

Type introduction illustrated

for casual haskellers

to get over the Foldable

Takenobu T.

“What is this description ?!”

`foldr :: Foldable t => (a -> b -> b) -> b -> t a -> b`

NOTE

- This document shows one of the mental model.
- Please see also references.
- This is written for Haskell, especially ghc7.10/8.0 and later.

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1. Introduction

- Values, Types, Type classes
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3. What is this?

Appendix I - Various types

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- Maybe, List, Either, Tuple

Appendix II - Various type classes

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- Num
- Foldable
- Functor, Applicative, Monad
- Monoid
- Traversable

Appendix III - Advanced topics

References

1. Introduction

1. Introduction

Values, Types, Type classes

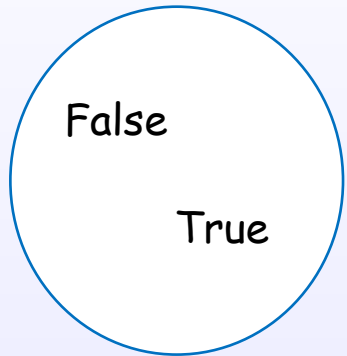
Values

False 1 2 1.0 'a' 'h'

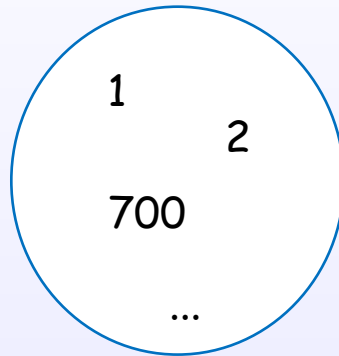
True 700 1.5 3.14 '5'

Types

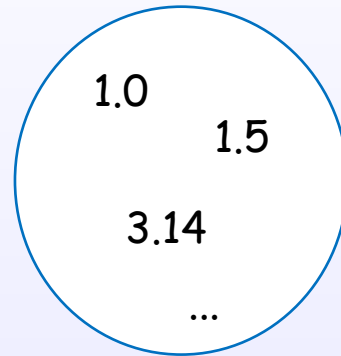
"Bool" type



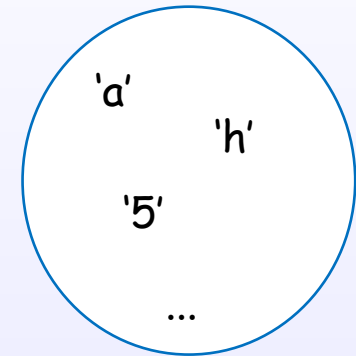
"Int" type



"Float" type

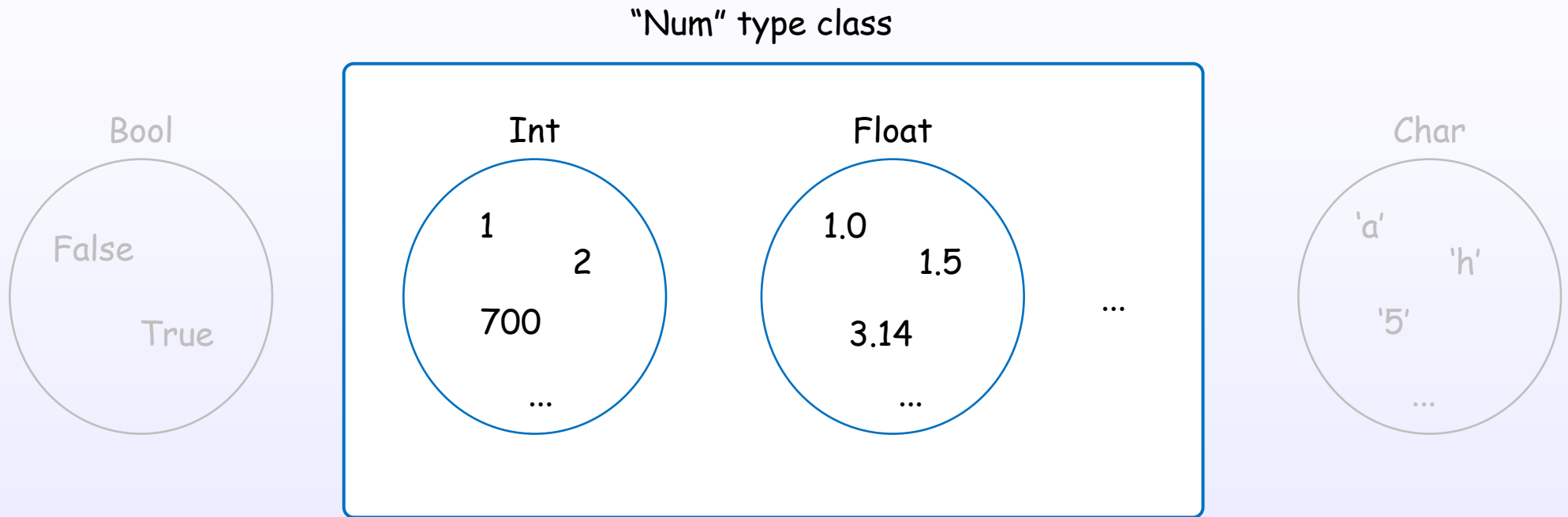


"Char" type



A type is a collection of values which have common property.

Type classes



A type class is a collection of types which have common operations.

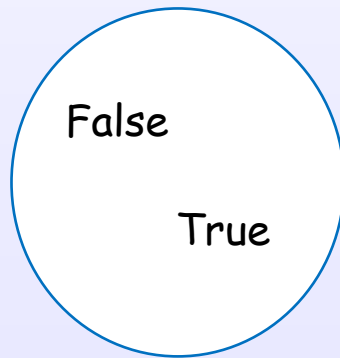
1. Introduction

Polymorphic types

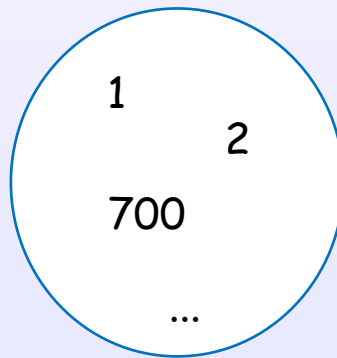
Proper types

Proper
types

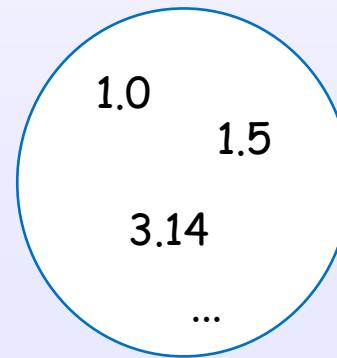
Bool



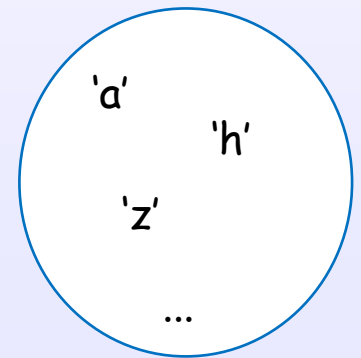
Int



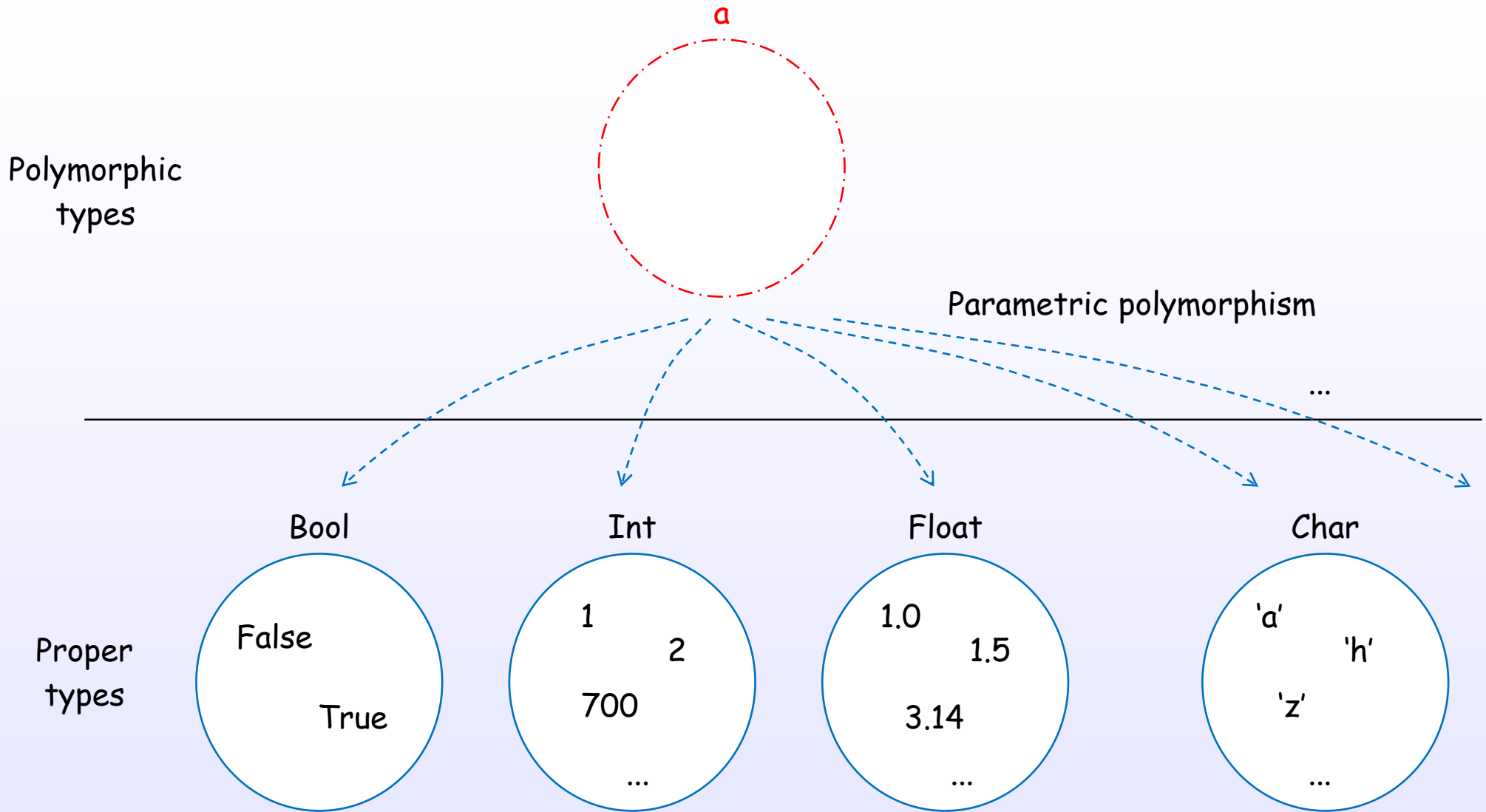
Float



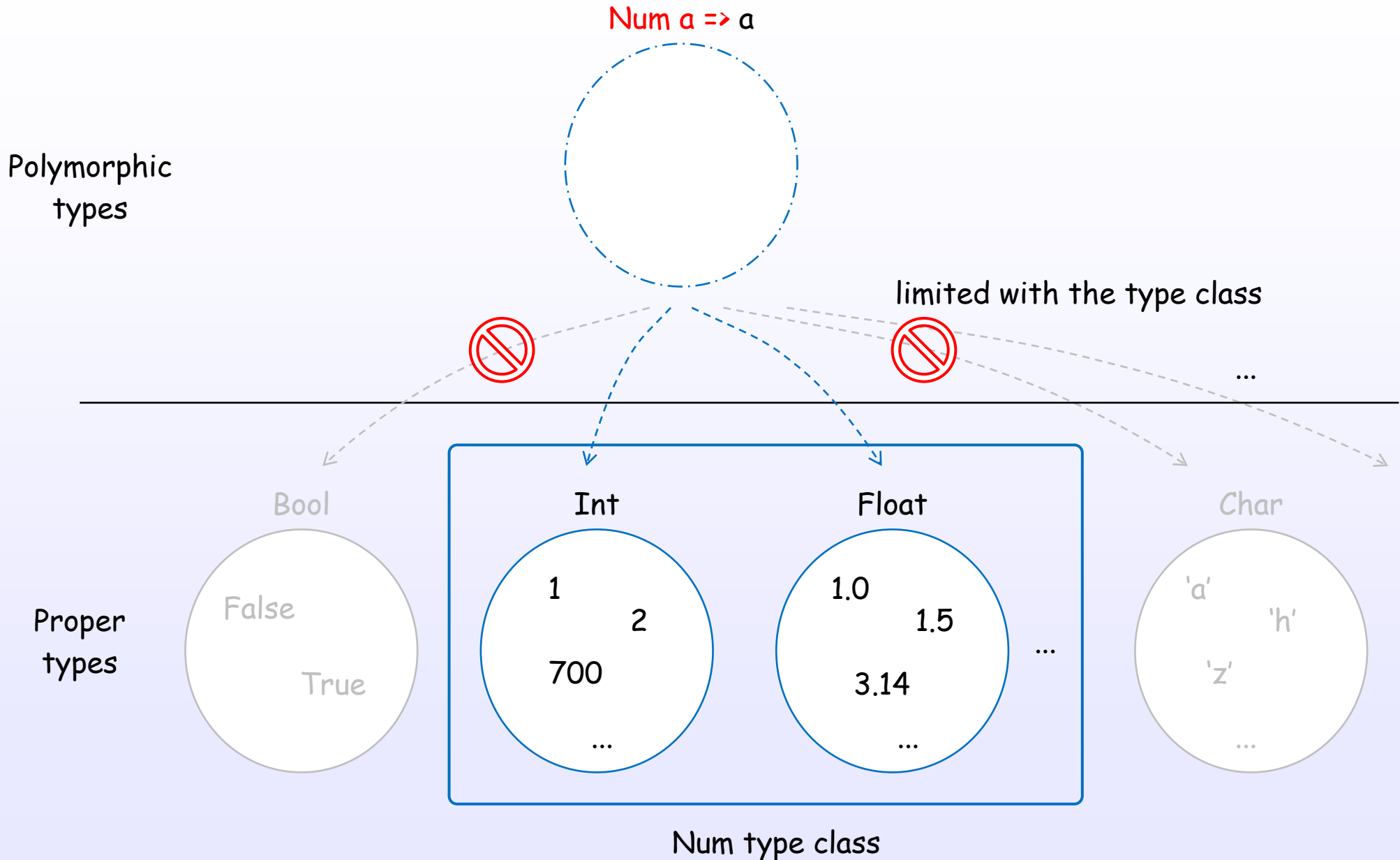
Char



Polymorphic types

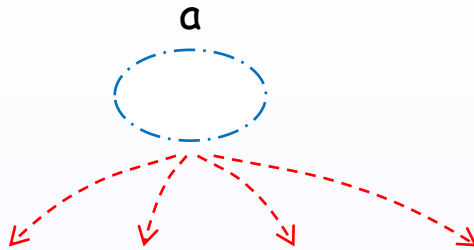


Polymorphic types restricted with type classes

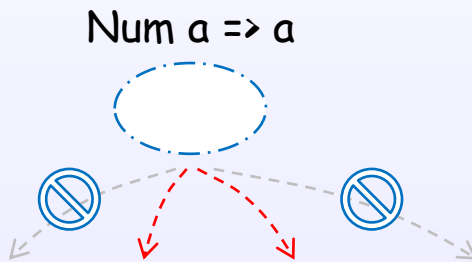


Polymorphic types

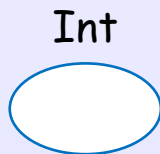
Polymorphic
types



polymorphic
types
with type class



Proper
types



1. Introduction

Type constructors

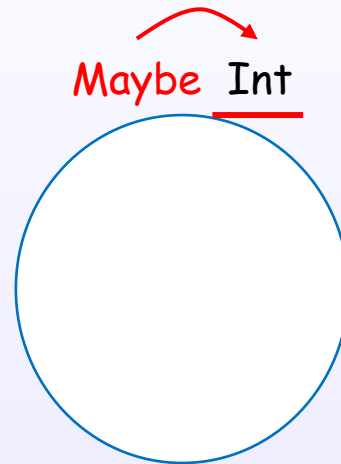
Type constructors

nullary type constructor



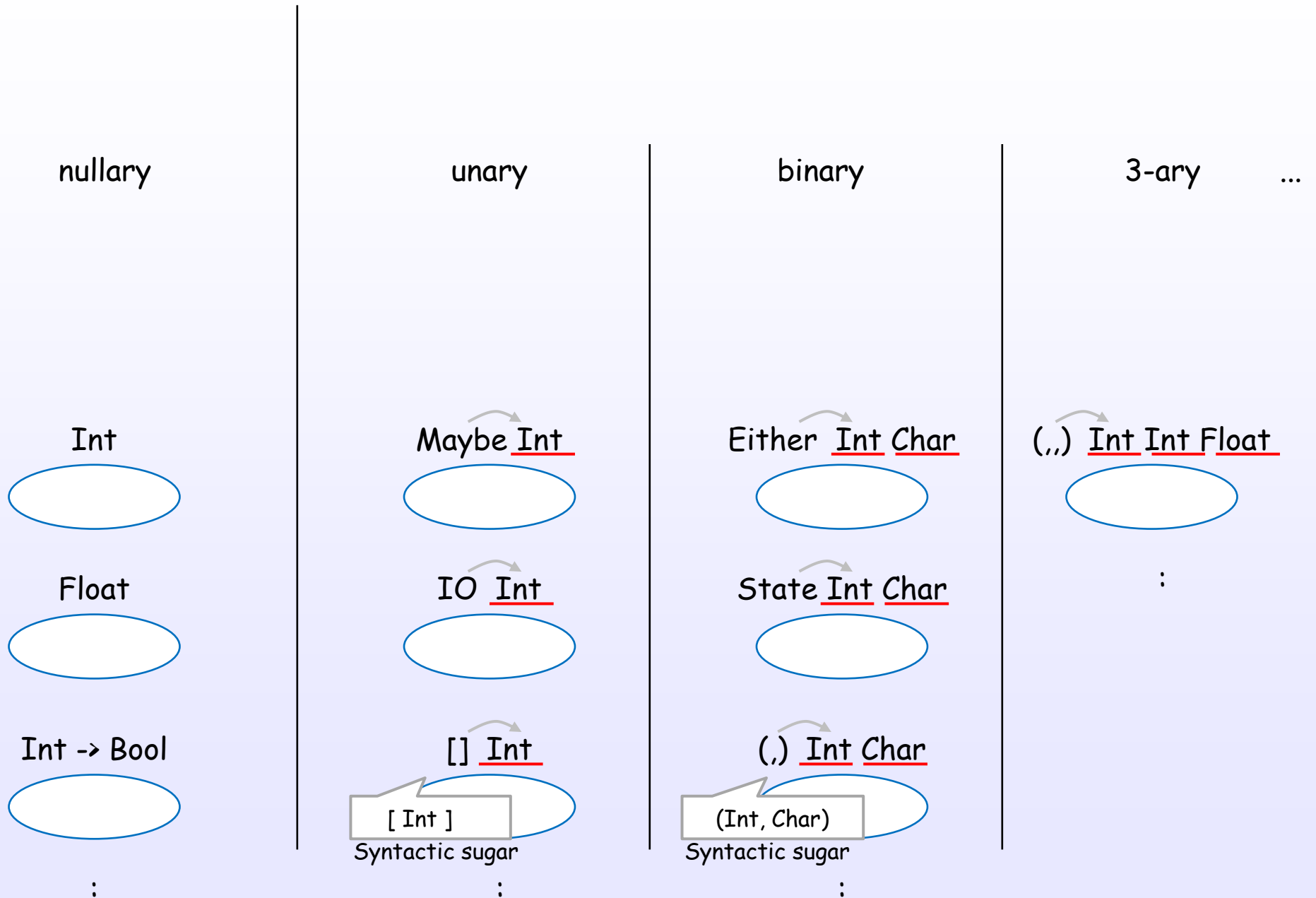
Type constructors

unary type constructor



"Maybe" type constructor takes one type argument (unary).

