

Intro to Python

- **Comments**: notes of explanation within a program
 - Ignored by Python interpreter
 - Intended for a person reading the program's code
 - Begin with a # character
- **End-line comment**: appears at the end of a line of code
 - Typically explains the purpose of that line

Variables

- **Variable**: name that represents a value stored in the computer memory
 - Used to access and manipulate data stored in memory
 - A variable references the value it represents
- **Assignment statement**: used to create a variable and make it reference data
 - General format is `variable = expression`
 - Example: `age = 29`
 - Assignment operator: the equal sign (=)

Variable Naming Rules

- **Rules for naming variables in Python:**
 - Variable name cannot be a Python key word
 - Variable name cannot contain spaces
 - First character must be a letter or an underscore
 - After first character may use letters, digits, or underscores
 - Variable names are case sensitive
- **Variable name should reflect its use**

Numeric Data Types, Literals, and the `str` Data Type

- **Data types**: categorize value in memory
 - e.g., `int` for integer, `float` for real number, `str` used for storing strings in memory
- **Numeric literal**: number written in a program
 - No decimal point considered `int`, otherwise, considered `float`
- **Some operations behave differently depending on data type**



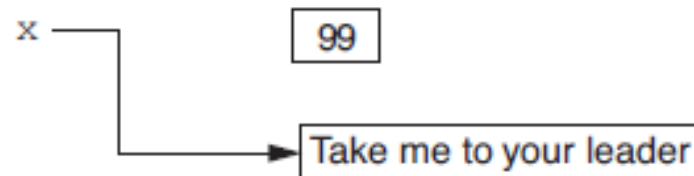
Reassigning a Variable to a Different Type

- A variable in Python can refer to items of any type

Figure 2-7 The variable `x` references an integer



Figure 2-8 The variable `x` references a string



Reading Input from the Keyboard

- Most programs need to read input from the user
- Built-in `input` function reads input from keyboard
 - Returns the data as a string
 - Format: `variable = input(prompt)`
 - `prompt` is typically a string instructing user to enter a value
 - Does not automatically display a space after the prompt

Reading Numbers with the `input` Function

- `input` function always returns a string
- **Built-in functions convert between data types**
 - `int(item)` converts *item* to an `int`
 - `float(item)` converts *item* to a `float`
 - Nested function call: general format:
`function1(function2(argument))`
 - value returned by `function2` is passed to `function1`
 - Type conversion only works if item is valid numeric value, otherwise, throws exception



Performing Calculations

- **Math expression: performs calculation and gives a value**
 - Math operator: tool for performing calculation
 - Operands: values surrounding operator
 - Variables can be used as operands
 - Resulting value typically assigned to variable
- **Two types of division:**
 - `/` operator performs floating point division
 - `//` operator performs integer division
 - Positive results truncated, negative rounded away from zero



Operator Precedence and Grouping with Parentheses

- **Python operator precedence:**
 1. Operations enclosed in parentheses
 - Forces operations to be performed before others
 2. Exponentiation (**)
 3. Multiplication (*), division (/ and //), and remainder (%)
 4. Addition (+) and subtraction (-)
- **Higher precedence performed first**
 - Same precedence operators execute from left to right

Breaking Long Statements into Multiple Lines

- Long statements cannot be viewed on screen without scrolling and cannot be printed without cutting off
- Multiline continuation character (\): Allows to break a statement into multiple lines

```
result = var1 * 2 + var2 * 3 + \  
        var3 * 4 + var4 * 5
```

Breaking Long Statements into Multiple Lines

- **Any part of a statement that is enclosed in parentheses can be broken without the line continuation character.**

```
print("Monday's sales are", monday,  
      "and Tuesday's sales are", tuesday,  
      "and Wednesday's sales are", Wednesday)
```

```
total = (value1 + value2 +  
         value3 + value4 +  
         value5 + value6)
```

More About Data Output

- **print function displays line of output**
 - Newline character at end of printed data
 - Special argument `end='delimiter'` causes `print` to place *delimiter* at end of data instead of newline character
- **print function uses space as item separator**
 - Special argument `sep='delimiter'` causes `print` to use *delimiter* as item separator

More About Data Output (cont'd.)

- **Special characters appearing in string literal**
 - Preceded by backslash (\)
 - Examples: newline (\n), horizontal tab (\t)
 - Treated as commands embedded in string
- **When + operator used on two strings in performs string concatenation**
 - Useful for breaking up a long string literal

Formatting Numbers

- **Can format display of numbers on screen using built-in `format` function**
 - Two arguments:
 - Numeric value to be formatted
 - Format specifier
 - Returns string containing formatted number
 - Format specifier typically includes precision and data type
 - Can be used to indicate scientific notation, comma separators, and the minimum field width used to display the value

Formatting Numbers (cont'd.)

- The `%` symbol can be used in the format string of `format` function to format number as percentage
- To format an integer using `format` function:
 - Use `d` as the type designator
 - Do not specify precision
 - Can still use `format` function to set field width or comma separator

Magic Numbers

- **A magic number is an unexplained numeric value that appears in a program's code.**

Example:

```
amount = balance * 0.069
```

- **What is the value 0.069? An interest rate? A fee percentage? Only the person who wrote the code knows for sure.**

The Problem with Magic Numbers

- It can be difficult to determine the purpose of the number.
- If the magic number is used in multiple places in the program, it can take a lot of effort to change the number in each location, should the need arise.
- You take the risk of making a mistake each time you type the magic number in the program's code.
 - For example, suppose you intend to type 0.069, but you accidentally type .0069. This mistake will cause mathematical errors that can be difficult to find.



