

# Machine Learning

Daniel Glez-Peña & Hugo López-Fernández & Alba Nogueira-Rodríguez

@SINGgroup 🐦

@lipido (Daniel) 🐦

www.sing-group.org

# Agenda



#### Machine Learning Introduction

Supervised learning

Unsupervised learning

Machine Learning in Bioinformatics

#### Supervised learning

Workflow

Overfitting

Feature selection

Classifier evaluation and comparison

**Basic Algorithms** 

Naïve Bayes

Instance-based

Decision trees

Linear

Classifier ensembles

#### Deep Learning

Convolutional Neural Networks. Transformers. Language Models.

Transformers and LLMs



## Machine Learning Introduction

# What is Machine Learning?



Trying to make machines able to solve problems without explicitly programming them

"Training" instead of programming

## Types

Supervised Learning

Unsupervised Learning

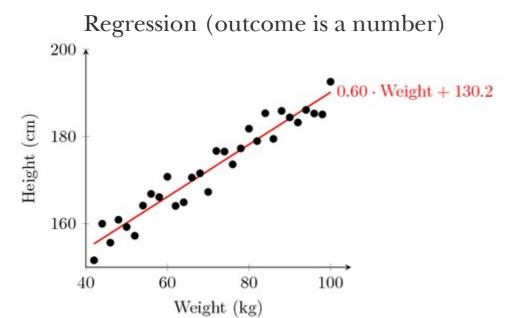
Reinforcement Learning



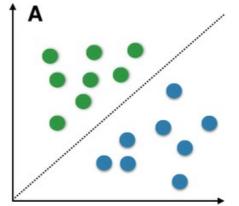
# Supervised learning

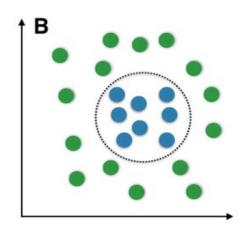


Given a set of "instances", each one with a set of measured "attributes" and an "outcome" value, we want to train a "model", that predicts the outcome in further problem instances.



Classification (outcome is a category)

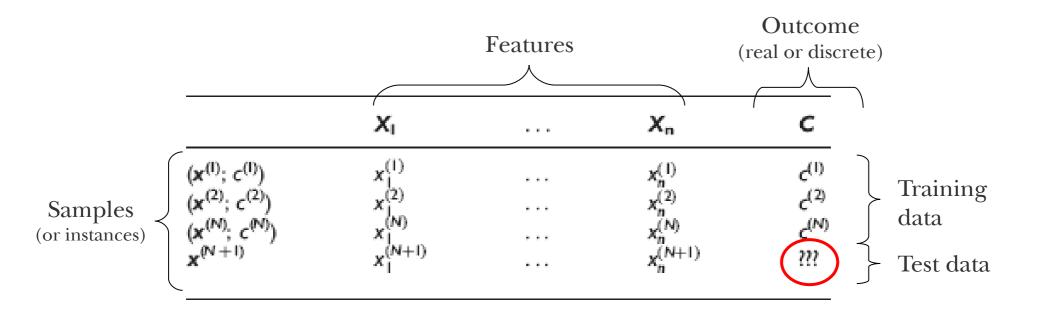




# Supervised learning



## Input dataset structure for learning



# Supervised learning



### Popular techniques

#### Bayesian classifiers:

Naive Bayes, semi-NB, Tree augmented NB, k dependence Bayesian...



CART, C4.5, RandomForest, J48...

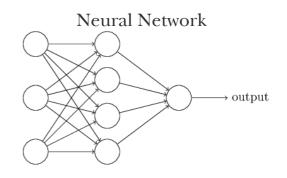
K-Nearest Neighbours

Linear/Logistic regression

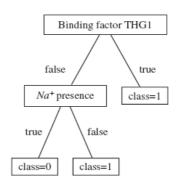
**Support Vector Machines** 

Neural networks

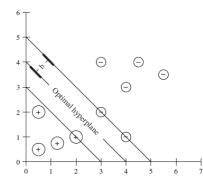
Meta: Bagging, Boosting

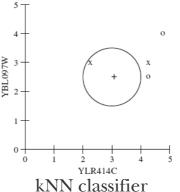


#### **Classification Tree**



#### Support Vector Machine





# Unsupervised learning



Learning underlying structures in data

Clustering (learn group of samples)

Partition a set of "instances" in several groups (clusters) given the differences between them

They are based on "distances" between instances that is a problemdependant issue

Typical: Euclidean, Pearson, Sperman

Dimensionality reduction (learn alternative representations)

Reduce the number of input variables while trying to keep the maximum information of the dataset

Very useful for visualization (n dimensions  $\rightarrow$  2D or 3D)

# Unsupervised learning



## Popular techniques

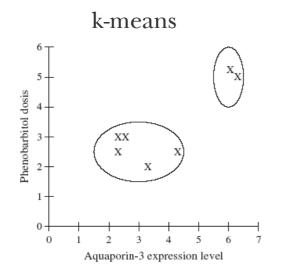
Partition clustering

k-means, SOM, GCS, PAM

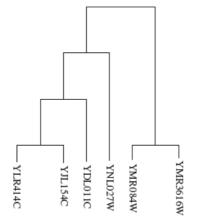
Hierarchical clustering with single-linkage, complete linkage, centroid linkage and wards-criterion

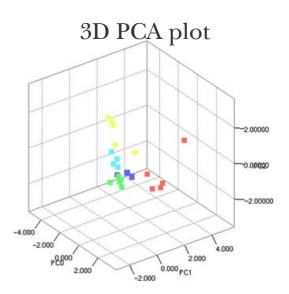
They produce the popular "dendograms"

### Model-based clustering









## **Bioinformatics**



Application of the Information Technologies to the field of Molecular Biology

**Databases** 

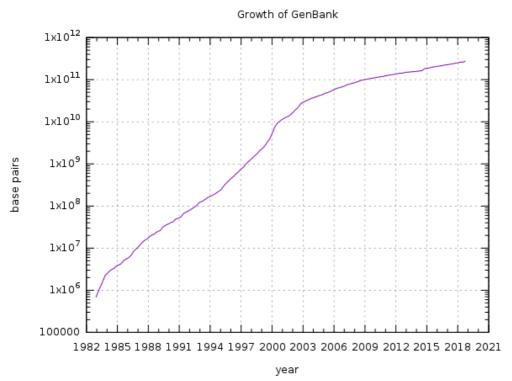
Algorithms

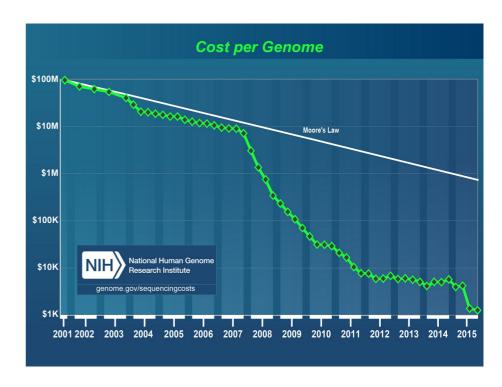
Statistical techniques

... to solve formal and practical problems arising from the management and analysis of biological data

## **Bioinformatics**



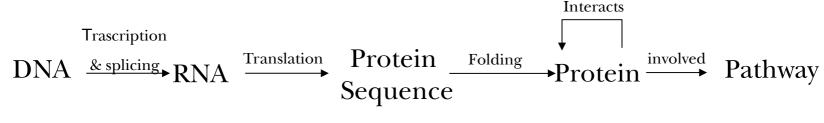




As of release 228, retrieved 2018-11-30

# The Dogma & Bioinformatics





Nucleotide	Transcripts	Aminoacid	3D	Set of Reactions
sequence		sequence	structure	
ACTTGTC		MEEPQSDPSV		
ATGGCGA		<b>EPPLSQETFSD</b>		
CTGTCCT		LWKLLPENNV		
TTGTGC		LS		
•••			Interactomics	

GENOMICS	PROTEOMICS	METABOLOMICS

Sequence analysis

Genome annotation

Analysis of mutations

[DNA-seq]

Gene expression analysis [microarrays/RNA-seq]

Protein expression analysis [mass spectometry]

Protein interaction prediction

[3D docking]

Protein structure prediction

[folding]

#### **Evolution**

Phylogenetic reconstruction Comparative genomics Modelling biological systems Functional analysis

## **Bioinformatics Data**



#### Genomics

#### Sequences

















Gene-centric

Entrez Gene



#### **Proteomics**

#### **Proteins**











#### Structure







#### **Domains**











#### Experimental data







#### Interactomics & **Metabolomics**

**Prot-Prot** interactions





#### **Pathways**







#### **Ontologies**









# Supervised learn. in Bioinformatics



#### Genomics

Gene finding (if a sequence is a coding region)

Splice site prediction (if a sequence is a splice site)

Predict disease genes (e.g. from its sequence length)

Prediction of mutation (SNP) effect

Cancer prediction from gene expression (microarrays/RNA-seq)

#### **Proteomics**

Prediction of secondary structure (alpha-helix, beta-sheet, etc.)

