

MRA: Multi Resolution Analysis

Denoising- Pyramids & Subbands

Dr. Tushar Sandhan

Introduction

- Image analysis at different resolutions



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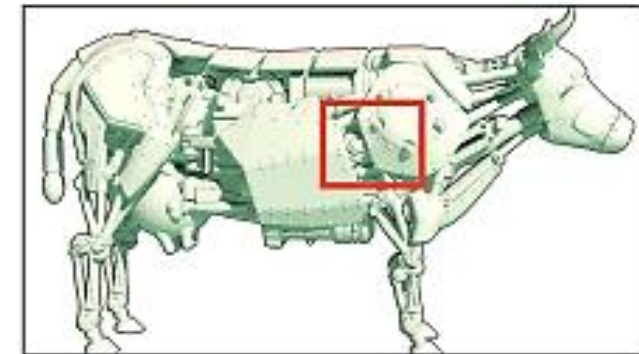


Image analysis

- Image statistics
 - change locally
 - info. is distributed at various scales
 - noise is present throughout the image

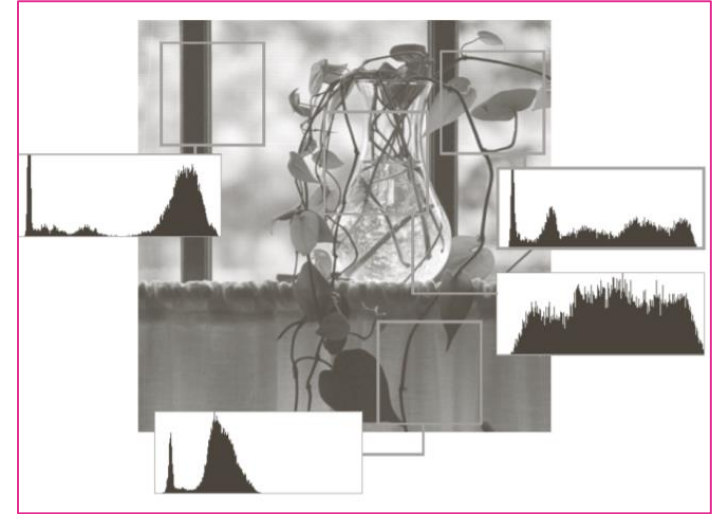


Image analysis

- Image statistics
 - change locally
 - info. is distributed at various scales
 - noise is present throughout the image
- Larger objects can be analyzed @ coarse/low resolution
- Smaller ones can be analyzed @ fine/high resolution

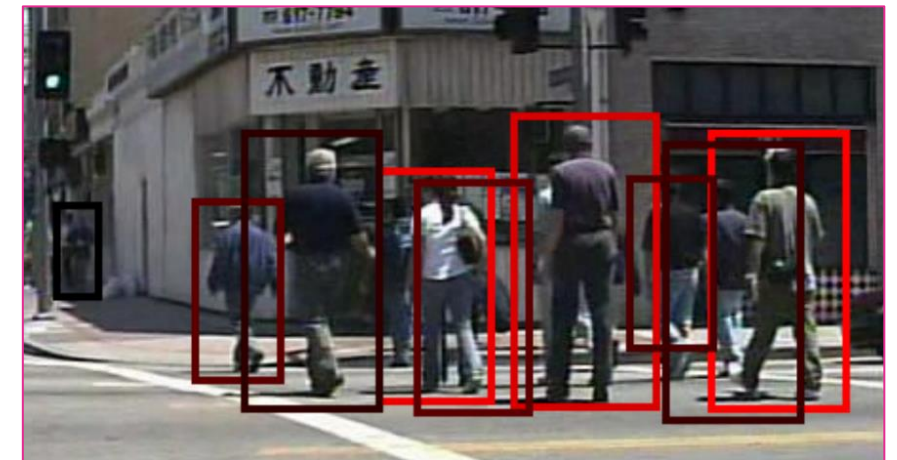
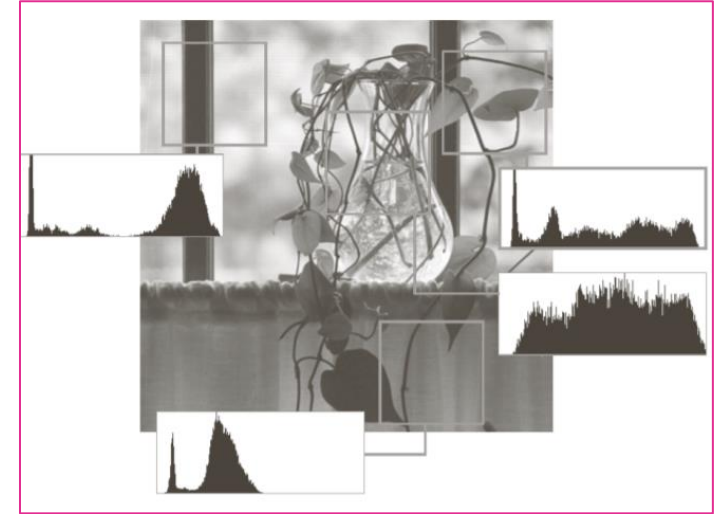


