Indira Gandhi Delhi Technical University For Women

(Formerly Indira Gandhi Institute of Technology) Kashmere Gate, Delhi-110006

APPLIED MATHEMATICS-1 (BAS-101) (Differential Calculus) TUTORIAL SHEET -8

- 1. Using Taylor's series , verify that $tan^{-1}(x+y) = x + y \frac{(x+y)^3}{3} + \frac{(x+y)^5}{5}$
- 2. Expand $\frac{1}{1+x-y}$ by Taylor's series up to second degree terms.

(Ans. 1-
$$x + y + x^2 - 2xy + y^2$$
)

3. Compute the approximate value of $(1.04)^{3.01}$

(Ans. 1.12)

4. The temperature T at any point (x,y,z) of space is given by T = 400 xy z^2 , find the highest temperature at the surface of the sphere $x^2+y^2+z^2=1$.

(Ans. Highest temperature 50 attained at
$$\left(\frac{1}{2}, \frac{1}{2}, \frac{\pm 1}{\sqrt{2}}\right)$$
 and $\left(\frac{-1}{2}, \frac{-1}{2}, \frac{\pm 1}{\sqrt{2}}\right)$

5. Find the point upon the plane ax + by + cz = p at which the function

 $f = x^2 + y^2 + z^2$ has minimum value and find this minimum f.

(Ans. f attains minimum at
$$\left(\frac{pa}{a^2+b^2+c^2}, \frac{pb}{a^2+b^2+c^2}, \frac{pc}{a^2+b^2+c^2}\right)$$
 and min $f = \frac{p^2}{a^2+b^2+c^2}$)

6. Find the minimum value of $x^2+y^2+z^2$, given that $xyz = a^3$

(Ans. $3a^2$)

7. A thin closed rectangular box is to have one edge equal to twice the other and a constant volume $72m^3$. Find the least surface area of the box.

(Ans. 108 m²)

8. Expand $e^x \log_e(1+y)$ in powers of x and y up to terms of third degree.

(Ans.
$$e^x \log_e(1+y) = y + xy - \frac{1}{2}y^2 + \frac{1}{2}x^2y - \frac{1}{2}xy^2 + \frac{1}{3}y^3 + ...$$
)