Prediction of 3D structure

Prediction of sub-cellular location of the protein

Cancer prediction from protein expression (mass spectra)

# Supervised learn. in Bioinformatics



## Systems biology

Predict the cell migration speed (high, low) from the phosphorilation levels of signaling proteins

Predict a gene regulatory level (up-regulated or down-regulated given the 'related' genes expression)

## Text mining

Protein/gene recognition in biomedical literature

is this word a gene/protein given some word features: ortographic, part-of-speech, suffix, trigger words, etc...??

# Unsupervised learn. in Bioinformatics



## Mainly in Genomics and Proteomics

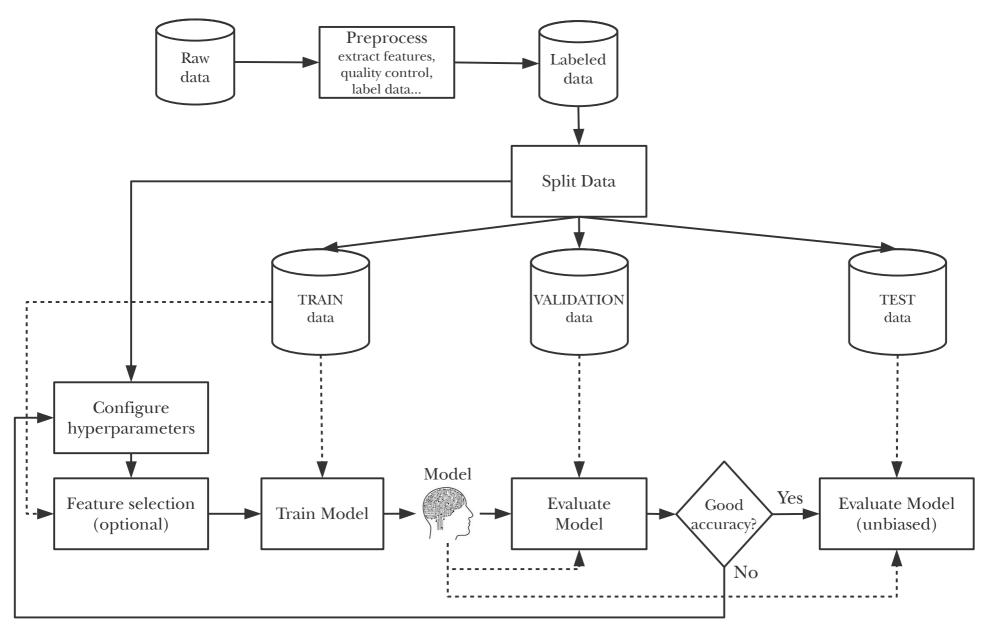
- Co-expression detection (group of genes/proteins with similar expression)
- Subclass discovery (group of samples given the expression of its genes)
- Expression data visualization with dendograms



Supervised Learning

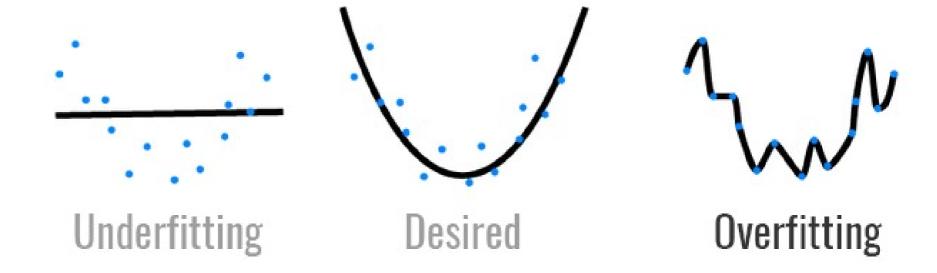
# Supervised learning workflow





# Overfitting

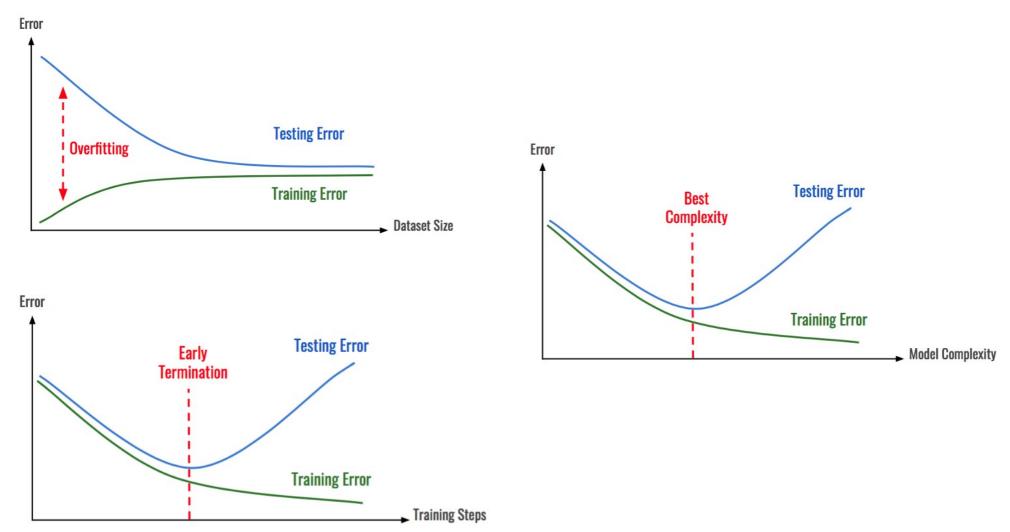




https://hackernoon.com/memorizing-is-not-learning-6-tricks-to-prevent-overfitting-in-machine-learning-820b091dc42

# Overfitting





https://hackernoon.com/memorizing-is-not-learning-6-tricks-to-prevent-overfitting-in-machine-learning-820b091dc42

## Feature selection



Are all input attributes useful?

Advantages: reduced cost in data acquisition, more interpretable models, faster training, and better accuracy

It is a search space problem (2<sup>n</sup>-1), in general:

1. Generate a subset

Brute force (all possible subsets)

Deterministic/not deterministic heuristic search

2. Evaluate subset

Statistical estimation: Information Gain, X2, t-test, DFP, CFS

Wrapper (use classifier accuracy in training/validation set)

3. if (!halt\_condition) GOTO 1



Classifier evaluation and comparison



## Performance metrics. In binary classification:

#### Actual

	Positive	Negative	
Positive	True Positives (TP)	False Positives (FP) Type-I error	Positive Predictive Value (PPV) or precision = TP / (TP + FP)  False Discovery Rate (FDR) = 1 - PPV
Negative	False Negatives (FN) Type-II error	True Negatives (TN)	Negative Predictive Value (NPV) = TN / (FN + TN)  False Omission Rate (FOR) = 1 - NPV
	Sensitivity or recall or True positive rate (TPR) = TP / (TP+FN)	Specificity or True Negative Rate(TNR)  = TN / (FP+TN)	Accuracy = (TP + TN) / N
	False Negative Rate (FNR) = 1 - TPR	False Positive Rate (FPR) = 1 - TNR	



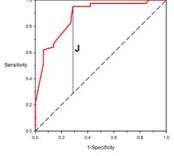
#### Combining measures in binary classification:

Accuracy is affected by class imbalance. E.g. a classifier of 80% of accuracy has no utility (random classifier) if the majority class is 80% of the samples. In this case, use measures that takes this into account.