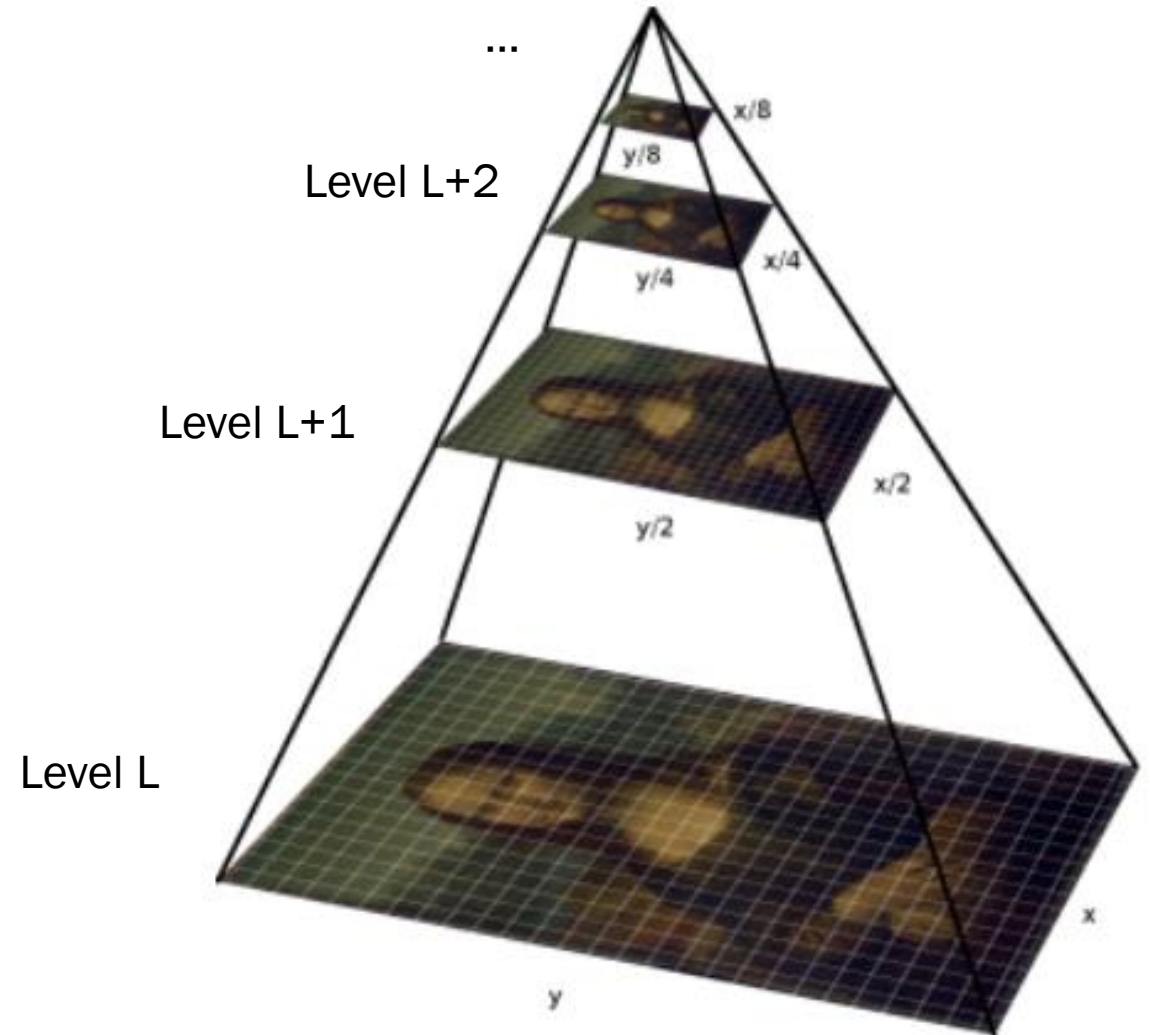
image: C. Nikou

MRA: Image Pyramid

- Image pyramid
 - a collection of images
 - gradually decreasing resolution
 - arranged in the shape of pyramid
 - researcher use Level numbers interchangeably
 - e.g. Level-0 might be bottom or top!

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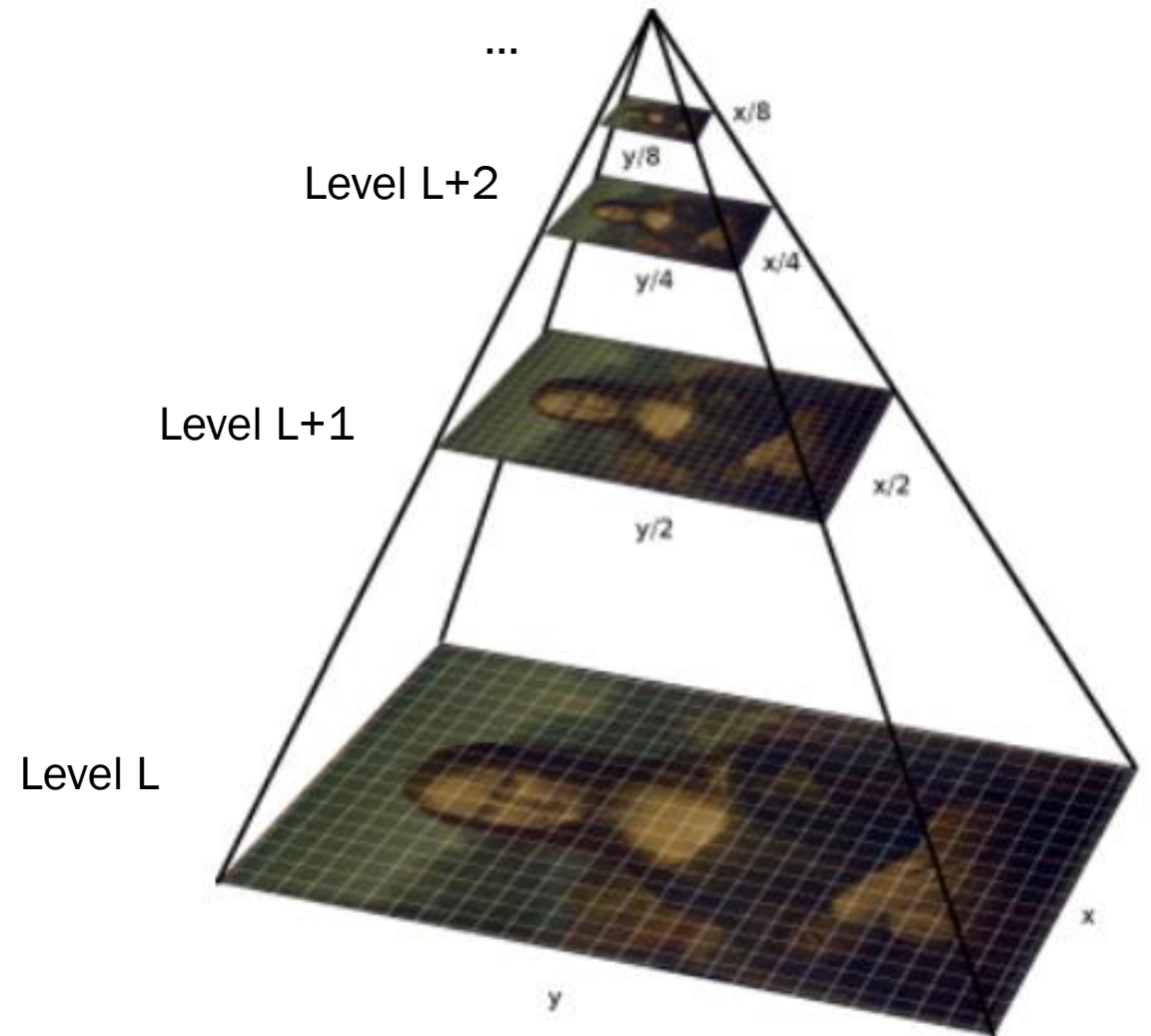
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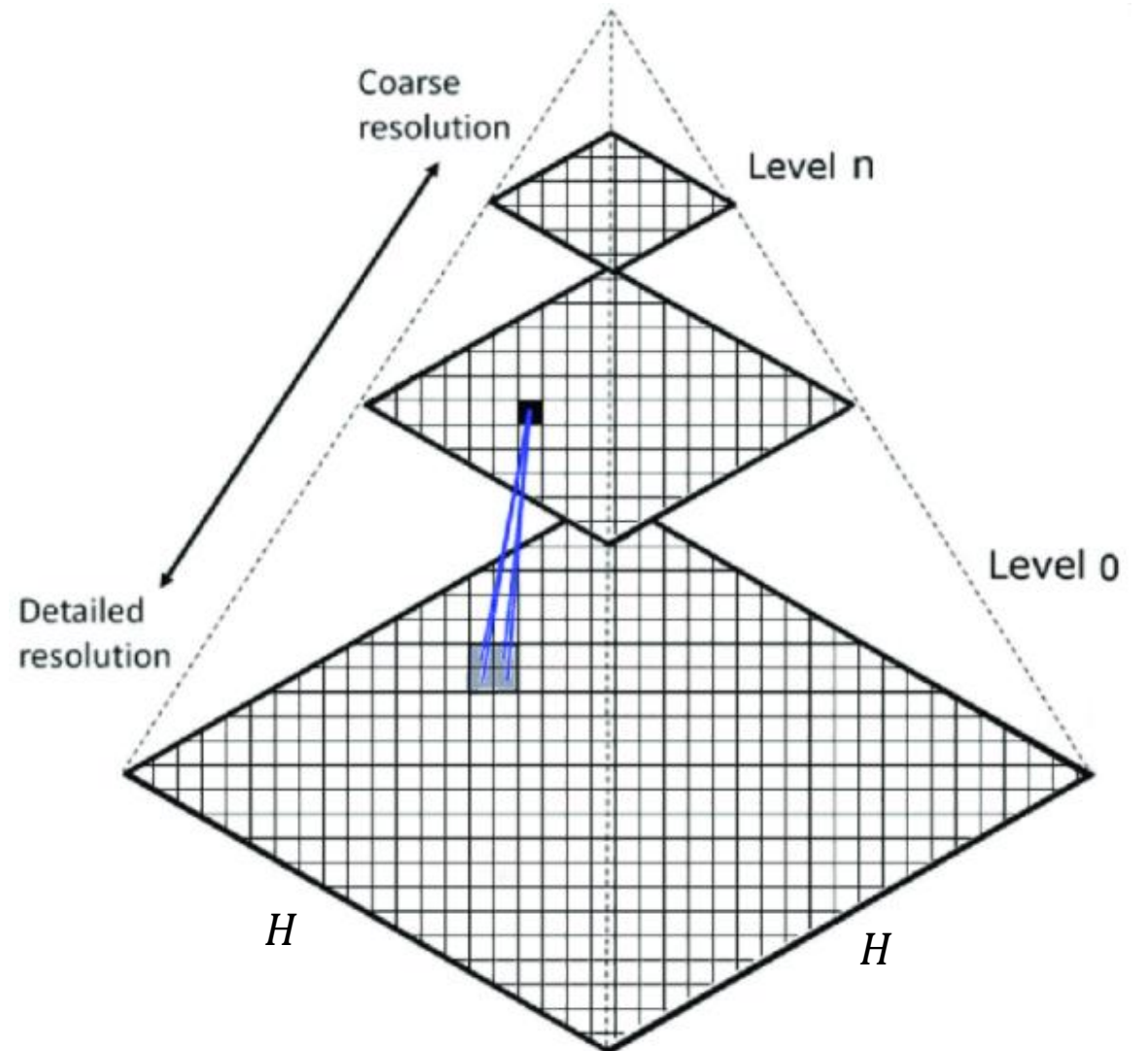
e.g. Level-0 might be bottom or top!