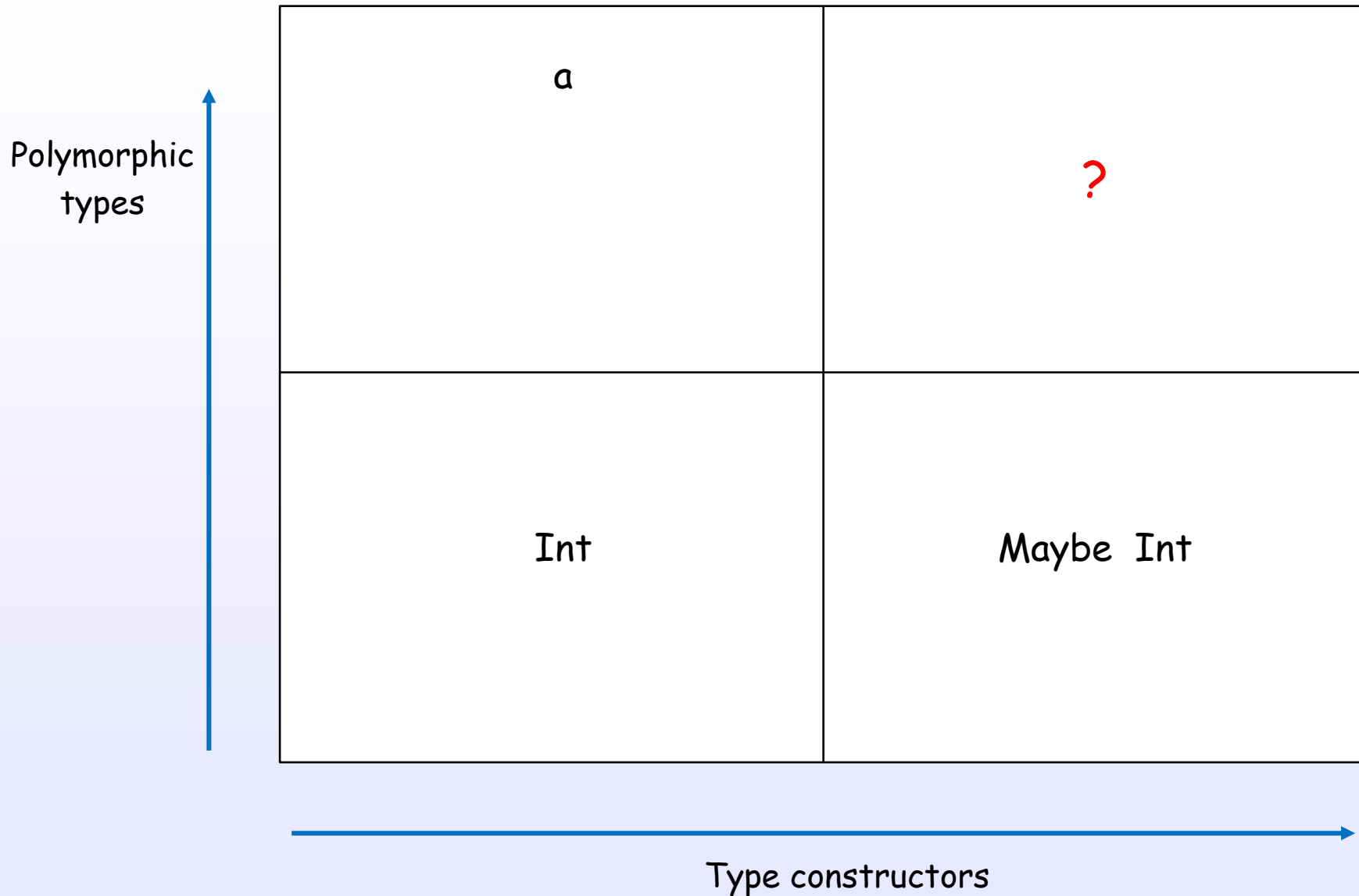
Type constructors



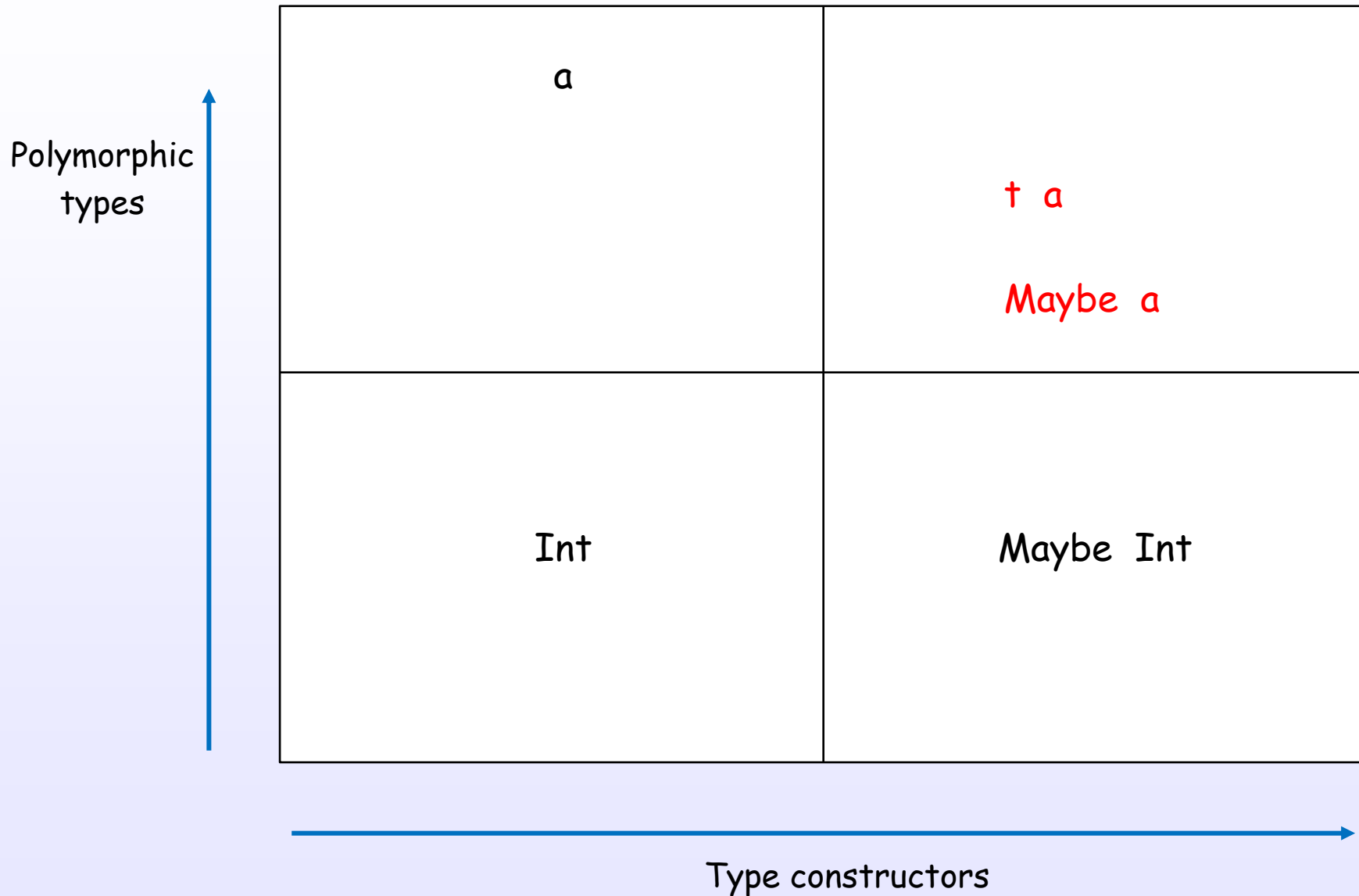
1. Introduction

Polymorphic types and type constructors

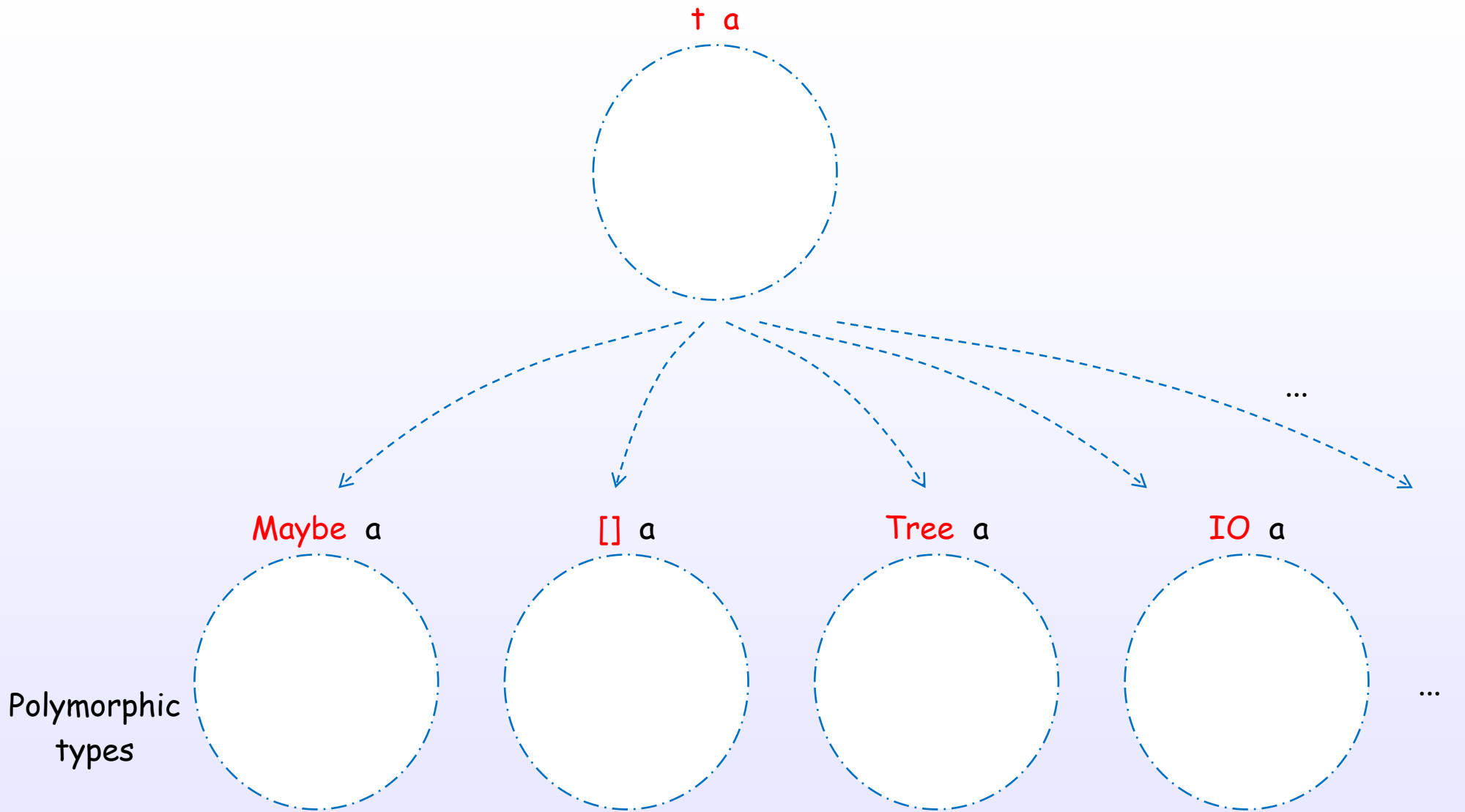
Polymorphic types and type constructors



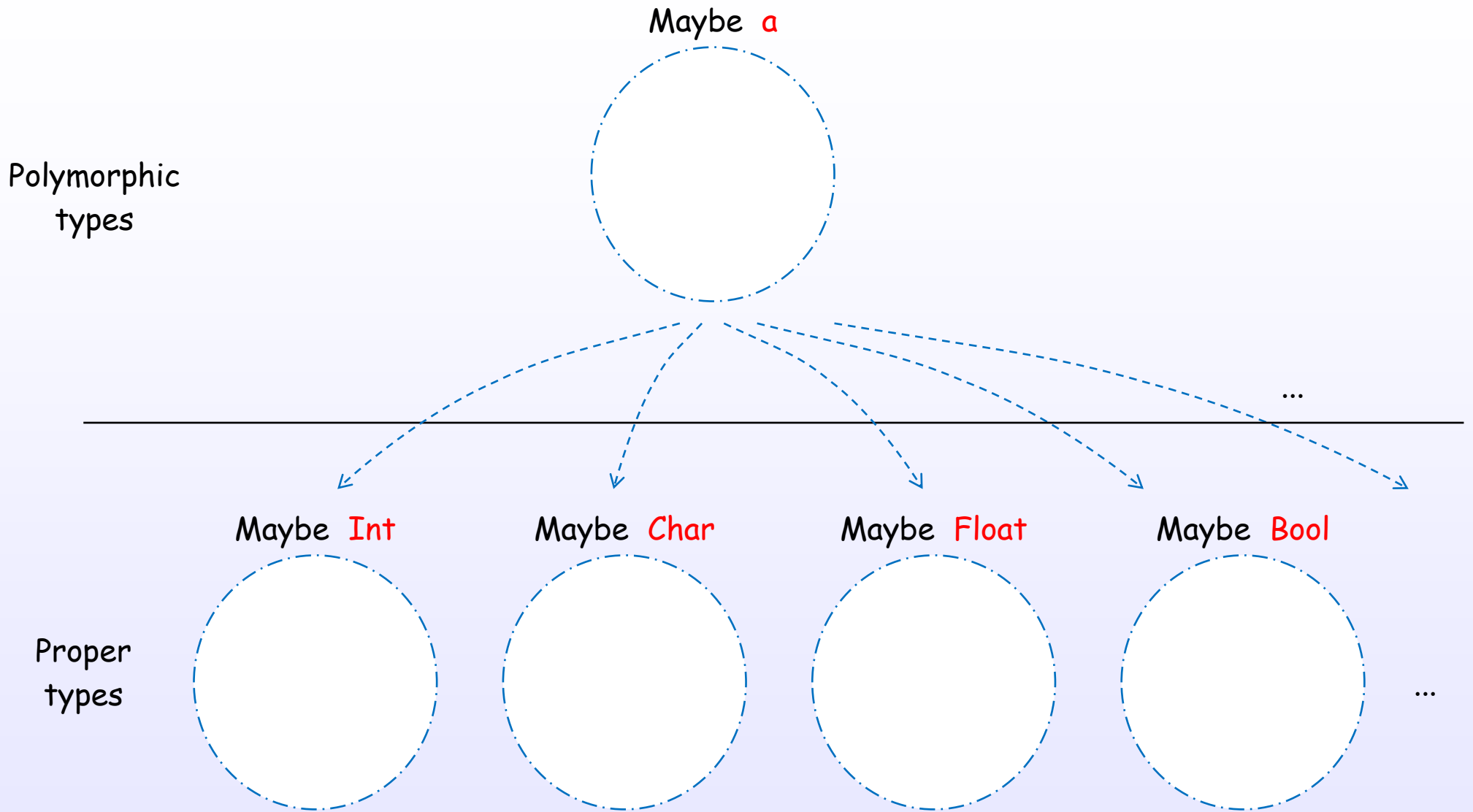
Polymorphic types and type constructors



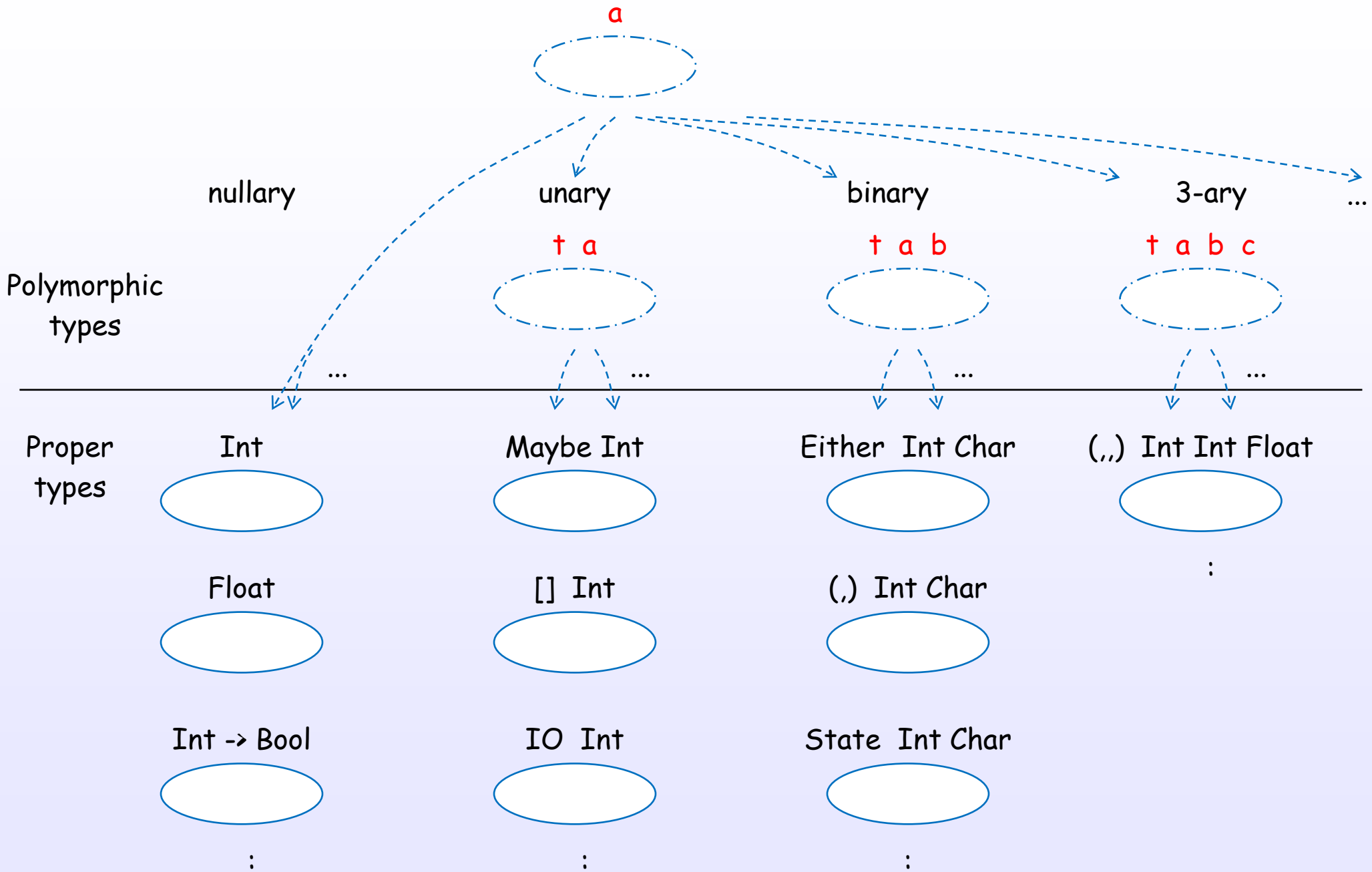
Polymorphic types and type constructors



Polymorphic types and type constructors



Polymorphic types and type constructors

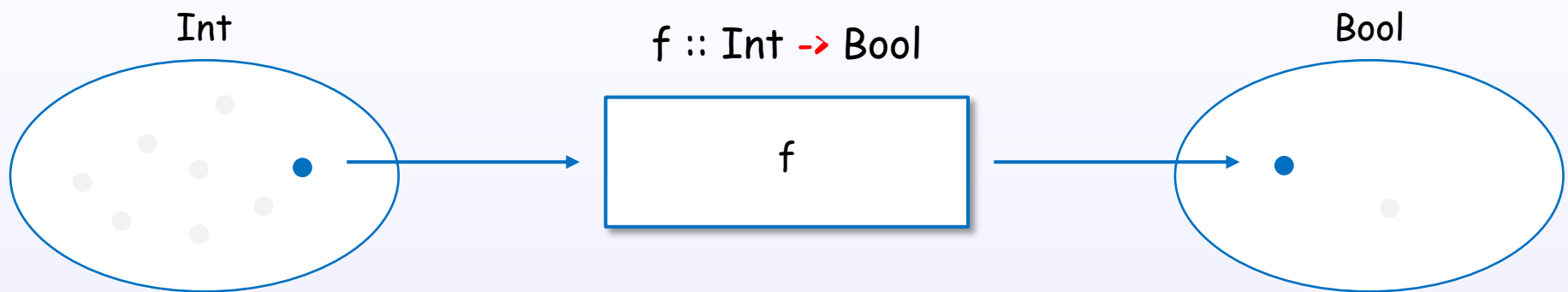


2. more, Types and Type classes

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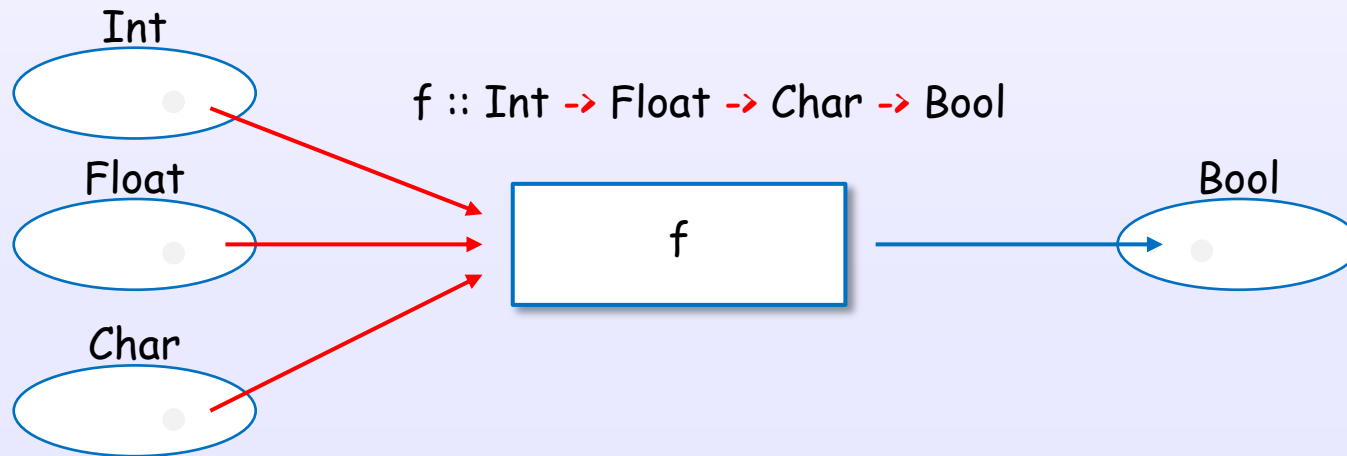
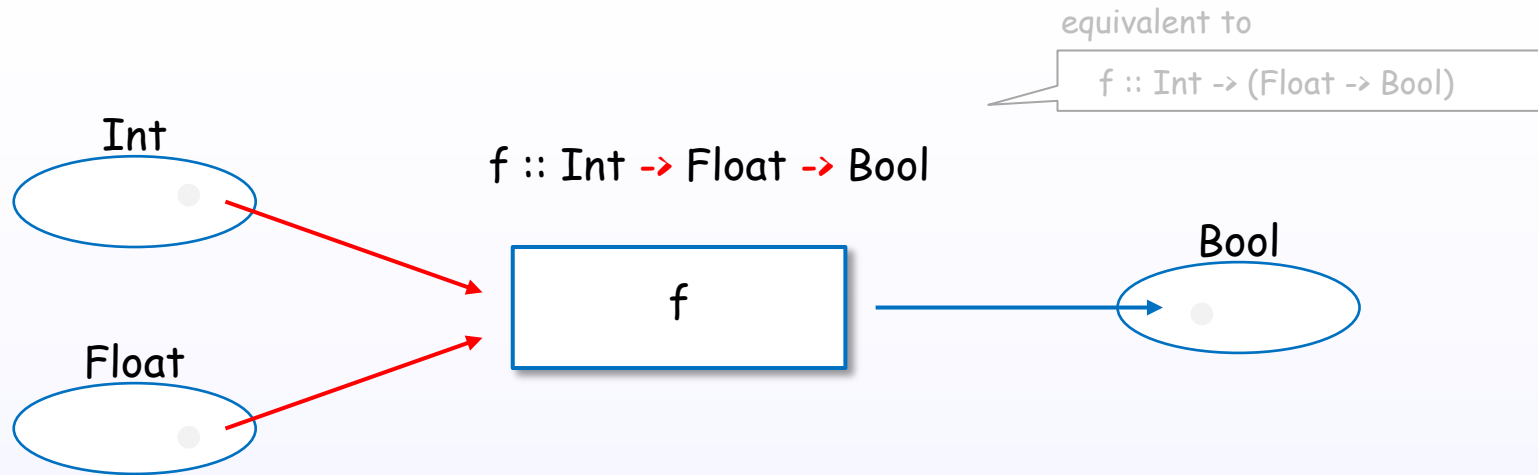
Function types

Function type

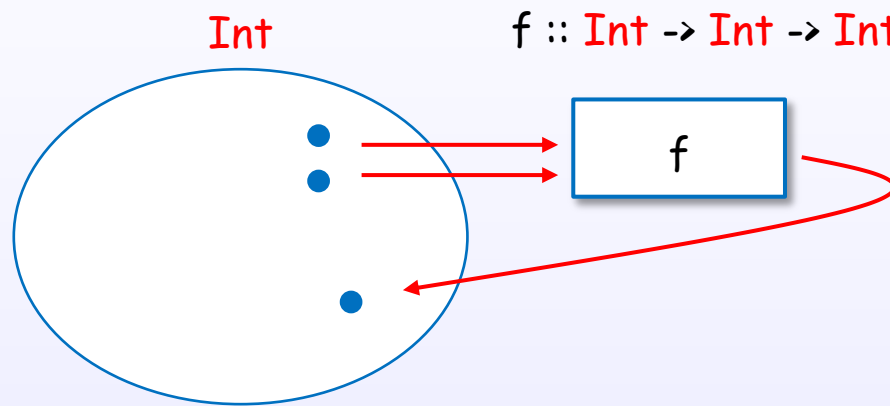


The " \rightarrow " represents the function type.

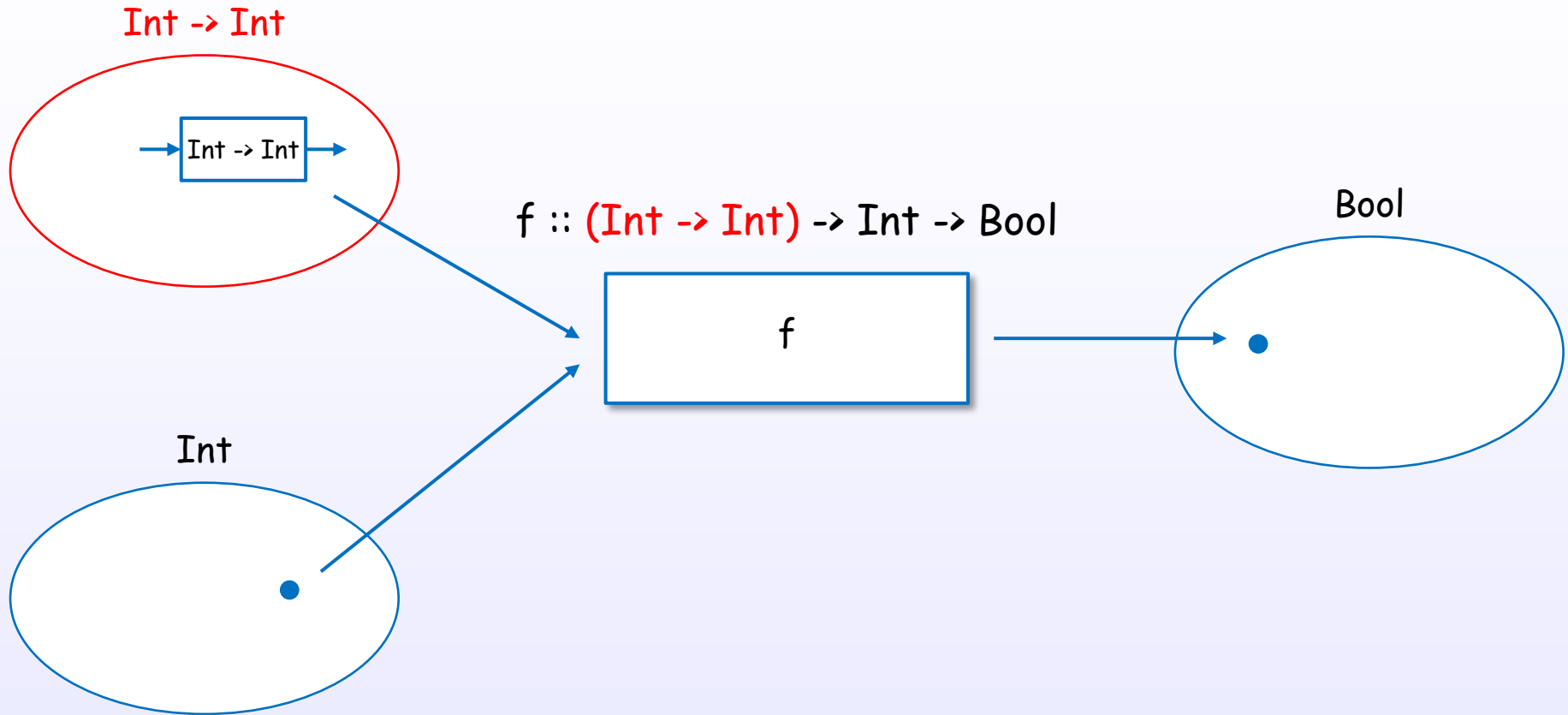
Function type with multiple arguments



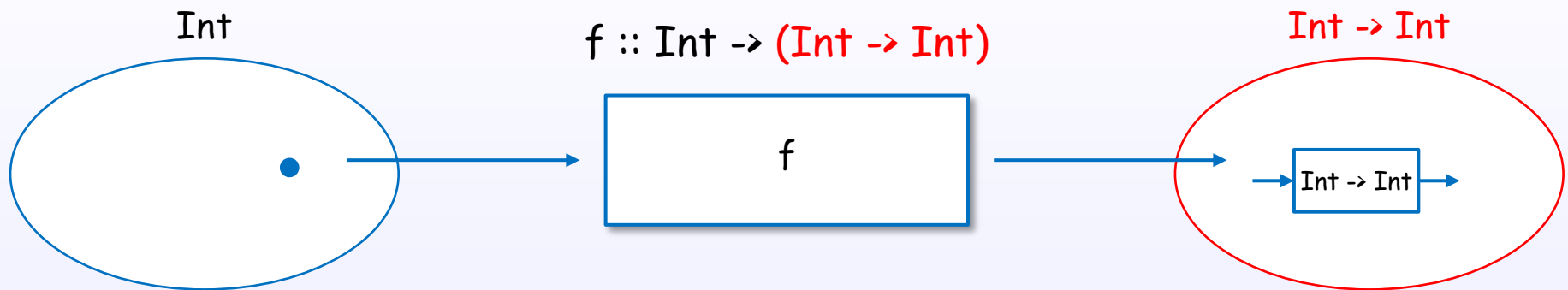