**AUC (Area Under ROC Curve)**, combines sensitivity and specificity. **0.5 means random**, 1 means perfect.

Youden's index (J), also combines sensitivity and specificity easily. 0 means random, 1 means perfect.

$$J = sensitivity + specificity - 1$$



Relation between AUC and Youden's J (only J > 0, if AUC > 0,5)

Matthews Correlation Coefficient. 0 means random, +1 means perfect, -1 total disagreement.

$$ext{MCC} = rac{TP imes TN - FP imes FN}{\sqrt{(TP + FP)(TP + FN)(TN + FP)(TN + FN)}}$$

**F-score**, combines recall and precision (PPV), however it has no gold "good values", it is relative. It should be used to compare different classifiers over the same test dataset.

$$F_1 = 2 \frac{precision \cdot recall}{precision + recall}$$



Performance metrics. In multi-class classification:

Accuracy and the multi-class version of MCC, or Cohen's Kappa are valid for multi-class classifier evaluation.

And both MCC and Kappa do take class imbalance into account.

We can also use the previous binary metrics for each class by considering

positive = class
negative = other classes

However, there will be multiple sensitivities, specificities, PPV, etc. (one per class)



Ideally, we should do several tests for a model in order to better estimate its real performance. If the test data is big enough, and not biased, the estimation is good

However, when we have a reduced number of samples, it is not easy. There are several validation frameworks:

Holdout

Bootstrapping

Cross-validation



## Holdout

Divide dataset randomly in several subsets

In general, we take 2/3 for train and the rest for test

Variant: "resampling"

It consists in conducing several holdout test over different train and test datasets



## Bootstrapping

Given a dataset with N samples

Create a training set of size N, taking samples N times randomly, with replacement

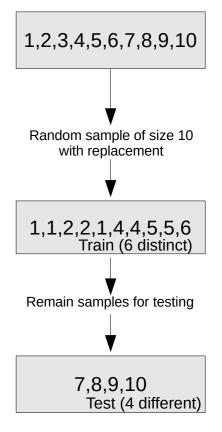
In general, with a size big enough, the number of different instances in the sample tends towards 63.2% of N

$$P(\text{of being selected with 1 trial}) = \frac{1}{N}$$

$$P(\text{not being selected}) = 1 - \frac{1}{N}$$

$$P(\text{not being selected in N trials}) = \left(1 - \frac{1}{N}\right)^n \approx e^{-1} = 0.368$$
Number of different samples on train = 1 - 0.368 = 0.632

The final error of this method can be weighted using the training error:





#### Cross-validation (CV)

Create K pairs of training and test

Example. With 10 samples, conduct a 3-fold CV, we get 3 pairs, with a 33% of samples for testing and the rest for training

Each sample appears as test sample in exactly one pair

K=10 is one of the most popular values

To better estimate the performance, we can repeat CV 10 times, giving a total of 100 train-test experiments

Stratified: keep the same class distribution of the complete dataset in each train/test subsamples

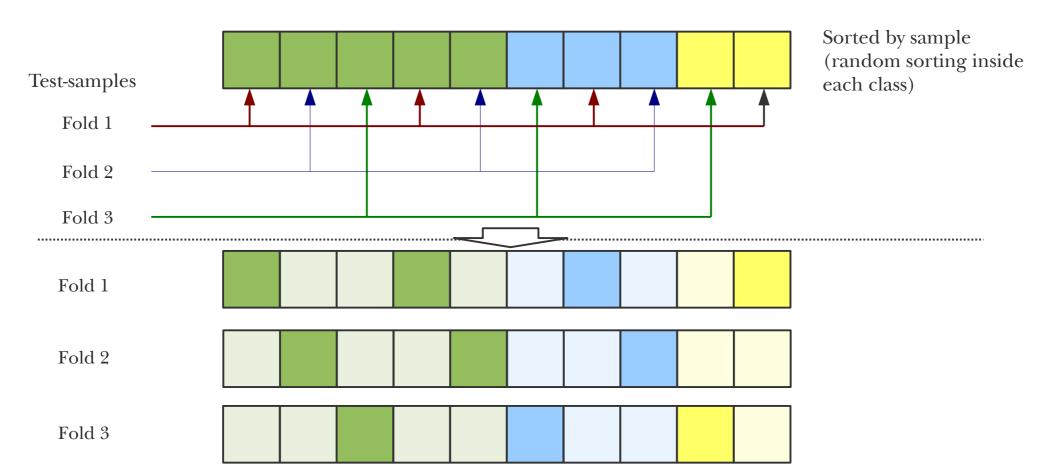
Leave-one-out. Variant where K=N, that is, the test subset in each pair has only one sample

Useful when there are very few training samples



## Cross validation.

## Example. Stratified 3-fold CV





## We can use the CV error directly

However, differences can be due to chance

We can employ statistical tests over CV estimations to tell if differences are statistically significant. Example methods

McNemar test

CV + Paired t-test

5x 2-fold-CV + Paired t-test

Repeated CVs + corrected resampled t-test (weka)



### McNemar test

Given the output of two classifiers (A,B) for each sample, we have 4 possibilities:

n <sub>00</sub> : Both classifiers fail	n <sub>01</sub> : A fails, B hits	
n <sub>10</sub> : B fails, A hits	n <sub>11</sub> : Both classifiers hit	

The next T score is based on observing differences between off-diagonal values ( $n_{10}$  y  $n_{01}$ ), which are cells counting when classifiers differ. **Null hypothesis**. Differences between  $n_{10}$  and  $n_{01}$  is 0.

$$T = \frac{(|n_{01} - n_{10}| - 1)^2}{n_{01} + n_{10}}$$

This score follows a chi-squared distribution with 1 degree of freedom. For example a T > 3.8414 gives p-values < 0.05.



CV + Paired t-test

Conduct a K-fold CV. We get K accuracies of each classifier

	Fold 1	Fold 2	Fold 3	Fold 4	•••	Fold K
Classifier A	0.7	0.75	0.78	0.79		0.77
Classifier B	0.6	0.65	0.64	0.62		0.69

Null hypothesis: both classifiers has the same mean accuracy

Conduct a Student's paired t-test

Problem: The t-test assumes independency of each pair However, CV generates overlapping training samples



#### 5x 2CV + Paired t-test

### Conduct 2-fold CV 5 times

The first replicate to estimate error; all replicates to estimate variance

## On each of the 5 experiments:

	Fold 1	Fold 2
Classifier A	0.7	0.75
Classifier B	0.6	0.65

$$p^{(1)}$$
: differences of A and B errors in fold 1  $p^{(2)}$ : differences of A and B errors in fold 2  $s^2 = (p^{(1)} - \bar{p})^2 + (p^{(2)} - \bar{p})^2$ 

Compute an statistic that follows a distribution similar to Student's t with 5 degrees of freedom:

$$\tilde{t} = \frac{p_1^{(1)}}{\sqrt{\frac{1}{5}\sum_{i=1}^5 s_i^2}}$$
 With t < 2.02 we get p-values < 0.05





Repeated CVs + corrected resampled t-test

Test included in Weka Experimenter

Conduct CV several times:

For example: 10x10-fold CV

We get 100 accuracy values for each classifier

Use a variant of Student's t-test which takes into account that samples are not independent(samples are repeated in different train-test samples) and also avoid the bias introduced with the total number of trials

$$t = \frac{\overline{d}}{\sqrt{\left(\frac{1}{k} + \frac{n_2}{n_1}\right)\sigma_d^2}}$$

 $\bar{d}$ : classifier A and B accuracy mean differences in each trial (100 trials) k: number of trials, in a 10x10CV, k is 100  $n_1$ : ratio for train,  $n_2$ : ratio for test. In a 10CV  $n_1$  is 0.9 and  $n_2$  is 0.1

This score follows a Student's t distribution with folds-1 degrees of freedom (9 for 10-fold CV)



## Supervised Learning Algorithms

# Bayesian



#### Naïve Bayes

Classification consist in find P(class | features)

With conditional dependencies (using Bayes). We need to know 2<sup>n</sup> different probabilities (n=number of features, unfeasible).