- Top level?

- it is not necessary to go till summit of the pyramid
- pyramid can be truncated at any level $L+k$
- requirement of speed & accuracy determines k

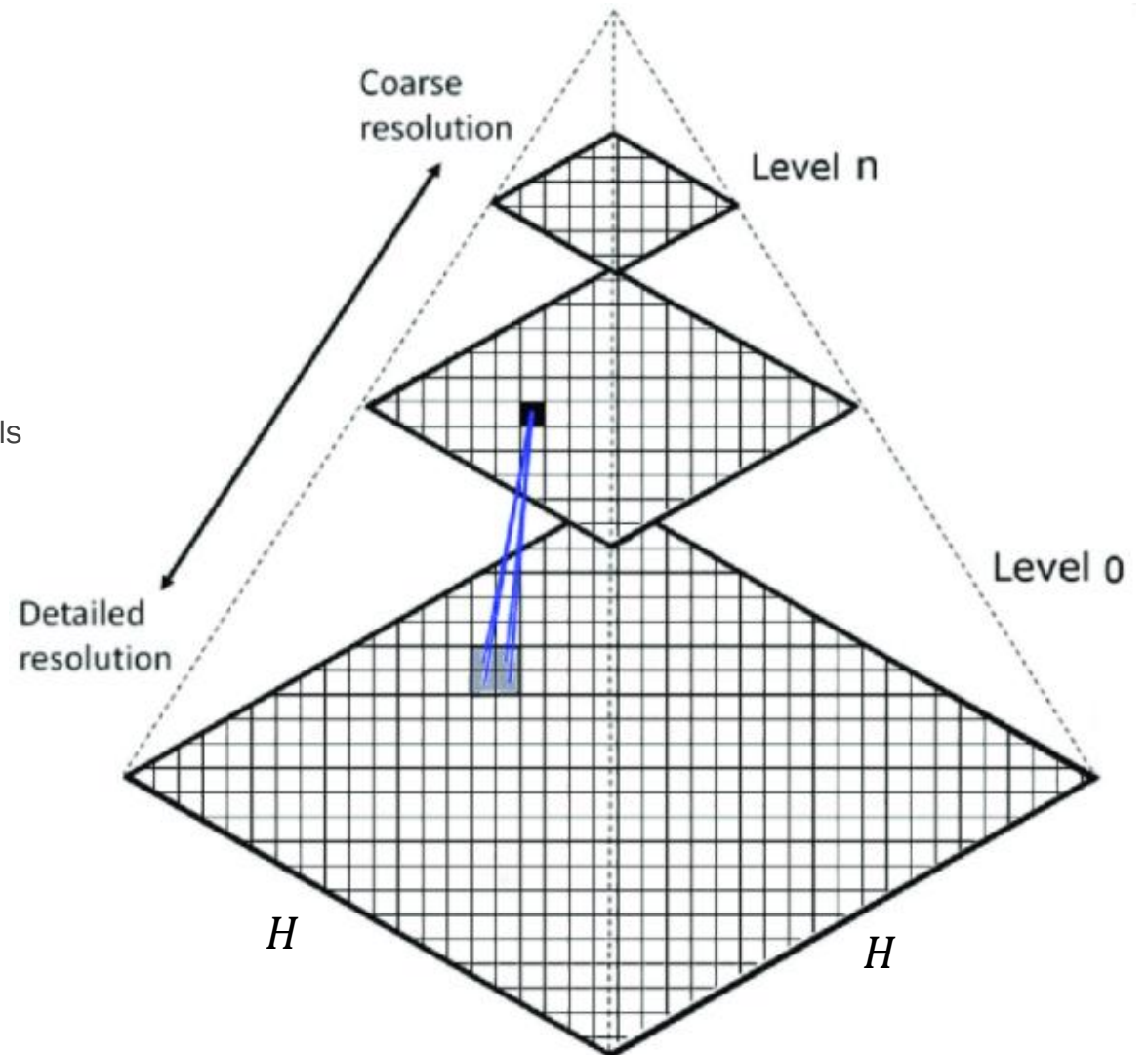


Pyramid



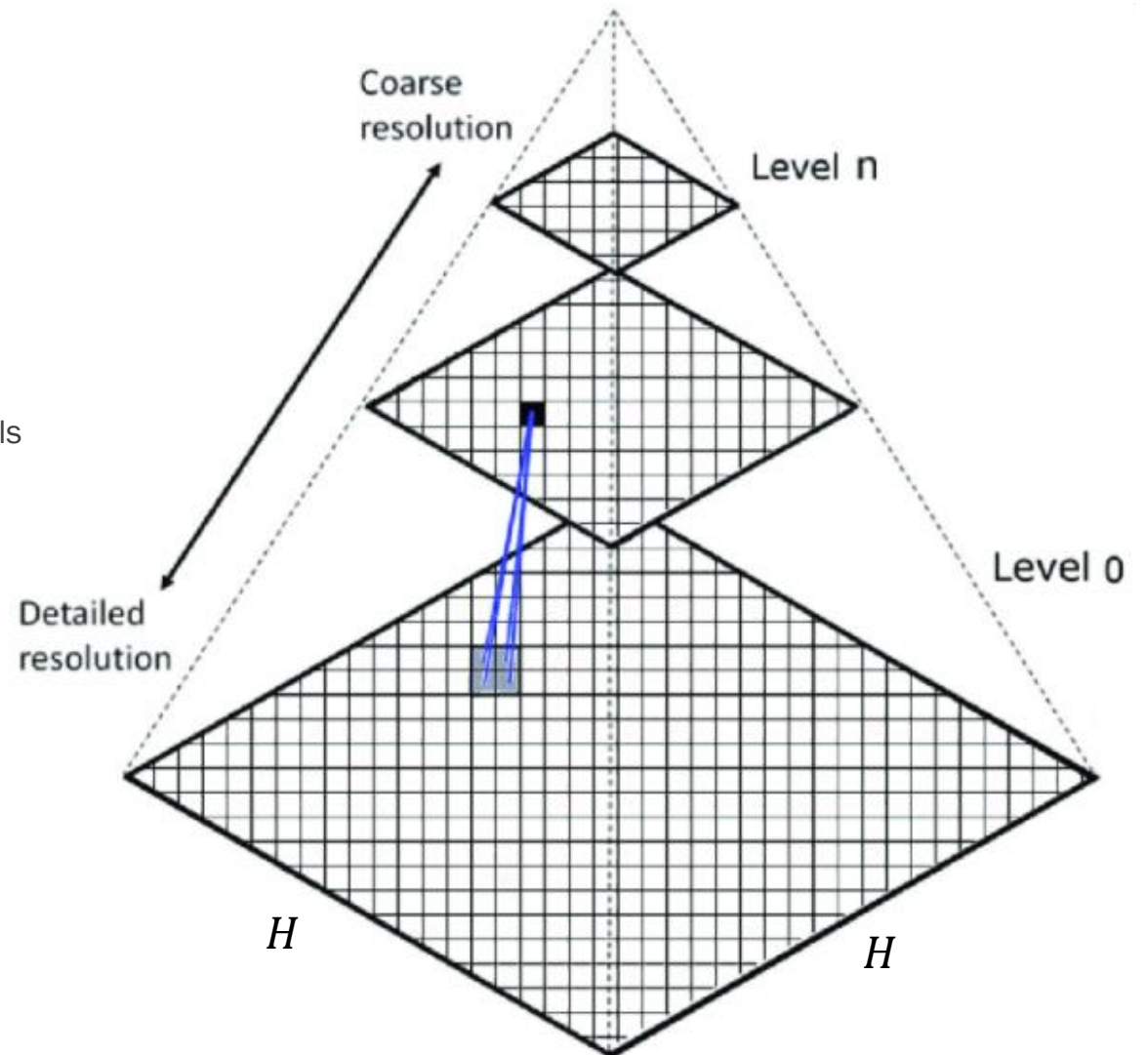
Pyramid