Function type with same type



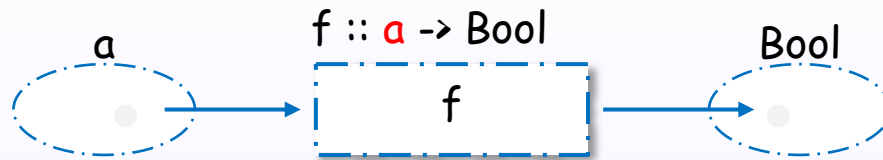
Function type with function as argument



Function type with function as result



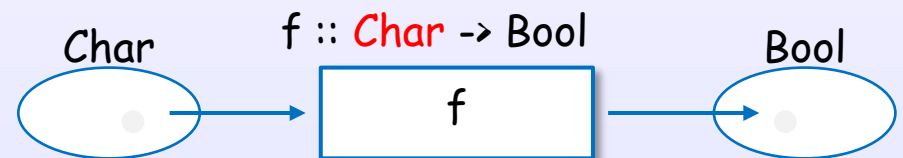
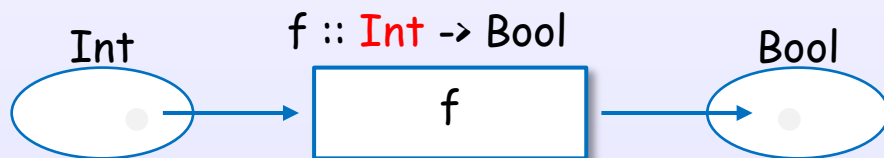
Function type with polymorphic function



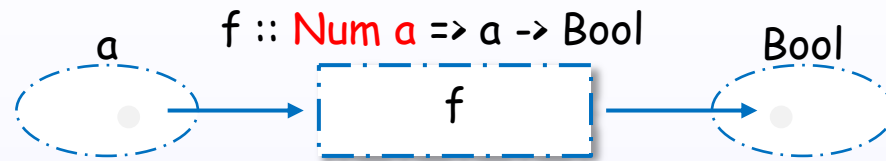
Polymorphic
types

Parametric polymorphism

Proper
types



Function type for polymorphic function with type class

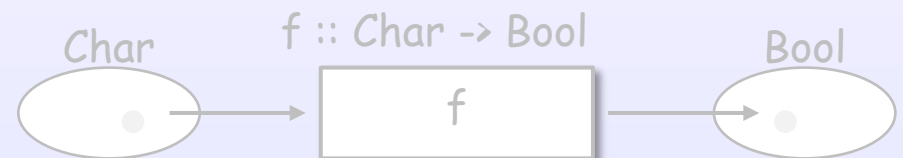
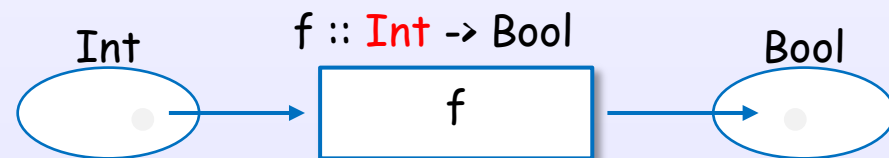


Polymorphic
types



limited with the type class

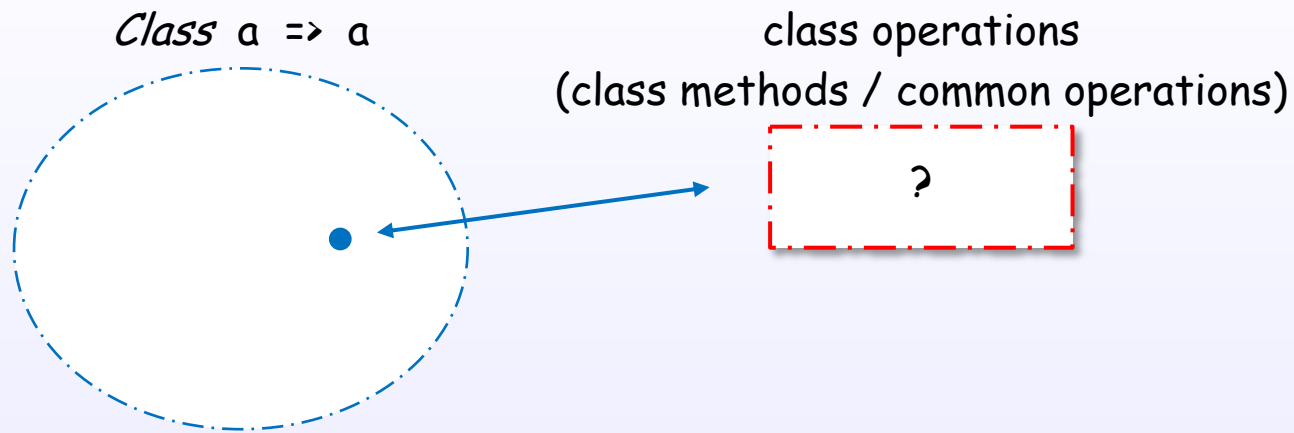
Proper
types



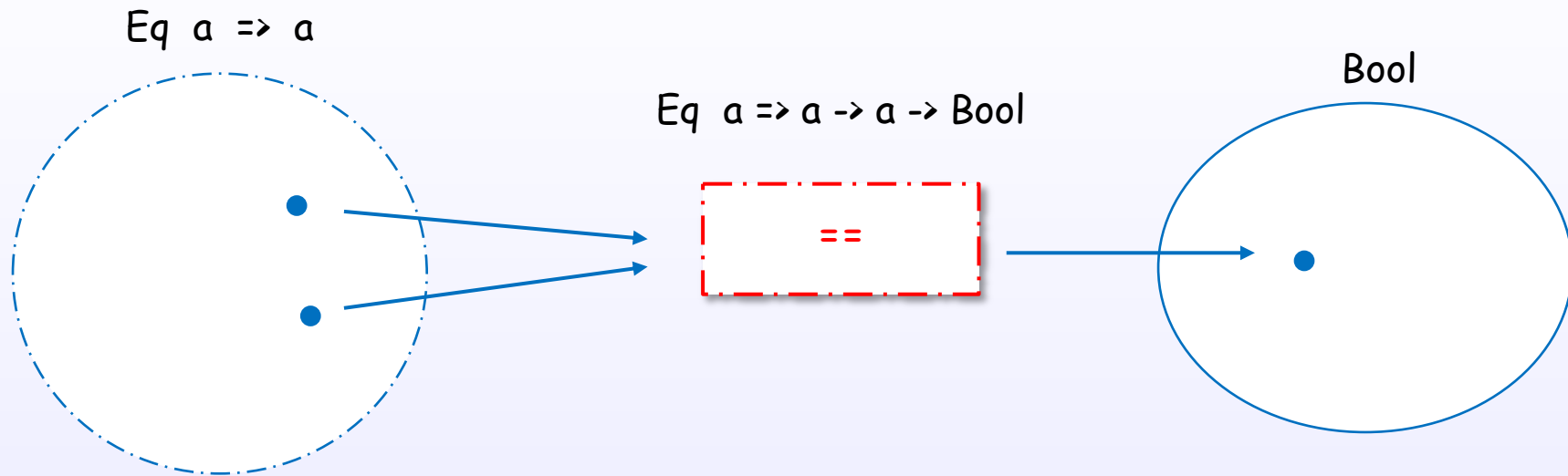
2. more, Types and Type classes

Type class operations

A type class has the class operations

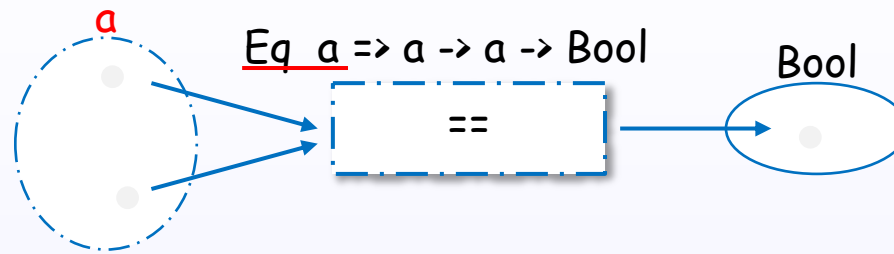


A type class has the class operations

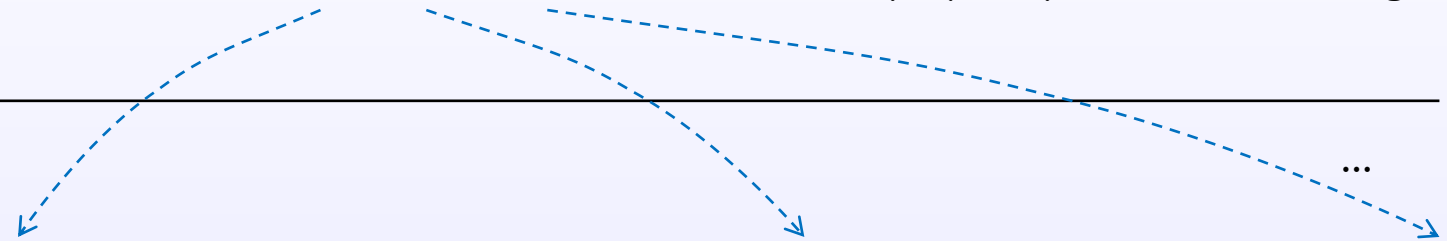


`Eq` class has `"=="` (equality) operation.