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

$$P(cavities|pain \land infection) = \frac{P(pain \land infection|cavities)P(cavities)}{P(pain \land infection)}$$

#### With conditional independence

Idea: two random variables can be independent once a third variable is known.

Mathematically:

 $P(pain \land infection | cavities) = P(pain | cavities) P(infection | cavities)$  pain and infection are independent once the value of cavities is known

Replacing in the previous Bayes formula:

$$P(cavities|pain \land infection) = \frac{P(pain|cavities)P(infection|cavities)P(cavities)}{P(pain \land infection)} P(cavities)P(ca$$

<u>Conditional indedepencence</u> allows us to scale probability-based systems; indeed, they are more available than those assuming total independence

# Bayesian



## Naïve Bayes

Conditional independence (cont)

So we have: effects(s)

 $\alpha$ =(1/denominator) in the Bayes function. It can be solved by considering that P(c) + P(¬c) = 1

cause 
$$P(C|F_1,...,F_n) = \alpha P(C) \prod_{i=1}^n P(F_i|C)$$

It is a typical pattern: One cause has multiple effects, all of them conditionally independent, once such cause is known.

Naïve-Bayes (or simple-Bayes)

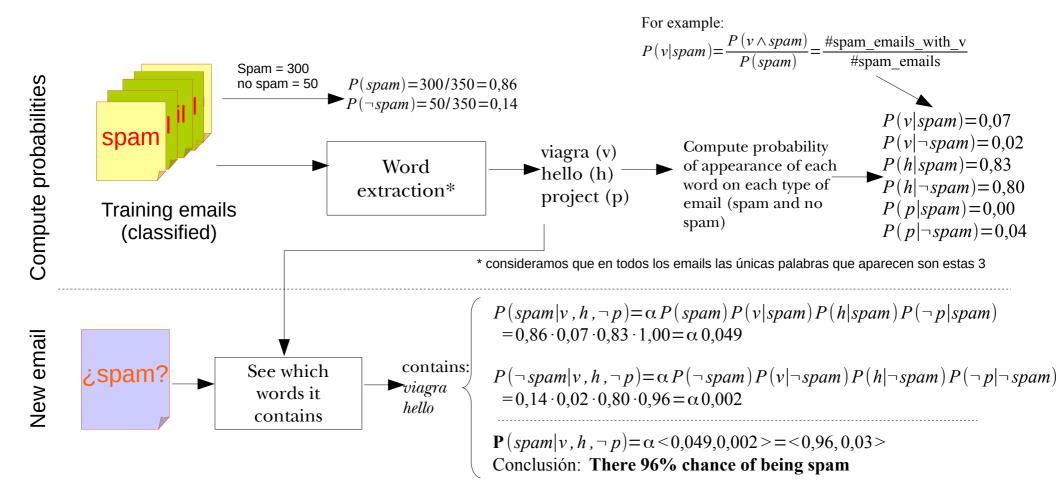
Sometimes, even when such conditional independence is not real, we make this assumption in order to make the system feasible

# Bayesian



#### Naïve Bayes

Naive-Bayes. Example: Detecting spam email



## Instance based



#### Introduction

During training, we save all samples without any modification.

With a distance function we find the nearest saved sample to the new sample and we give the class of the found sample as prediction.

#### Distance functions:

Euclidean 
$$dist(p,q) = \sqrt{\sum_{i=1}^{n} (p_i - q_i)^2}$$
  
Manhattan  $dist(p,q) = \sum_{i=1}^{n} |p_i - q_i|$ 

Manhattan 
$$dist(p,q) = \sum_{i=1}^{n} |p_i - q_i|$$

Euclidean, with exponent >2 (increases the influence in greater distances).

## Instance based



#### Normalization

If attributes have a different scale (for example, age [0, 100] and price [10k, 100k], attributes with larger values have bigger influence, so it is typical to normalize them, for example:

feature scaling:

$$scale(v_i) = \frac{v_i - \min v_i}{\max v_i - \min v_i}$$

stardardization (mean 0, sd 1):

$$z(v_i) = \frac{x - \mu}{\sigma}$$

#### Non numerical attributes

The distance between two nominal values is 1 if they are different and 0 if they are the same



Try to learn a decision tree from data

Basic iterative process:

Select an attribute

Create a branch for each value of the attribute

Each branch includes a set of samples

Repeat the process on each branch, taking only into account those samples under such branch

If the samples are of the same class, stop



#### Which attribute is the best?

We look for the attribute which gives more information about the class

Information gain

We try that on each branch there is a dominant class

It is important to take into account all branches

Some branch can include samples of the same class but other branches don't

Branch-size weighted mean

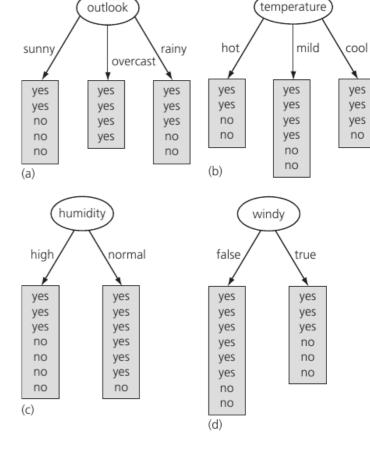
```
      outlook info
      3 branches
      (c)

      info([2,3]) = 0.971
      sunny branch

      info([4,0]) = 0.0
      overcast branch

      info([3,2]) = 0.971
      rainy branch

      info(outlook) = info([2,3], [4,0], [3,2]) = 5/14*0.971 + 4/14*0.5/14*0.971 = 0.693
```



Root attribute:  $\inf(root) = \inf([9,5]) = 0.940$   $Gain(outlook) = \inf(root) - \inf(outlook) = 0.940 - 0.693 = 0.247$  //best option Gain(temperature) = 0.029 Gain(humidity) = 0.152 Gain(windy) = 0.048



Function info([#classA, #classB, ..., #classN])

It should be:

**Multiclass** 

If all are of the same class, it should return 0

If all are distributed uniformly, it should be maximum

It should meet the *step-by-step* evaluation property

Example (3 classes: A,B,C):

 $\inf_{(2,3,4]} = \inf_{(2,7]} + (7/9) * \inf_{(3,4]}$ 

First we decide A vs. "others" and then (in 7 of 9 cases) we decide if it is B or C

An example of "info" function that meets these properties is *entropy* 

```
entropy([p_1,...,p_n]) = -p_1\log p_1 - ... - p_n\log p_n
info([p_1,...,p_n]) = entropy([p_1/N,...,p_n/N]), where N = p_1+...+p_n
```



If we have attributes with many possible values, we should make a correction

Many branches promotes gain, which is an undesired effect We compute *gain ratio*.

gain\_ratio(attribute) = gain(attribute) / split\_info(attribute)
where:

split\_info(attribute) = info([#branch1, ..., #branchN])

Necessary info to know which branch will be taken. It only takes into account how much members belong to each branch. The more branches, the more split\_info, so less gain

	Outlook		Temperature		Humidity		Windy	
	info:	0.693	info:	0.911	info:	0.788	info:	0.892
	gain: 0.940–	0.247	gain: 0.940–	0.029	gain: 0.940–	0.152	gain: 0.940–	0.048
Ĺ.,	0.693		0.911		0.788		0.892	
	split info:	1.577	split info:	1.557	split info:	1.000	split info:	0.985
	info([5,4,5])		info([4,6,4])		info ([7,7])		info([8,6])	
	gain ratio:	0.157	gain ratio:	0.019	gain ratio:	0.152	gain ratio:	0.049
	0.247/1.577		0.029/1.557		0.152/1		0.048/0.985	



Work with numerical attributes

They are intended to classify samples that are *linearly separable* 

#### Linear regression

The predicted value for a sample  $i = (a_1, ..., a_k)$  will be:

$$predict(a^{(i)}) = w_0 + \sum_{j=1}^{k} w_j \cdot a_j^{(i)}$$

w is a weight vector, which is computed by trying to minimize the training error ( $x^{(i)}$  = class of sample i)

$$error = \sum_{i=1}^{n} (x^{(i)} - (w_0 + \sum_{j=1}^{k} w_j \cdot a_j^{(i)}))$$



#### Linear Regression

How to compute w?

