

# Type introduction illustrated

## for Haskell newcomers

*get over the foldable*

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## NOTE

- This shows one of the mental model.
- Please see also references.
- This is written for Haskell, especially later ghc8.

# Contents

## 1. Introduction

- Simple question
- Type
- Typeclass

## 2. Types

- Type
- Parametric polymorphism type
- Constructed type

## 3. Typeclasses

- Typeclass

## Appendix I - various types

- Bool
- Char
- Int, Integer, Float
- List
- Maybe
- Either

## Appendix II - various typeclasses

- Eq, Ord
- Num
- Foldable
- Monoid
- Functor, Applicative, Monad

## References

# 1. Introduction

Simple question

# What is this ?!

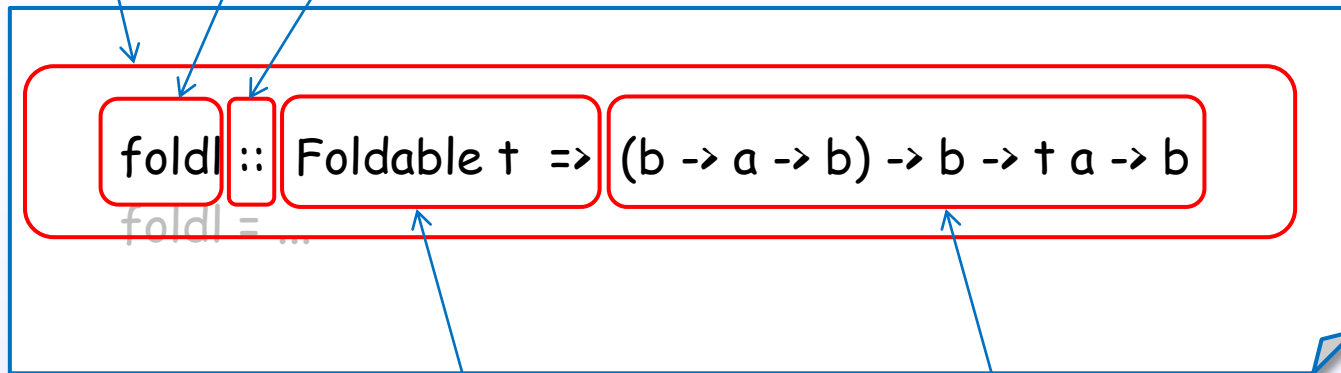
`foldl :: Foldable t => (b -> a -> b) -> b -> t a -> b`  
`foldl = ...` ?

# What is this ?!

type signature  
for the function

function name

syntax for type declaration



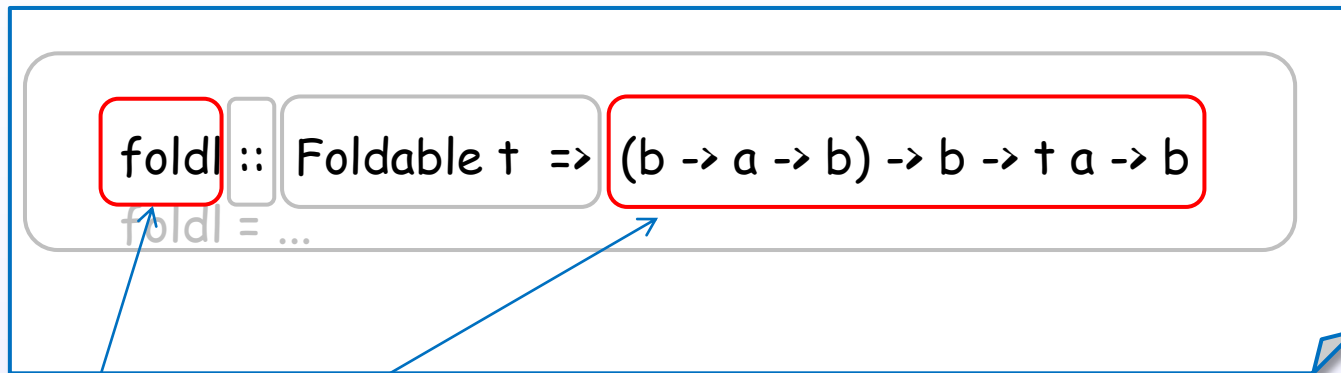
context (type class)

type expression

[H1] 4.1

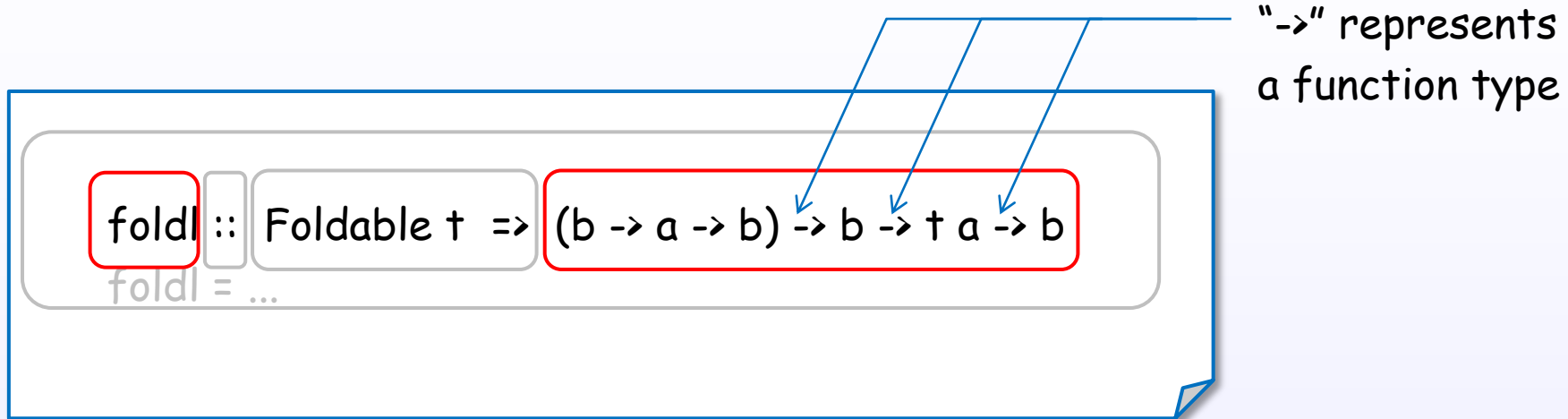
References : @@@

# What is this ?!



"foldl" function has a type "`(b -> a -> b) -> b -> t a -> b`".

# What is this ?!



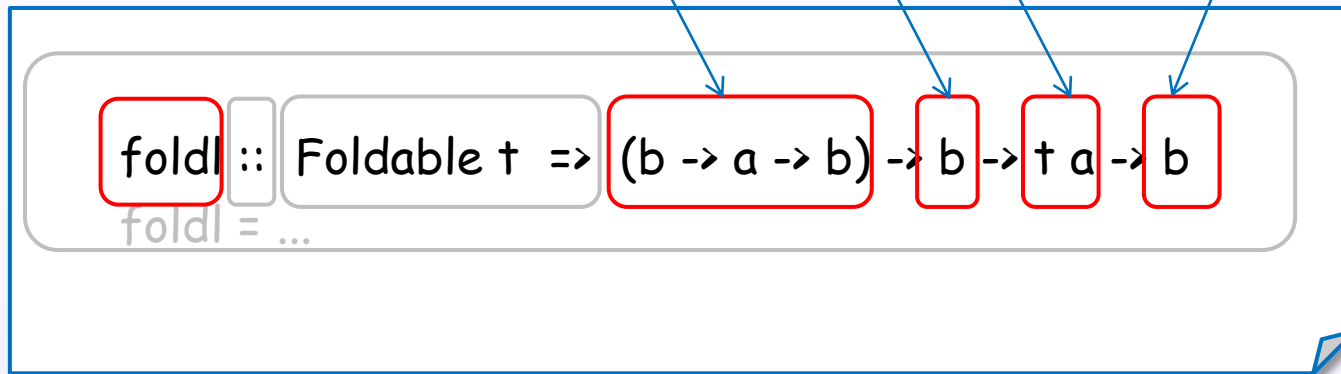
"foldl" is a function.



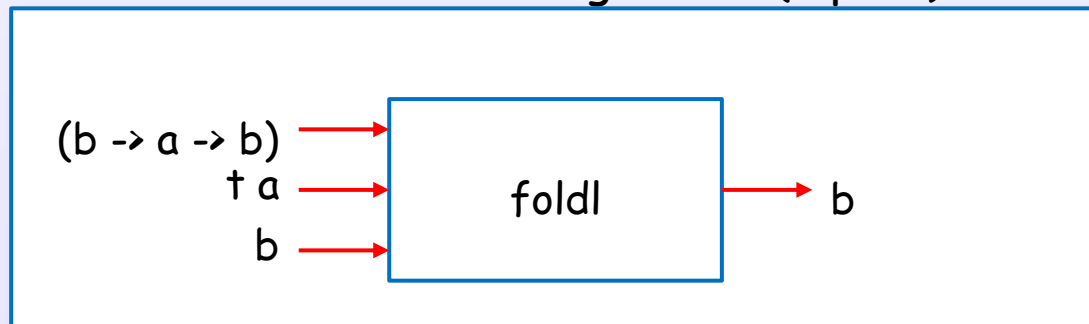
# What is this ?!

three arguments (inputs)

one result (output)

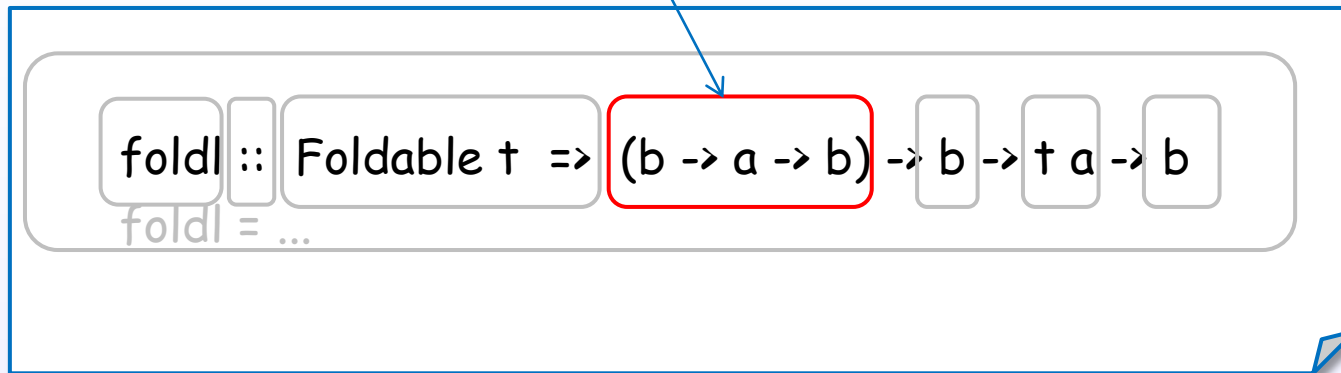


"foldl" function has three arguments(inputs) and one result(output).