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 - any image patch at lower level directly corresponds to a smaller patch at upper level
 - levels can be of color image or grey scale
 - pyramid consistency
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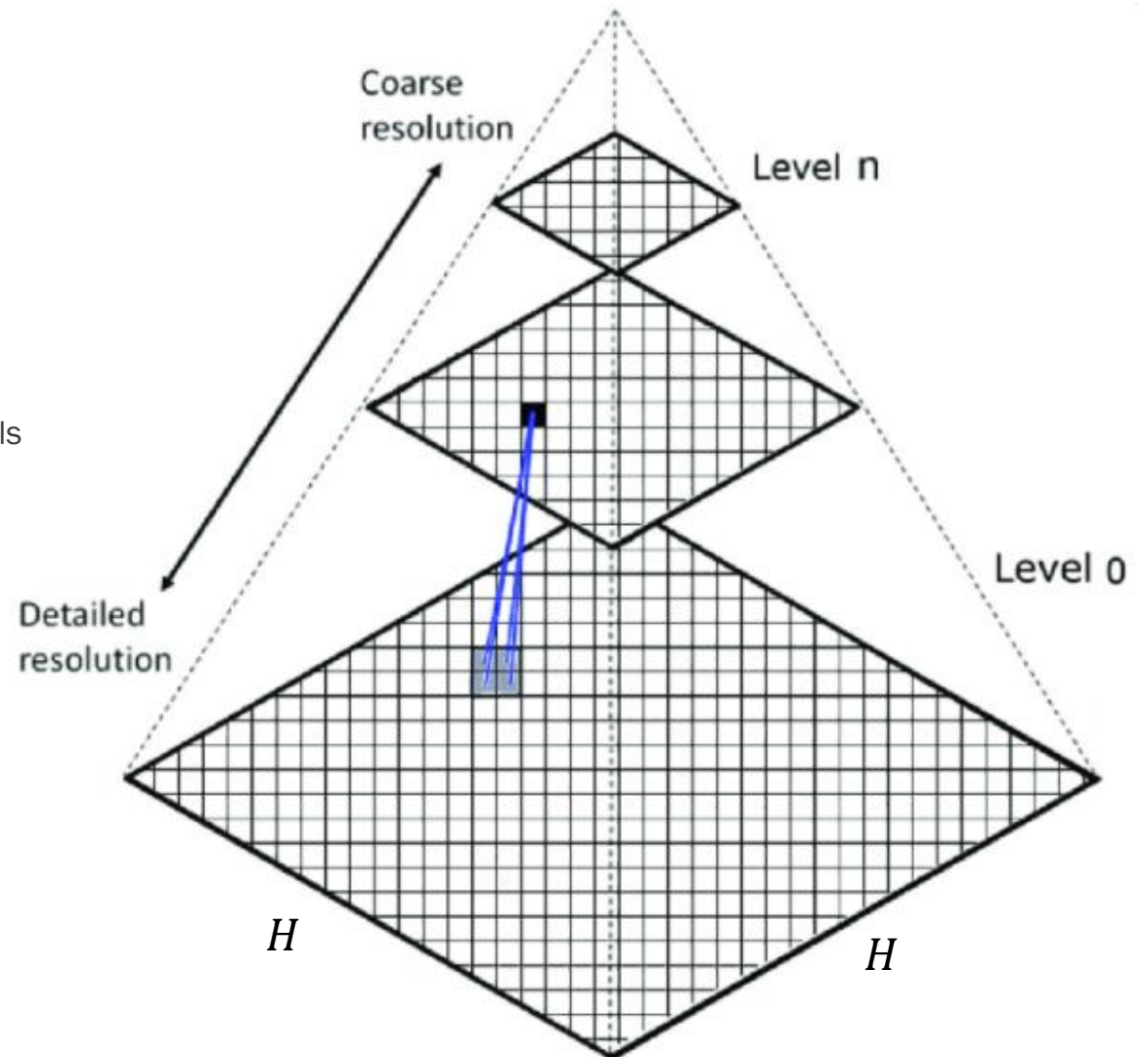