Named Constants

- You should use named constants instead of magic numbers.
- A named constant is a name that represents a value that does not change during the program's execution.
- Example:

```
INTEREST_RATE = 0.069
```

- This creates a named constant named `INTEREST_RATE`, assigned the value 0.069. It can be used instead of the magic number:

```
amount = balance * INTEREST_RATE
```

Advantages of Using Named Constants

- **Named constants make code self-explanatory (self-documenting)**
- **Named constants make code easier to maintain (change the value assigned to the constant, and the new value takes effect everywhere the constant is used)**
- **Named constants help prevent typographical errors that are common when using magic numbers**

The `if` Statement

- **Control structure**: logical design that controls order in which set of statements execute
- **Sequence structure**: set of statements that execute in the order they appear
- **Decision structure**: specific action(s) performed only if a condition exists
 - Also known as selection structure

The `if` Statement (cont'd.)

- **Python syntax:**

```
if condition:
```

```
    Statement
```

```
    Statement
```

- **First line known as the `if` clause**

- Includes the keyword `if` followed by condition
 - The condition can be true or false
 - When the `if` statement executes, the condition is tested, and if it is true the block statements are executed. otherwise, block statements are skipped



Boolean Expressions and Relational Operators (cont'd.)

Table 3-2 Boolean expressions using relational operators

Expression	Meaning
$x > y$	Is x greater than y?
$x < y$	Is x less than y?
$x \geq y$	Is x greater than or equal to y?
$x \leq y$	Is x less than or equal to y?
$x == y$	Is x equal to y?
$x != y$	Is x not equal to y?

The `if-else` Statement

- **Dual alternative decision structure: two possible paths of execution**
 - One is taken if the condition is true, and the other if the condition is false
- Syntax:

```
if condition:
    statements
else:
    other statements
```
- `if` clause and `else` clause must be aligned
- Statements must be consistently indented



Nested Decision Structures and the `if-elif-else` Statement

- **A decision structure can be nested inside another decision structure**
 - Commonly needed in programs
 - Example:
 - Determine if someone qualifies for a loan, they must meet two conditions:
 - Must earn at least \$30,000/year
 - Must have been employed for at least two years
 - Check first condition, and if it is true, check second condition

The `if-elif-else` Statement

- **`if-elif-else` statement: special version of a decision structure**

- Makes logic of nested decision structures simpler to write
 - Can include multiple `elif` statements

- Syntax:

```
if condition_1:
    statement(s)
elif condition_2:
    statement(s)
elif condition_3:
    statement(s)
else
    statement(s)
```

Insert as many `elif` clauses as necessary.

Short-Circuit Evaluation

- **Short circuit evaluation**: deciding the value of a compound Boolean expression after evaluating only one sub expression
 - Performed by the `or` and `and` operators
 - For `or` operator: If left operand is true, compound expression is true. Otherwise, evaluate right operand
 - For `and` operator: If left operand is false, compound expression is false. Otherwise, evaluate right operand



Intro to Repetition Structures

- **Often have to write code that performs the same task multiple times**
 - Disadvantages to duplicating code
 - Makes program large
 - Time consuming
 - May need to be corrected in many places
- **Repetition structure: makes computer repeat included code as necessary**
 - Includes condition-controlled loops and count-controlled loops



The `while` Loop: a Condition-Controlled Loop

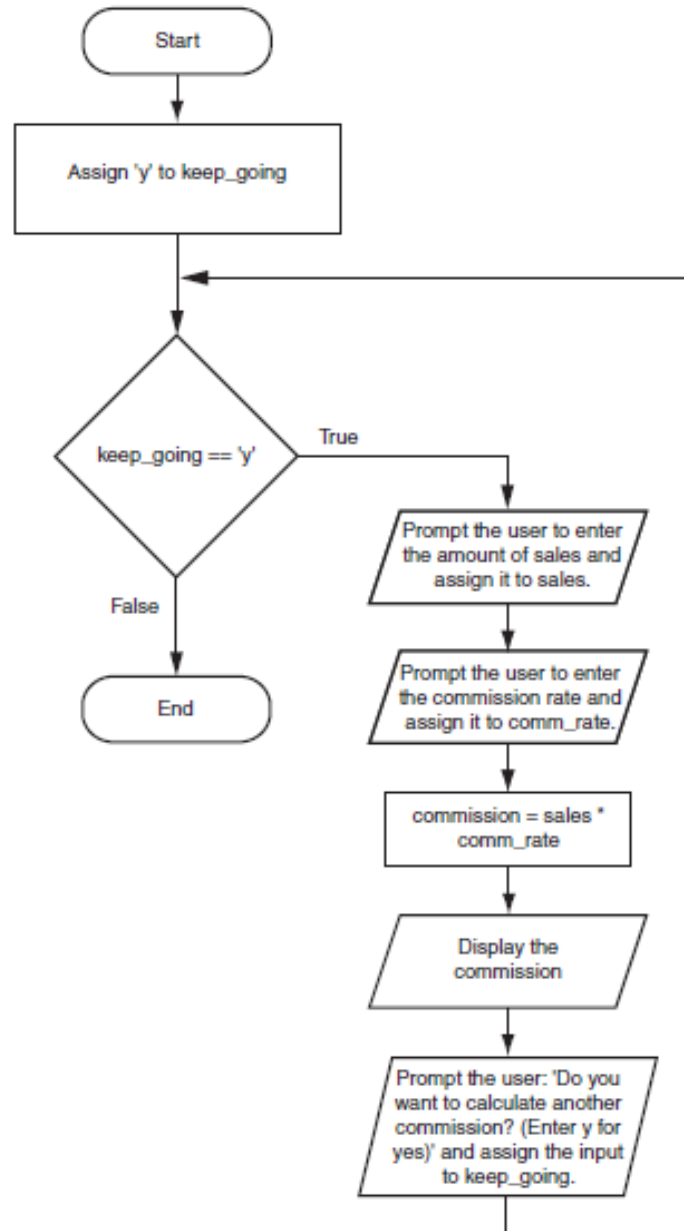
- **while loop**: while condition is true, do something
 - Two parts:
 - Condition tested for true or false value
 - Statements repeated as long as condition is true
 - In flow chart, line goes back to previous part
 - General format:

```
while condition:  
    statements
```