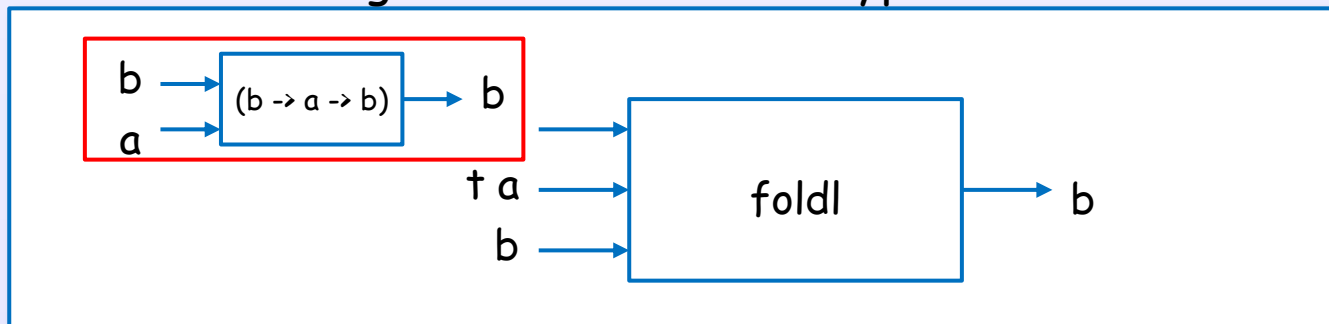


# What is this ?!

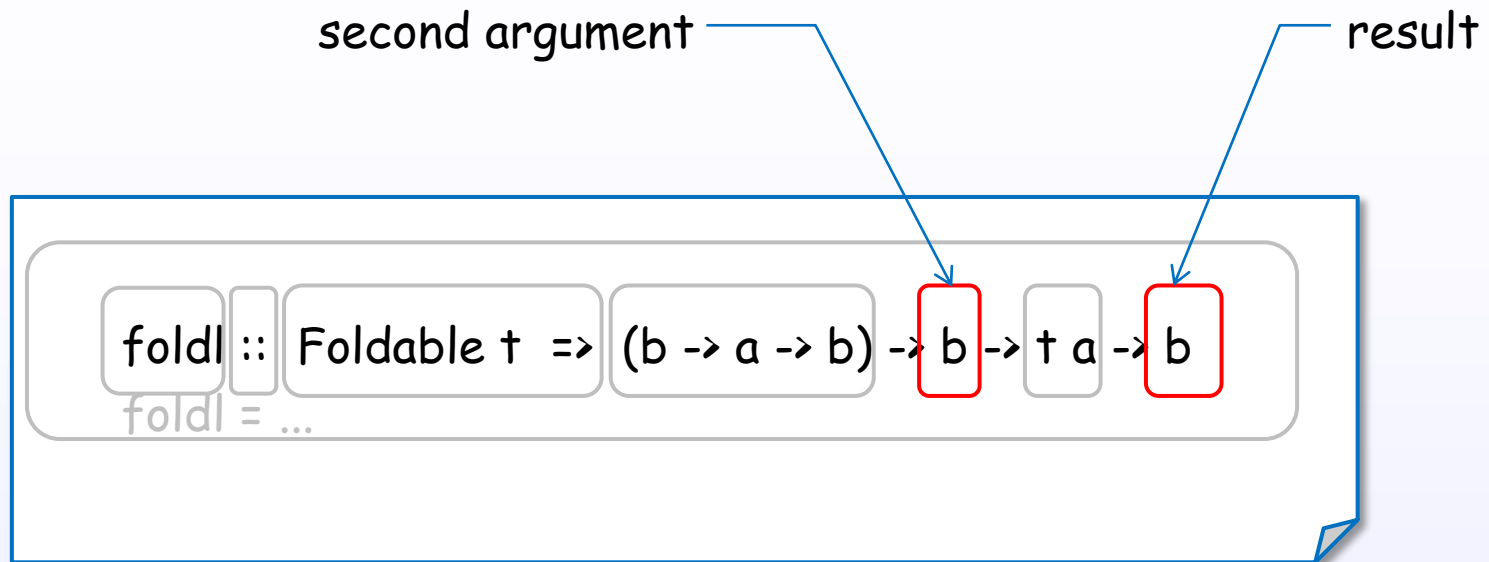
first argument



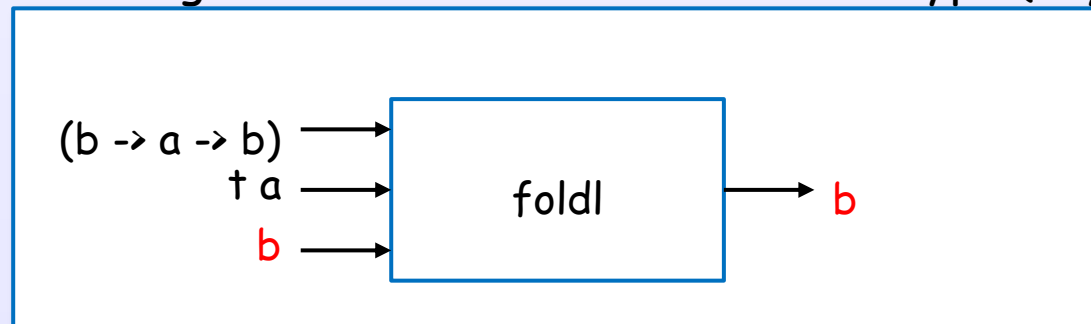
First argument is a function type.



# What is this ?!

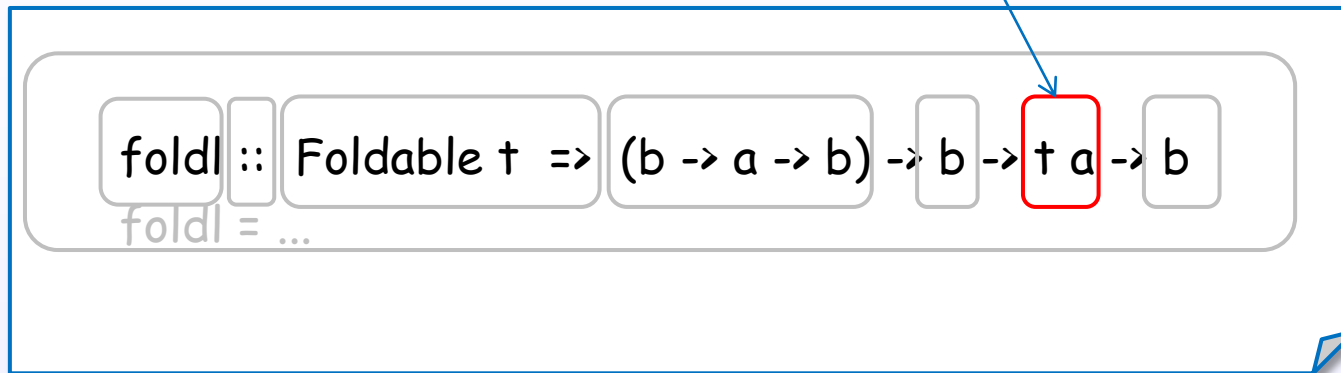


Second argument and the result are same type (any type "b").