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$$= N + \frac{N}{4} + \frac{N}{4^2} + \dots + \frac{N}{4^k} \quad N = H \times W$$

$$\leq \frac{4N}{3}$$



Pyramid

- Tiled Multi-Resolution (or Tiled Pyramidal) TIFF

- it is simply a tiled multi-page TIFF image
- each resolution is stored as a separate layer within the TIFF
- it's standard TIFF extension supported by most image procc applications including photoshop
- 'libtiff' library is capable of reading & writing such pyramids

ref: <http://www.libtiff.org>

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- Image pyramid processing

- while using pyramid MRA, construct your own pyramids inside that image processing algorithm

Pyramid construction

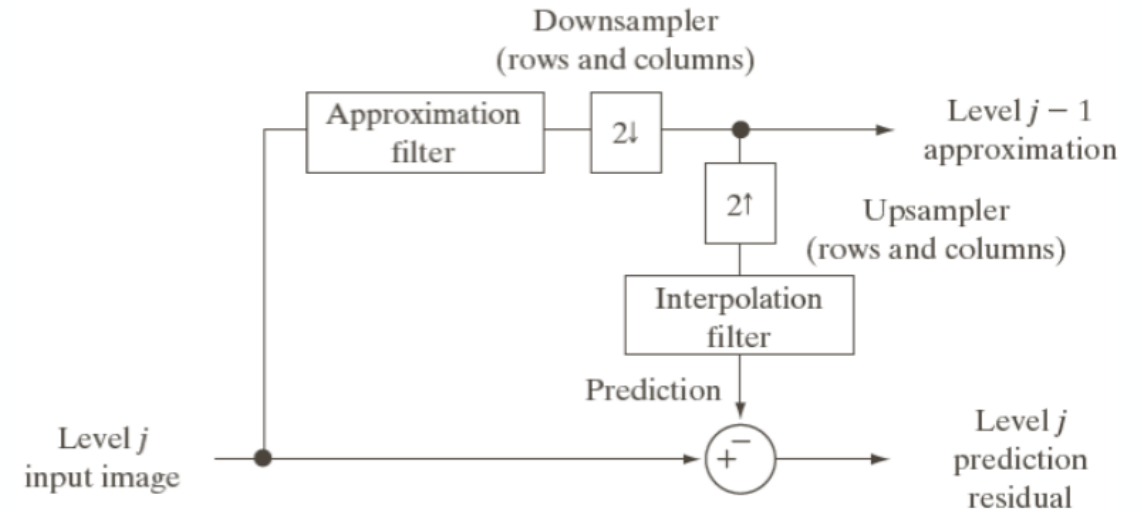
- Build the pyramid using below cornerstones

1. Approximation filter

- Gaussian filter
- Averaging/mean filter
- Low pass filter

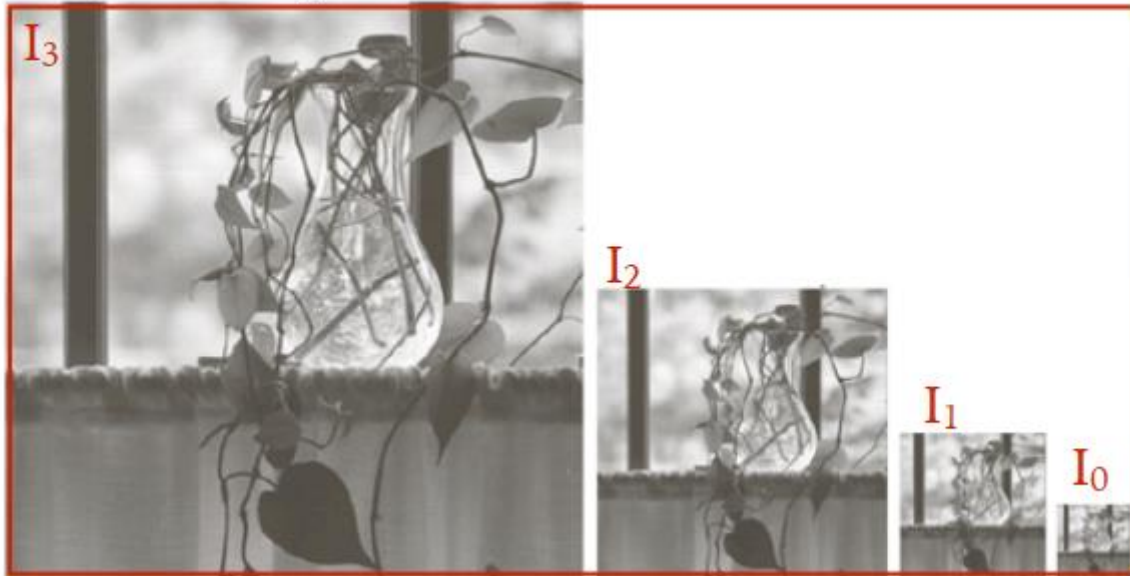
2. Detailed filter

- Bilinear interpolation
- Bicubic interpolation
- Upsampler

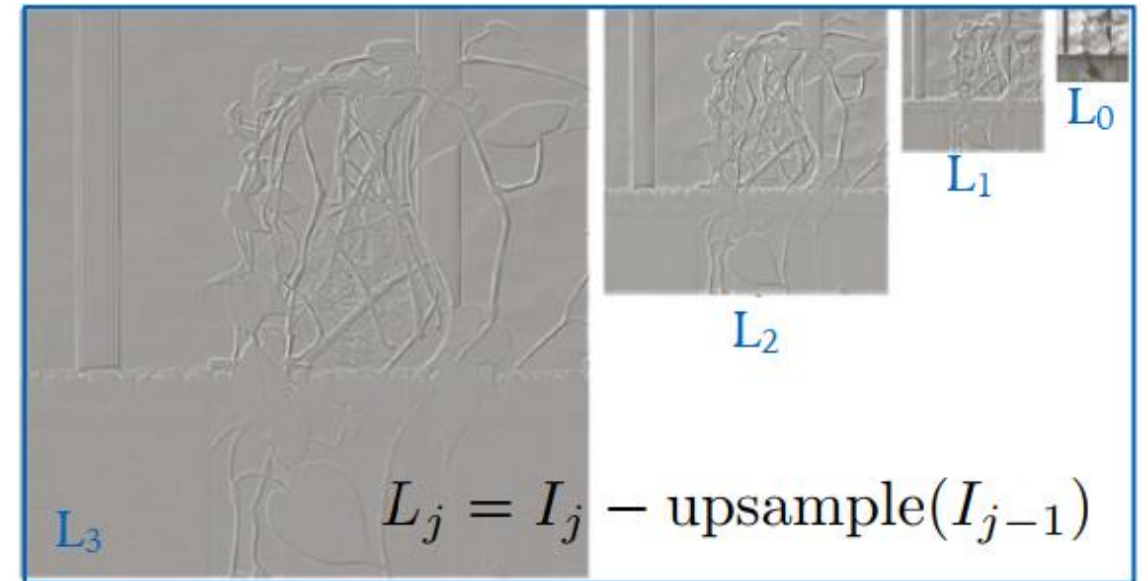


Gaussian Pyramid

original = I_j $I_{j-1} = \text{downsample}(I_j * G_\sigma)$



Approximation pyramid



Residual pyramid

Pyramid representation

- We mostly use residual format
 - note level-0 is same in approximation & residual
 - efficient representation