#### Gradient descent algorithm

Iterative algorithm to find the minimum of a function (the error function) Briefly:

At each step, the error is computed and weights are updated in order to reduce this error.

The algorithm stops when the error is small enough or a maximum number of iterations is reached.

#### How it works? It is based on the derivative of the *cost function*

The cost function is similar to the error given the weights, but we want it to be positive (independent of the direction of the error) and easily derivable

$$J(w, w_0) = \frac{1}{2} \sum_{i=1}^{n} (x^{(i)} - (w_0 + \sum_{j=1}^{k} w_j \cdot a_j^{(i)}))^2$$



#### **Linear Regression**

Gradient descent algorithm (cont)

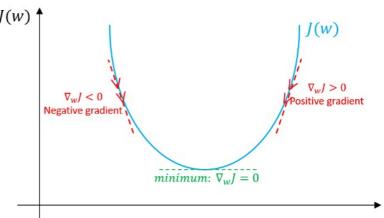
This algorithm needs the gradient, based on the derivative of the cost function

$$\frac{\partial J(w, w_0)}{\partial w_f} = -\sum_{i=1}^n (x^{(i)} - (w_0 + \sum_{j=1}^k w_j a_j^{(i)})) a_f^{(i)}$$

Intuition: the derivative means how the cost varies when changing the weight  $w_f$ . It depends both on the amount of current error and how big are the values of the attribute in the training set.

At each iteration, each weight  $w_f$  is updated in the opposite direction of its partial derivative and at a learning rate

$$w_f := w_f - \alpha \frac{\partial J(w, w_0)}{\partial w_f}$$



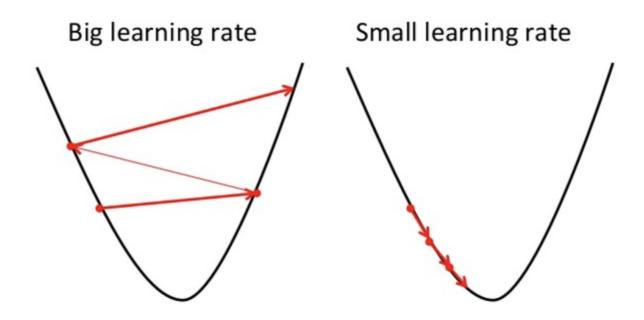


## Gradient descent algorithm (cont)

The learning rate  $\alpha$  must be carefully selected

Very small learning rates makes the training process slower

Very large learning rates makes the descent to jump over the minimum





#### Linear Regression

Adapting linear regression for classification seems to be easy: each data point is associated with 0 or 1, for each of the two possible classes

#### **Problems:**

Linear regression does not gives values between 0 and 1, which are intuitively associated to a probability of belonging to a class.

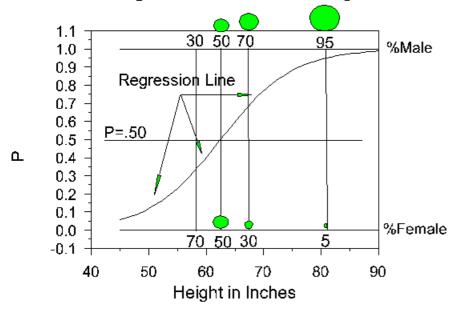
Not statistically sound: it assumes that error follows a normal distribution and the variance is constant, which is not true for binary outputs.

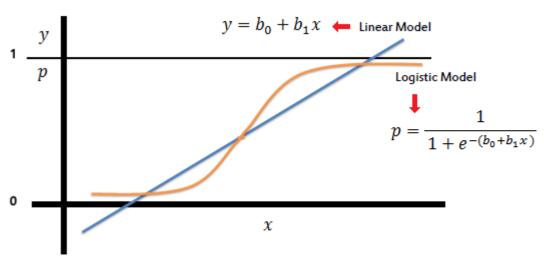


## Logistic regression

#### Graphical interpretation of the outcome

Regression of Sex on Height





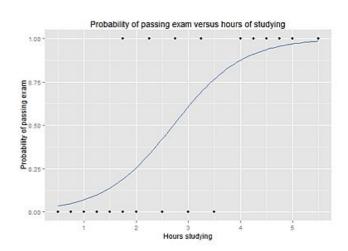
Linear regression vs. Logistic regression



#### Logistic regression

Gives output between 0 and 1. In bi-class, it can be assumed as the probability of belonging to class 1.

$$Pr(1|a^{(i)}) = \frac{1}{1 + e^{-(w_0 + w_1 \cdot a_1 + \dots + w_k \cdot a_k)}}$$



The cost function is different and based on logarithms, which gives high cost for confident wrong predictions:

$$J(w, w_0) = -\sum_{i=0}^{n} (1 - x^{(i)}) \left[ \log(1 - Pr[1|a_1^{(i)}, a_2^{(i)}, \dots, a_k^{(i)}]) + x^{(i)} \left[ \log(Pr[1|a_1^{(i)}, a_2^{(i)}, \dots, a_k^{(i)}]) \right] \right] + x^{(i)} \left[ \log(Pr[1|a_1^{(i)}, a_2^{(i)}, \dots, a_k^{(i)}]) \right] + x^{(i)} \left[ \log(Pr[1|a_1^{(i)},$$



## Logistic regression

For multiclass (K classes), there are several methods

Take a "pivot" class (say class K)

Do a regression for each other class (K-1 classes) against the pivot class (class K)

Adjust probabilities to sum up 1

Choose the class with major probability



#### Neural Networks

A neural network can be seen as a complex linear classifier able to learn **non-linear**, multiclass datasets

It also uses gradient descent for training

Basic architecture

Neurons disposed in layers

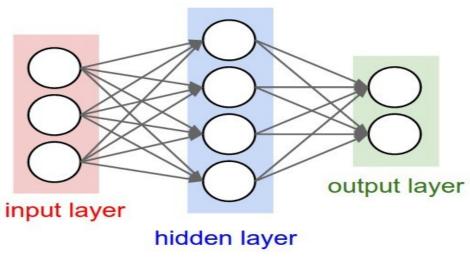
The input layer receives a sample

For example: each gene expression value

The hidden layer(s) combine(s) the output from previous layers

The output layer gives predictions

For example: one output neuron gives the score for each possible class (patient possible conditions)





#### **Neural Networks**

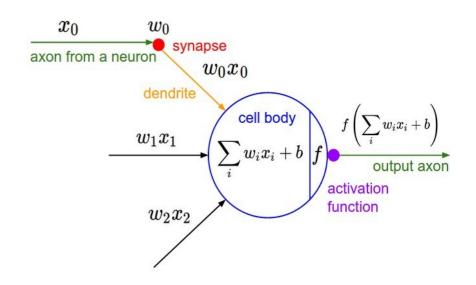
Each neuron is composed with a set of weights w, a bias b and an activation function f (a.ka. Non-linearity)

Neuron output (known as "activation"):

$$a(x) = f\left(\sum_{i} w_{i} x_{i} + b\right)$$

Possible activation functions *f*:

Sigmoid
$$\sigma(x) = \frac{1}{(1+e^{-x})}$$
Tanh
$$\tanh(x) = 2\sigma(2x) - 1$$
ReLU (Rectified Linear Unit)
$$f(x) = \max(0, x)$$





#### **Neural Networks**

#### Training. Backpropagation algorithm

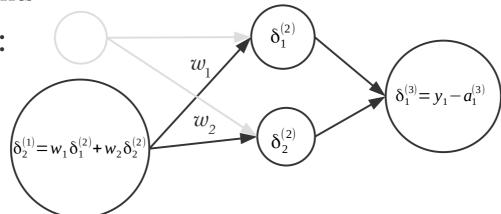
It is a method to compute the partial derivative  $(\delta)$  at each neuron in order to update its weights with gradient descent (as in previous methods)

is calculated from the last layer down to the first

In the last layer, the gradient depends only on the expected output

In intermediate layers, the gradient depends on the gradient of the next connected neurons, weighted by the connection's weights

Intuition:





#### Neural Networks

Training. Backpropagation algorithm

Once  $\delta_n$  is calculated for each neuron n, and given that (which is proven):

$$\frac{\partial J}{\partial w_{ij}^{(L)}} = \delta_n^{(L)} a_n$$

We can apply gradient descent to update weights a learning rate

$$w_{ij} := w_{ij} - \alpha \delta_n^{(L)} a_n$$



#### Support Vector Machines (SVM)

Binary classifier (easily extensible to multiclass)

Samples are represented in n-dimensional space (n = no. features)
Learn:

$$y = f(x), y \in \{\pm 1\}, x \in \mathbb{R}^n$$

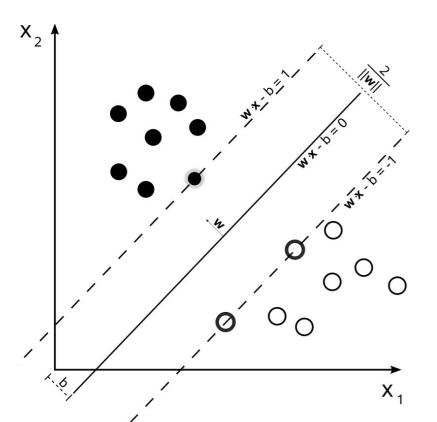
The objective is to find an hyperplane (n-1 dimension) which separates positive from negative instances.