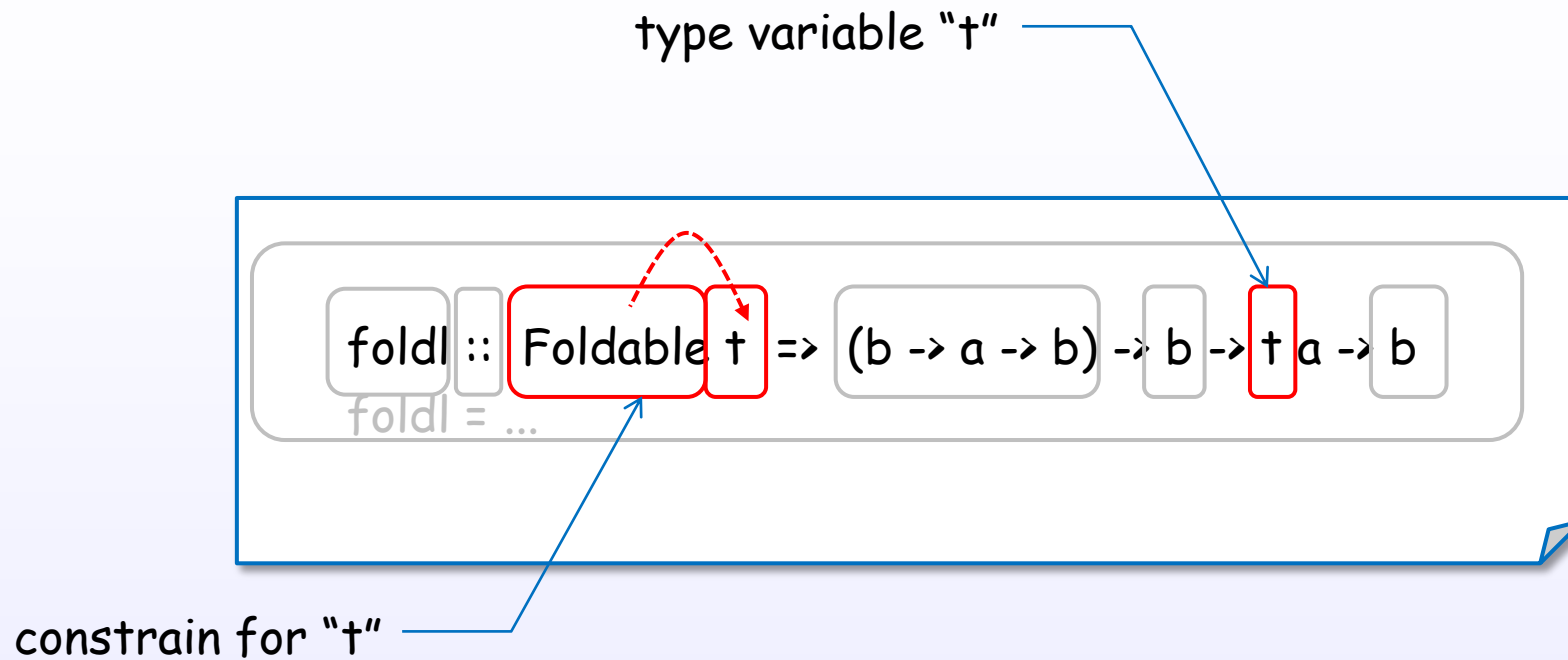
# What is this ?!

third argument



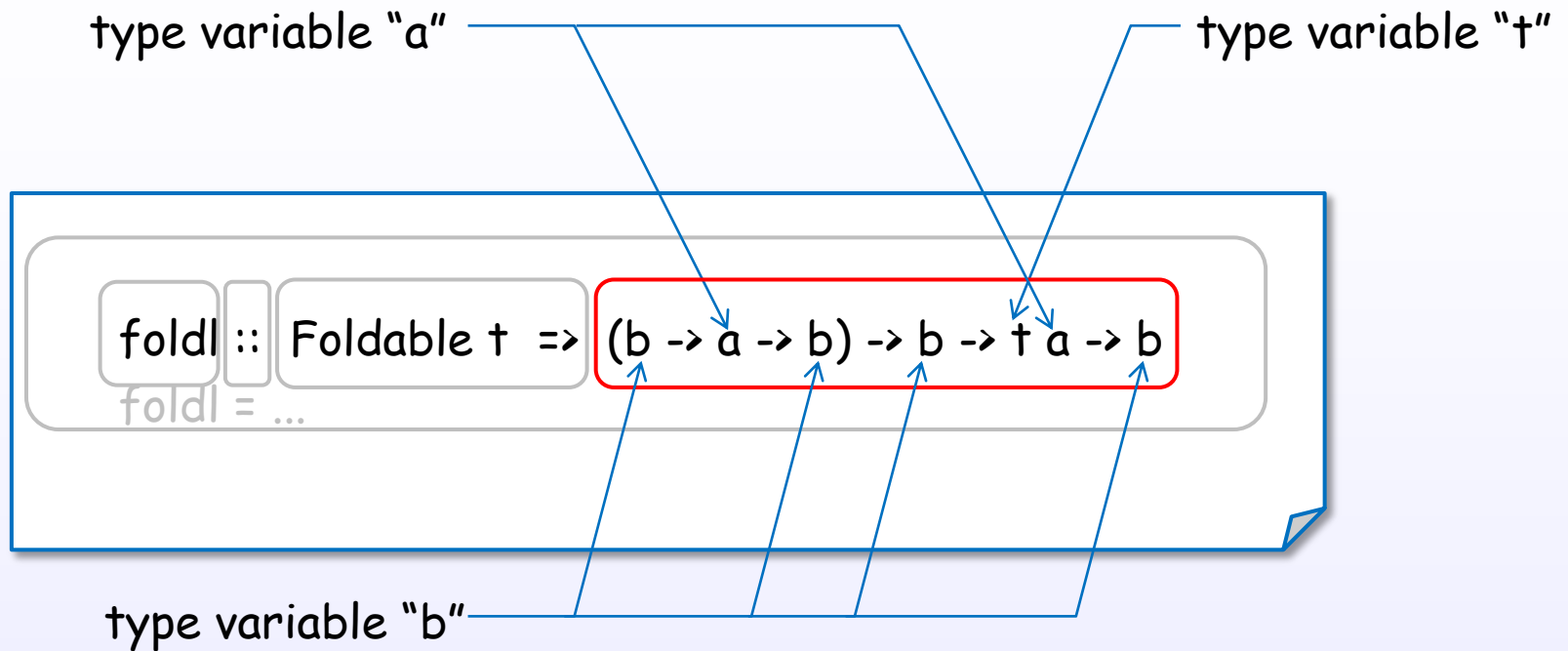
Third argument is a constructed type with type variable "t" and "a".

# What is this ?!

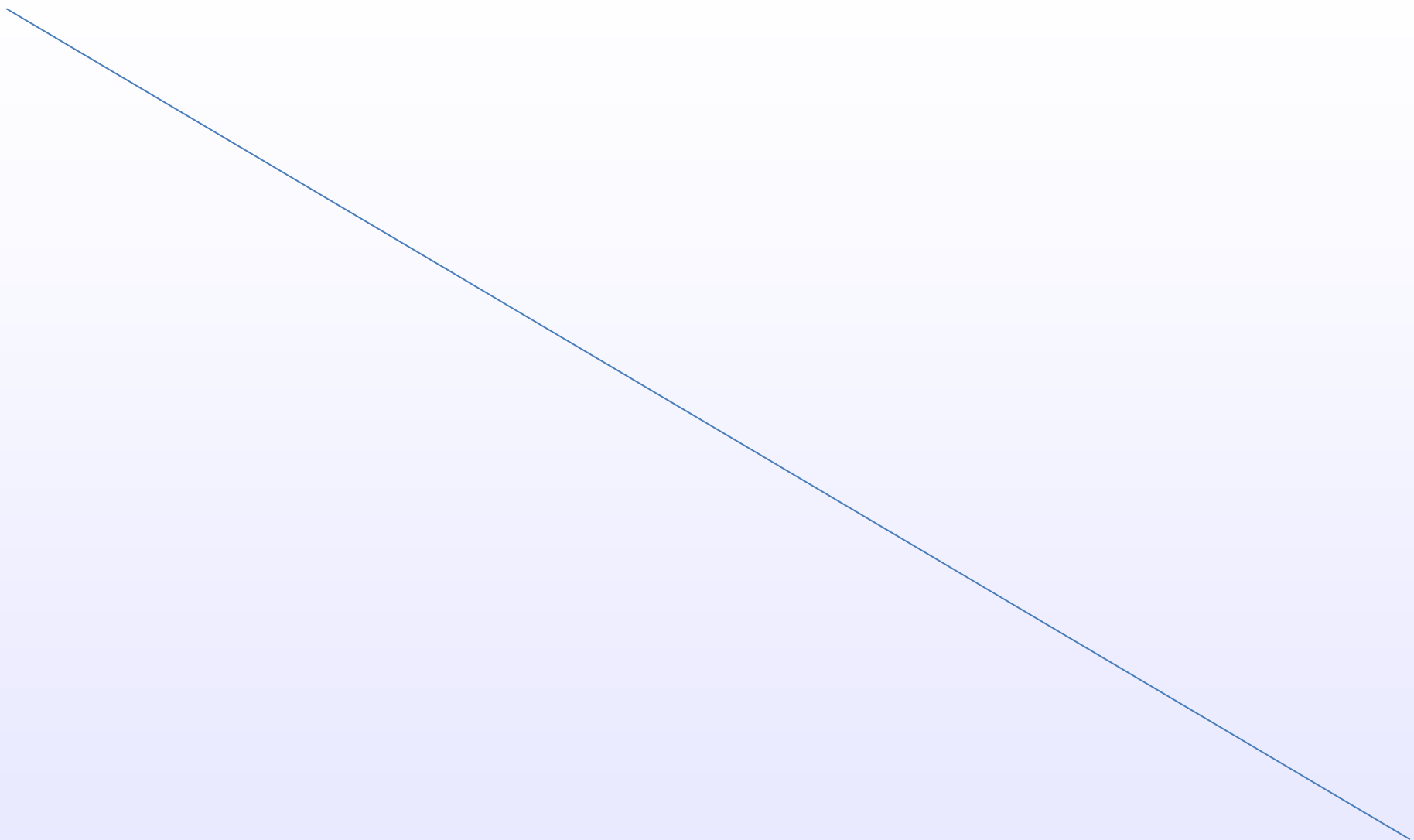
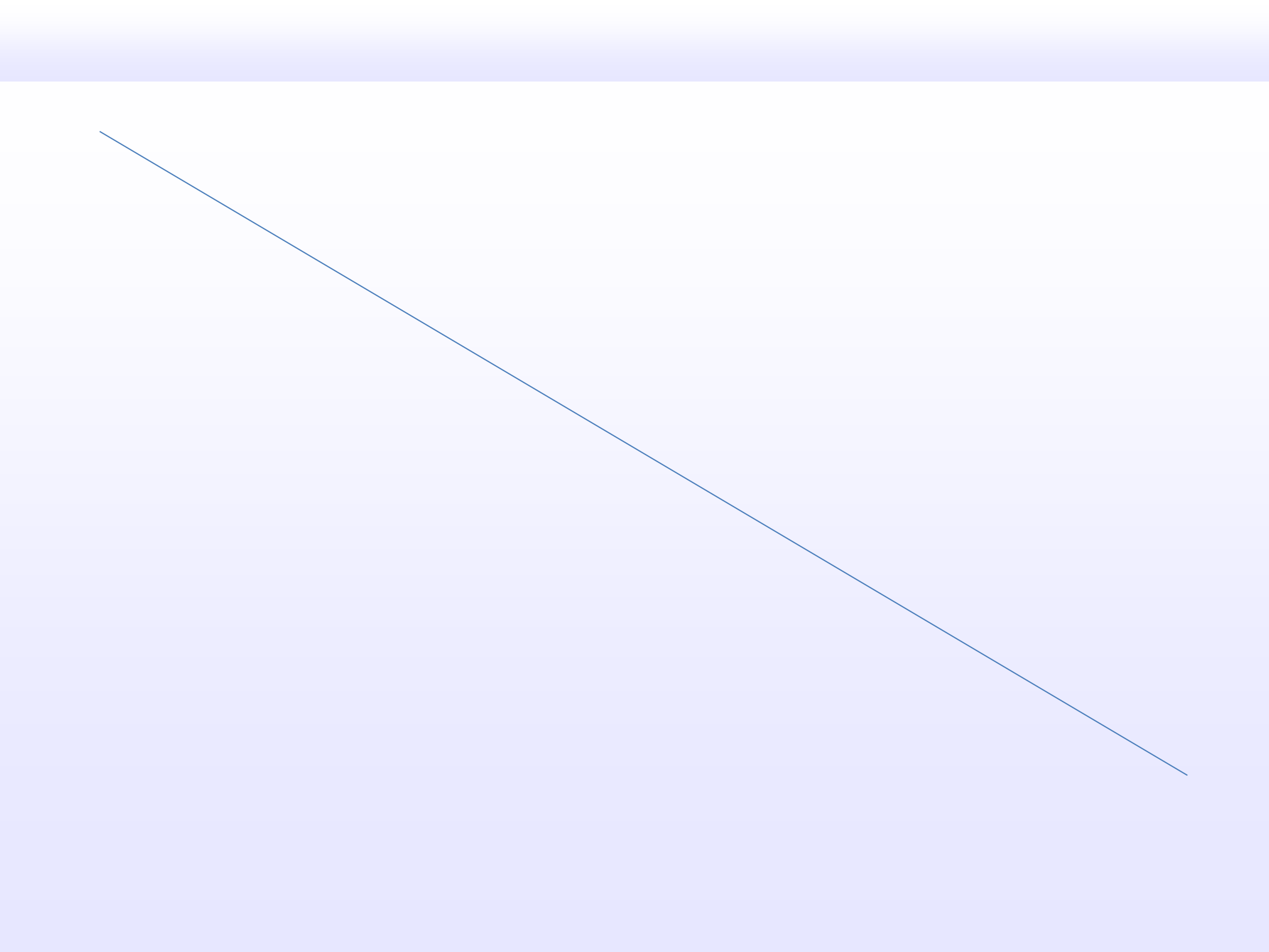