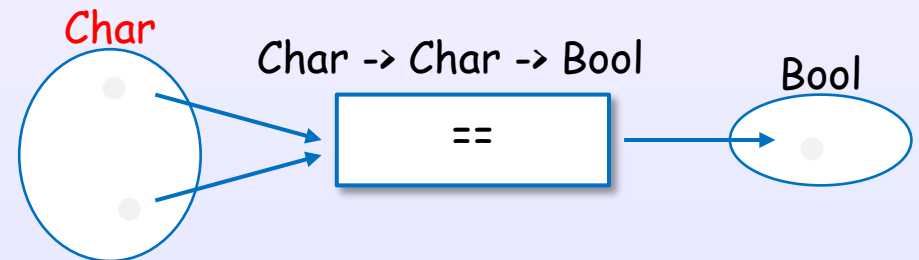
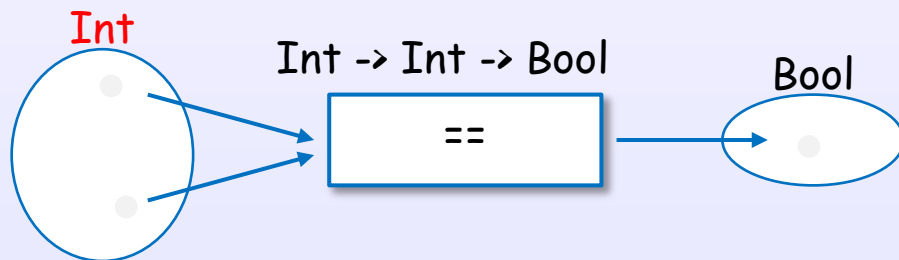
A type class has the class operations



Ad-hoc polymorphism (overloading)



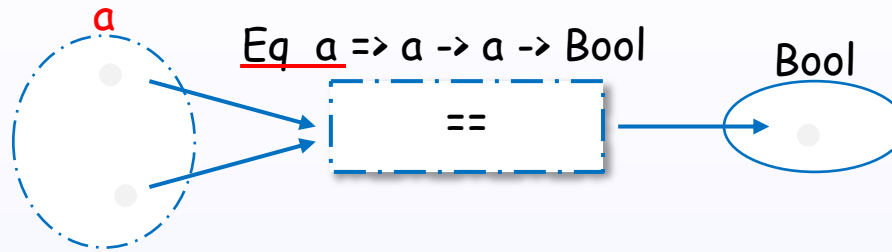
Proper types



Each type, that belongs to the type class, must be support the overloaded operations.

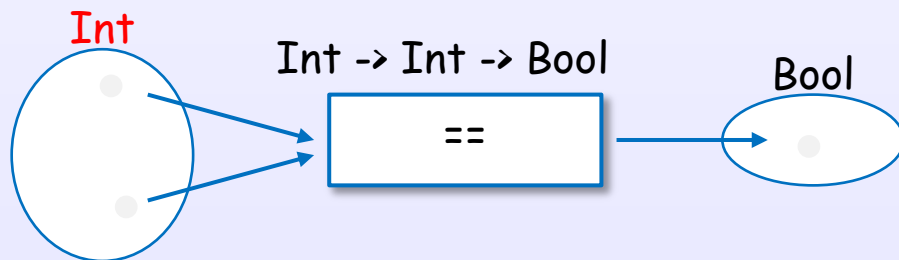
Declaration of a type class and instances

```
class Eq a where  
  (==) :: a -> a -> Bool
```

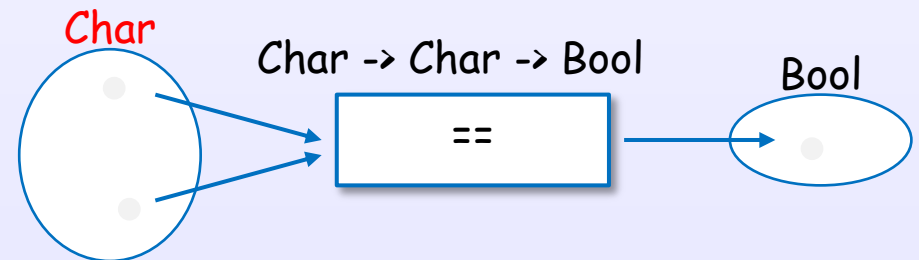


Polymorphic
types

Proper
types



```
instance Eq Int where  
  (==) = eqInt
```



```
instance Eq Char where  
  (==) = ...
```

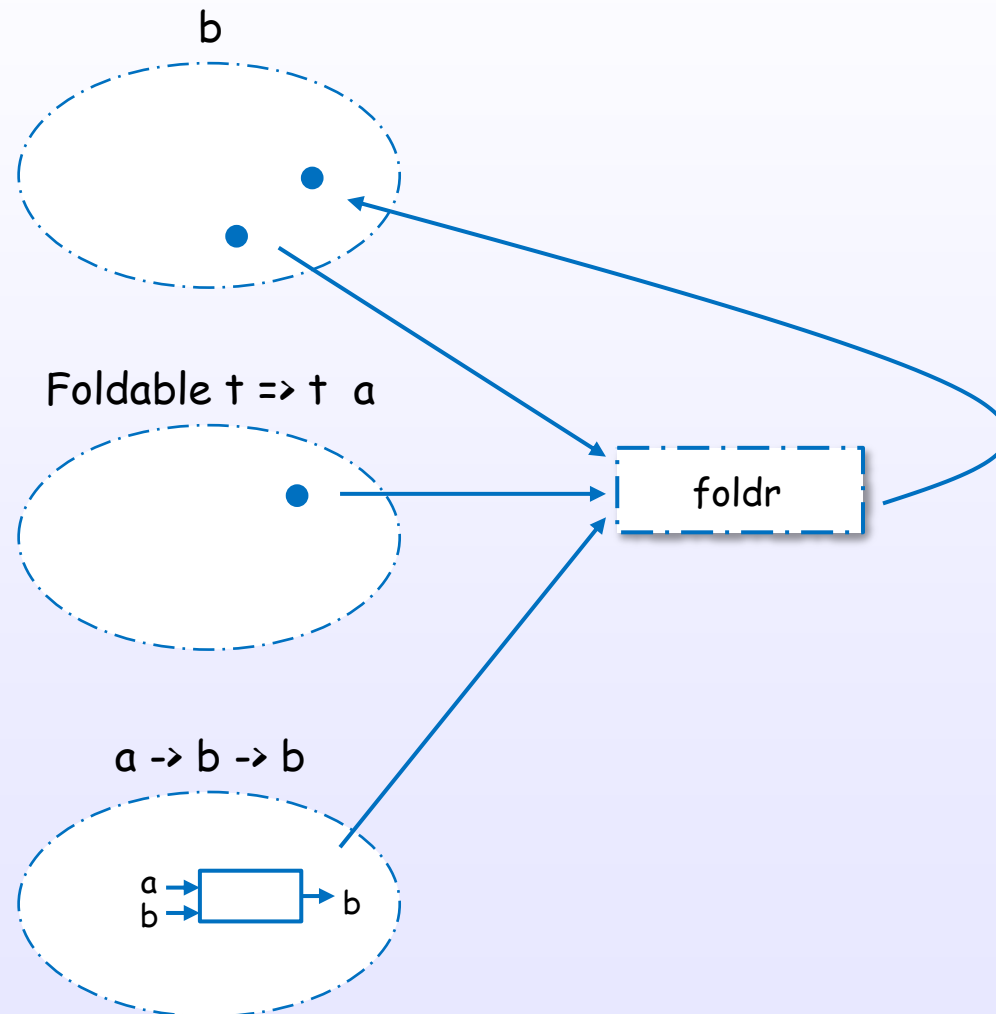
3. What is this?

What is this ?!

`foldr :: Foldable t => (a -> b -> b) -> b -> t a -> b`
`foldr = ...` ?

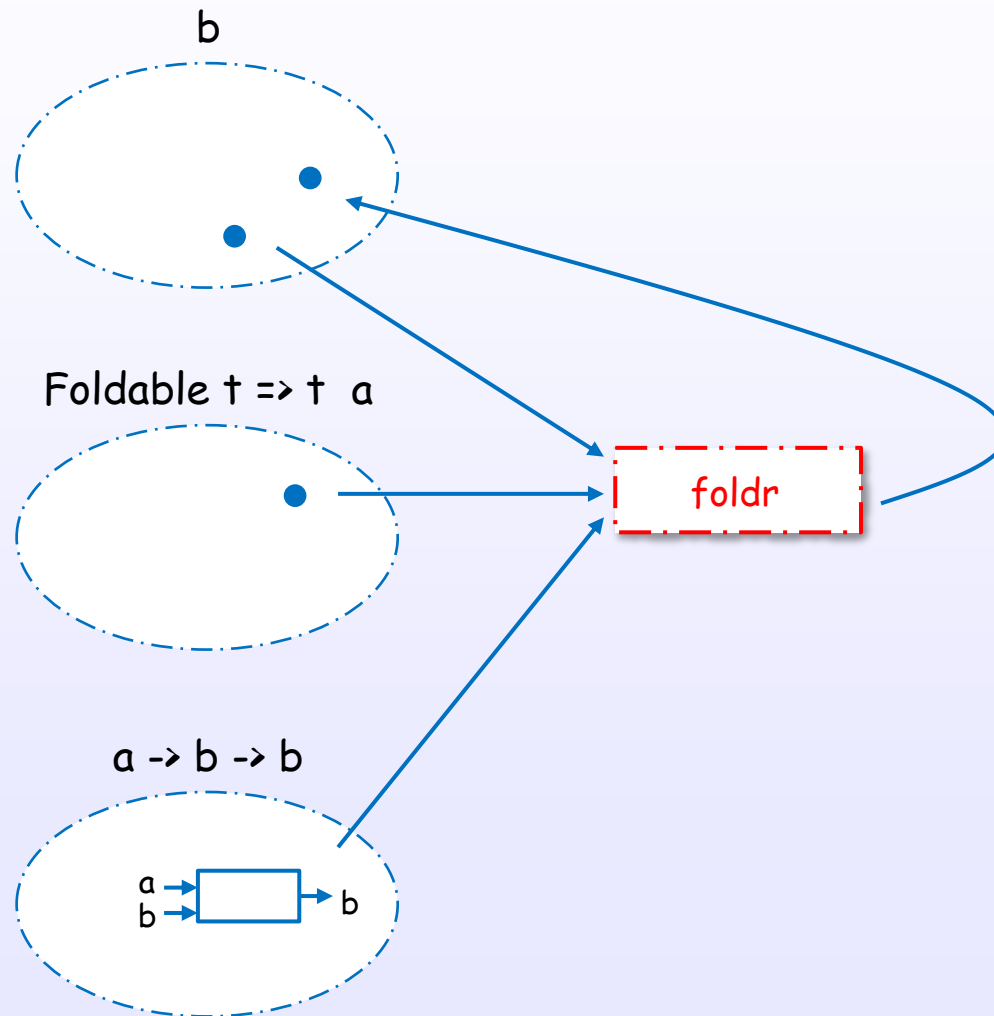
What is this ?!

$\text{foldr} :: \text{Foldable } t \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow t\ a \rightarrow b$



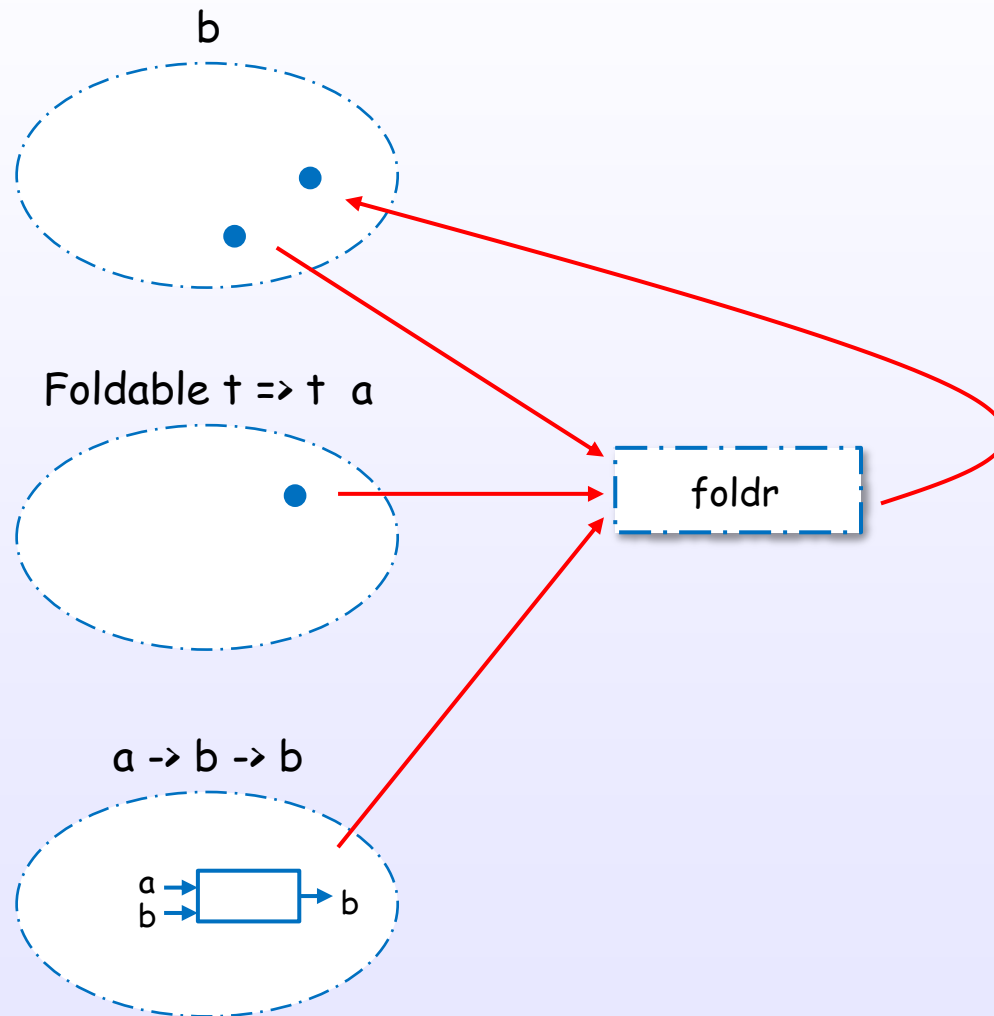
What is this ?!

foldr :: Foldable t => (a -> b -> b) -> b -> t a -> b



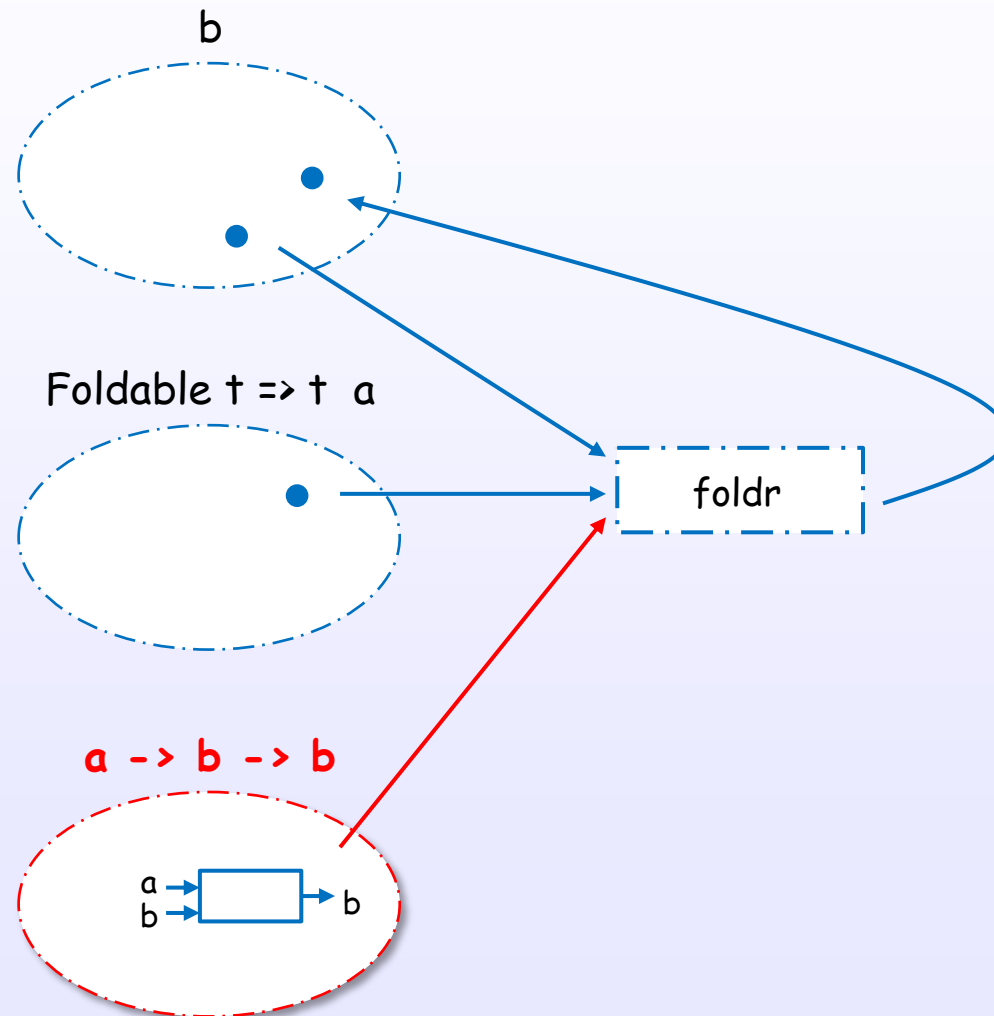
What is this ?!

