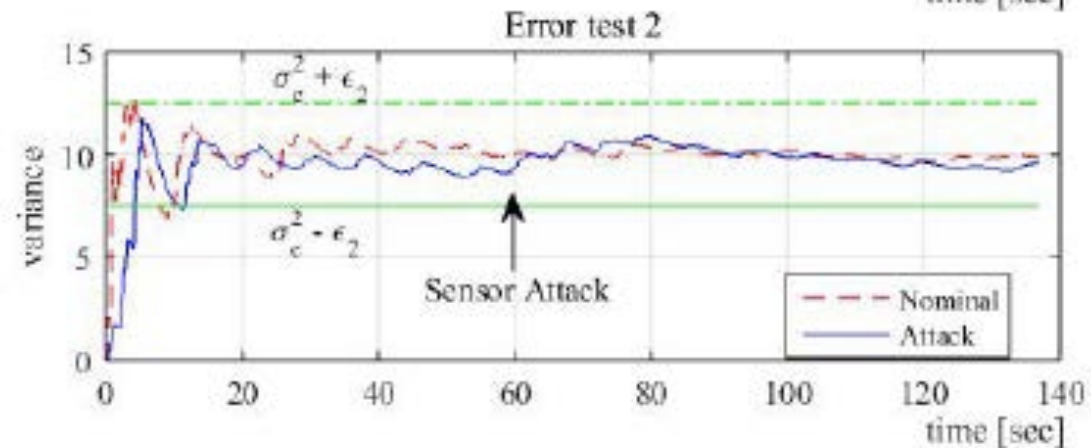
- ◆ This attack passes Test 2, but fails Test 1

Test Statistics

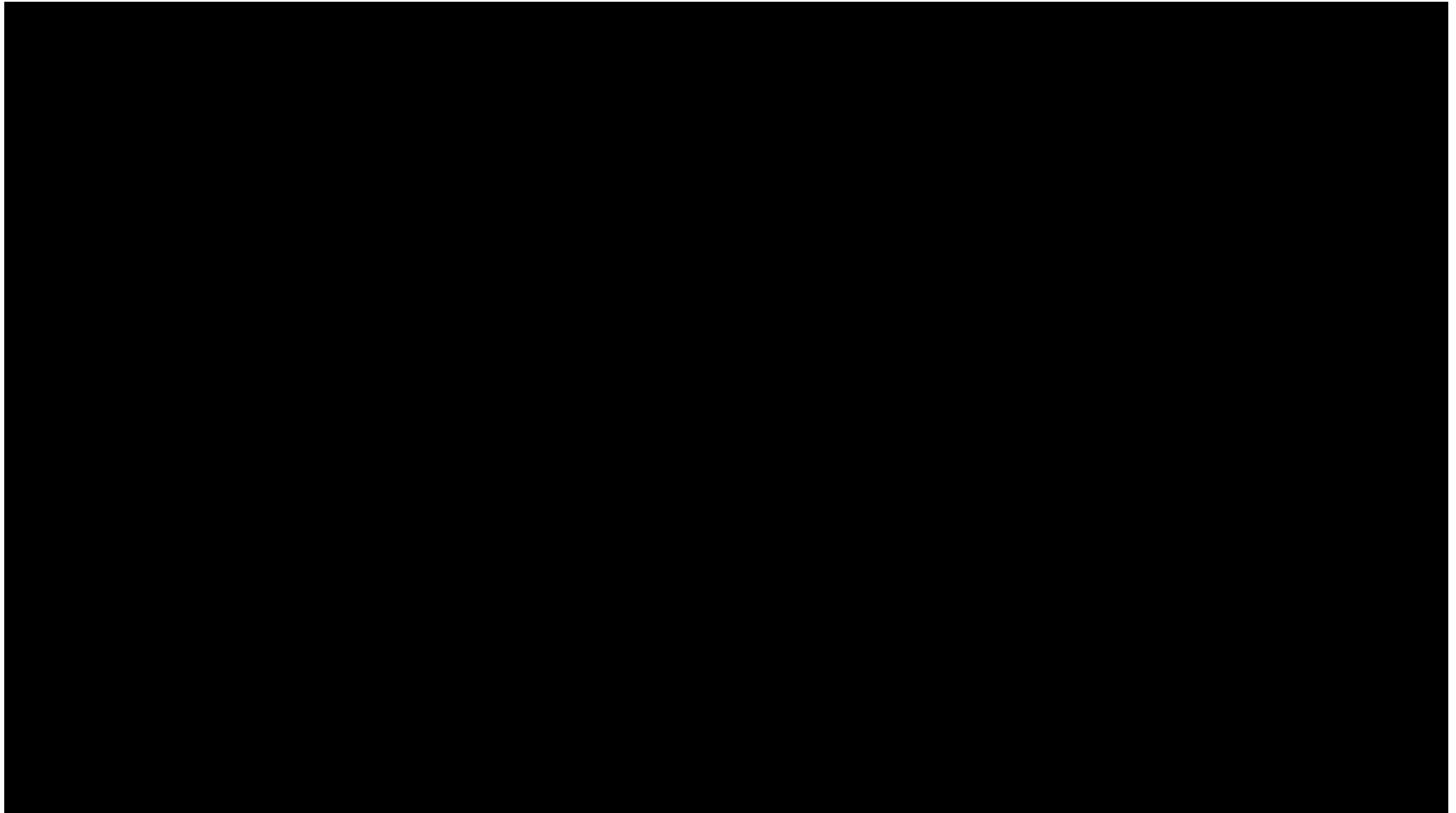
◆ Fails Test 1



◆ Passes Test 2



Defending against arbitrary sensor attacks



See the video “Tackling Autonomous Vehicle Cybersecurity Issues” at <https://cesg.tamu.edu/faculty/p-r-kumar/convergencelab/>

Remarks

- ◆ CPS is important for society and economy
- ◆ Lot of future infrastructure may be CPS
- ◆ Societally and economically important
- ◆ Security of CPS is a very rapidly emerging area
- ◆ Critical for safety of future infrastructure
- ◆ Lots of attacks have already been demonstrated

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Thank you