The type variable "t" is belonged with "Foldable" typeclass.

# What is this ?!



"foldl" function has three type variables ("a", "b" and "t").  
Type variable "a" and "b" is any type.  
Type variable "t" is belonged with "Foldable" typeclass.



# Value, Type, Typeclass

Typeclasses

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Types

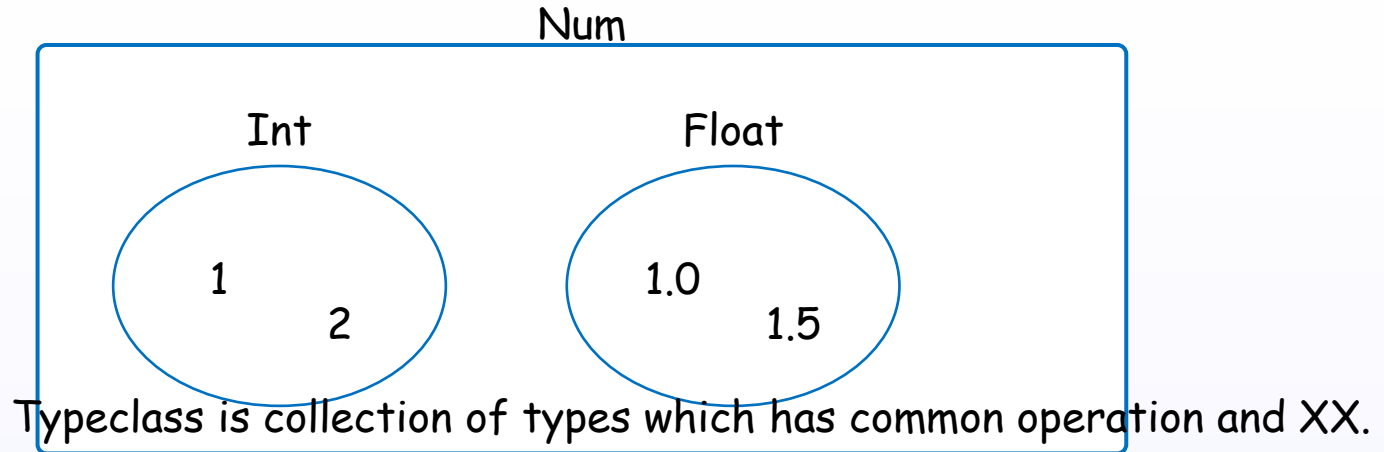
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Values

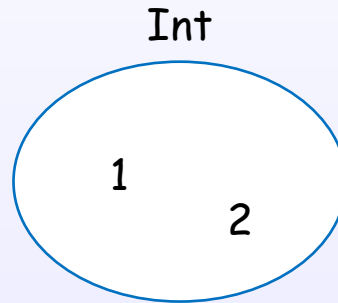


# Value, Type, Typeclass

Typeclasses



Types



Values

1                      2                      A

# Value, Type, Typeclass

Typeclasses

$a$

Maybe  $a$

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Types

$\text{Num} \Rightarrow a$

$\text{Num} \Rightarrow \text{Maybe } a$

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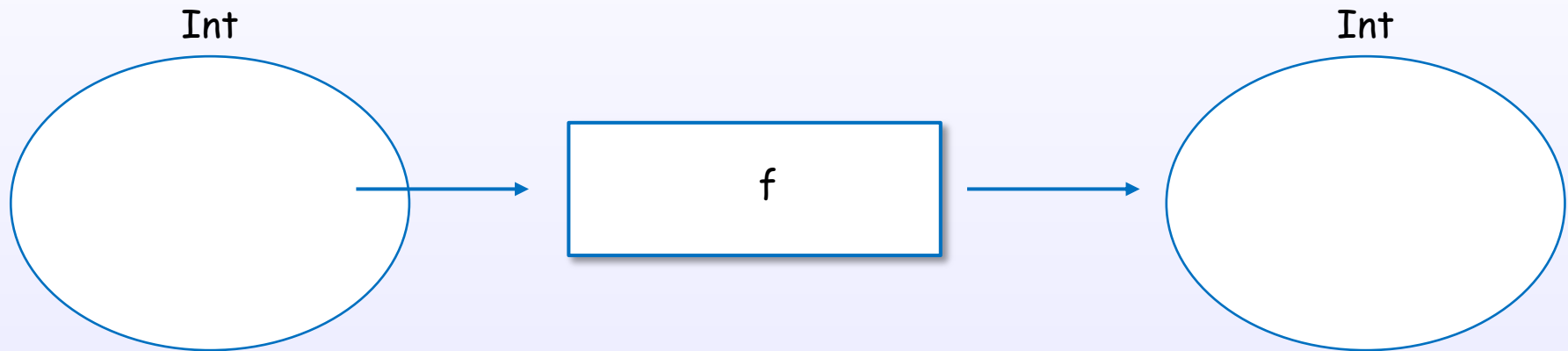
Values

$\text{Int}$

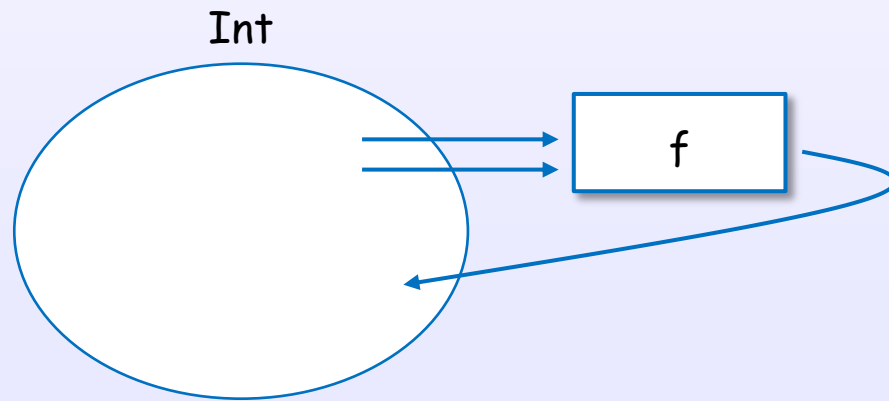
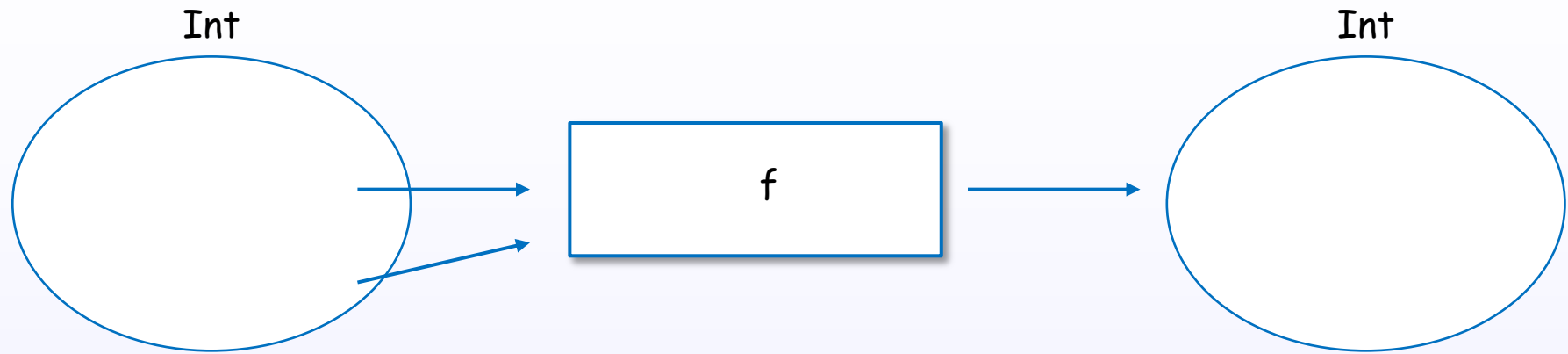
Maybe  $\text{Int}$

# type

$f :: \text{Int} \rightarrow \text{Int}$



# Each view



# type

$f :: a \rightarrow a$

for all



All or concrete?