The `while` Loop: a Condition-Controlled Loop (cont'd.)

- In order for a loop to stop executing, something has to happen inside the loop to make the condition false
- Iteration: one execution of the body of a loop
- `while` loop is known as a *pretest* loop
 - Tests condition before performing an iteration
 - Will never execute if condition is false to start with
 - Requires performing some steps prior to the loop

Figure 4-3 Flowchart for Program 4-1



Infinite Loops

- **Loops must contain within themselves a way to terminate**
 - Something inside a `while` loop must eventually make the condition false
- **Infinite loop: loop that does not have a way of stopping**
 - Repeats until program is interrupted
 - Occurs when programmer forgets to include stopping code in the loop

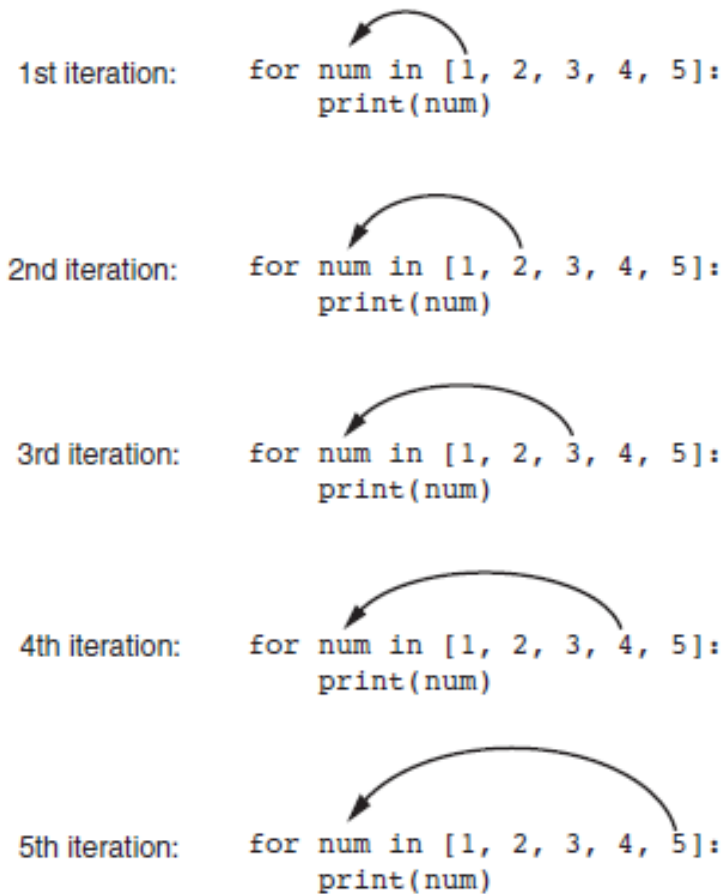
The for Loop: a Count-Controlled Loop

- **Count-Controlled loop**: iterates a specific number of times
 - Use a `for` statement to write count-controlled loop
 - Designed to work with sequence of data items
 - Iterates once for each item in the sequence
 - General format:

```
for variable in [val1, val2, etc]:  
    statements
```
 - **Target variable**: the variable which is the target of the assignment at the beginning of each iteration



Figure 4-4 The for loop



Using the range Function with the for Loop

- **The range function simplifies the process of writing a for loop**
 - `range` returns an iterable object
 - Iterable: contains a sequence of values that can be iterated over
- **range characteristics:**
 - One argument: used as ending limit
 - Two arguments: starting value and ending limit
 - Three arguments: third argument is step value



Using the Target Variable Inside the Loop

- **Purpose of target variable is to reference each item in a sequence as the loop iterates**
- **Target variable can be used in calculations or tasks in the body of the loop**
 - Example: calculate square root of each number in a range

Letting the User Control the Loop Iterations

- Sometimes the programmer does not know exactly how many times the loop will execute
- Can receive range inputs from the user, place them in variables, and call the `range` function in the `for` clause using these variables
 - Be sure to consider the end cases: `range` does not include the ending limit

Generating an Iterable Sequence that Ranges from Highest to Lowest

- The `range` function can be used to generate a sequence with numbers in descending order
 - Make sure starting number is larger than end limit, and step value is negative
 - Example: `range (10, 0, -1)`

The Augmented Assignment Operators (cont'd.)