$\text{foldr} :: \text{Foldable } t \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow t\ a \rightarrow b$



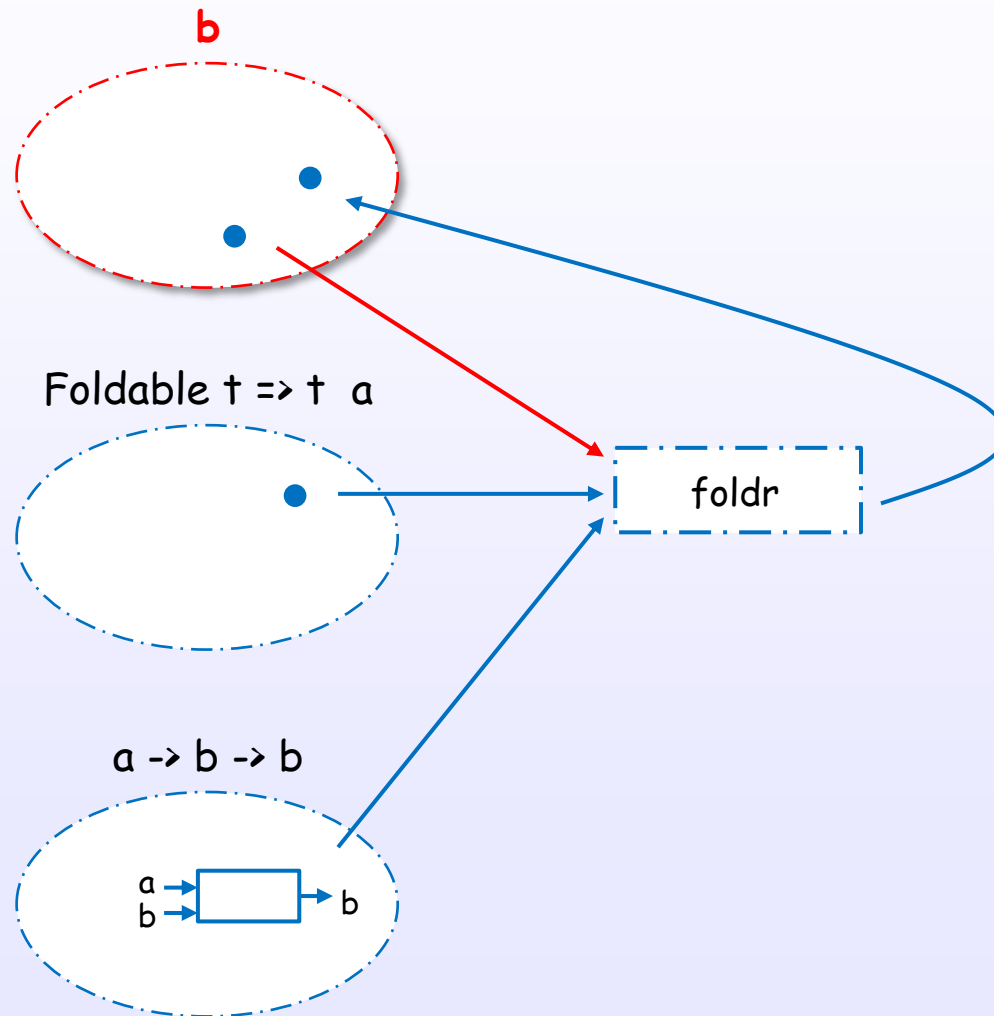
What is this ?!

$\text{foldr} :: \text{Foldable } t \Rightarrow \underline{(a \rightarrow b \rightarrow b)} \rightarrow b \rightarrow t\ a \rightarrow b$



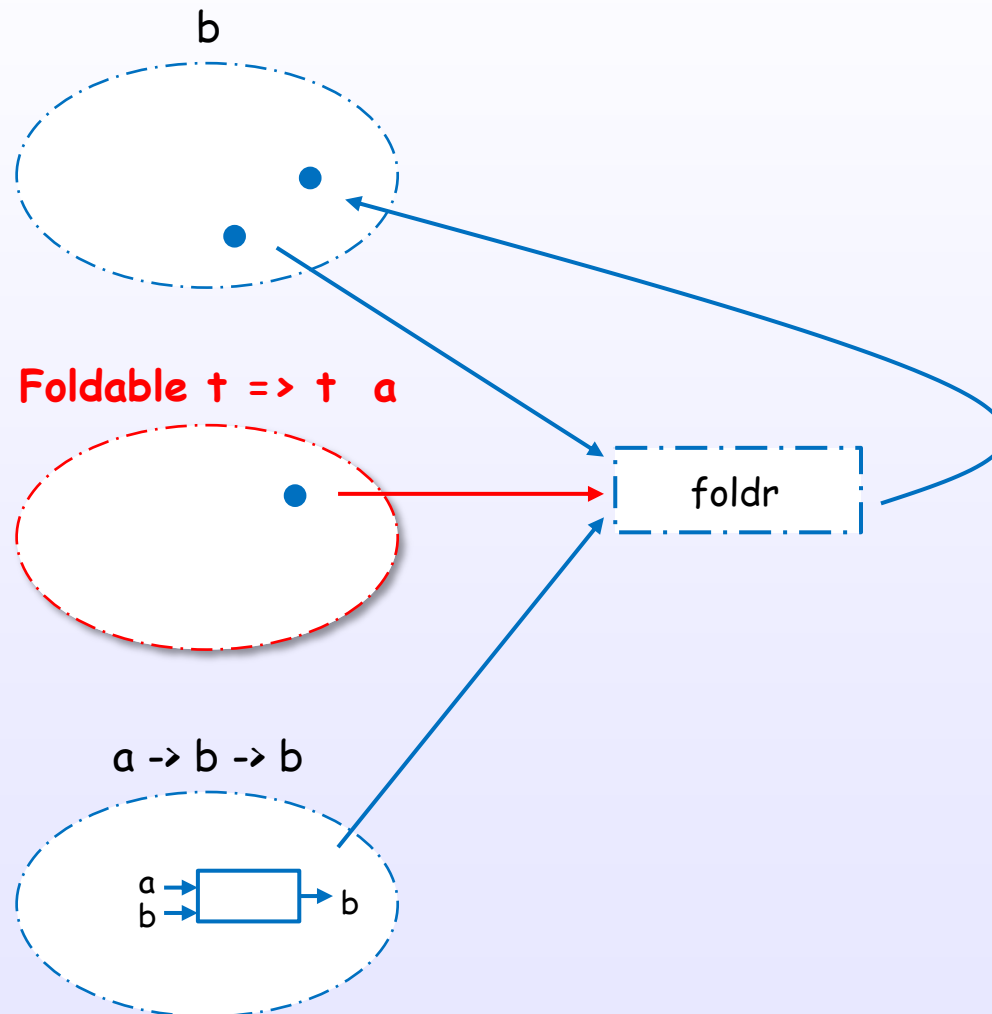
What is this ?!

$\text{foldr} :: \text{Foldable } t \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow \underline{b} \rightarrow t\ a \rightarrow b$



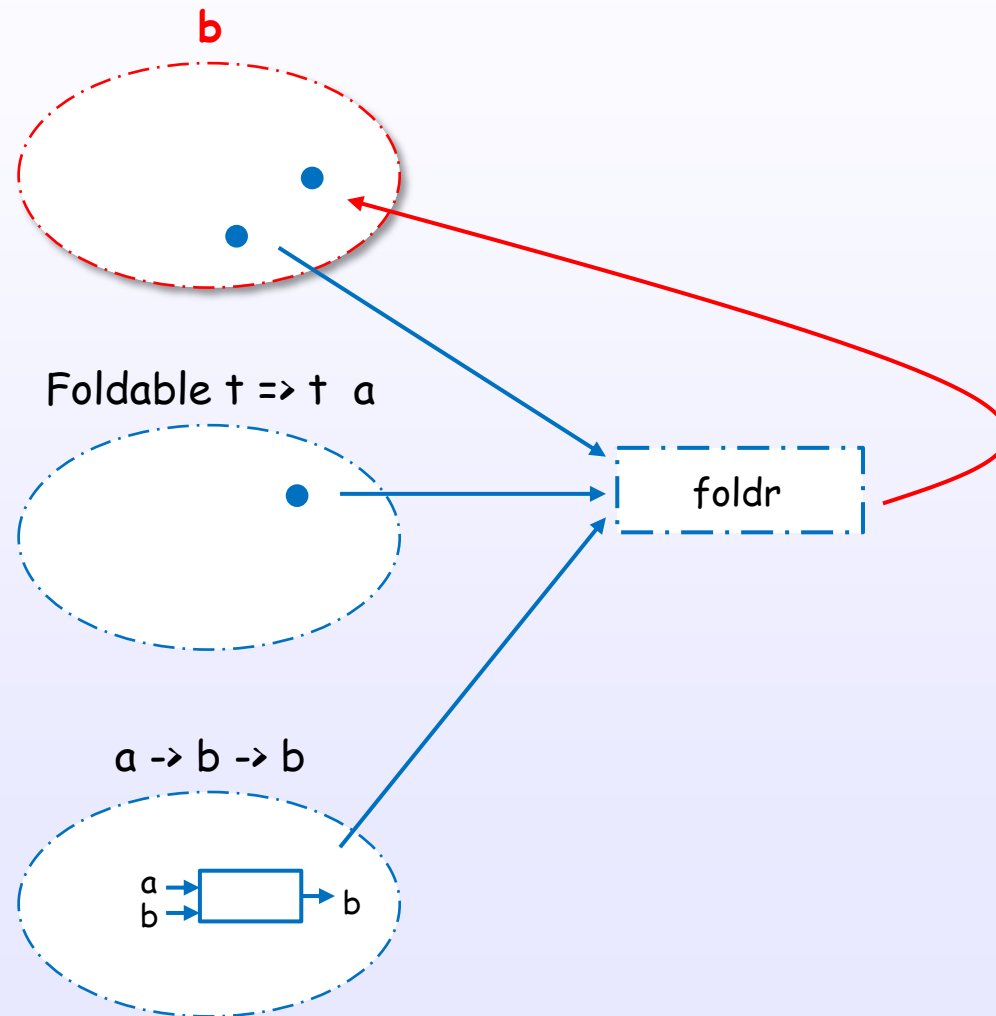
What is this ?!

$\text{foldr} :: \text{Foldable } \underline{t} \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow \underline{t} \, a \rightarrow b$



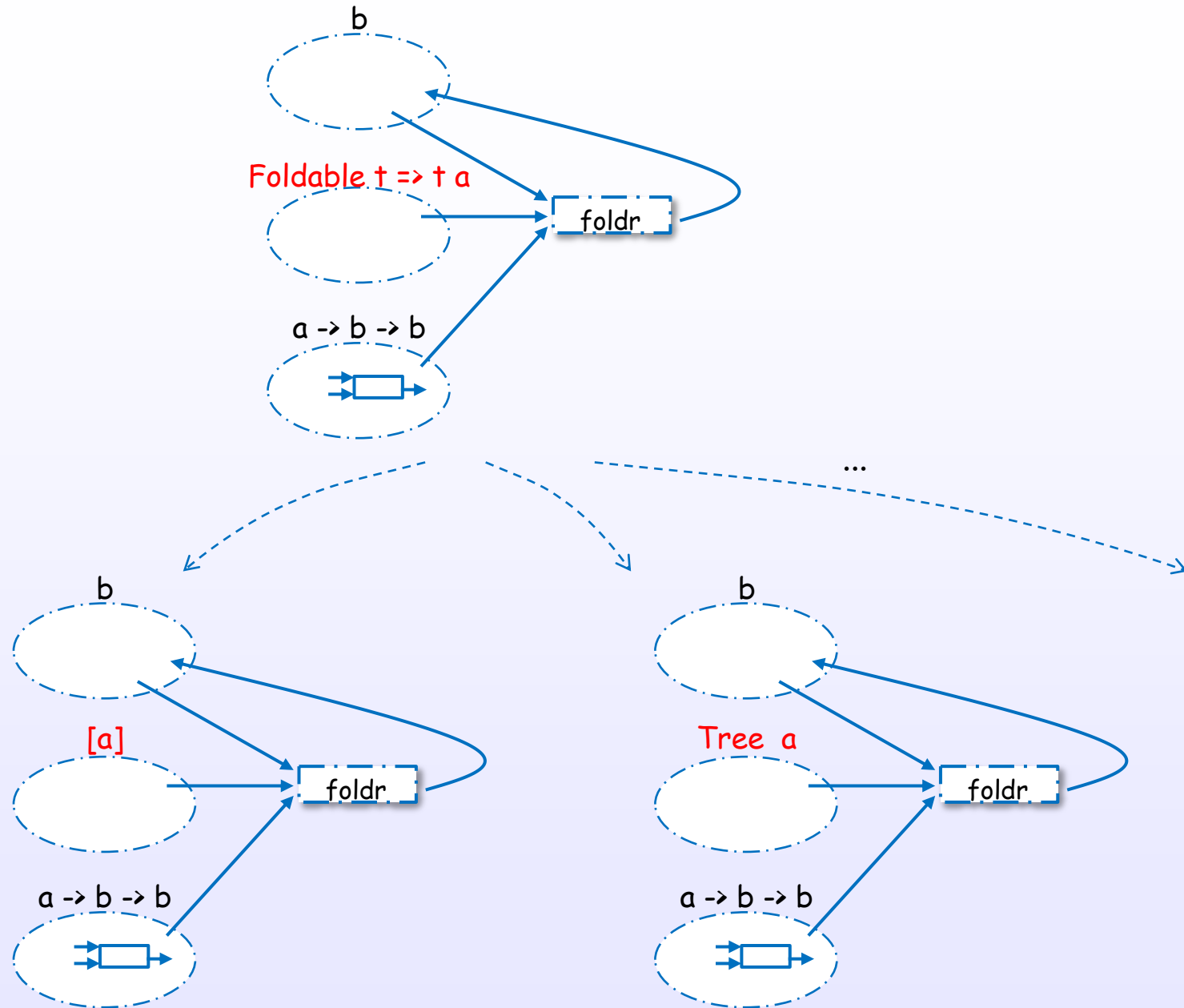
What is this ?!

$\text{foldr} :: \text{Foldable } t \Rightarrow (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow t\ a \rightarrow \underline{b}$



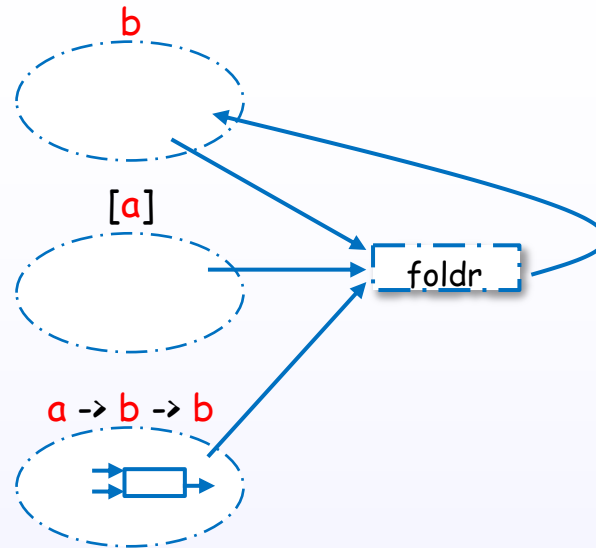
Example of polymorphism on foldr

Polymorphic
types

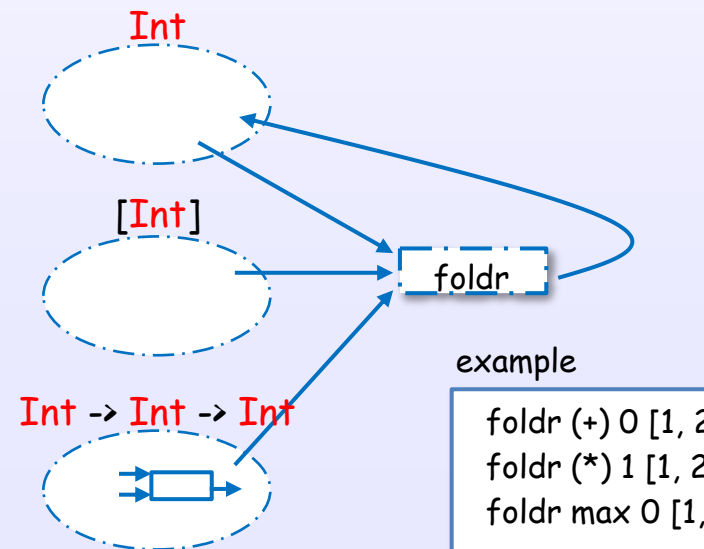
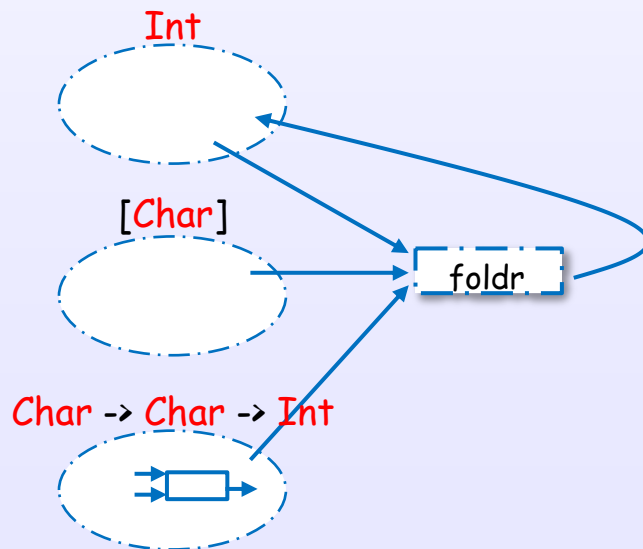


Example of polymorphism on foldr

Polymorphic
types



Proper
types



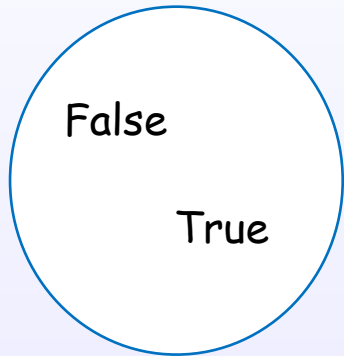
example

```
foldr (+) 0 [1, 2, 3]
foldr (*) 1 [1, 2, 3]
foldr max 0 [1, 2, 3]
:
```