$$I_0 = L_0$$

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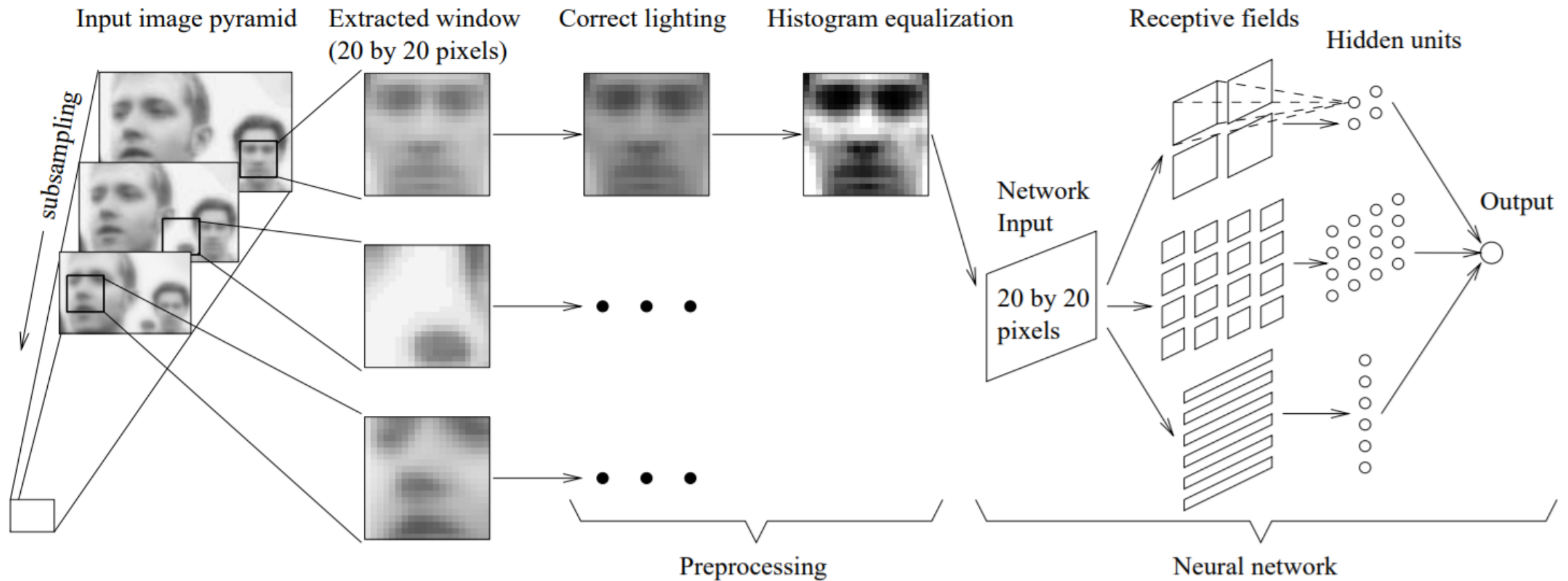
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- Entire approximation pyramid can be obtained via residual pyramid

Pyramid processing

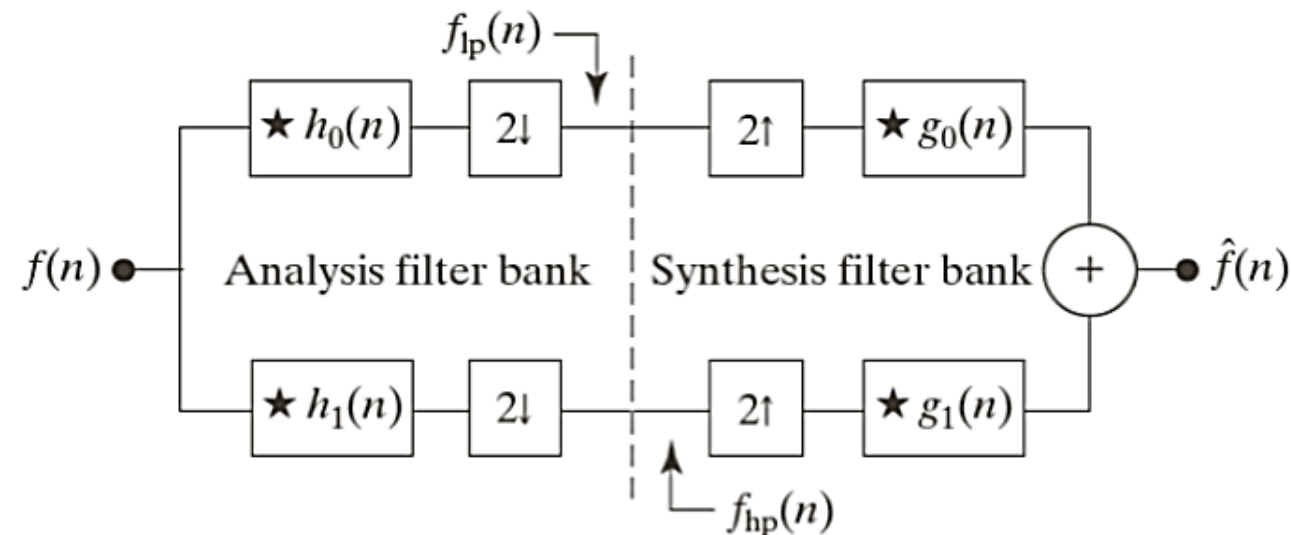
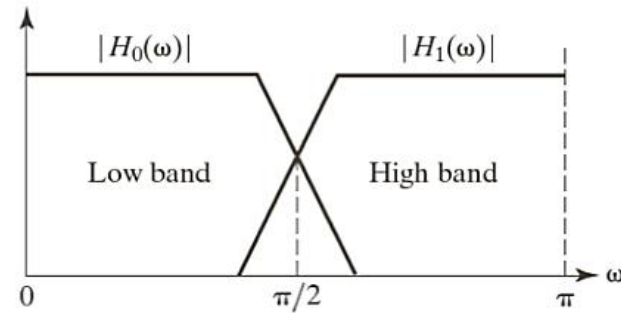