Table 4-2 Augmented assignment operators

Operator	Example Usage	Equivalent To
<code>+=</code>	<code>x += 5</code>	<code>x = x + 5</code>
<code>-=</code>	<code>y -= 2</code>	<code>y = y - 2</code>
<code>*=</code>	<code>z *= 10</code>	<code>z = z * 10</code>
<code>/=</code>	<code>a /= b</code>	<code>a = a / b</code>
<code>%=</code>	<code>c %= 3</code>	<code>c = c % 3</code>

Sentinels

- **Sentinel: special value that marks the end of a sequence of items**
 - When program reaches a sentinel, it knows that the end of the sequence of items was reached, and the loop terminates
 - Must be distinctive enough so as not to be mistaken for a regular value in the sequence
 - Example: when reading an input file, empty line can be used as a sentinel



Introduction to Functions

- **Function**: group of statements within a program that perform as specific task
 - Usually one task of a large program
 - Functions can be executed in order to perform overall program task
 - Known as *divide and conquer* approach
- **Modularized program**: program wherein each task within the program is in its own function



Figure 5-1 Using functions to divide and conquer a large task

This program is one long, complex sequence of statements.

[illegible]

In this program the task has been divided into smaller tasks, each of which is performed by a separate function.

```
def function1():
    statement
    statement
    statement
```

```
def function2():
    statement
    statement
    statement
```

```
def function3():
    statement
    statement
    statement
```

```
def function4():
    statement
    statement
    statement
```

Benefits of Modularizing a Program with Functions

- **The benefits of using functions include:**
 - Simpler code
 - Code reuse
 - write the code once and call it multiple times
 - Better testing and debugging
 - Can test and debug each function individually
 - Faster development
 - Easier facilitation of teamwork
 - Different team members can write different functions



Void Functions and Value-Returning Functions

- **A void function:**
 - Simply executes the statements it contains and then terminates.
- **A value-returning function:**
 - Executes the statements it contains, and then it returns a value back to the statement that called it.
 - The `input`, `int`, and `float` functions are examples of value-returning functions.

Defining and Calling a Function

- **Functions are given names**
 - Function naming rules:
 - Cannot use key words as a function name
 - Cannot contain spaces
 - First character must be a letter or underscore
 - All other characters must be a letter, number or underscore
 - Uppercase and lowercase characters are distinct

Defining and Calling a Function (cont'd.)

- **Function name should be descriptive of the task carried out by the function**
 - Often includes a verb
- **Function definition: specifies what function does**

```
def function_name() :  
    statement  
    statement
```

Defining and Calling a Function (cont'd.)

- **Function header**: first line of function
 - Includes keyword `def` and function name, followed by parentheses and colon
- **Block**: set of statements that belong together as a group
 - Example: the statements included in a function

Defining and Calling a Function (cont'd.)

- **Call a function to execute it**
 - When a function is called:
 - Interpreter jumps to the function and executes statements in the block
 - Interpreter jumps back to part of program that called the function
 - Known as function return

Defining and Calling a Function (cont'd.)

- **main function**: called when the program starts
 - Calls other functions when they are needed
 - Defines the *mainline logic* of the program

Indentation in Python

- **Each block must be indented**
 - Lines in block must begin with the same number of spaces
 - Use tabs or spaces to indent lines in a block, but not both as this can confuse the Python interpreter
 - IDLE automatically indents the lines in a block
 - Blank lines that appear in a block are ignored

Designing a Program to Use Functions

- **In a flowchart, function call shown as rectangle with vertical bars at each side**
 - Function name written in the symbol
 - Typically draw separate flow chart for each function in the program
 - End terminal symbol usually reads `Return`
- **Top-down design: technique for breaking algorithm into functions**



