CTA200H1 – Problem Set #1 Karandeep Basi May 11, 2017

Question 1.

```
Location - p1/q1/q1.sh
```

Bash script that creates a copy of all txt files in the same directory in the folder "replace" with the first arg replaced by the arg.

./q1.sh tomato potato //(instances of tomato replaced by potato)

```
Source -
#! /bin/bash
find=$1
replace=$2
mkdir replace
cp ./*.txt ./replace
sed -i -e "s/$find/$replace/g" ./replace/*.txt
```

Question 2.

a.

Routine found in p1/q2.sh

```
def NChooseK(n, k):
    if (k == 0):
        return 1
    numerator = n
    for i in range(n - k + 1, n):
        numerator *= i
    denominator = k
    for i in range(2, k):
        denominator *= i
    return int(numerator/denominator)
```

b.

Routine found in p1/q2.sh

Run python p1/pascals.py to run method

Output:

```
1 1
121
1 3 3 1
14641
1 5 10 10 5 1
1 6 15 20 15 6 1
1 7 21 35 35 21 7 1
1 8 28 56 70 56 28 8 1
1 9 36 84 126 126 84 36 9 1
1 10 45 120 210 252 210 120 45 10 1
1 11 55 165 330 462 462 330 165 55 11 1
1 12 66 220 495 792 924 792 495 220 66 12 1
1 13 78 286 715 1287 1716 1716 1287 715 286 78 13 1
1 14 91 364 1001 2002 3003 3432 3003 2002 1001 364 91 14 1
1 15 105 455 1365 3003 5005 6435 6435 5005 3003 1365 455 105 15 1
1 16 120 560 1820 4368 8008 11440 12870 11440 8008 4368 1820 560 120 16 1
1 17 136 680 2380 6188 12376 19448 24310 24310 19448 12376 6188 2380 680 136 17 1
1 18 153 816 3060 8568 18564 31824 43758 48620 43758 31824 18564 8568 3060 816 153 18 1
1 19 171 969 3876 11628 27132 50388 75582 92378 92378 75582 50388 27132 11628 3876 969 171 19 1
1\ 20\ 190\ 1140\ 4845\ 15504\ 38760\ 77520\ 125970\ 167960\ 184756\ 167960\ 125970\ 77520\ 38760\ 15504\ 4845\ 1140\ 190\ 20\ 1
c.
Routine found in p1/q2/q2.sh
Run python p1/q2/hitter.py to run routine
42.1875% of the time the hitter will get atleast one hit.
def biasedCoin(p, k, n):
         return NChooseK(n, k) * math.pow(p, k) * math.pow(1 - p, n - k)
d.
Routine found in p1/q2.sh
Run python p1/experiment.py to run experiment
def runExperiment(N, p, k, n):
         random.seed()
         successCount = 0
         probability = biasedCoin(p, k, n)
         for i in range (1, N):
                  if random.random() > probability:
                           successCount += 1
         return successCount
def experiment():
         for i in range(1, 4):
```

print runExperiment(int(math.pow(10, i)), 0.250, 1, 4) / math.pow(10, I)

Output:

```
Experiment #1
```

N = 10.0, Fraction of success = 0.3

N = 100.0, Fraction of success = 0.52

N = 1000.0, Fraction of success = 0.567

Experiment #2

N = 10.0, Fraction of success = 0.5

N = 100.0, Fraction of success = 0.58

N = 1000.0, Fraction of success = 0.6

Experiment #3

N = 10.0, Fraction of success = 0.6

N = 100.0, Fraction of success = 0.57

N = 1000.0, Fraction of success = 0.599

Question 3.

a. I used an approximation algorithm as well as a recurrence algorithm. The recurrence algorithm lost accuracy as m increased but it ran quicker.

Table of results -

M, X	Result
(1, 1)	0.440050585745
(2, 1)	0.114903484932
(3, 1)	0.0195633539827
(4, 1)	0.00247663896411
(5, 1)	0.000249757730211

```
# This recurrence is quicker but loses accuracy dramatically when v > 9 def besselRecurrence(v, x):

if v == 0 or v == 1:

return besselApprox(v, x)

else:

return (2 * (v - 1) / x) * besselRecurrence(v - 1, x) - besselRecurrence(v - 2, x)
```

#Slower calculation but more accurate than recurrence

```
\begin{aligned} &\text{def besselApprox}(v, \, x); \\ &\text{sum} = 0.0 \\ &\text{for } k \text{ in range}(0, \, 10); \\ &\text{numerator} = \text{ math.pow}(\text{-}1, \, k) * \text{math.pow}(x \, / \, 2, \, v + (2 * \, k)) \\ &\text{denominator} = \text{math.factorial}(k) * \text{math.factorial}(v + k) \\ &\text{sum} += (\text{numerator} \, / \, \text{denominator}) \\ &\text{return sum} \end{aligned}
```

b.
Routine in p1/q3/q3.py
Can be run using p1/q3/createPointSpread.py outputFile

I.e python createPointSpread.py test.png

will create the point spread image as test.png in the current directory

Created Image -



c. Routine in p1/q3/q3.py

Can be run using p1/convolve.py imageToConvolve outputFile I.e python convolve.py space.jpg testSpace.jpg









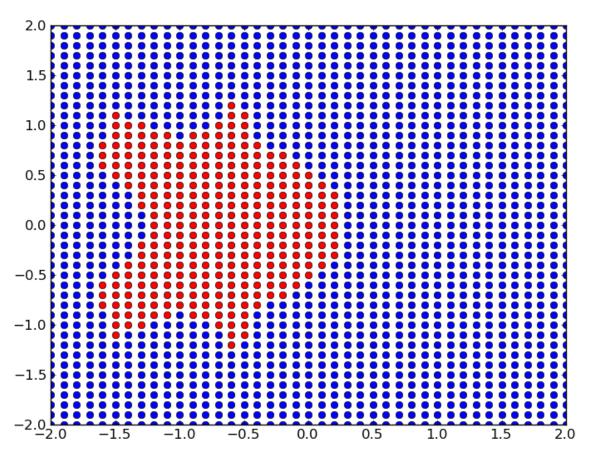
Question 4.