Sub-bands

- Sub-bands are the bandpass filters
 - a series of bandpass filters also known as filter bank
 - Equi-rate: equal bandwidth sub-bands
 - Multi-rate: different bandwidth sub-bands
 - similar to image pyramid, we use below corner stones :
 1. Analysis
 - decompose image into set of images of different freq bands
 2. Synthesis
 - original image should be reconstructed from bands of analysis stage

Sub-bands

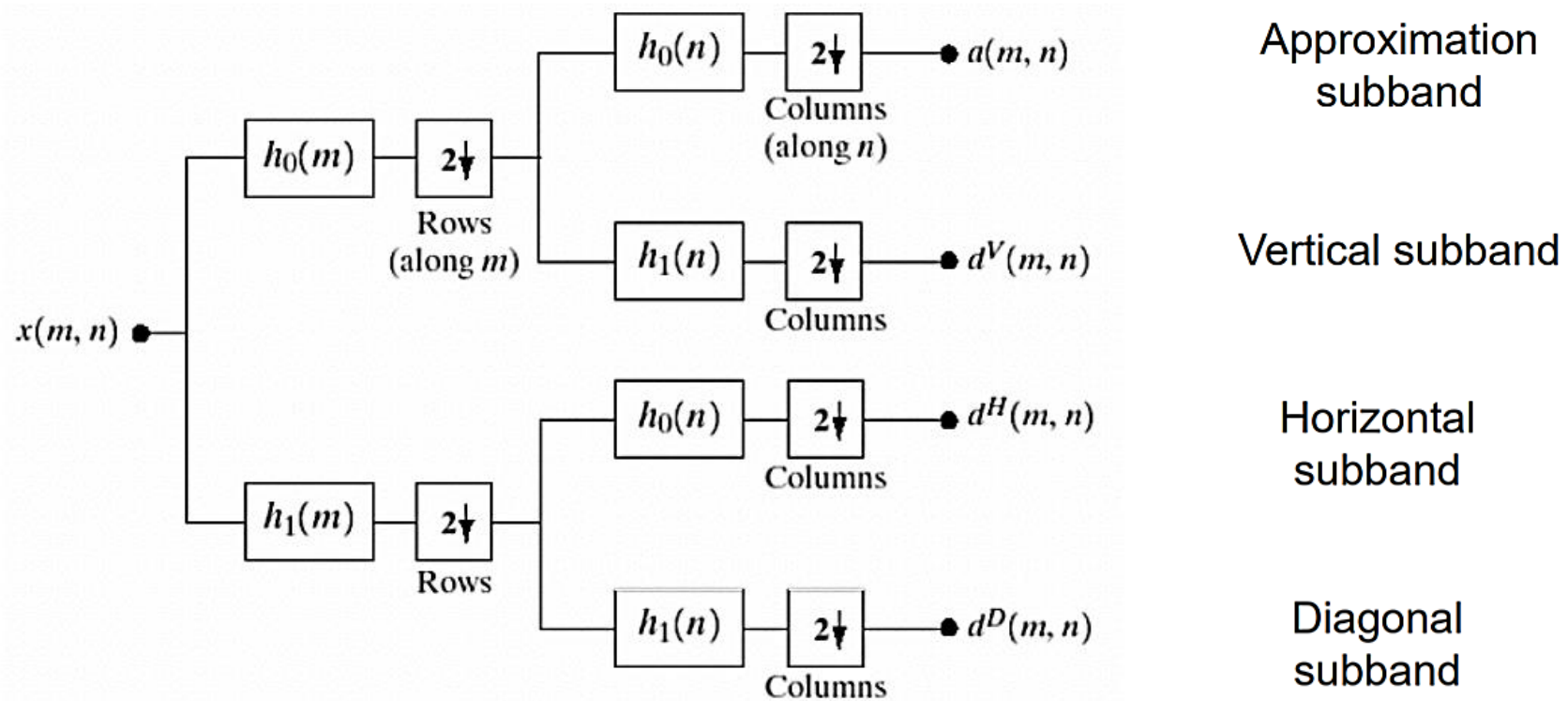
- Double bands
 - 2 band decomposition
 - filtering + $2\downarrow$



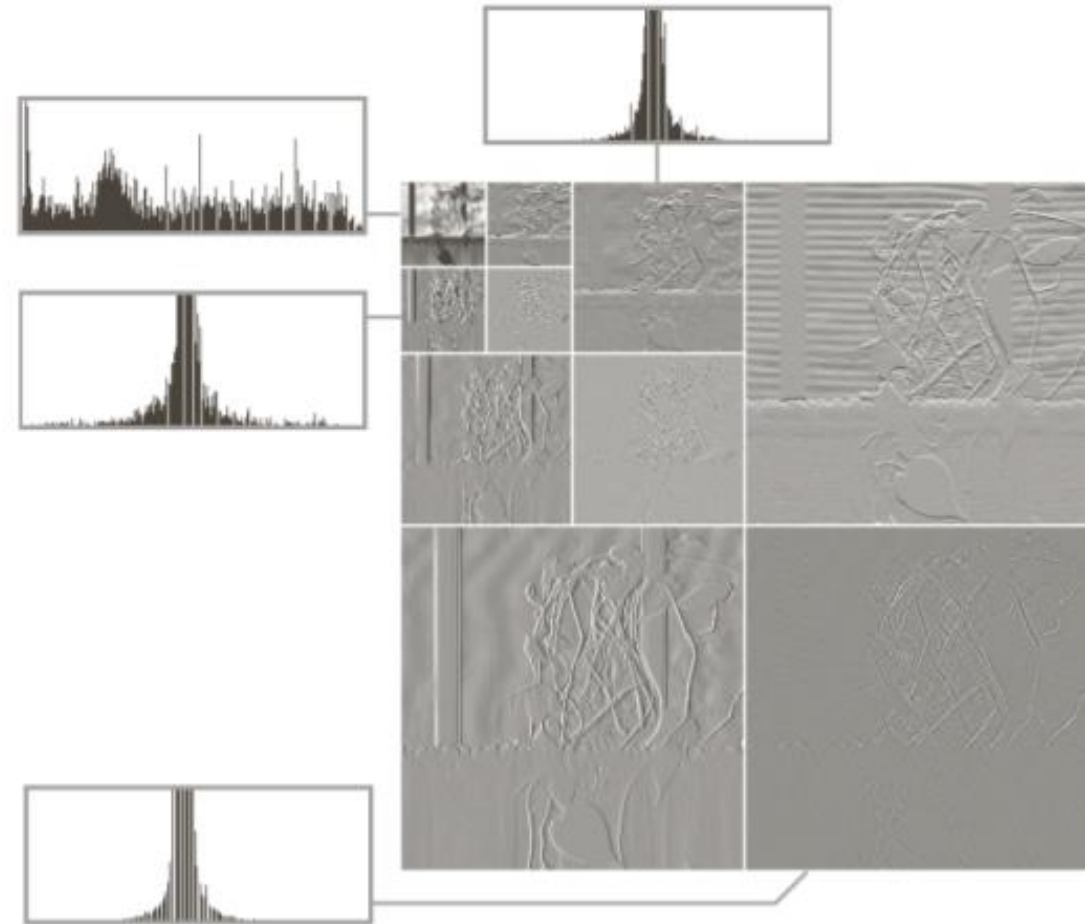
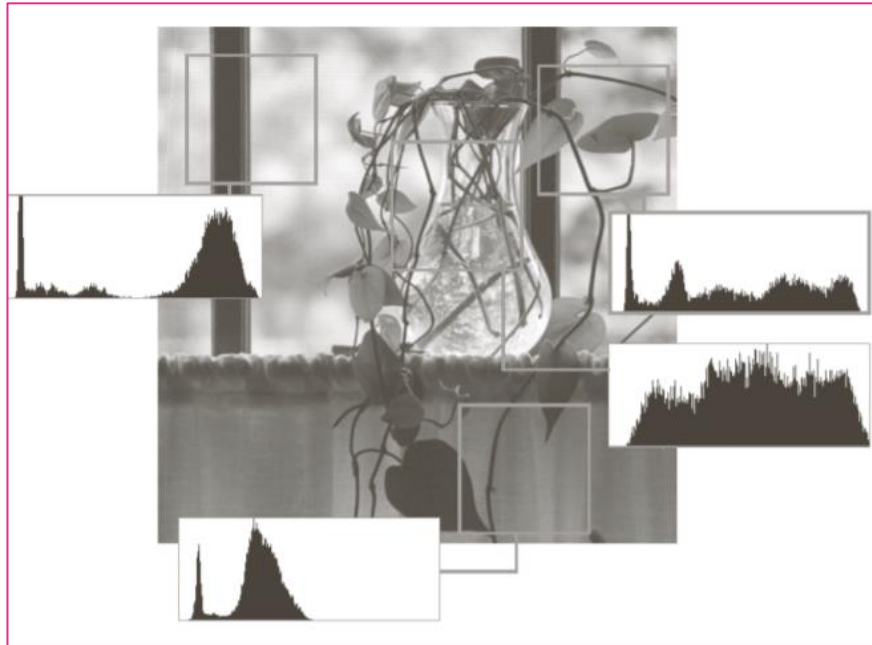
$$g_0(n) = (-1)^n h_1(n)$$
$$g_1(n) = (-1)^{n+1} h_0(n)$$

