

## Anagram

↳ HEART      EARTH      EARTH  
(both are permutation of each other)

ex → abaac      abacc

LIS TEN      SILENT

S and t

rat car



## CARES RACE

### Observations

① if the length of the strings are different then we can never form permutations of each other.

② Once we know that length is same, then all we need to ensure that there is no mismatch in char.

unique char  
should be same

(both string should possd some set of chars  
with same frequency of occurrence)

$\langle k, v \rangle$

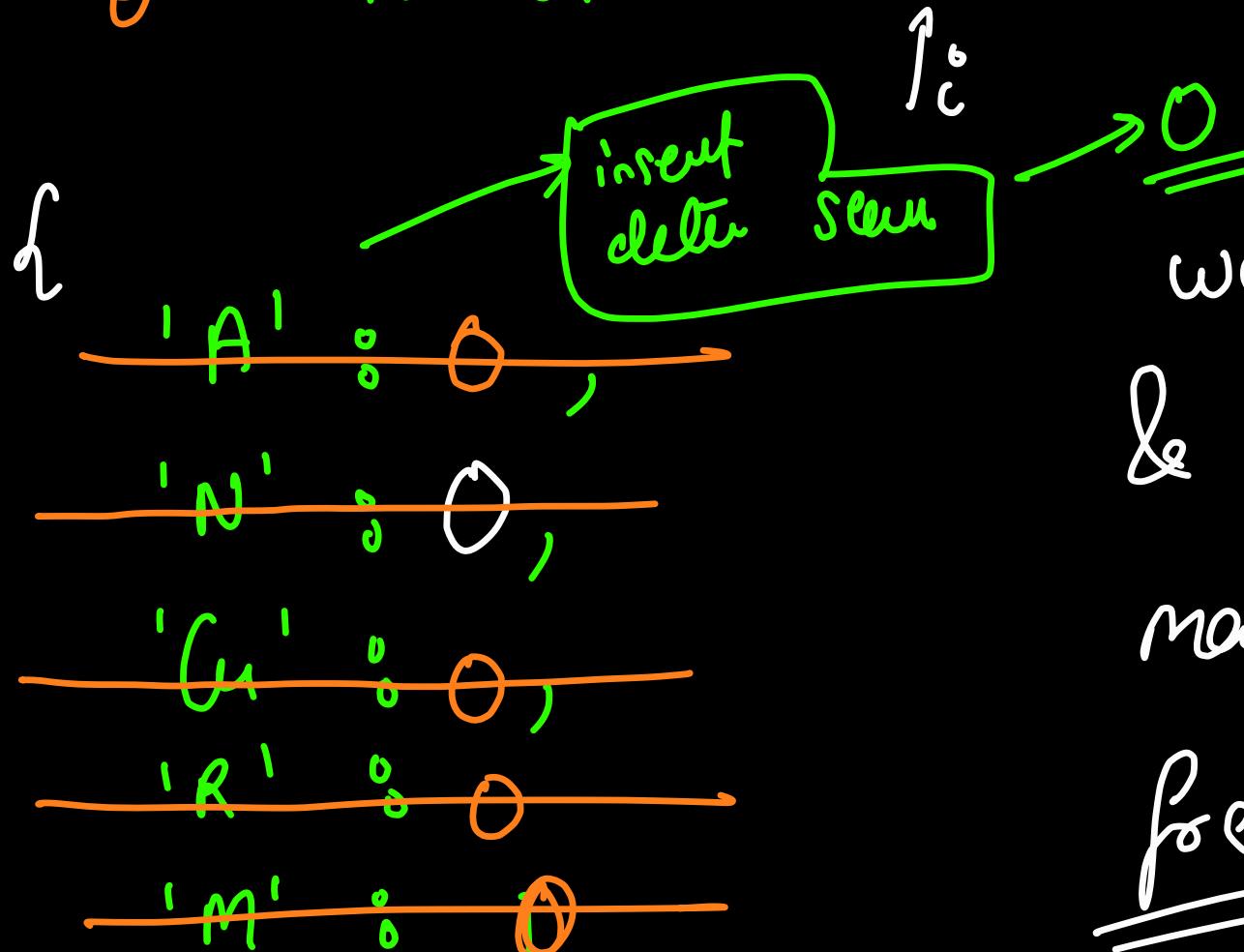
Note → Order doesn't matter

frequency map

Ex

$S \rightarrow \text{ANAGRAM}$

$t \rightarrow \text{NAGRAM}$



Key, value  
 $\downarrow$   $\downarrow$   
char      freq

$O(i)$

we can one by one process change,

& if we find this char in the  
mapping we will reduce the  
freq.

Once freq becomes 0, remove the  
char from mapping.

)

at last if  
mapping is empty,  
we have pair of anagram.