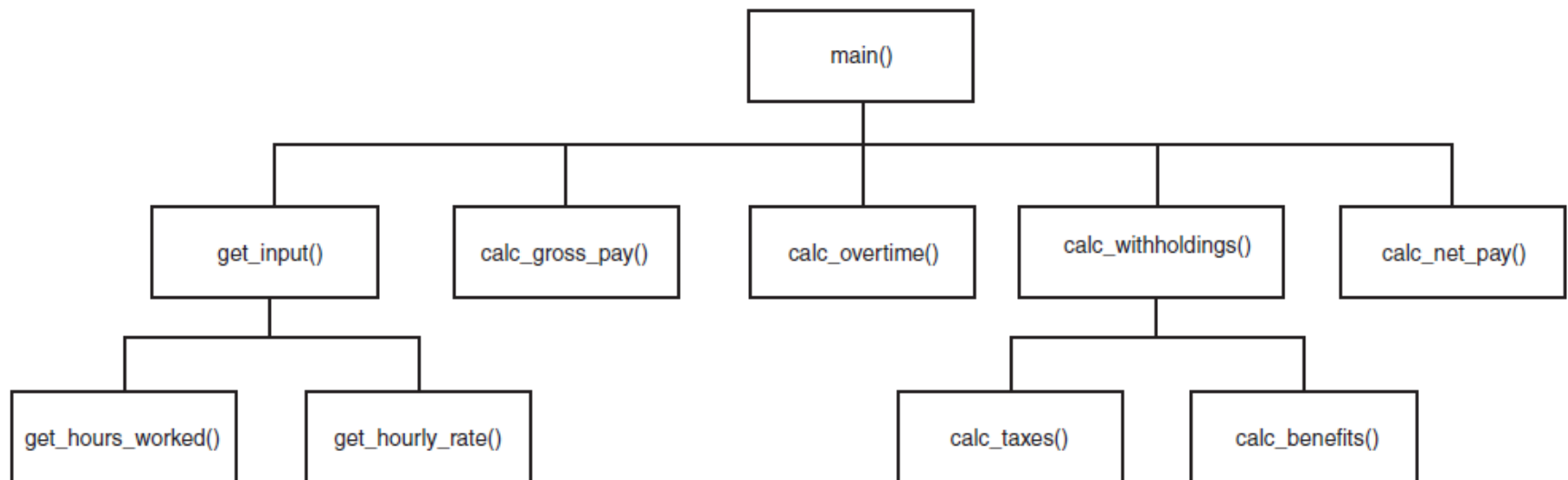
Designing a Program to Use Functions (cont'd.)

- **Hierarchy chart**: depicts relationship between functions
 - AKA structure chart
 - Box for each function in the program, Lines connecting boxes illustrate the functions called by each function
 - Does not show steps taken inside a function
- **Use `input` function to have program wait for user to press enter**



Designing a Program to Use Functions (cont'd.)

Figure 5-10 A hierarchy chart



Local Variables

- **Local variable**: variable that is assigned a value inside a function
 - Belongs to the function in which it was created
 - Only statements inside that function can access it, error will occur if another function tries to access the variable
- **Scope**: the part of a program in which a variable may be accessed
 - For local variable: function in which created



Local Variables (cont'd.)

- **Local variable cannot be accessed by statements inside its function which precede its creation**
- **Different functions may have local variables with the same name**
 - Each function does not see the other function's local variables, so no confusion

Passing Arguments to Functions

- **Argument: piece of data that is sent into a function**
 - Function can use argument in calculations
 - When calling the function, the argument is placed in parentheses following the function name

Passing Arguments to Functions (cont'd.)

Figure 5-13 The `value` variable is passed as an argument

```
def main():  
    value = 5  
    show_double(value)  
  
def show_double(number):  
    result = number * 2  
    print(result)
```

A diagram consisting of a vertical line from the `show_double(value)` call in the `main()` function, followed by a horizontal line to the right, and then a vertical line ending in an arrowhead pointing down to the `show_double(number):` function definition. This illustrates the flow of the argument `value` to the parameter `number`.

Passing Arguments to Functions (cont'd.)

- **Parameter variable**: variable that is assigned the value of an argument when the function is called
 - The parameter and the argument reference the same value
 - General format:
 - `def function_name(parameter) :`
 - **Scope of a parameter**: the function in which the parameter is used

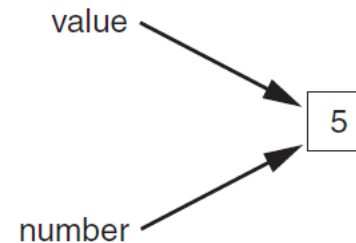


Passing Arguments to Functions (cont'd.)

Figure 5-14 The `value` variable and the `number` parameter reference the same value

```
def main():  
    value = 5  
    show_double(value)
```

```
def show_double(number):  
    result = number * 2  
    print(result)
```



Passing Multiple Arguments

- **Python allows writing a function that accepts multiple arguments**
 - Parameter list replaces single parameter
 - Parameter list items separated by comma
- **Arguments are passed *by position* to corresponding parameters**
 - First parameter receives value of first argument, second parameter receives value of second argument, etc.

Passing Multiple Arguments (cont'd.)

Figure 5-16 Two arguments passed to two parameters

```
def main():  
    print('The sum of 12 and 45 is')  
    show_sum(12, 45)
```

```
def show_sum(num1, num2):  
    result = num1 + num2  
    print(result)
```

num1 → 12

num2 → 45

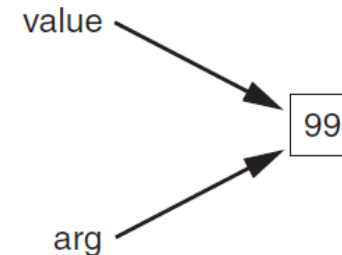
Making Changes to Parameters

- **Changes made to a parameter value within the function do not affect the argument**
 - Known as *pass by value*
 - Provides a way for unidirectional communication between one function and another function
 - Calling function can communicate with called function

Making Changes to Parameters (cont'd.)

Figure 5-17 The value variable is passed to the `change_me` function

```
def main():  
    value = 99  
    print('The value is', value)  
    change_me(value)  
    print('Back in main the value is', value)  
  
def change_me(arg):  
    print('I am changing the value.')  
    arg = 0  
    print('Now the value is', arg)
```



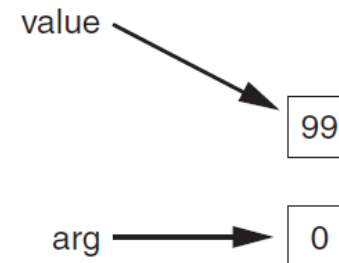
Making Changes to Parameters (cont'd.)