Sub-bands

- sub-band coding
 - 2 band decomposition expanded recursively



Sub-band decomposition



Sub-band denoise

- Different bit-rates or different coding technique can be used for each sub-band
 - useful in compression as well
- Denoise
 - noise types
 - uniform
 - speckle
 - band-limited
 - sub-band denoise
 - different bands show different response to noise types
 - it allows errors to be distributed across sub-bands
 - filter each sub-band image separately with specific filtering parameters dedicated to those bands

Sub-band denoising

original



noisy



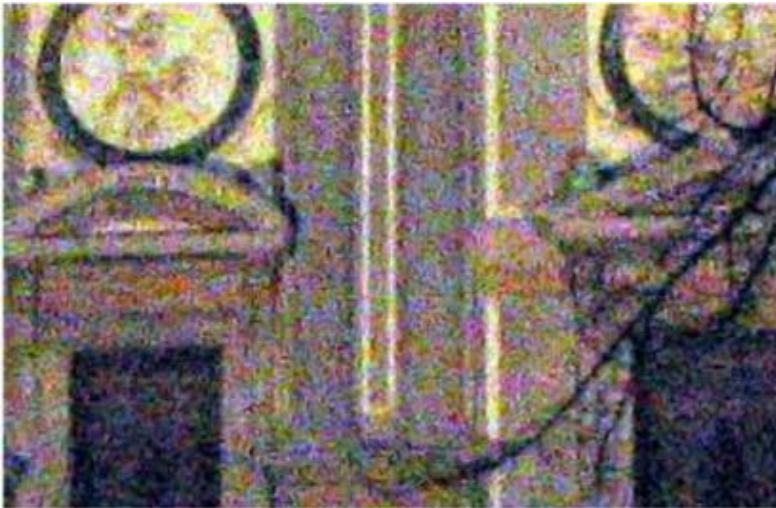
denoised



Multiresolution BF

- Results

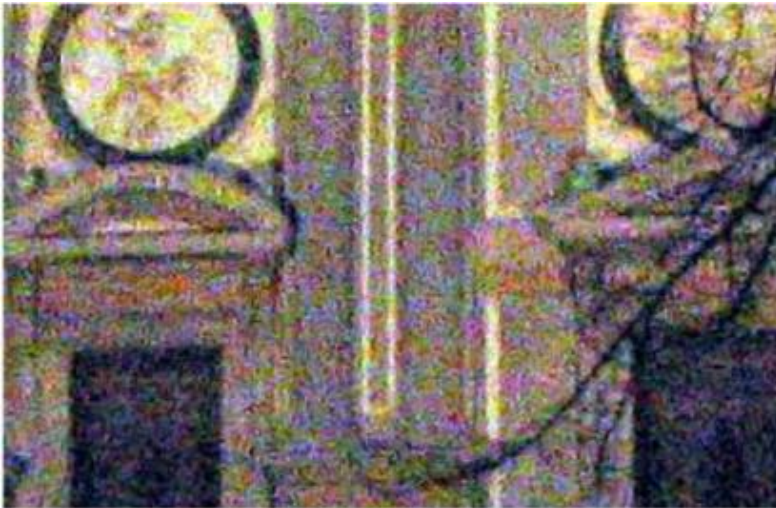
input



Multiresolution BF

- Results

input



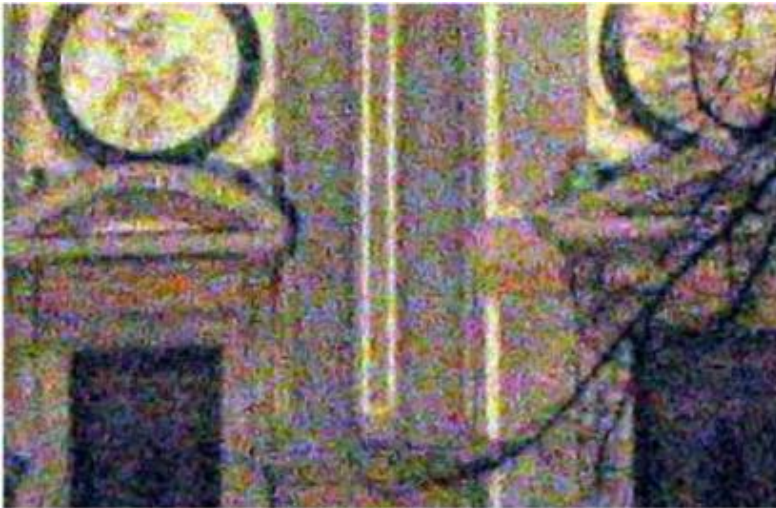
BF (psnr 29.6)



Multiresolution BF

- Results

input



BF (psnr 29.6)



MRBF (psnr 31.4)



Conclusion

- Denoising
- Multiresolutions
 - Pyramids
 - Sub-bands



BF



MRBF



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❑ Multiresolutions

- Pyramids
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❑ Denoising

- Even minute imperceptible improvement in the denoising is very important for scientific images



BF



MRBF



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BF



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