Routines in p1/q4/q4.py

Running will generate a plot indicating divergence for all x, y values in increments of 0.1.

Output on next page -

Blue = Diverts, Red = Does not divert



Question 5

Routines in q1/q5/q5.py

Derivative,
$$f'(x) = 2x - 1$$

 $f'(1) = 1$

What do you find?

The smaller the delta the more accurate the answer we get, however after 10^-13 the answers remain the same. (10^-13) is also more inaccurate than 10^-12)

Output:

Delta	Output
	±.

10^-4	1.0001
10^-5	1.00001000001
10^-6	1.00000099992
10^-7	1.00000010058
10^-8	1.00000000392
10^-9	1.00000008374
10^-10	1.00000008284
10^-11	1.00000008275
10^-12	1.00008890058
10^-13	0.999200722163
10^-14	0.999200722163

Q6.

Routines in p1/q6/q6.py Run it to simulate a battle.

Sample output:

python q6.py

Warship fired a missile at Speeder!

Speeder dodged Warship's attack!

Speeder fired a laser at Standard Ship!

Standard Ship took 50 shield damage from Speeder! Shield is now at 50

Standard Ship fired a laser at Warship!

Warship took 50 shield damage from Standard Ship! Shield is now at 50

Standard Ship fired a laser at Speeder!

Speeder took 50 shield damage from Standard Ship! Shield is now at 50

Speeder fired a laser at Warship!

Warship took 50 shield damage from Speeder! Shield is now at 0

Warship fired a missile at Standard Ship!

Standard Ship took 100 shield damage from Warship! Shield is now at -50

Standard Ship took 25 hull damage from Warship! Hull Strength is now at 75.0

Speeder fired a laser at Warship!

Warship took 25 hull damage from Speeder! Hull Strength is now at 75.0

Warship fired a laser at Speeder!

Speeder dodged Warship's attack!

Standard Ship fired a laser at Speeder!

Speeder took 50 shield damage from Standard Ship! Shield is now at 0 Speeder fired a laser at Standard Ship!

Standard Ship took 25 hull damage from Speeder! Hull Strength is now at 50.0 Warship fired a laser at Speeder!

Speeder took 25 hull damage from Warship! Hull Strength is now at 75.0

Standard Ship fired a laser at Warship!

Warship took 25 hull damage from Standard Ship! Hull Strength is now at 50.0 Speeder fired a laser at Warship!

Warship took 25 hull damage from Speeder! Hull Strength is now at 25.0

Standard Ship fired a laser at Speeder!

Speeder took 25 hull damage from Standard Ship! Hull Strength is now at 50.0

Warship fired a missile at Speeder!

Speeder took 50 hull damage from Warship! Hull Strength is now at 0.0

Speeder was destroyed!

Standard Ship fired a laser at Warship!

Warship took 25 hull damage from Standard Ship! Hull Strength is now at 0.0

Warship was destroyed!

Standard Ship is the victor!

#2

python q6.py

Speeder fired a laser at Standard Ship!

Standard Ship took 50 shield damage from Speeder! Shield is now at 50

Warship fired a missile at Standard Ship!

Standard Ship took 100 shield damage from Warship! Shield is now at -50

Standard Ship took 25 hull damage from Warship! Hull Strength is now at 75.0

Standard Ship fired a laser at Warship!

Warship took 50 shield damage from Standard Ship! Shield is now at 50

Speeder fired a laser at Standard Ship!

Standard Ship took 25 hull damage from Speeder! Hull Strength is now at 50.0

Warship fired a missile at Speeder!

Speeder dodged Warship's attack!

Standard Ship fired a laser at Warship!

Warship took 50 shield damage from Standard Ship! Shield is now at 0

Standard Ship fired a laser at Warship!

Warship took 25 hull damage from Standard Ship! Hull Strength is now at 75.0

Warship fired a laser at Speeder!

Speeder took 50 shield damage from Warship! Shield is now at 50

Speeder fired a laser at Standard Ship!

Standard Ship took 25 hull damage from Speeder! Hull Strength is now at 25.0 Speeder fired a laser at Warship!

Warship took 25 hull damage from Speeder! Hull Strength is now at 50.0

Warship fired a missile at Speeder!

Speeder dodged Warship's attack!

Standard Ship fired a laser at Warship!

Warship took 25 hull damage from Standard Ship! Hull Strength is now at 25.0

Standard Ship fired a laser at Warship!

Warship took 25 hull damage from Standard Ship! Hull Strength is now at 0.0

Warship was destroyed!

Standard Ship fired a laser at Speeder!

Speeder dodged Standard Ship's attack!

Speeder fired a laser at Standard Ship!

Standard Ship took 25 hull damage from Speeder! Hull Strength is now at 0.0

Standard Ship was destroyed!

Speeder is the victor!