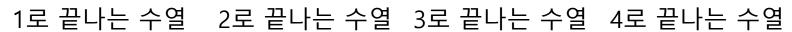
• 순열



• P(n,n) = n * (n-1)!

1 2 3 4	2 1 3 4	3 1 2 4	4 1 2 3
1 2 4 3	2 1 4 3	3 1 4 2	4 1 3 2
1 3 2 4	2 3 1 4	3 2 1 4	4213
1 3 4 2	2 3 4 1	3 2 4 1	4 2 3 1
1 4 2 3	2 4 1 3	3 4 1 2	4 3 1 2
1 4 3 2	2 4 3 1	3 4 2 1	4 3 2 1



2 3 4 <u>1</u>	1 3 4 <u>2</u>	1 2 4 <u>3</u>	1 2 3 <u>4</u>
2 4 3 <u>1</u>	1 4 3 <u>2</u>	1 4 2 <u>3</u>	1 3 2 <u>4</u>
3 2 4 <u>1</u>	3 1 4 <u>2</u>	2 1 4 <u>3</u>	2 1 3 <u>4</u>
3 4 2 <u>1</u>	3 4 1 <u>2</u>	2 4 1 <u>3</u>	2 3 1 <u>4</u>
4 2 3 <u>1</u>	4 1 3 <u>2</u>	4 1 2 <u>3</u>	3 1 2 <u>4</u>
4 3 2 <u>1</u>	4 3 1 <u>2</u>	4 2 1 <u>3</u>	3 2 1 <u>4</u>



• 순열 생성 재귀적 알고리즘1

```
perm(n, r)
      if (r == 0) print_arr()
      else
             for (i : n - 1 \sim 0)
                    swap(a[i], a[n - 1])
                    t[r - 1] = a[n - 1]
                    perm(n - 1, r - 1)
                    swap(a[i], a[n - 1])
```



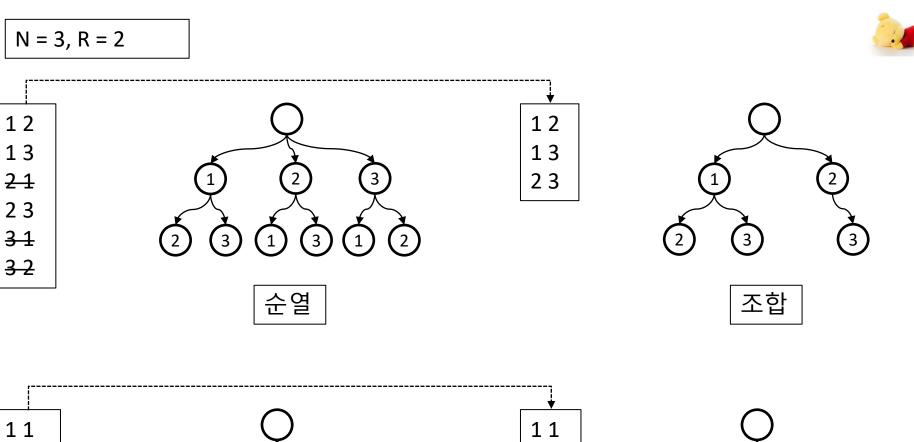
• 순열 생성 재귀적 알고리즘2

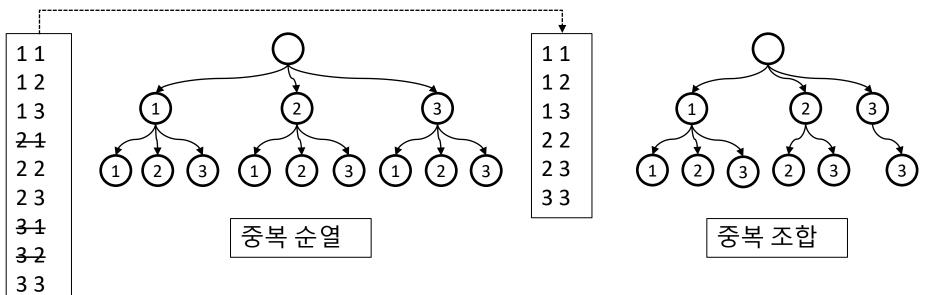
```
perm(k)
    if (k == R) print_arr()
    else
        for (i : k ~ N - 1)
            swap(k, i)
            perm(k + 1)
            swap(k, i)
```