$s = aab$        $t = ab\textcolor{brown}{b}$       if we don't find a char of  
 $\downarrow$                        $\nearrow i$       t inside mapping of s,  
 $\{ a : \cancel{z1}$   
~~b : \cancel{z0}~~  
 3

we don't have angrms.

Space Complexity  $\rightarrow \underline{\underline{O(1)}}$   
Time Complexity  $\rightarrow \underline{\underline{O(n+n)}} \Rightarrow \underline{\underline{O(n)}}$

if ( s.length != t.length )   
return false;

Ans  $\Rightarrow [eat, tea, tan, ate, nat, bat] \underset{?}{=} f_1([eat, tea])$

Club anagrams together  $\rightarrow$  anagrams are permutation of each other.

anagrams have same set of permutations  $\rightarrow$  length is always same  
 $\rightarrow$  char set with freq is same.

eat  $\rightarrow$  eat, eta, tea, tae, ate, aet  $\leftarrow$   
tea  $\rightarrow$  cat, ela, tha, tar, ate, aut

$\hookrightarrow$  This permutation is special  
Why?? because we have chars in sorted inc order.

[ eat , tea , tan, ate, nat , bat ] ,  
2<sup>nd</sup> corr → bat-  
abt set

{ "act" : [ eat, tea, ate ] }

unique  
key - value  
Scorted  
permutation

set of anagrams

"ant" : [ tan, nat ]

"abt" : [ bat ]

)

↳ returns all the values of  
the mapping by storing in an

array.

we can find more strings like  
eat whose sorted permutation  
will be act.

Space →

→ In the worst case , we might have all  $N$  string  
different.

Every string will form a new key value pair

↪ if we assume max length of a string to be  $K$   
( $K < 10^2$ )

↪  $O(NK)$  ← Space

$O(NK \log K)$  ← Time

$\rightarrow 10^4 \times 10^2 \log 10^2$   
 $\hookrightarrow 10^6 \times 7$

# Subarray With Sum 0.

## PROBLEM STATEMENT

[Try Problem](#)

You are given 'N' integers in the form of an array 'ARR'. Count the number of subarrays having their sum as 0.

For Example :

$N \leq 10^6$

Let 'ARR' be: [1, 4, -5]

The subarray [1, 4, -5] has a sum equal to 0. So the count is 1.

[1, 4, -5] → [1]      [1, 4]  
                        [4]      [-5, 4]  
                        [-5]     [1, 4, -5]

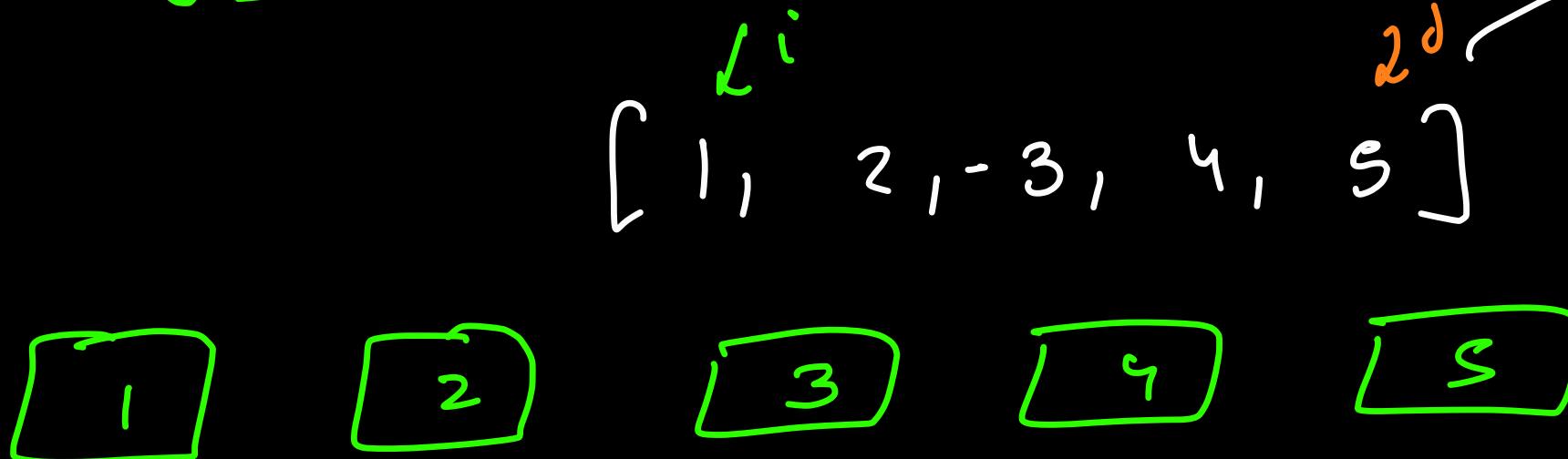
# Subarray  $\rightarrow$  So subarray is a contiguous cross-section  
of the given array.