- **Figure 5-18**
 - The `value` variable passed to the `change_me` function cannot be changed by it

Figure 5-18 The `value` variable is passed to the `change_me` function

```
def main():  
    value = 99  
    print('The value is', value)  
    change_me(value)  
    print('Back in main the value is', value)
```

```
def change_me(arg):  
    print('I am changing the value.')  
    arg = 0  
    print('Now the value is', arg)
```



Keyword Arguments

- **Keyword argument: argument that specifies which parameter the value should be passed to**
 - Position when calling function is irrelevant
 - General Format:
 - ```
function_name(parameter=value)
```
- **Possible to mix keyword and positional arguments when calling a function**
  - Positional arguments must appear first





# Global Variables and Global Constants

- **Global variable**: created by assignment statement written outside all the functions
  - Can be accessed by any statement in the program file, including from within a function
  - If a function needs to assign a value to the global variable, the global variable must be redeclared within the function
    - General format: `global variable_name`



# Global Variables and Global Constants (cont'd.)

- **Reasons to avoid using global variables:**
  - Global variables making debugging difficult
    - Many locations in the code could be causing a wrong variable value
  - Functions that use global variables are usually dependent on those variables
    - Makes function hard to transfer to another program
  - Global variables make a program hard to understand



# Global Constants

- **Global constant**: global name that references a value that cannot be changed
  - Permissible to use global constants in a program
  - To simulate global constant in Python, create global variable and do not re-declare it within functions

# Introduction to Value-Returning Functions: Generating Random Numbers

- **void function**: group of statements within a program for performing a specific task
  - Call function when you need to perform the task
- **Value-returning function**: similar to void function, returns a value
  - Value returned to part of program that called the function when function finishes executing

# Standard Library Functions and the `import` Statement

- **Standard library**: library of pre-written functions that comes with Python
  - *Library functions* perform tasks that programmers commonly need
    - Example: `print`, `input`, `range`
    - Viewed by programmers as a “black box”
- **Some library functions built into Python interpreter**
  - To use, just call the function



# Standard Library Functions and the `import` Statement (cont'd.)

- **Modules**: files that stores functions of the standard library
  - Help organize library functions not built into the interpreter
  - Copied to computer when you install Python
- **To call a function stored in a module, need to write an `import` statement**
  - Written at the top of the program
  - Format: `import module_name`



# Standard Library Functions and the `import` Statement (cont'd.)

**Figure 5-19** A library function viewed as a black box

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# Generating Random Numbers

- Random numbers are useful in a lot of programming tasks
- random module: includes library functions for working with random numbers
- Dot notation: notation for calling a function belonging to a module
  - Format: `module_name.function_name()`



# Generating Random Numbers (cont'd.)

- **randint function: generates a random number in the range provided by the arguments**
  - Returns the random number to part of program that called the function
  - Returned integer can be used anywhere that an integer would be used
  - You can experiment with the function in interactive mode

# Generating Random Numbers (cont'd.)

**Figure 5-20** A statement that calls the `random` function

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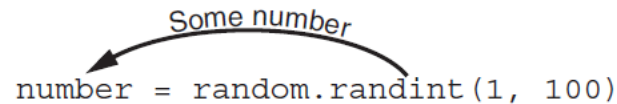
number = random.randint(1, 100)

The diagram shows the code `number = random.randint(1, 100)`. A horizontal bracket underneath the `random.randint(1, 100)` portion is labeled "Function call". Above the parentheses, a horizontal line with two downward-pointing arrows is labeled "Arguments", pointing to the `1` and `100` values.

# Generating Random Numbers (cont'd.)

**Figure 5-21** The `random` function returns a value

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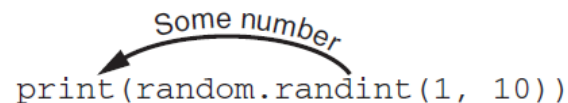


```
number = random.randint(1, 100)
```

A random number in the range of 1 through 100 will be assigned to the `number` variable.