Mathematically

Large margin

Find 
$$(w, b)$$
, minimising:  $||w||$  subject to:  $y_i(w \cdot x_i - b) \ge 1$ 

The hyperplane separates each class instances





Support Vector Machines (SVM)

Once w y b are found, classification is given by:

$$f(x) = w \cdot x + b$$

Giving the value +1 if f(x) > 0, or -1 otherwise



## Support Vector Machines (SVM)

If not all samples can be separated.

Soft-margin SVM. Allows an error that should be minimized. C parameter indicates the cost of an error during training.

Now the objective is:

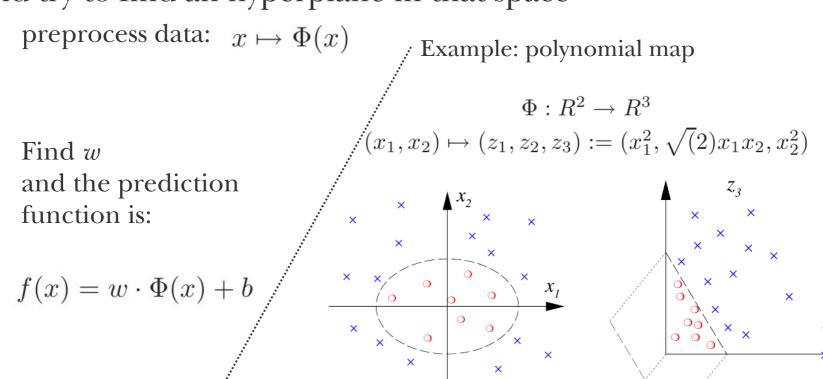
Find 
$$(w,b)$$
, minimizing:  $||w|| + C \cdot \sum_{i=1}^{m} \xi_i$  subject to:  $y_i(w \cdot x_i - b) \ge 1 - \xi_i, \xi_i \ge 0$ 



## Support Vector Machines (SVM)

#### Non linear case

Alternative: Map input data to a higher dimensional space and try to find an hyperplane in that space





Support Vector Machines (SVM)

Problem: The map function could lead to a very high dimensionality, making it difficult to keep w in memory and solve the optimization problem.

Solution: dual form + kernel trick



#### Support Vector Machines (SVM)

Dual form. The optimization problem can be presented in its dual form, with Lagrangian multipliers

We try to find:

Find 
$$\alpha_i$$
, minimising: 
$$\sum_{i=1}^{m} \alpha_i - \frac{1}{2} \sum_{i=1}^{m} \sum_{j=1}^{m} \alpha_i \alpha_j y_i y_j x_i x_j$$
subject to:

$$\sum_{i=1}^{m} y_i \alpha_i = 0$$

$$0 \le \alpha_i \le C, i = 1, ..., m$$

The classification function is now:

$$f(x) = \sum_{i}^{n} \alpha_{i} y_{i} x_{i} \cdot x + b$$

Moreover, there is a relation between w y  $\alpha$  $w = \sum_{i=1}^{n} \alpha_i y_i x_i$ 



#### Support Vector Machines (SVM)

#### Dual form

Advantage: Both in the function to solve and the decision function data appear as dot products

$$\sum_{i=1}^{m} \alpha_i - \frac{1}{2} \sum_{i=1}^{m} \sum_{j=1}^{m} \alpha_i \alpha_j y_i y (x_i \cdot x_j)$$

$$f(x) = \sum_{i} \alpha_{i} y_{i} x_{i} \cdot x + b$$

For the non linear problem, we include a map  $\Phi$ :

$$\sum_{i=1}^{m} \alpha_{i} - \frac{1}{2} \sum_{i=1}^{m} \sum_{j=1}^{m} \alpha_{i} \alpha_{j} y_{i} y_{j} \Phi(x_{i}) \cdot \Phi(x_{j})$$

$$f(x) = \sum_{i} \alpha_{i} y_{i} \Phi(x_{i}) \cdot \Phi(x) + b$$



#### Support Vector Machines (SVM)

#### Kernel trick

Lets consider the function K (kernel):

$$K(x_i, x) = \Phi(x_i) \cdot \Phi(x)$$

If K is the dot product, we maintain the problem in the same input space, but by varying K we could get something like:

Map + dot product (but without making an explicit mapping!)

#### Example:

Polynomial kernel:

$$K(x, x') = (x \cdot x')^2$$

Which is equivalent to the previous mapping:

$$\Phi: \mathbb{R}^2 \to \mathbb{R}^3 \quad (x_1, x_2) \to (z_1, z_2, z_3) := (x_1^2, \sqrt{2} x_1 x_2, x_2^2)$$



### Support Vector Machines (SVM)

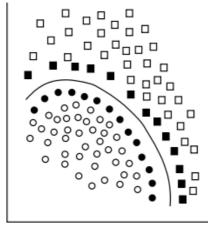
#### Kernel trick:

Other kernels.

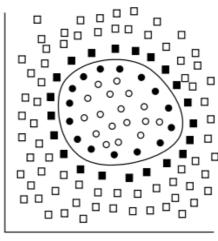
Polynomial 
$$K(x, x') = (x \cdot x' + c)^q$$

RBF (adds a small "hill" on each point)

$$K(x, x') = e^{-\gamma ||x_i - x||^2}$$



polinomial



**RBF** 





#### Employ several classifiers in order to improve performance

Ensemble vs. other classifier combination approaches:

Ensembles employ many classifiers (of one or several types). Moreover, its number usually varies depending on the training data

The combination of a reduced number of classifiers is not considered an ensemble (less than 10), specially when they are intended to integrate data from heterogeneous sources

#### Motivation:

#### Improve the statistical performance

Probably, the performance of the classifier combination is lower than a specific classifier, but the risk of choosing a bad classifier is reduced

#### Computational aspects

Usually it is unfeasible to try all classifiers to see which is the best one. By combining several types, the risk is reduced

#### Representation capabilities: divide and conquer

Making each classifier to focus on a subpart of the input data space, results can be improved

#### Advantages regarding data volume

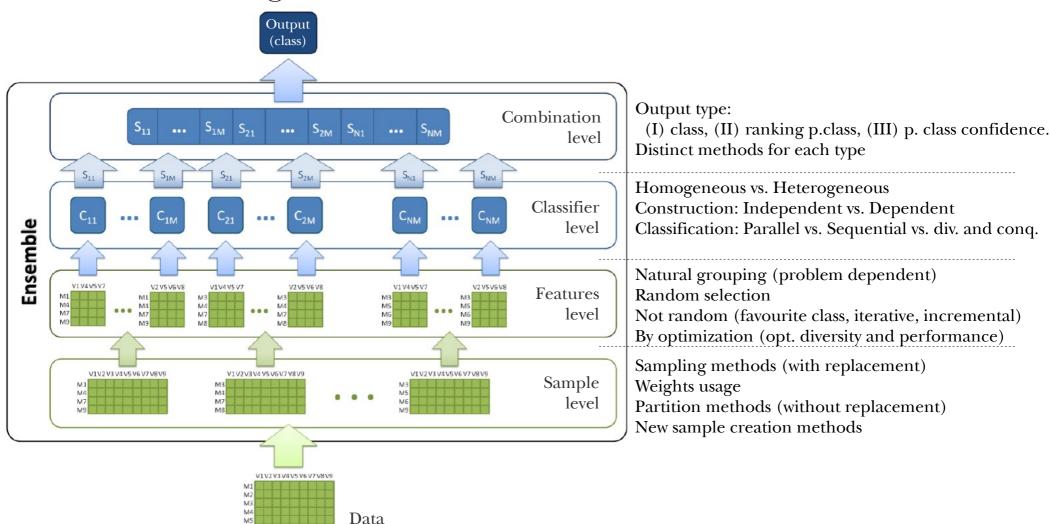
Very high data volume. Scalability, due to the possibility of train several classifiers per data subspace concurrently

Very low data volume. Resampling data and train a classifier on each sample



## Classifier ensembles

#### Ensembles general framework





## Classifier ensembles

#### Diversity

Central and desired feature in classifier ensembles

If we find a set of classifiers diverse enough, that do not make the same errors, then we can improve the performance of the base classifiers

#### How to achieve diversity:

Modify classifier parameters.

