

Lab 2 :

Question 1 :

Write a program to find GCD using consecutive integer checking method and analyze its time efficiency.

```
...
```

```
#include <stdio.h>
#include <stdlib.h>
```

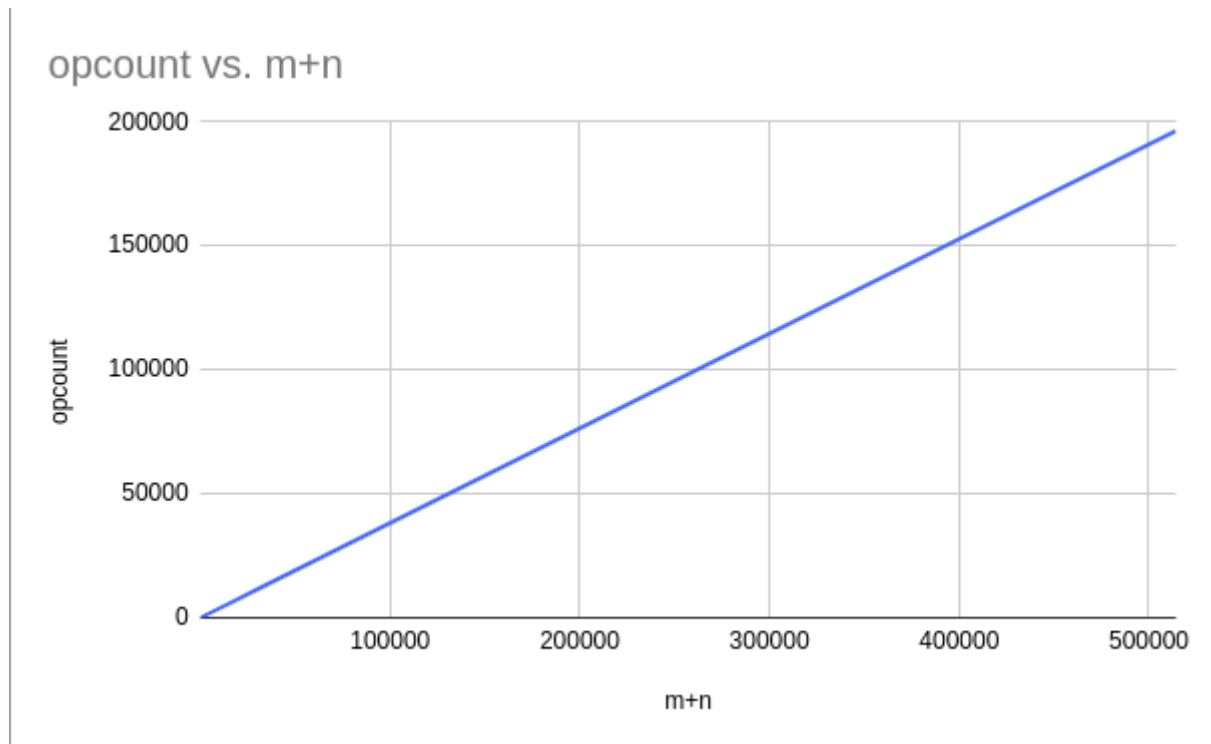
```
int gcd(int m, int n, int *opr)
{
    for (int i = (m > n ? n : m); i > 0; i--)
    {
        (*opr)++;
        if (m % i == 0 && n % i == 0)
        {
            return i;
        }
    }
}
```

```
int main()
{
    int m, n;
    scanf("%d %d", &m, &n);
    int opr = 0;
    int result = gcd(m, n, &opr);
    printf("The gcd is %d and the operation count is -
> %d\n", result, opr);
}
...
```

```
dipe@dops: ~/Desktop/DAA/Lab/Lab 2
dipe@dops:~/Desktop/DAA/Lab/Lab 2$ ./con_int
0 1
The gcd is 0 and the operation count is -> 0
dipe@dops:~/Desktop/DAA/Lab/Lab 2$ ./con_int
3 5
The gcd is 1 and the operation count is -> 3
dipe@dops:~/Desktop/DAA/Lab/Lab 2$ ./con_int
2 8
The gcd is 2 and the operation count is -> 1
dipe@dops:~/Desktop/DAA/Lab/Lab 2$ ./con_int
15 30
The gcd is 15 and the operation count is -> 1
dipe@dops:~/Desktop/DAA/Lab/Lab 2$ ./con_int
45 46
The gcd is 1 and the operation count is -> 45
dipe@dops:~/Desktop/DAA/Lab/Lab 2$ ./con_int
1000 1001
The gcd is 1 and the operation count is -> 1000
dipe@dops:~/Desktop/DAA/Lab/Lab 2$ |
```