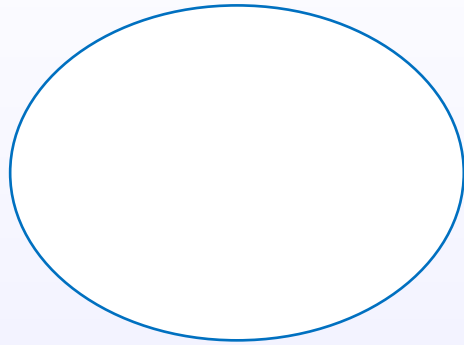
Are there intermediate?

$f :: \text{Int} \rightarrow \text{Int}$

concrete, specialize

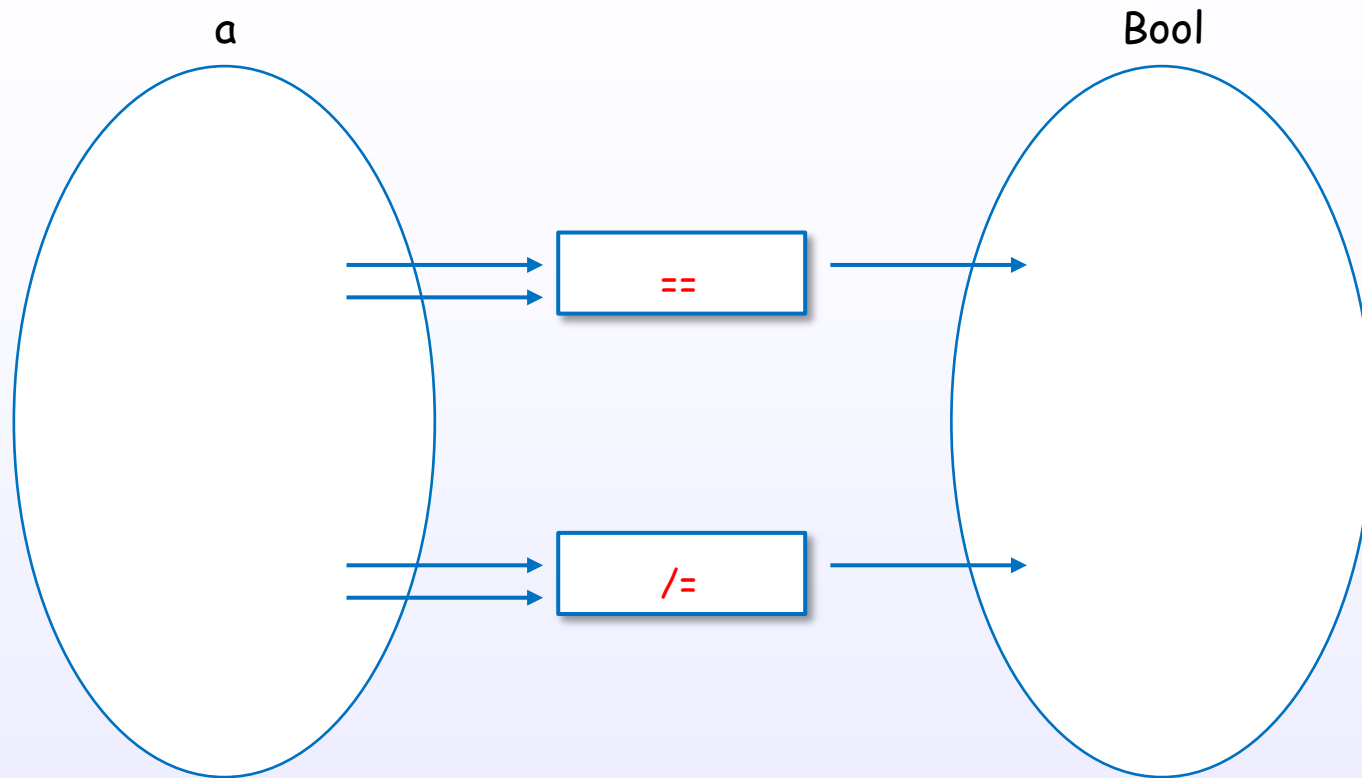
# typeclass

a



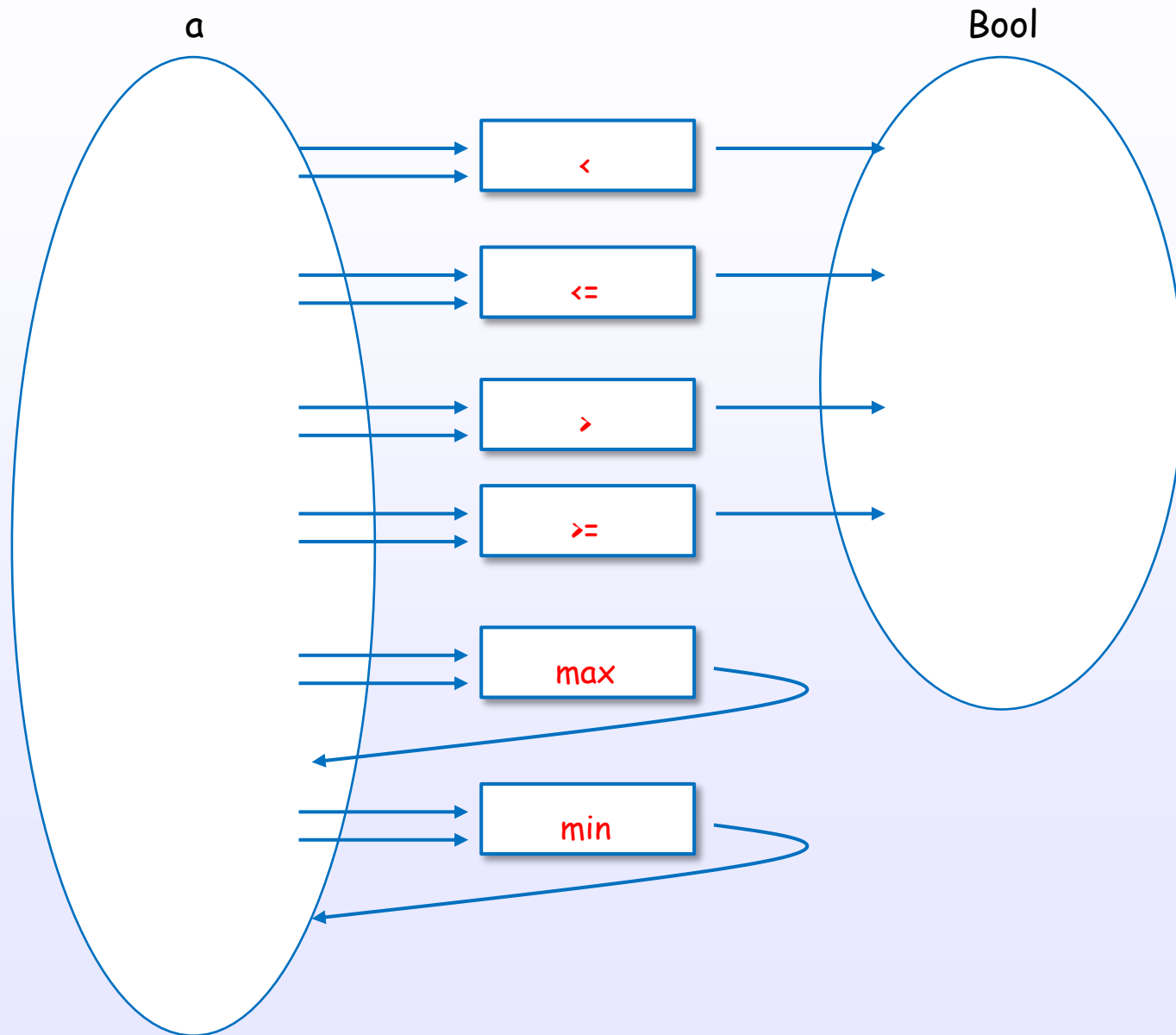
```
class Num  
(+) :: ...
```

# Eq class



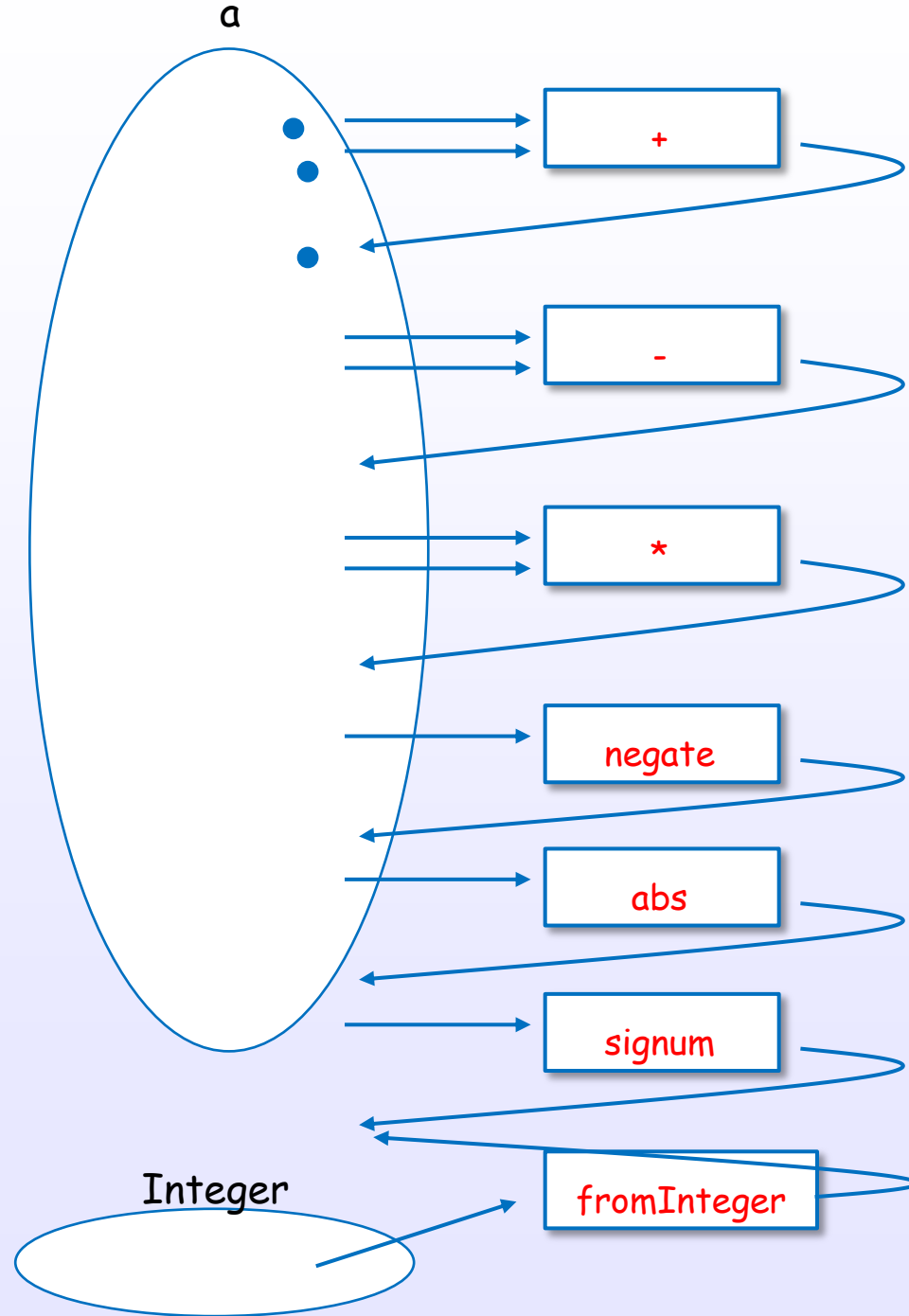
```
class Eq a where  
  (==) :: a -> a -> Bool  
  (/=) :: a -> a -> Bool
```