Modify input training data (sampling, partition, creation).

Divide search space (divide and conquer).

Mix several types of classifiers.





## **Diversity**

#### Measuring diversity

Pairwise diversity

Taking this matrix:

	C <sub>j</sub> hit (1)	C <sub>j</sub> fail (0)
C <sub>i</sub> hit (1)	$N^{11}$	$N^{10}$
C <sub>i</sub> fail (0)	$N^{01}$	$N^{00}$

$$Q_{i,j} = \frac{N^{11}N^{00} - N^{01}N^{10}}{N^{11}N^{00} + N^{01}N^{10}}$$

Q statistic [-1, 1]. 0 = independent

$$Q_{i,j} = \frac{N^{11}N^{00} - N^{01}N^{10}}{N^{11}N^{00} + N^{01}N^{10}} \qquad \qquad \rho_{i,j} = \frac{N^{11}N^{00} - N^{01}N^{10}}{\sqrt{(N^{11} + N^{10})(N^{01} + N^{00})(N^{11} + N^{01})(N^{10} + N^{00})}} \qquad \qquad Des_{i,j} = \frac{N^{01} + N^{10}}{N} \qquad \qquad DF_{i,j} = \frac{N^{00}}{N} = \frac{N$$

p correlation coefficient Similar to Q

$$Des_{i,j} = \frac{N^{01} + N^{10}}{N}$$

Disagreement score

Doble fault

#### Non-pairwise diversity

Entropy

$$E = \frac{1}{N} \sum_{i=1}^{N} \frac{1}{(L - \lceil L/2 \rceil)} \min\{l(\mathbf{z}_j), L - l(\mathbf{z}_j)\}.$$

Kohavi-Wolpert Variance (T=number of classifiers)

$$KW = \frac{1}{NL^2} \sum_{j=1}^{N} l(\mathbf{z}_j) (L - l(\mathbf{z}_j))$$

 $(l(\mathbf{z}_i))$  number of classifiers correctly guessing j sample). L=number of classifiers)



## Classifier ensembles

### Some examples

#### Bagging (Bootstrap AGGregatING)

Several classifiers over subsamples by using resampling with replacement Combining by majority vote

#### Random Forest

Bagging variation

Builds multiple decision trees by varying:

Parameters randomly

Taking a subset of samples and/or attributes randomly

#### AdaBoost

Sequential training of several classifiers of the same type and parameters

On each iteration failing samples of the previous iteration have more weight

Combination by performance-weighted voting



## Classifier ensembles

### Some examples

#### Non-ensemble approaches

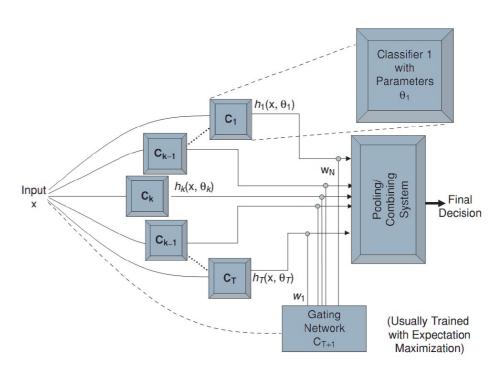
#### **Stacking**

A classifier learns how to generate a classification taking as input the output of base classifiers

#### Classifier 1 with **Parameters** $h_1(\mathbf{x}, \theta_1)$ $C_{k-1}$ Parameters $\theta_{T+}$ Classifier T+1 $h_k(\mathbf{x}, \theta_k)$ Input Final Decision $h_T(x, \theta_T)$ First Level Second Level Base Classifiers Meta Classifier

#### Mixture of experts

A neural network learns which classifiers should vote given input data







### Convolutional Neural Networks (CNN)

Deep Learning: subfield of Machine Learning able to learn from datasets without doing feature engineering

For example, in order to detect objects in an image, a preprocessing step trying to find basic shapes (features) focusing on the specific task was explicitly programmed. Deep Learning techniques try to avoid this step, working with raw data directly.

Convolutional Neural Network (CNN): A special type of *deep* neural network intended for image processing.



CNN vs classic Neural Networks. Key differences:

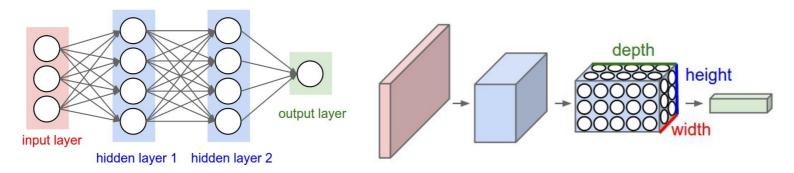
In CNN, layers are *volumes* of neurons having width, height and depth.

Neurons are not *fully connected* to the previous layer, because it will not scale well for images (huge number of connections).

They only process a square portion of the input.

Weights are *shared*. Neurons at the same depth in the same volume *share* they weights.

It is reasonable for image processing as well as it reduces dramatically the number of parameters.





### Convolutional Neural Networks (CNN)

### Types of layers in a CNN:

### Convolutional Layer.

The most important layer. Neurons are connected to portions of the input volume.

#### RELU layer.

Applies an element-wise activation, such as max(0, x). The input volume's dimensions are not changed

#### POOL layer.

Reduces the spatial dimensions (width and height).

#### Fully connected layer.

Typical final layer, which is fully connected to the input and has a neuron per desired output (for example, 10 neurons for a 10-class classification problem)



### Convolutional Neural Networks (CNN)

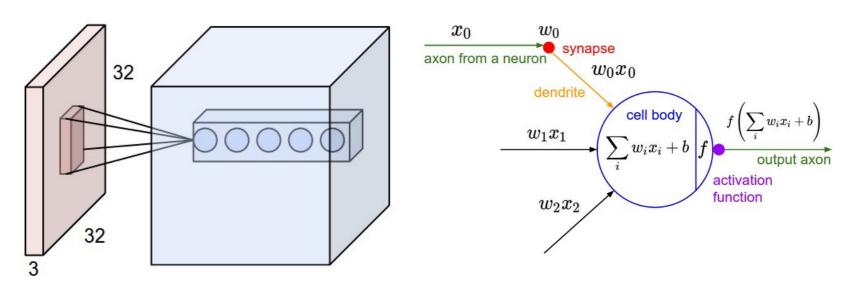
#### Convolutional Layer

Each neuron receives a small portion of the input's width and height (but all the input's depth)

Neurons in at the same depth in the conv. layer share they weights.