**Figure 5-22** Displaying a random number

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```
print(random.randint(1, 10))
```

A random number in the range of 1 through 10 will be displayed.



# Generating Random Numbers (cont'd.)

- **randrange function:** similar to `range` function, but returns randomly selected integer from the resulting sequence
  - Same arguments as for the `range` function
- **random function:** returns a random float in the range of 0.0 and 1.0
  - Does not receive arguments
- **uniform function:** returns a random float but allows user to specify range



# Random Number Seeds

- Random number created by functions in random module are actually pseudo-random numbers
- **Seed value**: initializes the formula that generates random numbers
  - Need to use different seeds in order to get different series of random numbers
    - By default uses system time for seed
    - Can use `random.seed()` function to specify desired seed value



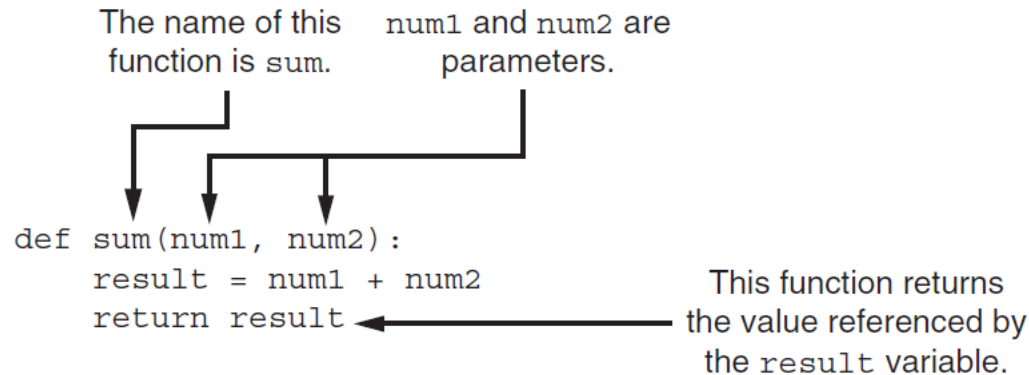
# Writing Your Own Value-Returning Functions

- To write a value-returning function, you write a simple function and add one or more **return statements**
  - Format: `return expression`
    - The value for *expression* will be returned to the part of the program that called the function
  - The expression in the `return` statement can be a complex expression, such as a sum of two variables or the result of another value-returning function



# Writing Your Own Value-Returning Functions (cont'd.)

**Figure 5-23** Parts of the function



# How to Use Value-Returning Functions

- **Value-returning function can be useful in specific situations**
  - Example: have function prompt user for input and return the user's input
  - Simplify mathematical expressions
  - Complex calculations that need to be repeated throughout the program
- **Use the returned value**
  - Assign it to a variable or use as an argument in another function





# Using IPO Charts

- **IPO chart: describes the input, processing, and output of a function**
  - Tool for designing and documenting functions
  - Typically laid out in columns
  - Usually provide brief descriptions of input, processing, and output, without going into details
    - Often includes enough information to be used instead of a flowchart



# Using IPO Charts (cont'd.)

**Figure 5-25** IPO charts for the `getRegularPrice` and `discount` functions

| IPO Chart for the <code>get_regular_price</code> Function |                                                   |                          |
|-----------------------------------------------------------|---------------------------------------------------|--------------------------|
| Input                                                     | Processing                                        | Output                   |
| None                                                      | Prompts the user to enter an item's regular price | The item's regular price |

| IPO Chart for the <code>discount</code> Function |                                                                                                                        |                     |
|--------------------------------------------------|------------------------------------------------------------------------------------------------------------------------|---------------------|
| Input                                            | Processing                                                                                                             | Output              |
| An item's regular price                          | Calculates an item's discount by multiplying the regular price by the global constant <code>DISCOUNT_PERCENTAGE</code> | The item's discount |



# Returning Strings

- You can write functions that return strings
- For example:

```
def get_name():
 # Get the user's name.
 name = input('Enter your name: ')
 # Return the name.
 return name
```



# Returning Boolean Values

- **Boolean function: returns either True or False**
  - Use to test a condition such as for decision and repetition structures
    - Common calculations, such as whether a number is even, can be easily repeated by calling a function
  - Use to simplify complex input validation code

# Returning Multiple Values

- In Python, a function can return multiple values
  - Specified after the `return` statement separated by commas
    - Format: `return expression1, expression2, etc.`
  - When you call such a function in an assignment statement, you need a separate variable on the left side of the `=` operator to receive each returned value



# The math Module

- **math module**: part of standard library that contains functions that are useful for performing mathematical calculations
  - Typically accept one or more values as arguments, perform mathematical operation, and return the result
  - Use of module requires an `import math` statement

# The math Module (cont'd.)

**Table 5-2** Many of the functions in the `math` module

| <code>math</code> Module Function | Description                                                                                          |
|-----------------------------------|------------------------------------------------------------------------------------------------------|
| <code>acos(x)</code>              | Returns the arc cosine of <code>x</code> , in radians.                                               |
| <code>asin(x)</code>              | Returns the arc sine of <code>x</code> , in radians.                                                 |
| <code>atan(x)</code>              | Returns the arc tangent of <code>x</code> , in radians.                                              |
| <code>ceil(x)</code>              | Returns the smallest integer that is greater than or equal to <code>x</code> .                       |
| <code>cos(x)</code>               | Returns the cosine of <code>x</code> in radians.                                                     |
| <code>degrees(x)</code>           | Assuming <code>x</code> is an angle in radians, the function returns the angle converted to degrees. |
| <code>exp(x)</code>               | Returns $e^x$                                                                                        |
| <code>floor(x)</code>             | Returns the largest integer that is less than or equal to <code>x</code> .                           |
| <code>hypot(x, y)</code>          | Returns the length of a hypotenuse that extends from (0, 0) to ( <code>x</code> , <code>y</code> ).  |
| <code>log(x)</code>               | Returns the natural logarithm of <code>x</code> .                                                    |
| <code>log10(x)</code>             | Returns the base-10 logarithm of <code>x</code> .                                                    |
| <code>radians(x)</code>           | Assuming <code>x</code> is an angle in degrees, the function returns the angle converted to radians. |
| <code>sin(x)</code>               | Returns the sine of <code>x</code> in radians.                                                       |
| <code>sqrt(x)</code>              | Returns the square root of <code>x</code> .                                                          |
| <code>tan(x)</code>               | Returns the tangent of <code>x</code> in radians.                                                    |



# The math Module (cont'd.)

- The `math` module defines variables `pi` and `e`, which are assigned the mathematical values for *pi* and *e*
  - Can be used in equations that require these values, to get more accurate results
- Variables must also be called using the dot notation
  - Example:

```
circle_area = math.pi * radius**2
```



# Storing Functions in Modules

- In large, complex programs, it is important to keep code organized
- **Modularization**: grouping related functions in modules
  - Makes program easier to understand, test, and maintain
  - Make it easier to reuse code for multiple different programs
    - Import the module containing the required function to each program that needs it



# Storing Functions in Modules (cont'd.)

- **Module is a file that contains Python code**
  - Contains function definition but does not contain calls to the functions
    - Importing programs will call the functions
- **Rules for module names:**
  - File name should end in `.py`
  - Cannot be the same as a Python keyword
- **Import module using `import` statement**



# Menu Driven Programs

- **Menu-driven program**: displays a list of operations on the screen, allowing user to select the desired operation
  - List of operations displayed on the screen is called a *menu*
- **Program uses a decision structure to determine the selected menu option and required operation**
  - Typically repeats until the user quits



# Turtle Graphics: Modularizing Code with Functions

- **Commonly needed turtle graphics operations can be stored in functions and then called whenever needed.**
- **For example, the following function draws a square. The parameters specify the location, width, and color.**

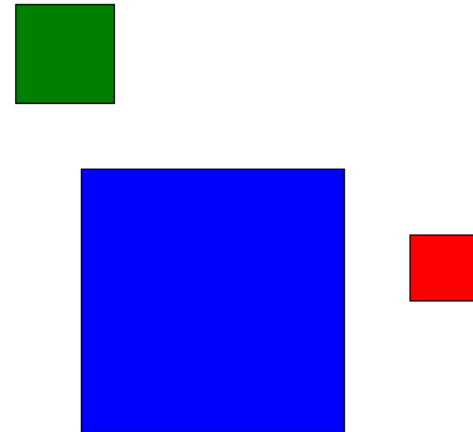
```
def square(x, y, width, color):
 turtle.penup() # Raise the pen
 turtle.goto(x, y) # Move to (X,Y)
 turtle.fillcolor(color) # Set the fill color
 turtle.pendown() # Lower the pen
 turtle.begin_fill() # Start filling
 for count in range(4): # Draw a square
 turtle.forward(width)
 turtle.left(90)
 turtle.end_fill() # End filling
```



# Turtle Graphics: Modularizing Code with Functions

- The following code calls the previously shown square function to draw three squares:

```
square(100, 0, 50, 'red')
square(-150, -100, 200, 'blue')
square(-200, 150, 75, 'green')
```



# Turtle Graphics: Modularizing Code with Functions

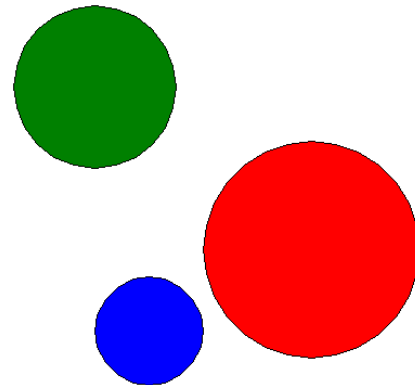
- The following function draws a circle. The parameters specify the location, radius, and color.

```
def circle(x, y, radius, color):
 turtle.penup() # Raise the pen
 turtle.goto(x, y - radius) # Position the turtle
 turtle.fillcolor(color) # Set the fill color
 turtle.pendown() # Lower the pen
 turtle.begin_fill() # Start filling
 turtle.circle(radius) # Draw a circle
 turtle.end_fill() # End filling
```

# Turtle Graphics: Modularizing Code with Functions

- The following code calls the previously shown `circle` function to draw three circles:

```
circle(0, 0, 100, 'red')
circle(-150, -75, 50, 'blue')
circle(-200, 150, 75, 'green')
```



# Turtle Graphics: Modularizing Code with Functions

- The following function draws a line. The parameters specify the starting and ending locations, and color.

```
def line(startX, startY, endX, endY, color):
 turtle.penup() # Raise the pen
 turtle.goto(startX, startY) # Move to the starting point
 turtle.pendown() # Lower the pen
 turtle.pencolor(color) # Set the pen color
 turtle.goto(endX, endY) # Draw a square
```



# Turtle Graphics: Modularizing Code with Functions

- The following code calls the previously shown `line` function to draw a triangle:

```
TOP_X = 0
TOP_Y = 100
BASE_LEFT_X = -100
BASE_LEFT_Y = -100
BASE_RIGHT_X = 100
BASE_RIGHT_Y = -100
line(TOP_X, TOP_Y, BASE_LEFT_X, BASE_LEFT_Y, 'red')
line(TOP_X, TOP_Y, BASE_RIGHT_X, BASE_RIGHT_Y, 'blue')
line(BASE_LEFT_X, BASE_LEFT_Y, BASE_RIGHT_X, BASE_RIGHT_Y, 'green')
```