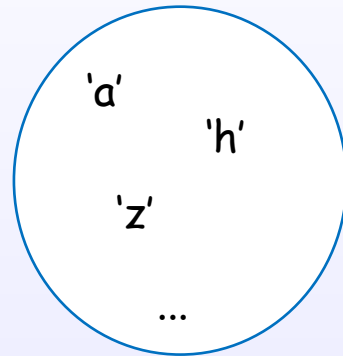
Appendix I - Various types

Bool, Char, Int, Float types

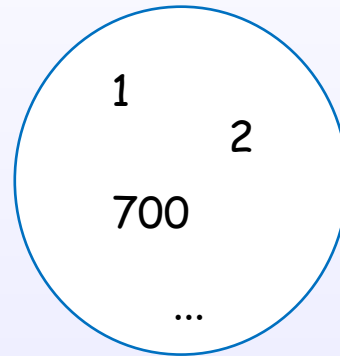
Bool



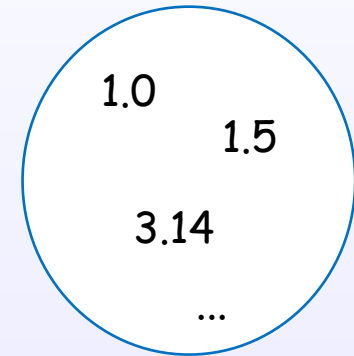
Char



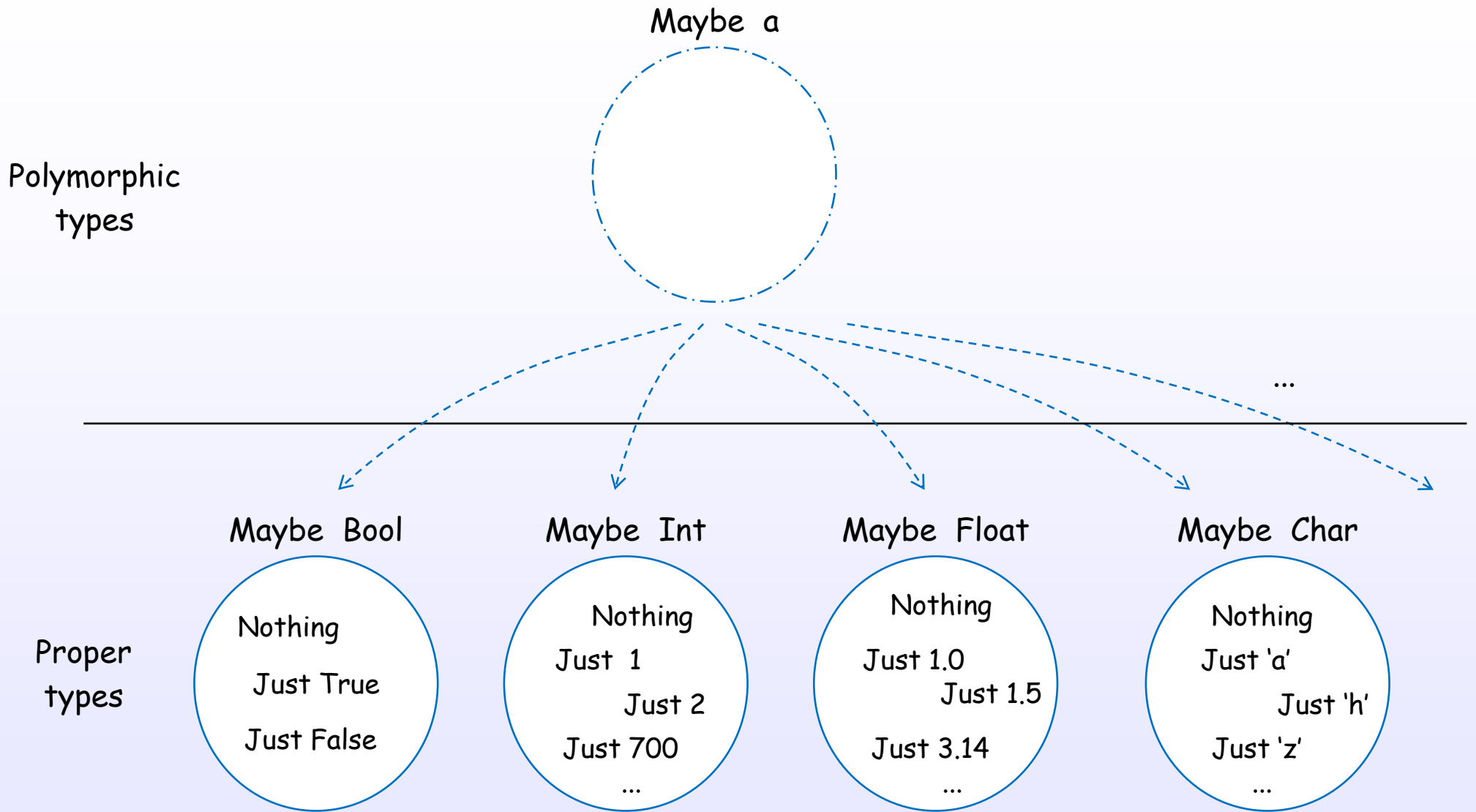
Int



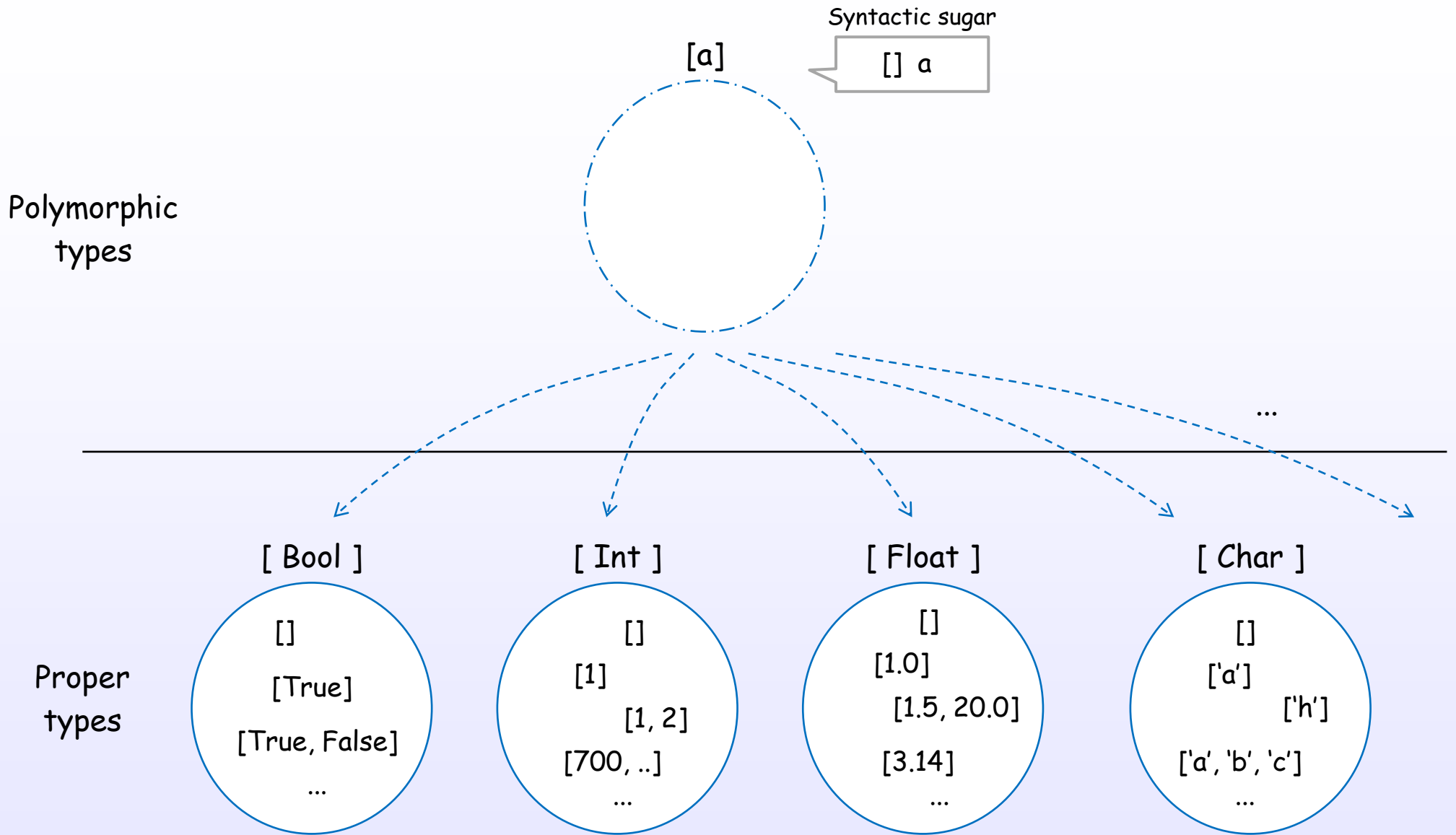
Float



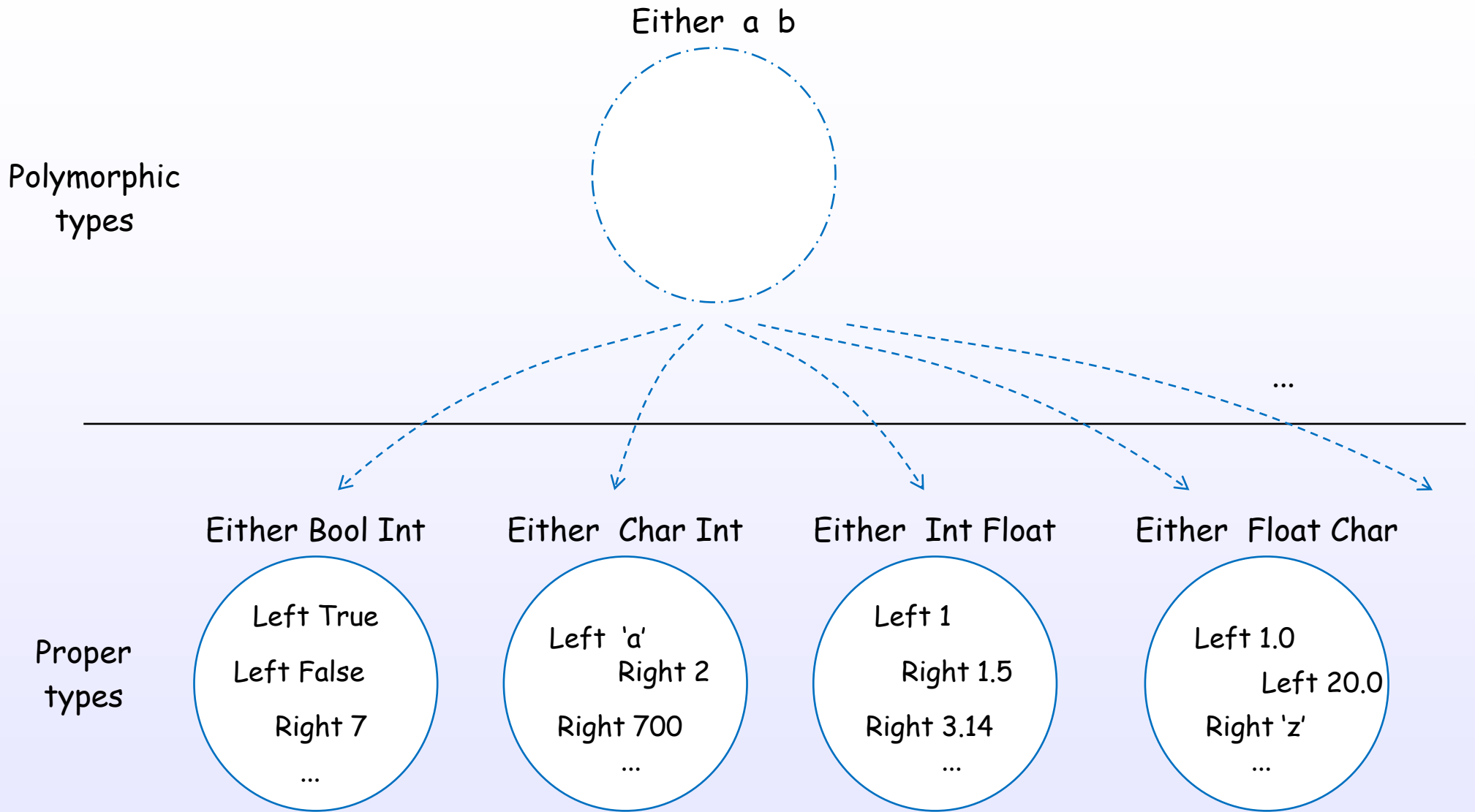
Maybe type



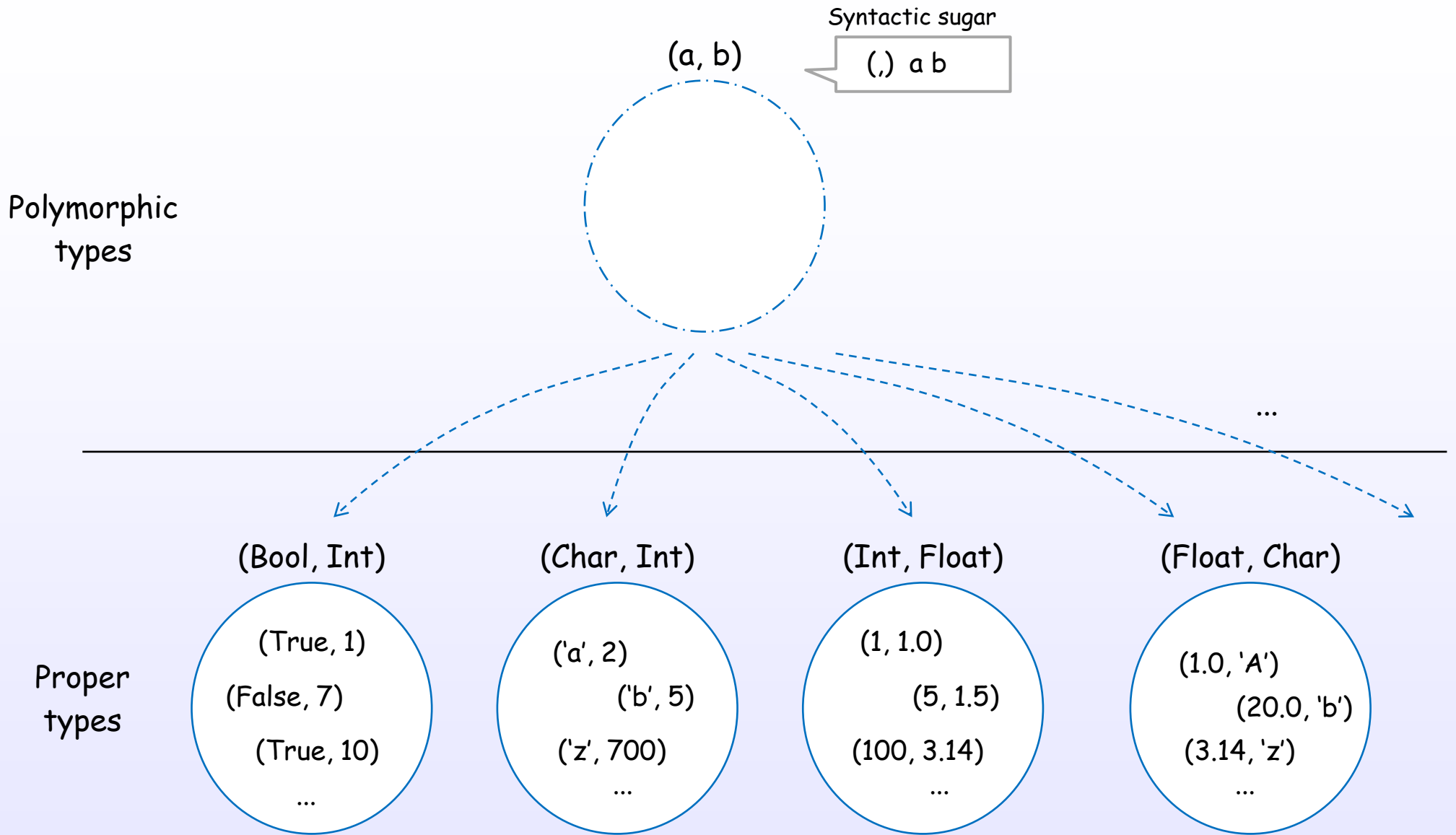
List type



Either type

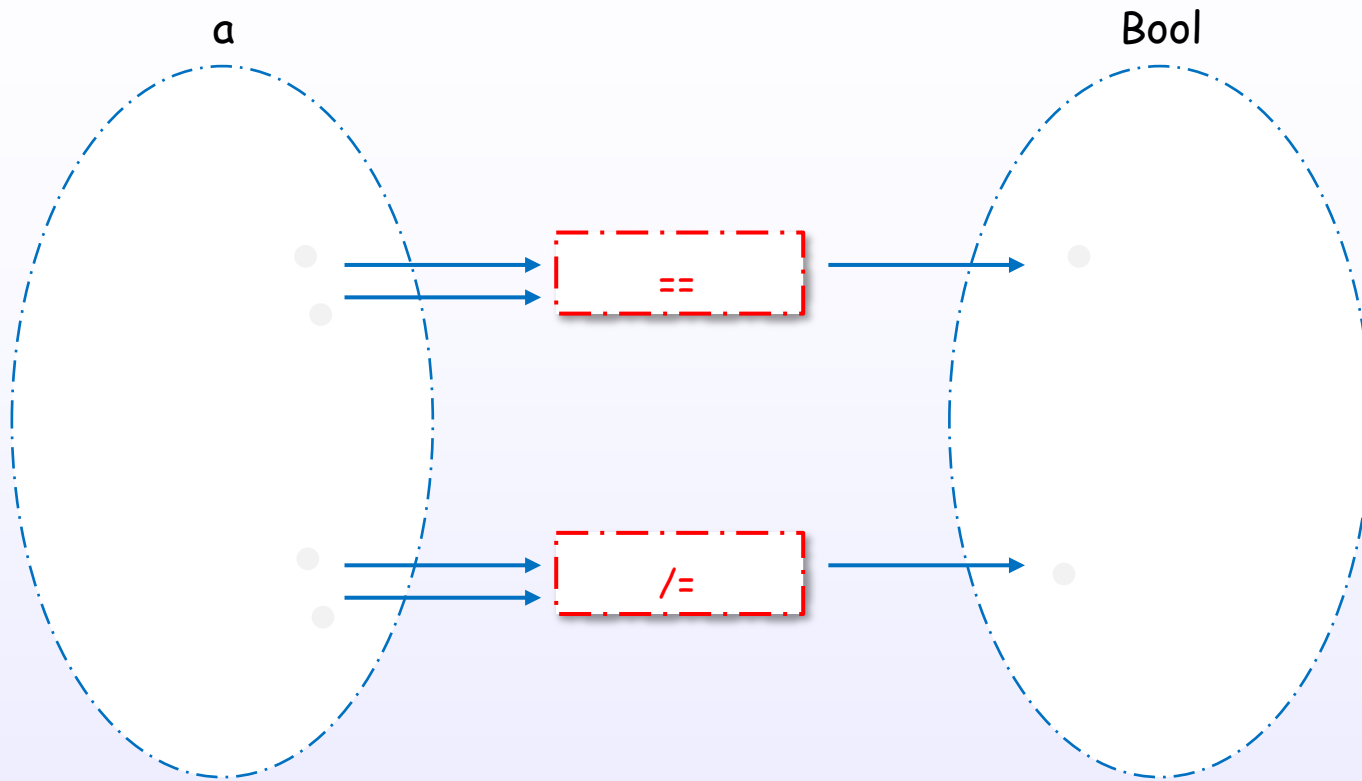


Tuple (pair) type



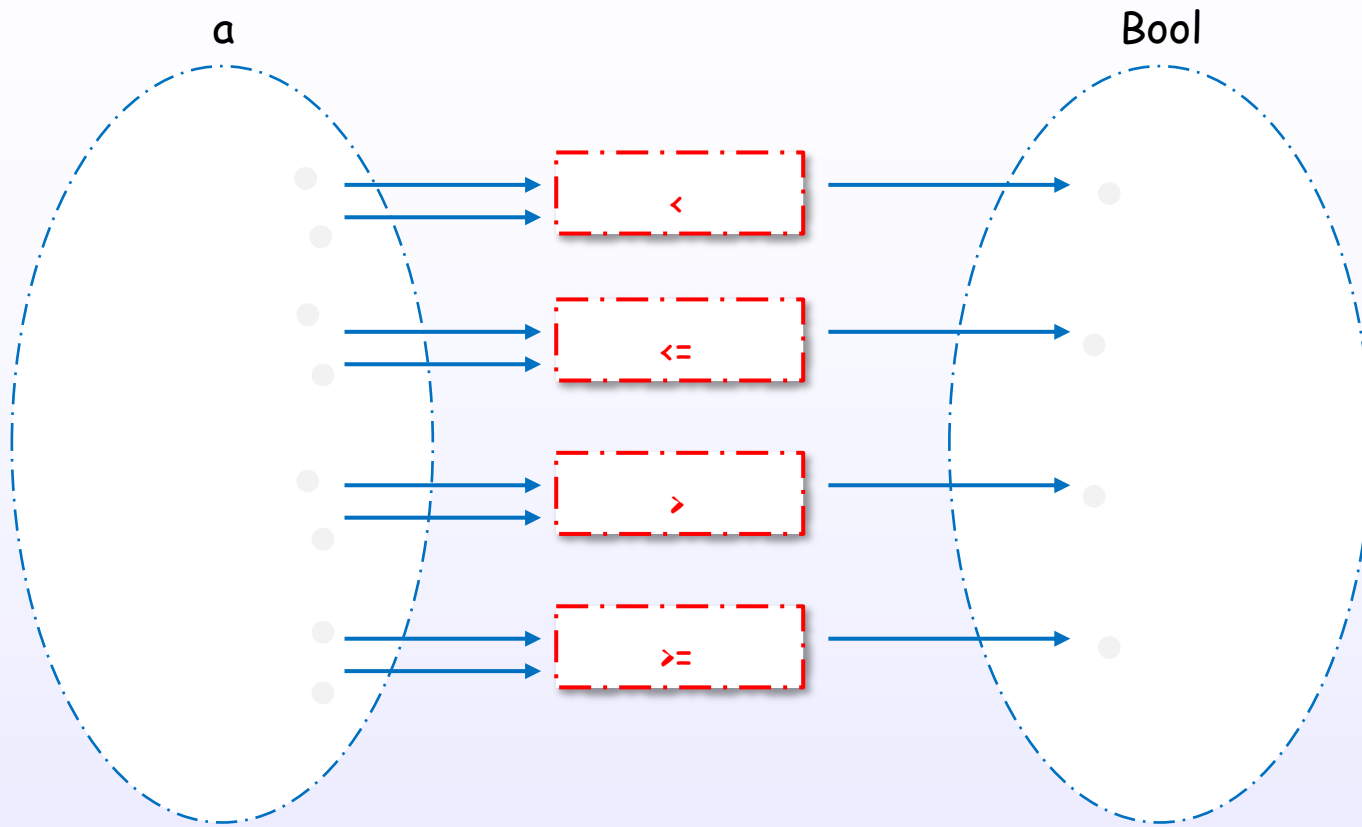
Appendix II - Various type classes