Each set of neurons at the same depth is called a filter

They process the input image applying the same operation in a sliding window (convolution), so they are like applying a filter to the image

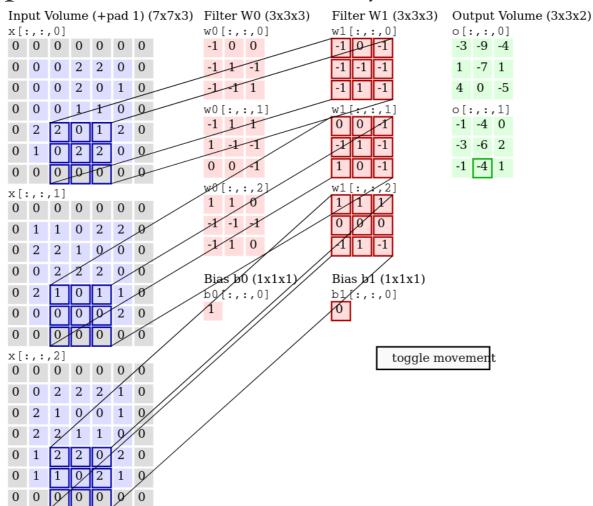






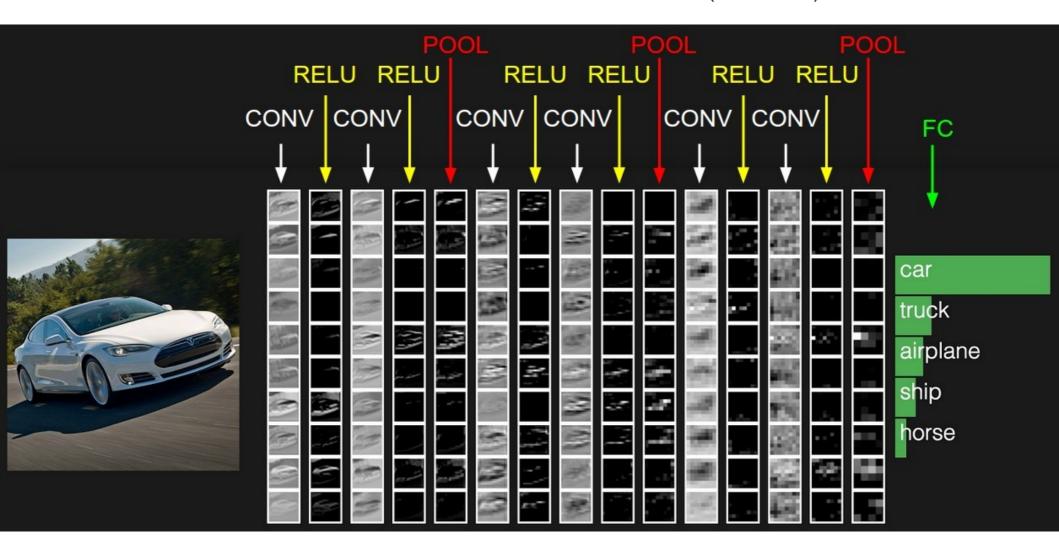
### Convolutional Neural Networks (CNN)

### Example of convolutional layer values





Convolutional Neural Networks (CNN)





#### Convolutional Neural Networks (CNN)

CNN Example: YOLO (object detection)

YOLO is a CNN specially intended to detect, localize and classify objects in an image.

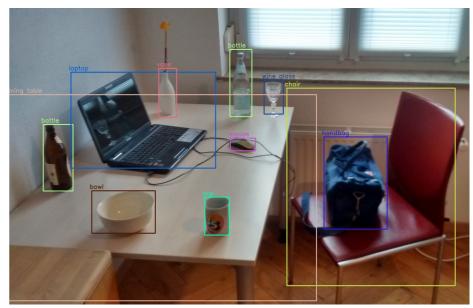
It "only looks once (YOLO)" to the image (one forward pass) and gives an output of all objects, their locations and their classes.

It can work in "real-time"

It divides the space in SxS cells where K objects can be detected, localized and classified.

YOLO v2. Can detect the class for each object, not for each cell.

YOLO v3. Better performance in objects with different scale.



Source: Wikimedia Commons. Author: MTheiler



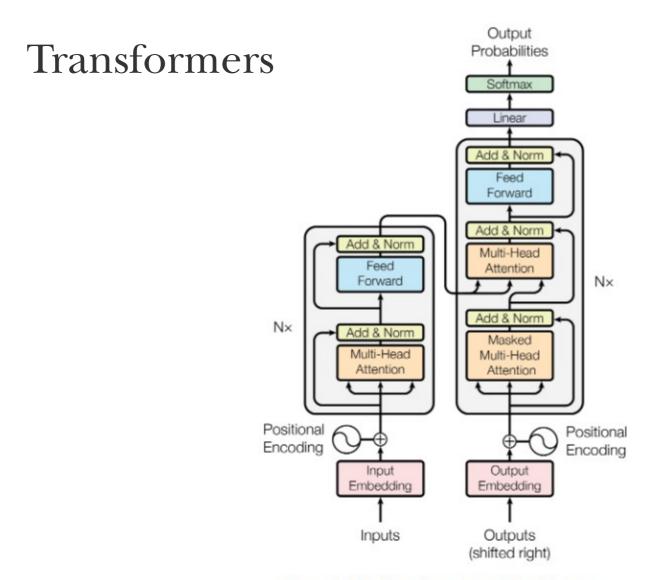
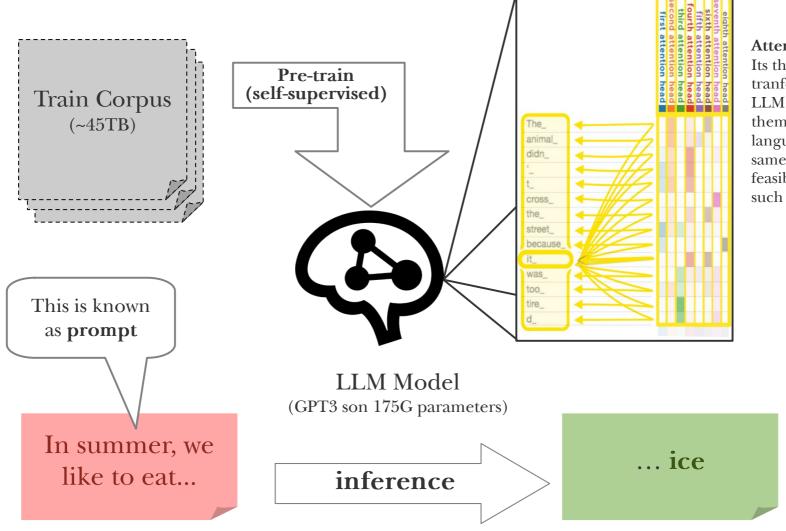


Figure 1: The Transformer - model architecture.

Vaswani, A., Shazeer, N., Parmar, N., Uszkoreit, J., Jones, L., Gomez, A.N., Kaiser, Ł. and Polosukhin, I., 2017. Attention is all you need. Advances in neural information processing systems, 30.



Large Language Models (LLMs)



#### **Attention Mechanism**

Its the core of tranformers and thus of LLM models, enabling them to model natural language and, at the same time, making feasible to train them at such large scale

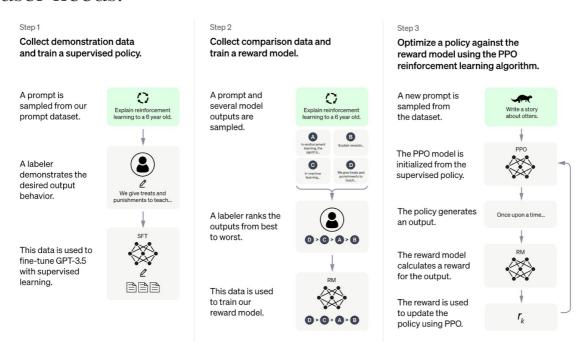


#### From LLMs to assistant Chat Bots

Generating text from an input with a pre-trained LLM over massive text, does not follow user instructions:

Prompt: "I want a small introduction to the Machine Learning topic..." LLM: "You have two weeks to do the job".

Solution: Continue transining the LLM with feedback that scores answers (from the most appropriate to the less one), aiming at align the responses to the user needs.



Source: OpenAI

### References



Witten I.H. & Frank E (2005) Data Mining: Practical Machine Learning Tools And Techniques. Morgan Kaufmann. 2<sup>nd</sup> Edition.

Kuncheva, L.I. (2004). Combinining Pattern Classifiers: Methods and Algorithms. Wiley-Intersciente. 1st Edition.

Convoluational Neural Networks for Visual Recognition http://cs231n.github.io

Wikipedia



### Machine Learning

Daniel Glez-Peña & Hugo López-Fernández

@SINGgroup 🐦

@lipido (Daniel) 🐦

www.sing-group.org