# Ord class

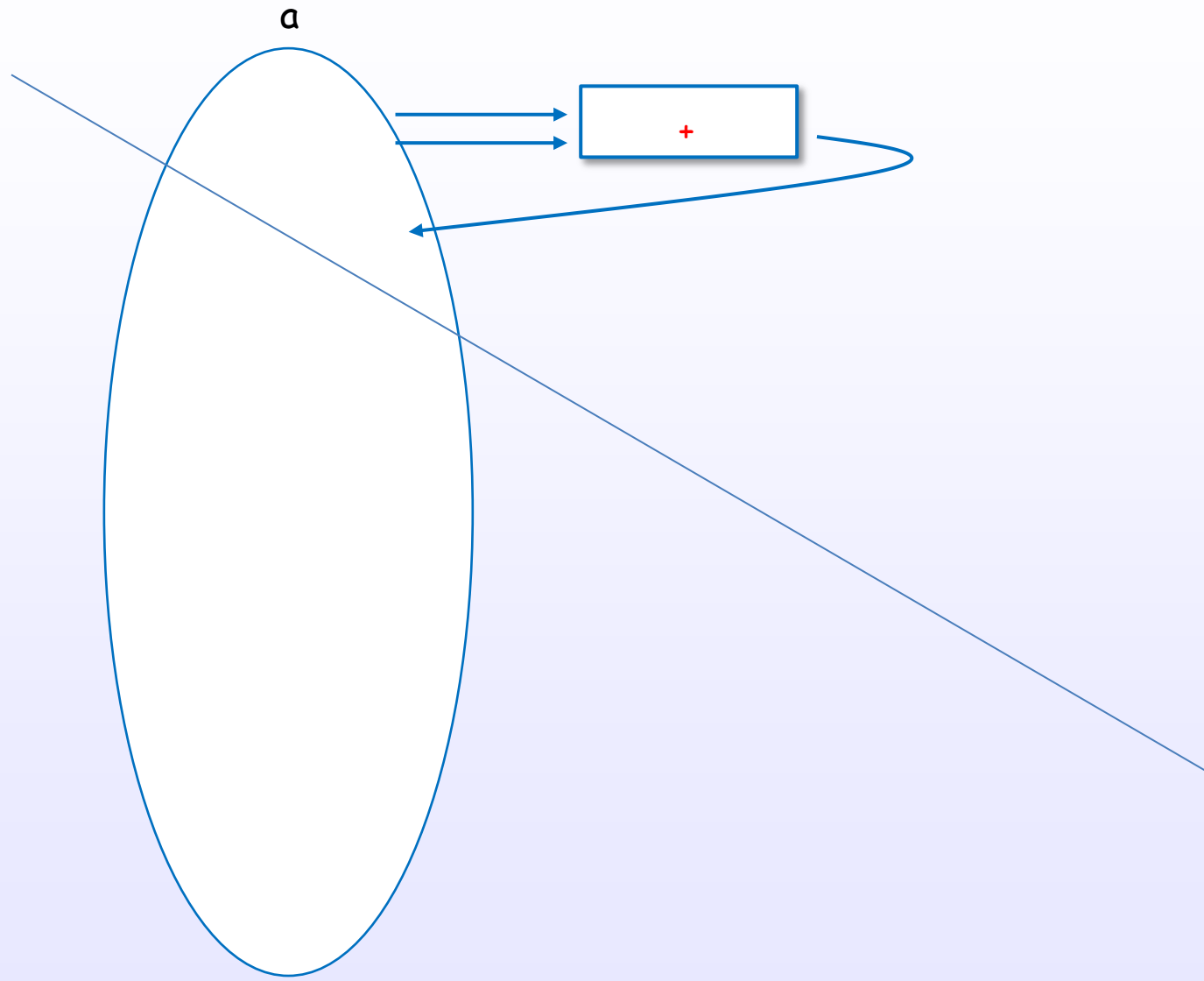




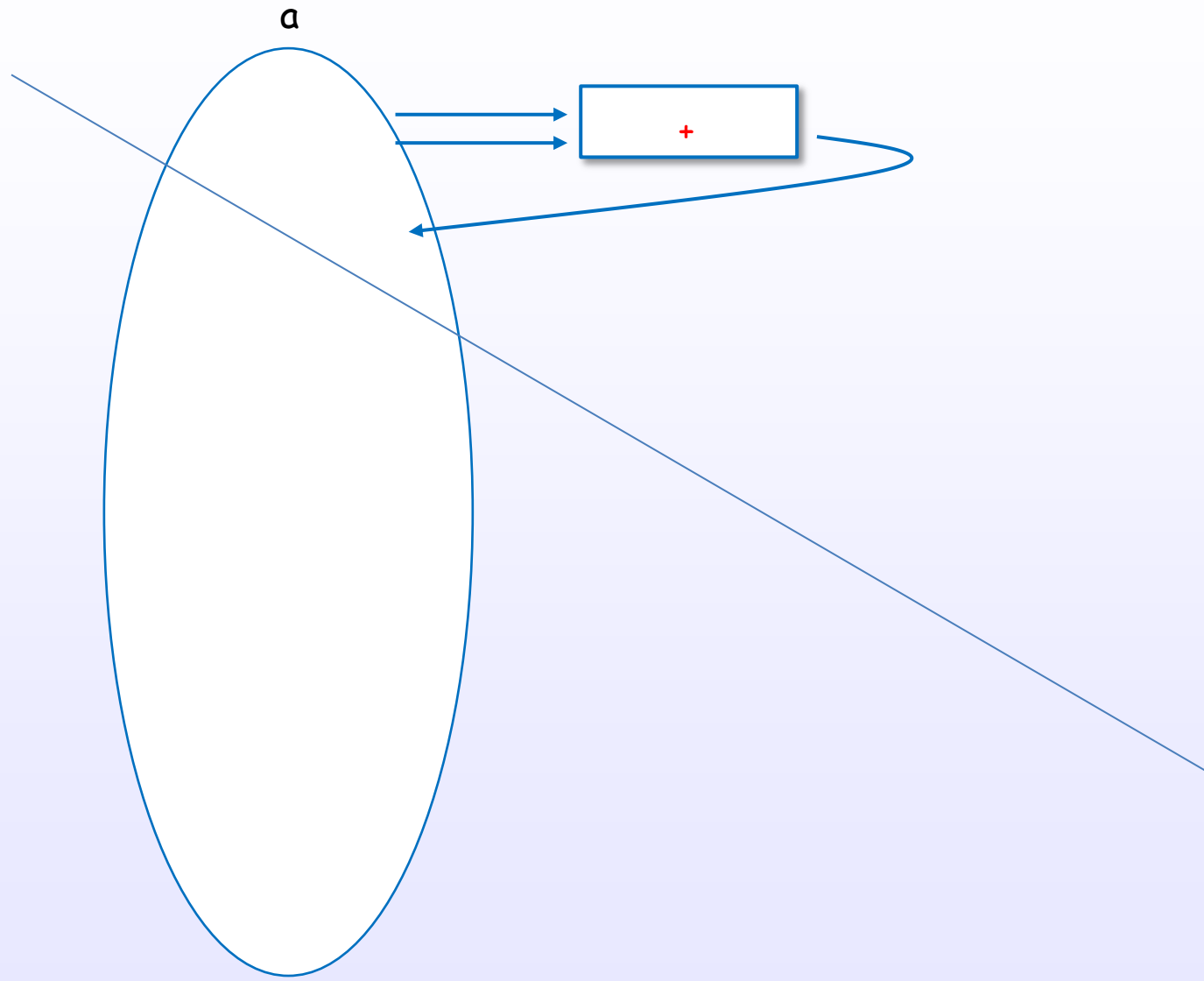
# Num class



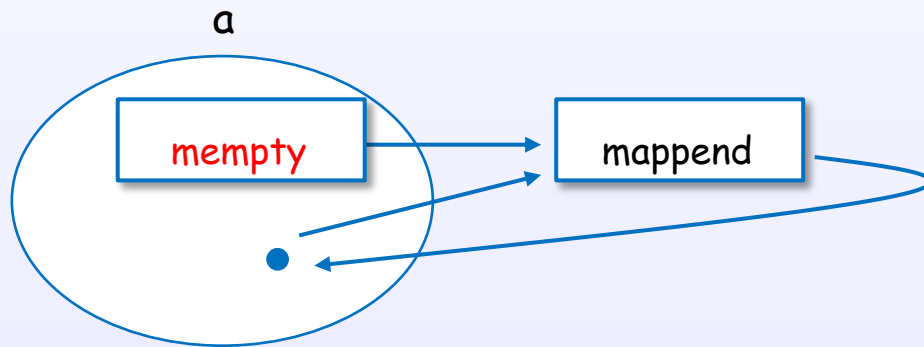
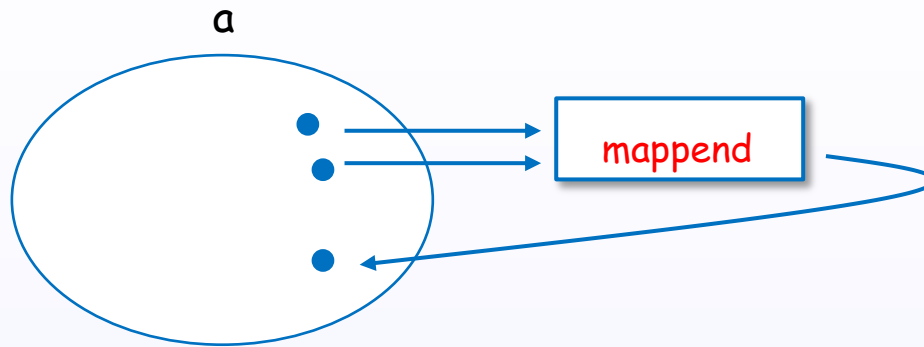
# Foldable class