Eq class's characteristic operations



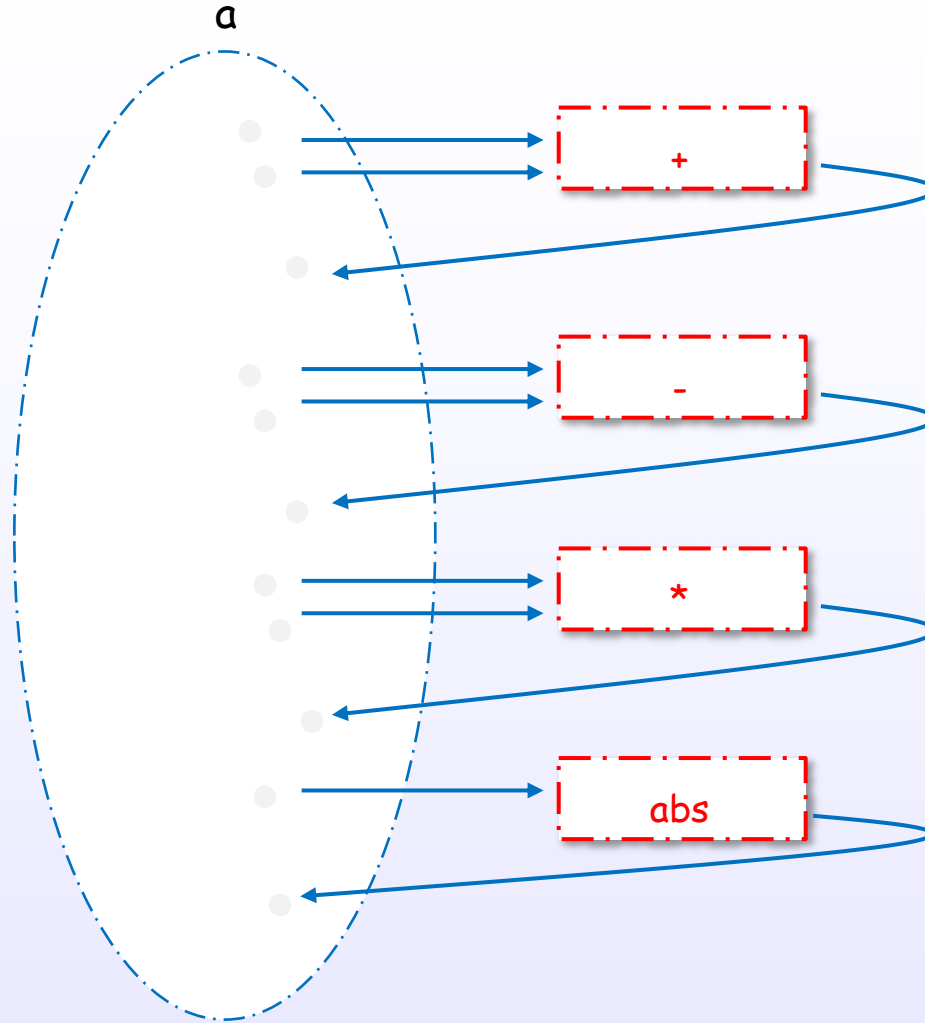
The Eq class has equality operations.

Ord class's characteristic operations



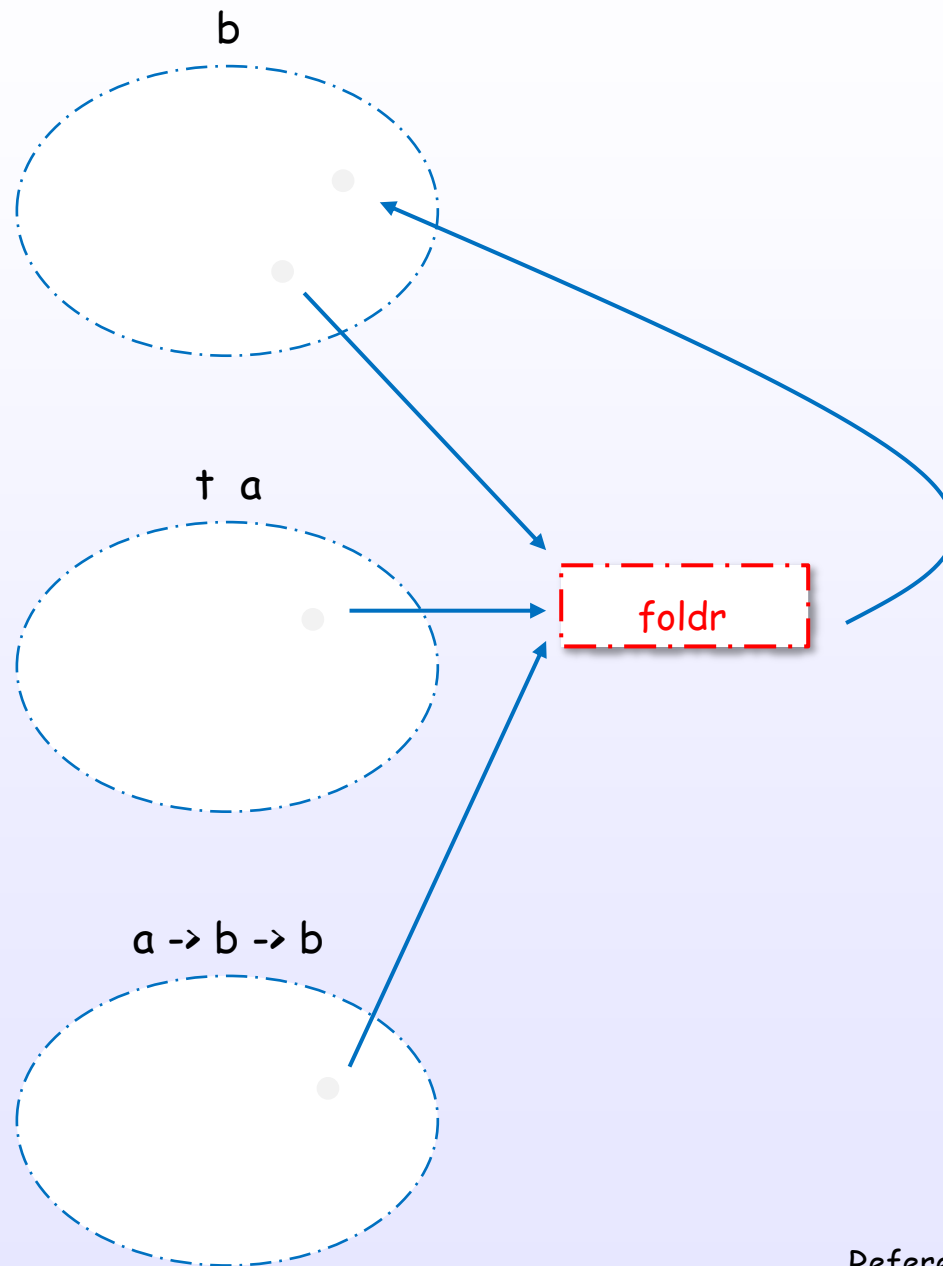
The Ord class has comparison operations.

Num class's characteristic operations

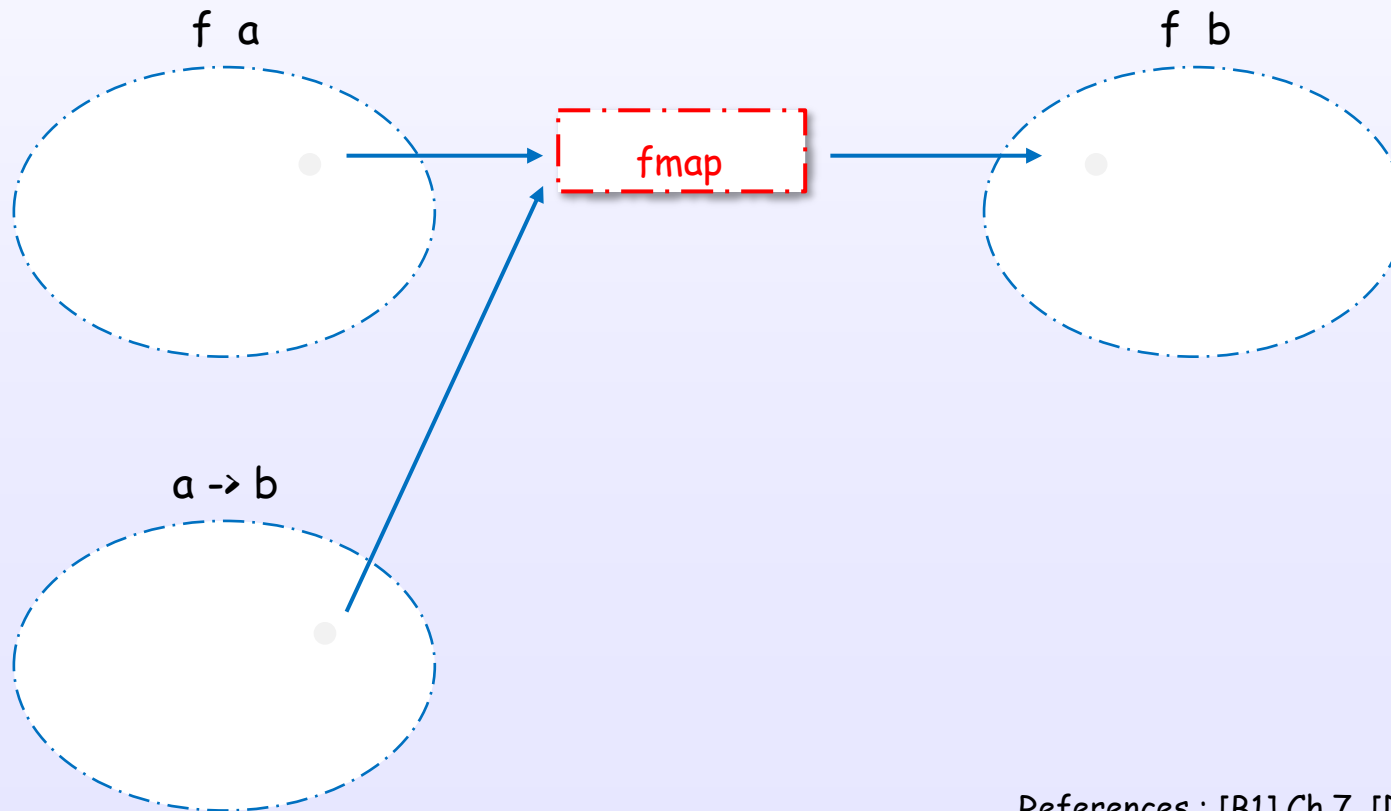


The Num class has arithmetic operations.

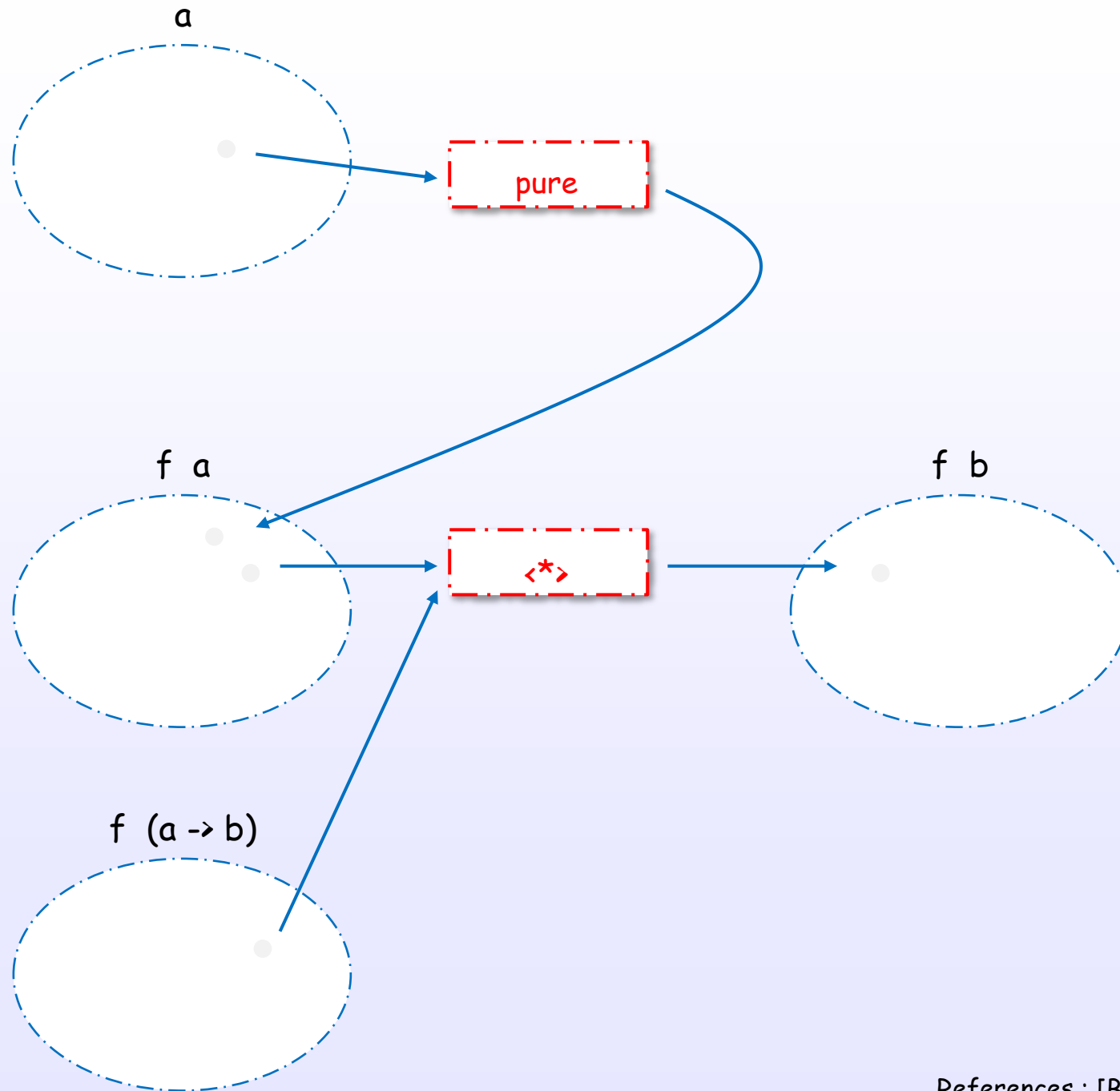
Foldable class's characteristic operations



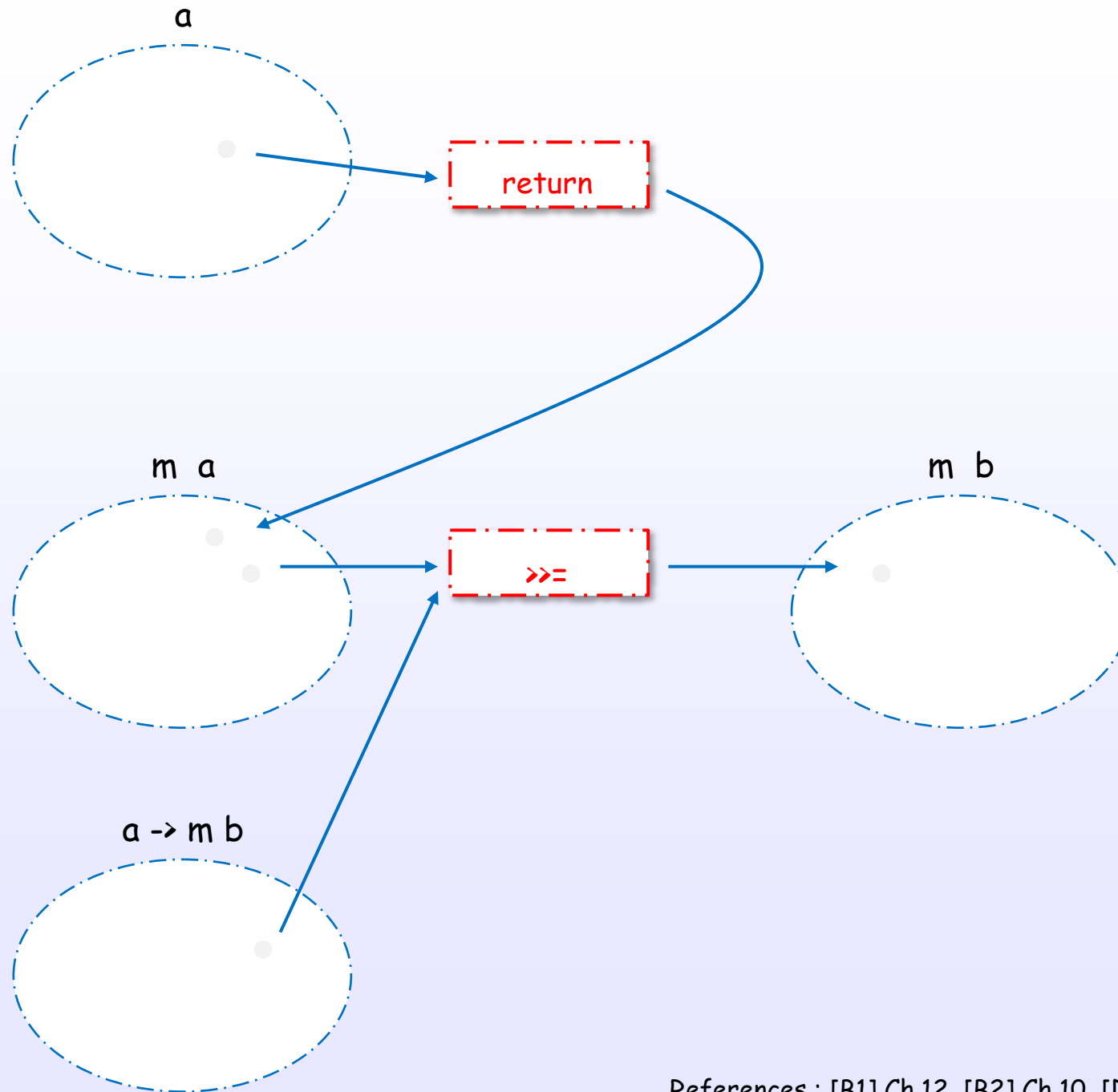
Functor class's characteristic operations



