# Potential Modules for p5.math.js

# Linear Algebra and Matrices

### Simple matrix operations

- Implementing iterable matrices of size  $n \times m$  (utilizing existing p5.Matrix, or completely new implementation using vectors)
- Matrix addition
- Matrix multiplication

# Slightly more complicated matrix operations

- Calculating reduced row echelon form
- Matrix inverter
- Linear system solver
- Matrix determinant calculator
- Matrix norm calculator

# Most computationally intense matrix operations

- Performing Gram-Schmidt orthogonalization on a matrix
- Finding eigenvalues and eigenvectors of a matrix
- Finding rank of a matrix

# **Complex Numbers**

#### **Basic complex numbers**

- Unit vectors  ${\bf i}$  and  ${\bf j}$
- Implementing complex numbers a + bi as vectors (a, b)
- Addition, multiplication, and conjugate of complex numbers
- Modulus (magnitude) of complex numbers
- Computing phase angles of complex numbers

#### More complex complex numbers

- Calculating exponents  $a^z$  where z is complex (Euler's formula)
- Calculating exponents  $z^n$  where z is complex (de Moivre's formula)
- Eventually, this class can be used to express solutions to equations with complex roots

# Fun additions for visual learning

- Showing relationship between complex numbers and the real plane visually
- Visualization of the Mandelbrot set, demonstrating complex exponentiation
- Plots of the Riemann zeta function

#### Calculus (both single and multiple variable)

#### Simple calculus operations

- Limits
- Derived functions and derivatives at specified points
- Indefinite and definite integrals

#### Slightly more complicated calculus operations

- Calculating continuity intervals for a given function
- Gradient, curl, divergence, and Laplacian
- Hessian and Jacobian matrices

#### Most computationally intense calculus operations

- Series divergence/convergence calculator
- Riemann sum calculator
- Finding n'th order Maclaurin polynomials for given functions
- Finding n'th order Taylor polynomials for given functions about a point

#### Algebra

#### Basic algebra

- Solving linear equations
- Adding polynomials

#### More advanced algebra

- Quadratic equation solver
- n'th order polynomial solver
- Finding asymptotes of given functions

#### Most intense algebra/visual algebra

- Graphing equations
- Multiplying polynomials (Karatsuba's algorithm)

# Geometry

# **Basic geometry**

- Determining whether points are collinear/coplanar

#### More advanced geometry

- App where students can walk through common theorems and proofs

#### Visualization of geometry

- Interactive app explaining  $\pi$  and angles
- Interactive app where students can draw shapes and objects

#### Trigonometry

# Basic trig

- Implementing all trig functions and inverses
- Support for both degrees and radians

#### More advanced trig

- Checking if two trig functions are identical; simplifying trig identities

#### Visualization of trig

- Interactive app explaining trig functions in relation to a triangle and to the unit circle