The basic operation for this algorithm is **comparison**.

m+n	opcount
1	0
2	1
5	2
8	3
13	5
21	8
34	13
55	21
89	34
144	55
233	89
377	144
28657	10946
514229	196418



As we can observe from the graph plot that the time complexity for the following algorithm is $O(\min(m,n))$ which belongs to $O(n+m)$.

Question 2 :

Write a program to find GCD using middle school method and analyze its time efficiency.

```

```
#include <stdio.h>
#include <stdlib.h>

void sieve(int m, int arr[])
{
 for (int i = 2; i < m + 1; i++)
 {
 arr[i] = i;
 }
 int j;
```

```

for (int i = 2; i < m + 1; i++)
{
 if (arr[i] != 0)
 {
 j = i * i;
 while (j <= m)
 {
 arr[j] = 0;
 j = j + i;
 }
 }
}

```

```

int pf(int n, int arr[], int *op)
{
 int narr[n + 1];
 sieve(n, narr);
 int i = 2;
 int cnt = 0;
 while (i <= n)
 {
 (*op)++;
 if (narr[i] != 0)
 {
 if (n % narr[i] == 0)
 {
 arr[cnt] = narr[i];
 n = n / narr[i];
 cnt++;
 }
 else
 {
 i++;
 }
 }
 else
 {
 i++;
 }
 }
}

```

```

}
return cnt;
}

int gcd(int m, int n, int *opr)
{
if (m == 0 || n == 0)
{
*opr = 1;
return m == 0 ? n : m;
}
int marr[m], narr[n], op1 = 0, op2 = 0;
int a = pf(m, marr, &op1);
int b = pf(n, narr, &op2);
*opr = op1 + op2;
printf("Prime factors of %d -> \t", m);
for (int i = 0; i < a; i++)
{
printf("%d\t", marr[i]);
}
printf("\nPrime factors of %d -> \t", n);
for (int i = 0; i < b; i++)
{
printf("%d\t", narr[i]);
}
printf("\n");
int i = 0, j = 0;
int result = 1;
while (i < a && j < b)
{
if (marr[i] == narr[j])
{
result *= marr[i];
i++;
j++;
}
else if (marr[i] < narr[j])
{
i++;
}
}

```

