

Assignment 2:-

Find the global minimum point and value for the function

$$f(x, y) = x^2 + y^2 + 10$$

* Do manual calculations for two iterations.

step 1:- $x = -1, y = 1, \eta = 0.1, \text{epochs} = 2$

step 2:- $\text{iter} = 1$

step 3:- $\frac{\partial f}{\partial x} \Big|_{x=-1} = 2x + 0 + 0 = 2(-1) = \underline{\underline{-2}}$

$$\frac{\partial f}{\partial y} \Big|_{y=1} = 0 + 2y + 0 = 2(1) = \underline{\underline{2}}$$

step 4:- $\Delta x = -\eta \frac{\partial f}{\partial x} = -(0.1)(-2) = 0.2$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(2) = -0.2$$

step 5:- $x = x + \Delta x = -1 + 0.2 = -0.8$

$$y = y + \Delta y = 1 - 0.2 = 0.8$$

step 6:- $\text{iter} = \text{iter} + 1 = 1 + 1 = 2$

step 7:- if ($\text{iter} > \text{epochs}$)
 $2 > 2$
false: goto step 3.

step 3:- $\frac{\partial f}{\partial x} \Big|_{x=-0.8} = 2x = 2(-0.8) = -1.6$

$$\frac{\partial f}{\partial y} \Big|_{y=0.8} = 2y = 2(0.8) = 1.6$$

step 4:- $\Delta x = -\eta \frac{\partial f}{\partial x} = -(0.1)(-1.6) = 0.16$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(1.6) = -0.16$$

step 5:- $x = x + \Delta x = -0.8 + 0.16 = -0.64$

$$y = y + \Delta y = 0.8 - 0.16 = 0.64$$

step 6:- $\text{iter} = \text{iter} + 1 = 2 + 1 = 3$

step 7:- $\text{if } (\text{iter} > \text{epochs})$
 $3 > 2$

True, goto step 8

step 8:- print x & y values

$$x = -0.64$$

$$y = 0.64$$

$$f(x, y) = x^2 + y^2 + 10$$

$$= (-0.64)^2 + (0.64)^2 + 10$$

$f(x, y) = 10.81$