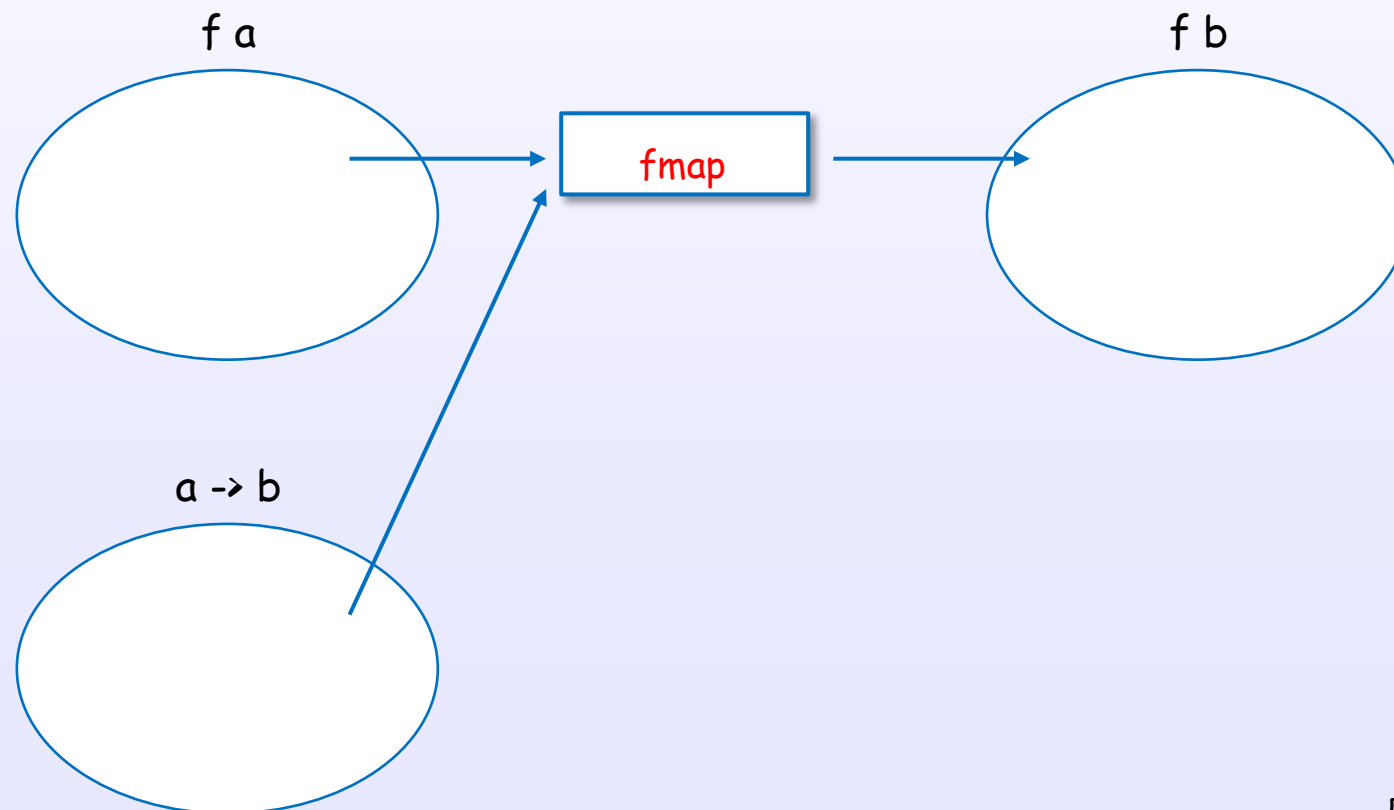
# Traversable class



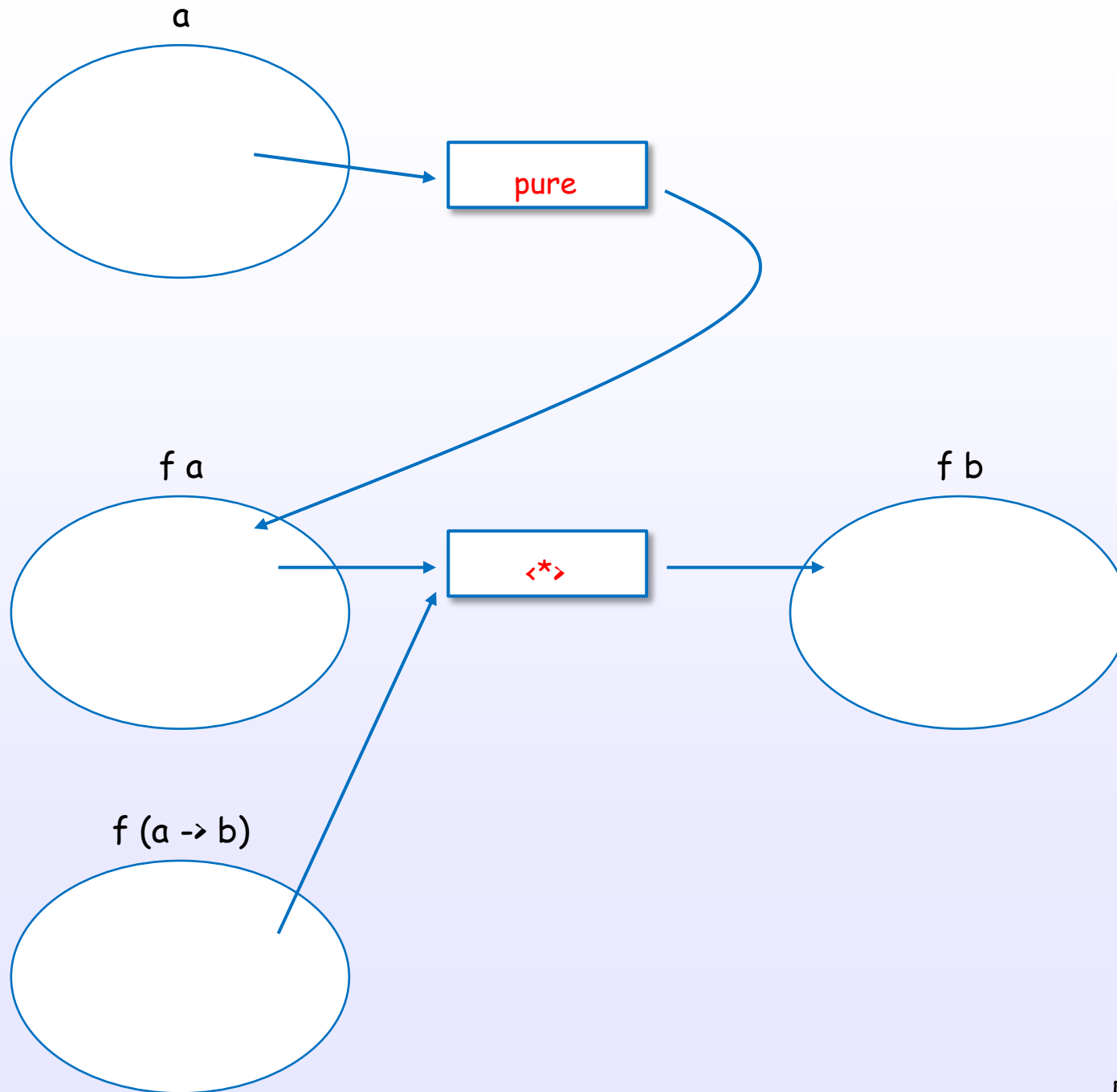
# Monoid class



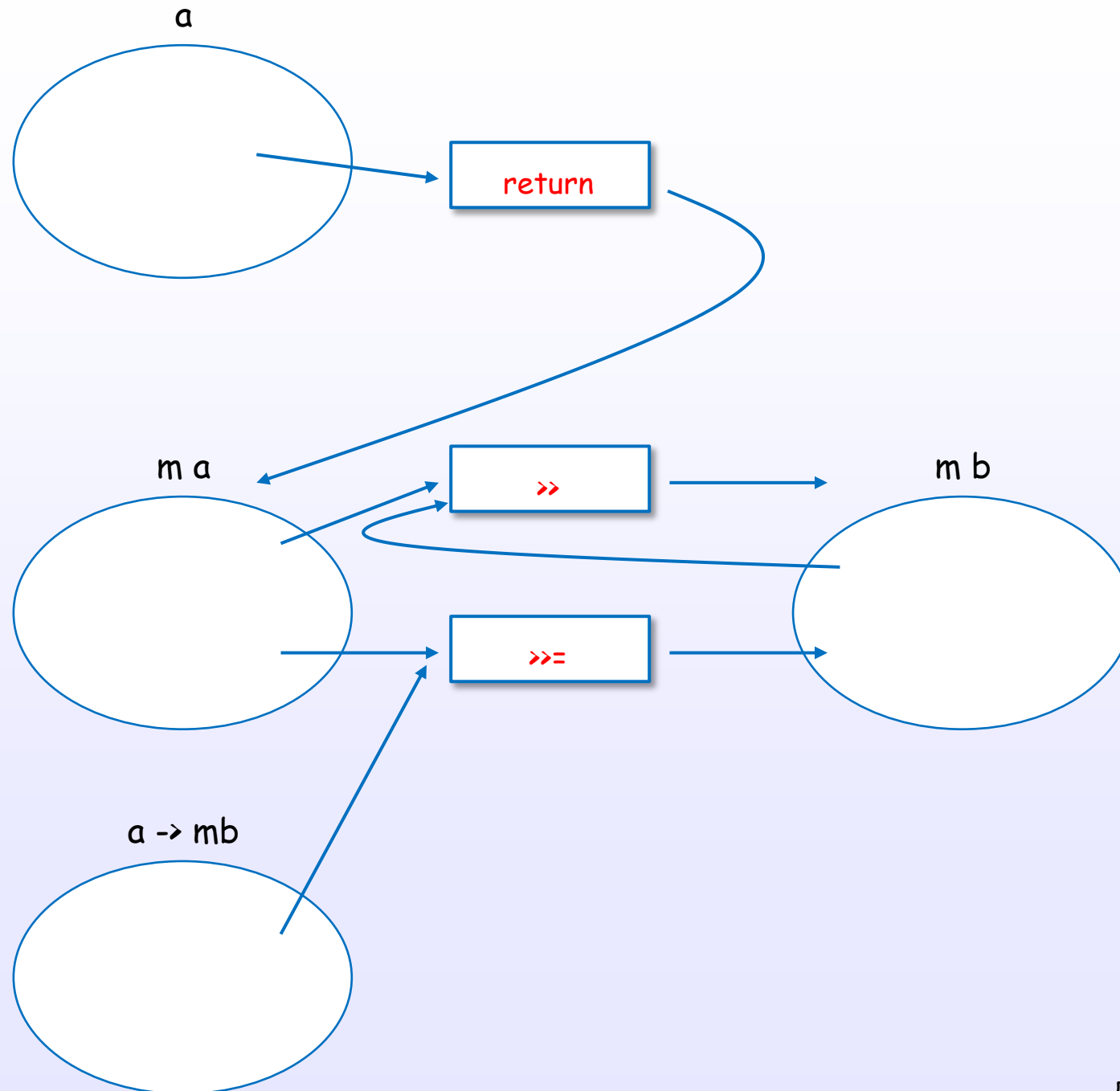
# Functor class



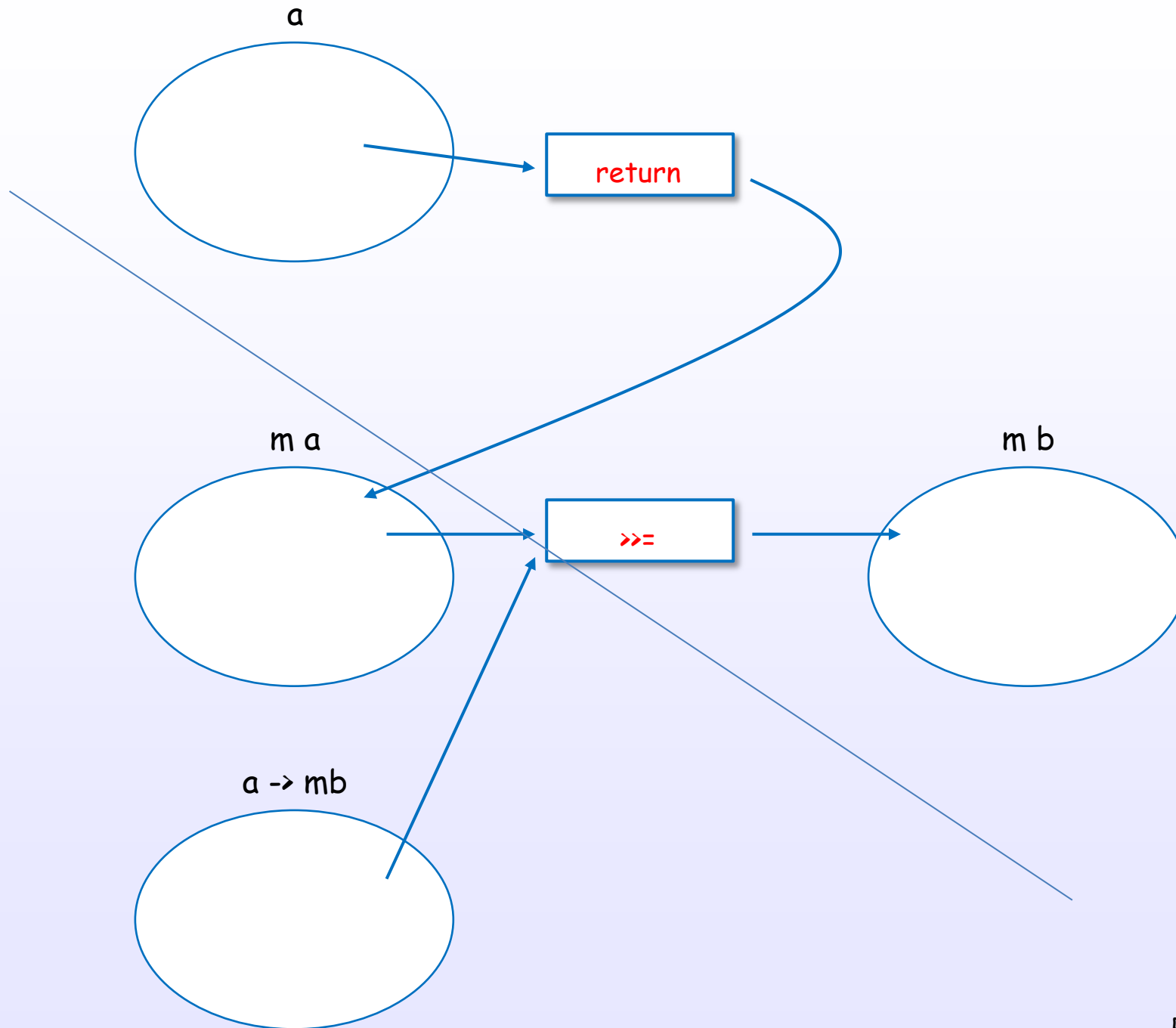
# Applicative class



# Monad class



# Monad class





# References

- [B1] Learn You a Haskell for Great Good!  
<http://learnyouahaskell.com/>
- [B2] Thinking Functionally with Haskell (IFPH 3rd edition)  
<http://www.cs.ox.ac.uk/publications/books/functional/>
- [B3] Programming in Haskell  
<https://www.cs.nott.ac.uk/~gmh/book.html>
- [B4] Types and Programming Languages (TAPL)  
<https://mitpress.mit.edu/books/types-and-programming-languages>

# References

- [D1] CIS 194: Introduction to Haskell  
<http://www.seas.upenn.edu/~cis194/lectures.html>
- [D2] Type Systems  
[http://dev.stephendiehl.com/fun/004\\_type\\_systems.html](http://dev.stephendiehl.com/fun/004_type_systems.html)
- [D3] Typeclassopedia  
<http://www.cs.tufts.edu/comp/150FP/archive/brent-yorgey/tc.pdf>  
<https://wiki.haskell.org/Typeclassopedia>

# References

- [S1] Hoogle  
<https://www.haskell.org/hoogle>

# References

- [H1] Haskell 2010 Language Report  
<https://www.haskell.org/definition/haskell2010.pdf>
- [H2] The Glorious Glasgow Haskell Compilation System (GHC user's guide)  
[https://downloads.haskell.org/~ghc/latest/docs/users\\_guide.pdf](https://downloads.haskell.org/~ghc/latest/docs/users_guide.pdf)