```

else
{
j++;
}
}
return result;
}

int main()
{
int m, n;
scanf("%d %d", &m, &n);
int opr = 0;
int result = gcd(m, n, &opr);
printf("The gcd is %d and the operation count is -
> %d\n", result, opr);
return 0;
}

```

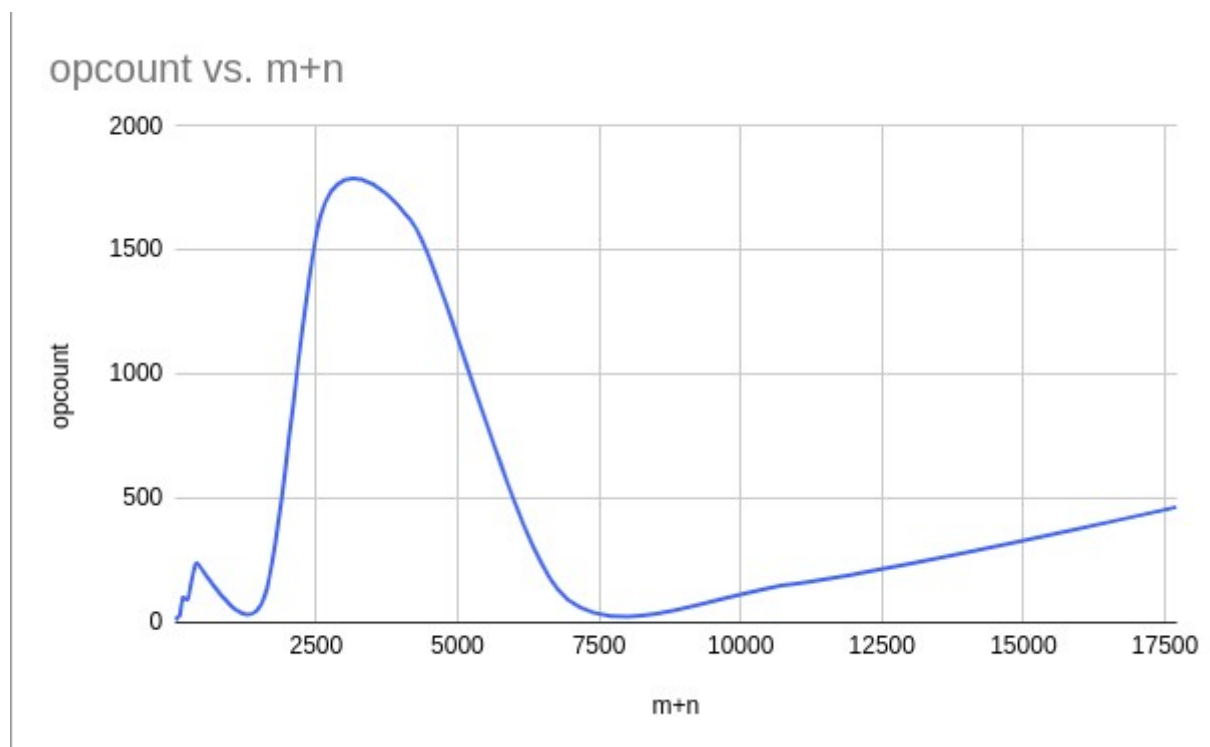
```

diye@dops:~/Desktop/DAA/Lab/Lab 2$./gcd_sieve
0 1
The gcd is 1 and the operation count is -> 1
diye@dops:~/Desktop/DAA/Lab/Lab 2$./gcd_sieve
2 3
Prime factors of 2 -> 2
Prime factors of 3 -> 3
The gcd is 1 and the operation count is -> 3
diye@dops:~/Desktop/DAA/Lab/Lab 2$./gcd_sieve
5 8
Prime factors of 5 -> 5
Prime factors of 8 -> 2 2 2
The gcd is 1 and the operation count is -> 7
diye@dops:~/Desktop/DAA/Lab/Lab 2$./gcd_sieve
4 8
Prime factors of 4 -> 2 2
Prime factors of 8 -> 2 2 2
The gcd is 4 and the operation count is -> 5
diye@dops:~/Desktop/DAA/Lab/Lab 2$./gcd_sieve
1000 1001
Prime factors of 1000 -> 2 2 2 5 5 5
Prime factors of 1001 -> 7 11 13
The gcd is 1 and the operation count is -> 23
diye@dops:~/Desktop/DAA/Lab/Lab 2$

```

The basic operation is **comparison**.

| m+n   | opcount |
|-------|---------|
| 1     | 1       |
| 2     | 1       |
| 5     | 3       |
| 8     | 6       |
| 13    | 7       |
| 21    | 15      |
| 34    | 19      |
| 55    | 24      |
| 89    | 28      |
| 144   | 99      |
| 233   | 95      |
| 377   | 239     |
| 1597  | 110     |
| 2584  | 1644    |
| 4181  | 1618    |
| 6765  | 135     |
| 10946 | 156     |
| 17711 | 465     |



As we can observe from the graph plot that the time complexity for the following algorithm is  **$O(n+m)$** .