• 순열 생성 재귀적 알고리즘3

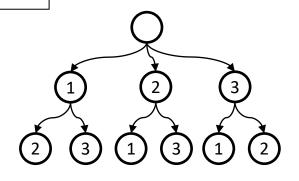
```
Visited[N-1]
perm(k)
       if (k == N) print_arr()
       else
             for (i : 0 \sim N - 1)
                    if (visited[i]) continue
                    t[k] = a[i]
                    visited[i] = true
                    perm(k + 1)
                    visited[i] = false
```



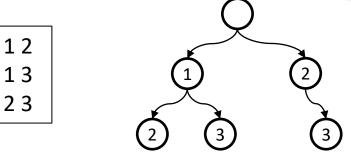




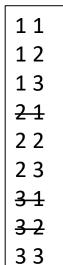


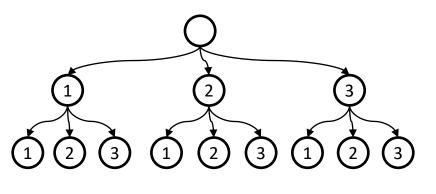


for x1 : 1 ~ 3 for x2 : 1 ~ 3 단, x2 != x1 print(x1, x2)

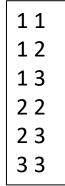


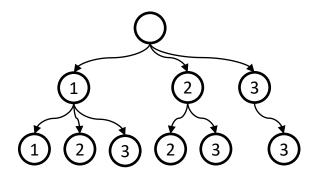
for x1 : 1 ~ 2 for x2 : 2 ~ 3 print(x1, x2)





for x1 : 1 ~ 3 for x2 : 1 ~ 3 print(x1, x2)





for x1 : 1 ~ 3 for x2 : x1 ~ 3 print(x1, x2)

조합



서로 다른 n개의 원소 중 r개를 순서 없이 골라낸 것을 조합



• 조합 생성 재귀적 알고리즘1

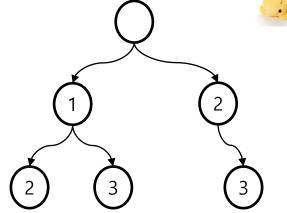
$$C(n,r) = C(n-1,r-1) + C(n-1,r)$$

```
comb(n, r)
      if( r == 0) print_arr()
      else if (n < r) return
      else
             t[r-1] = a[n-1]
             comb(n-1, r-1)
             comb(n-1, r)
```



• 조합 생성 재귀적 알고리즘2

• 초기값 : k = 0, s = 0, N, R



```
comb(k, s) // 깊이, 시작숫자

if (k == R) print_arr()

else

for (int i : s ~ N - R + k )

t[k] = a[i]

comb(k + 1, i + 1)
```



• 중복 순열 생성 재귀적 알고리즘1

```
PI(n, r)

if (r == 0) print()

else
```

```
perm(n, r)
    if (r == 0) print()
    else
        for (i : n - 1 ~ 0)
            swap(a[i], a[n - 1])
        t[r - 1] = a[n - 1]
        perm(n - 1, r - 1)
        swap(a[i], a[n - 1])
```



• 중복 순열 생성 재귀적 알고리즘2 n^r

```
PI(k) // 깊이

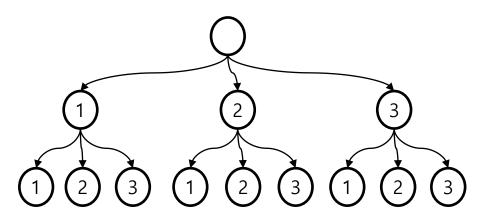
if (k == R) print_arr()

else

for (i : 0 ~ N - 1)

t[k] = a[i]

pi_r(k + 1)
```



GE

• 중복조합 생성 재귀적 알고리즘1

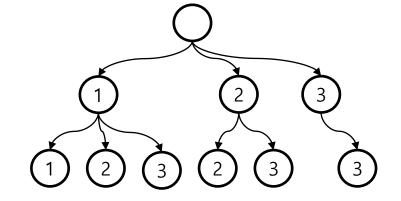
```
H(n, r)
    if( r == 0) print_arr()
    else if (n == 0) return
    else
    t[r-1] = a[n-1]
    H(n, r-1)
    H(n-1, r)
```

$$H(n,r) = H(n,n-1) + H(n-1,r)$$



• 중복조합 생성 재귀적 알고리즘2

● 초기값 : K = 0, s = 1, N, R



```
H(k, s) // 깊이, 시작숫자

if (k == R) print_arr()

else

for (int i : s ~ N )

t[k] = a[i]

H(k + 1, i)
```