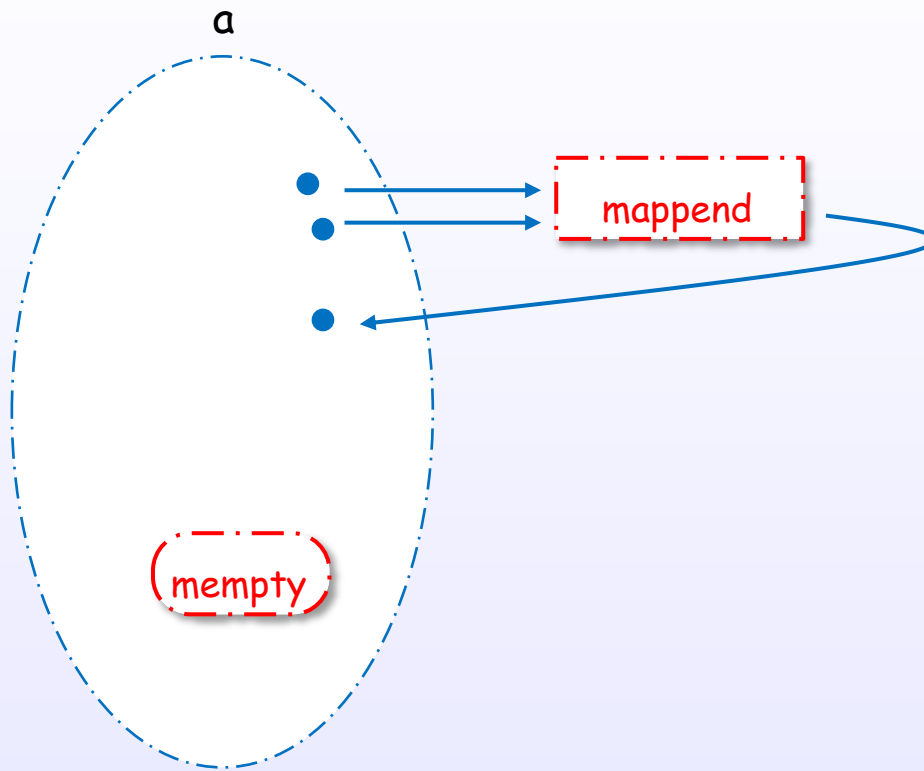
Applicative class's characteristic operations



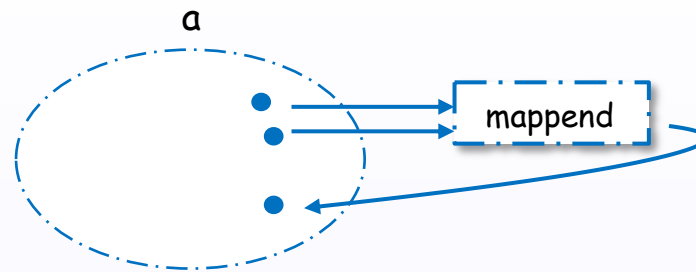
Monad class's characteristic operations



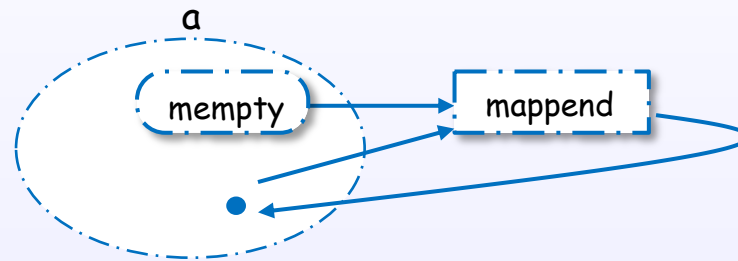
Monoid class's characteristic operations



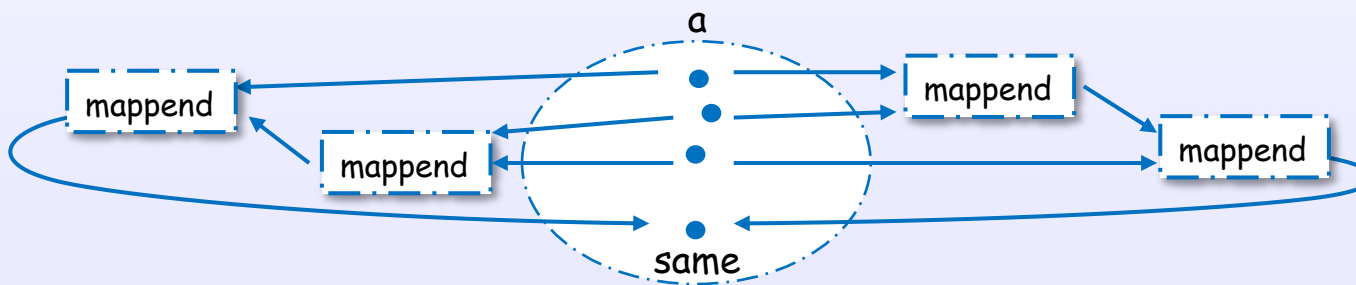
Related topics: monoid laws



binary operation



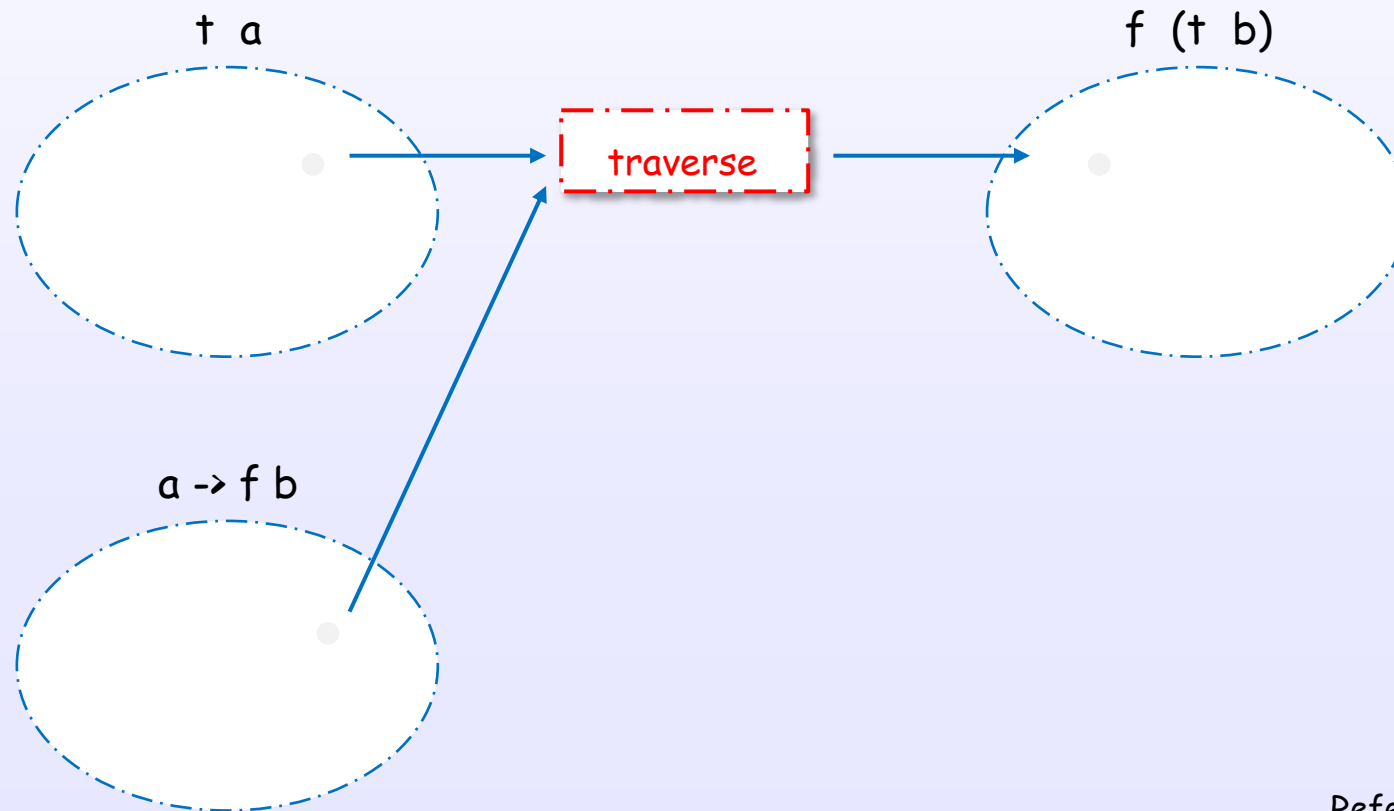
unit law



associative law

Programmers should satisfy the monoid laws.

Traversable class's characteristic operations



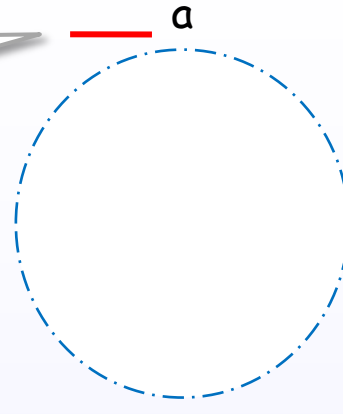
Appendix III - Advanced topics

Universally quantified types

forall a . a

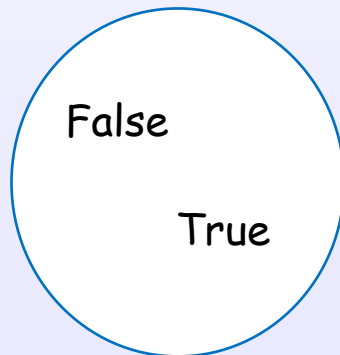
implicitly quantified with
universal quantification ($\forall a .$)

Polymorphic
types

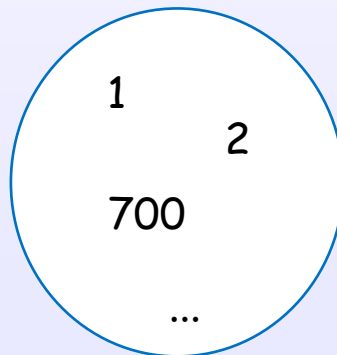


Proper
types

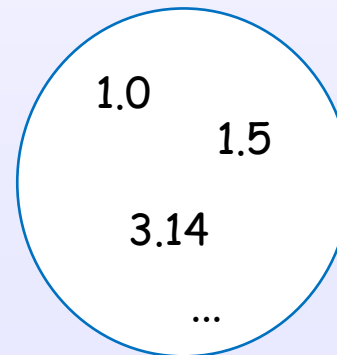
Bool



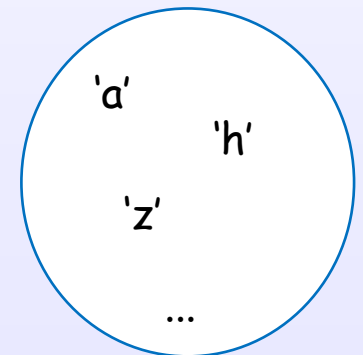
Int



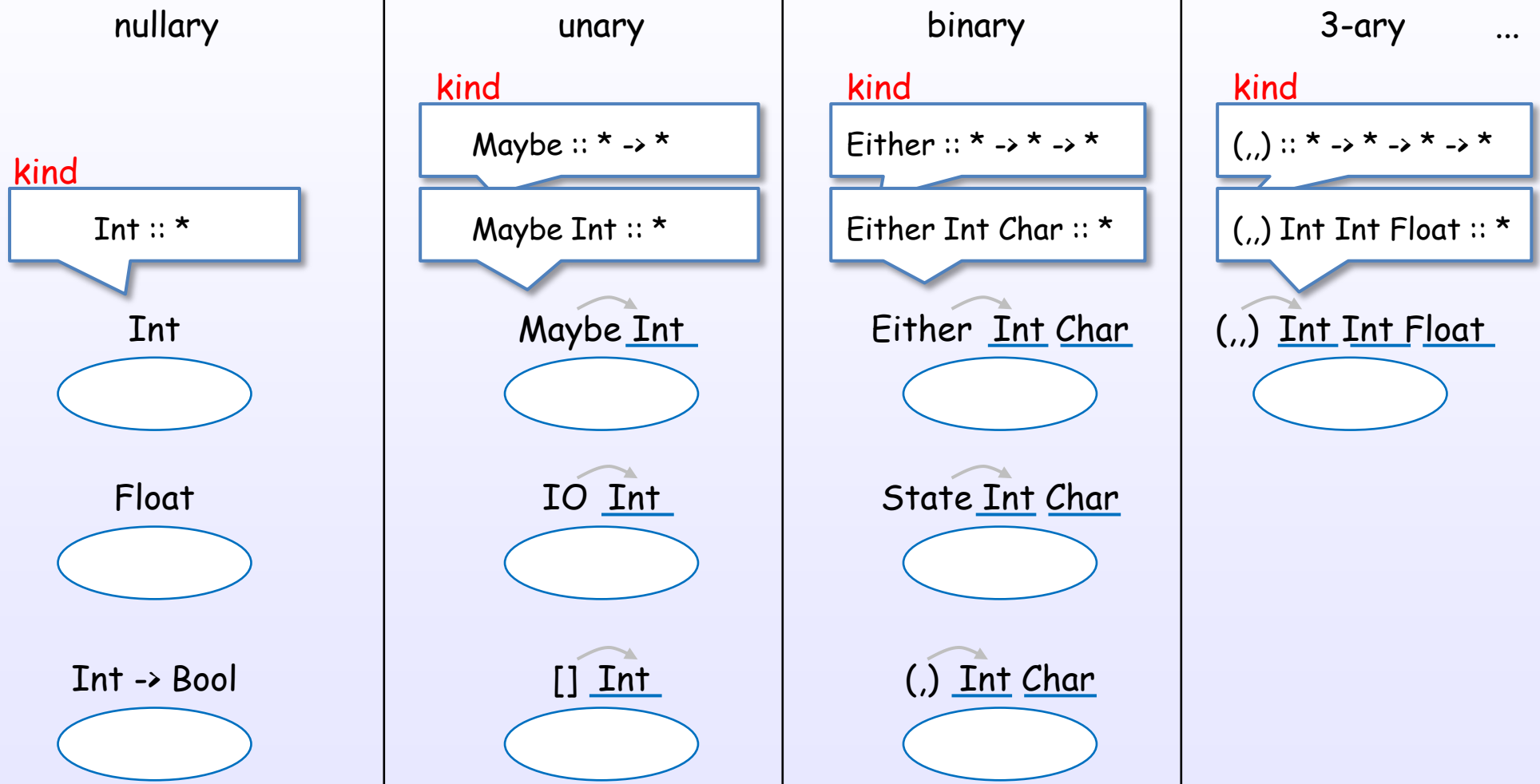
Float



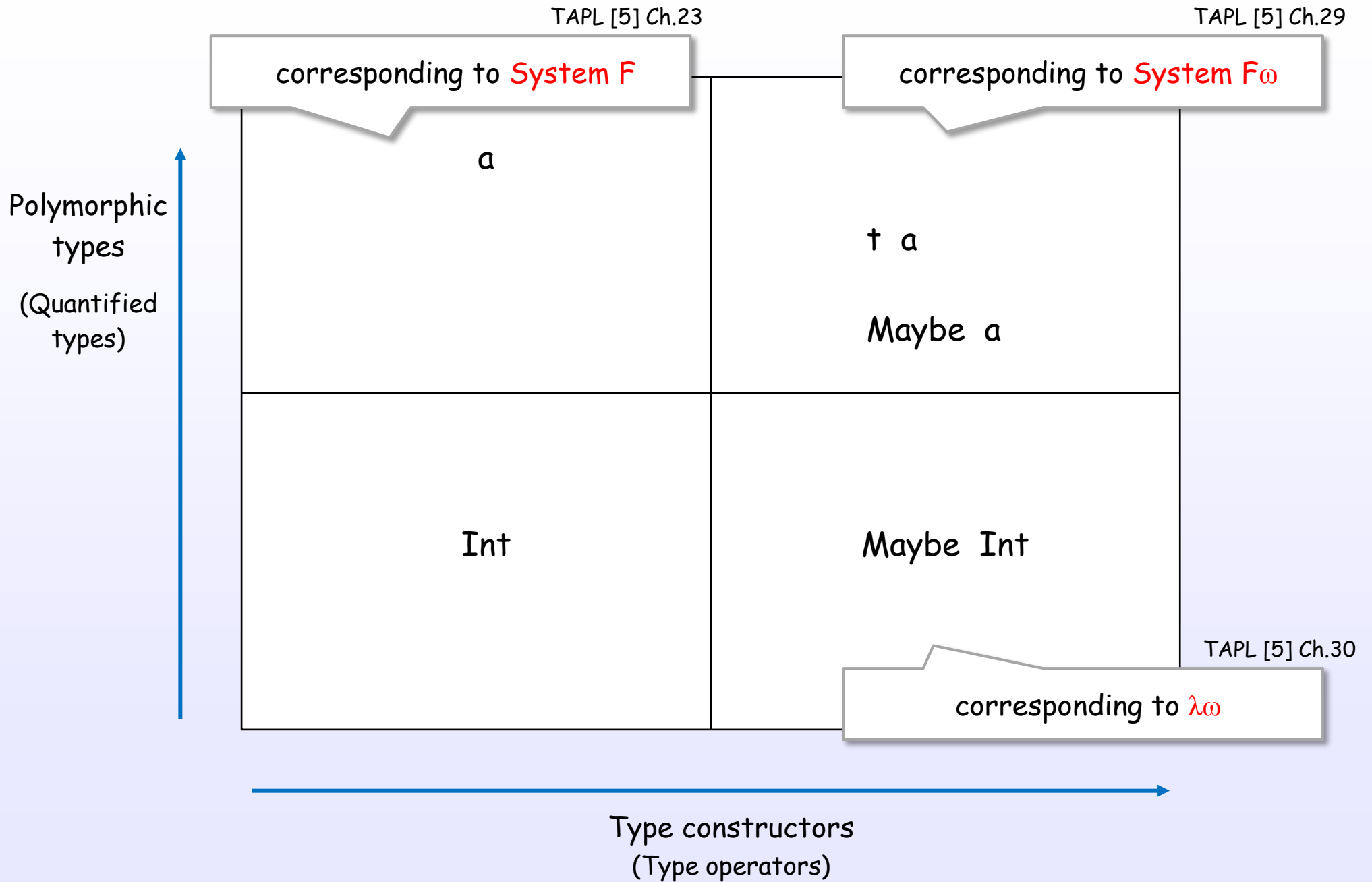
Char



Kinds and type constructors



Type systems



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