$$\text{Sum} = 1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + 9$$

2<sup>0</sup>

So, [2, 4] is not

a subarray because  
they are not present  
consecutively



[1, 2] [2, 3] [3, 4] [4, 5]

[1, 2, 3] [2, 3, 4] [3, 4, 5]

[1, 2, 3, 4] [2, 3, 4, 5]

[1, 2, 3, 4, 5]

nestd loop

# Brute  
force

→ We can generate all possible subarrays  
and then calculate their sum & then check  
if sum is 0.

[  
↓  
 $i$       →  
, , , , , ]  
n

every subarray is a contiguous cross-section, so it will be  
having a start and end.

if we wish to generate all possible subarrays, we can  
try to form all possible pairs of (start and end).

```

for( i=0 ; i<n ; i++ ) { } → O(n^2)
    sum = 0
        for( j=i ; j<n ; j++ ) { }
            sum += a[j];
            if( sum == 0 )
                count++;

```

Time  $\rightarrow$   
 $O(n^2)$

movement of  
 $i$ , helps us  
 to get a new  
 subarray so  
 we add the  
 element to get  
 the sum

$j$


**TLE**

Given an array of length  $N$ , check if there is any subarray with sum 0. Return true if there is even 1 subarray with sum 0 else return false

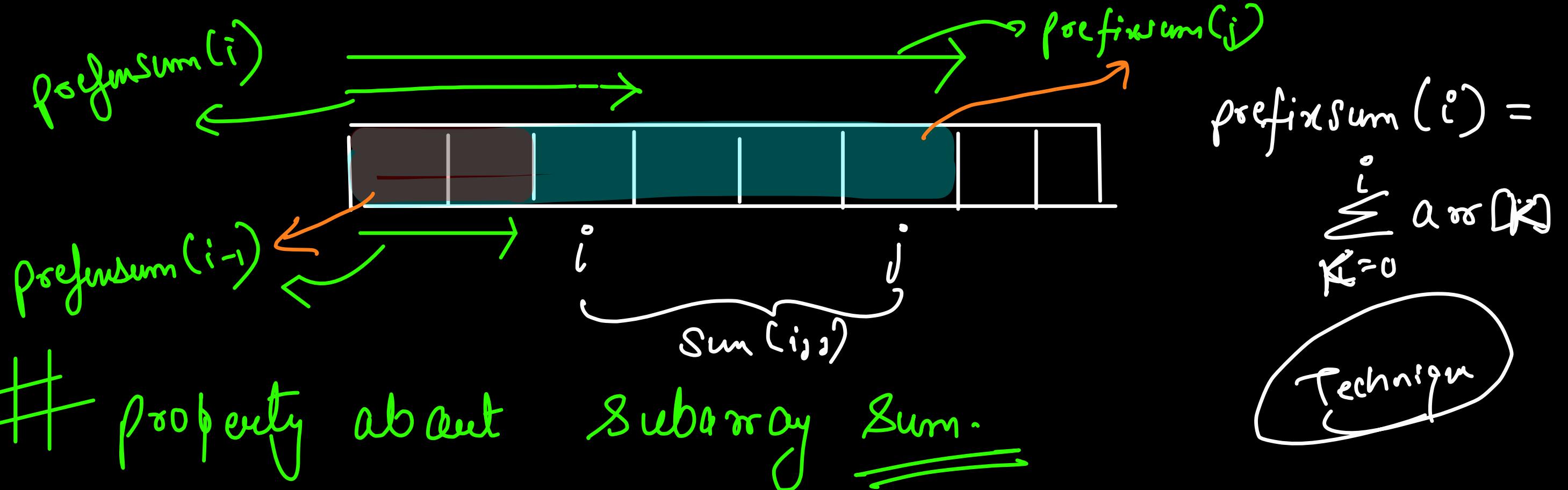
$0 \longrightarrow i$   
[1, 2, -3, 4, 5]  $\rightarrow$  true

[1, 2, 3, 4, 5]  $\rightarrow$  false

{1, 2, -2, 5}  $\rightarrow$  true

i j

$N \leq 10^6$



$$\begin{aligned}
 \text{Sum}(i, j) &= \text{prefixsum}(j) - \text{prefixsum}(i-1) \\
 &= \text{prefixsum}(j) - \text{prefixsum}(i) + \text{arr}[i]
 \end{aligned}$$

Sum of Subarray  
 starting with index  $i$   
 and ending at  $j$

Sum of a range can be calculated by  
 prefix Sums

Create freq map & check if any elelt is found more than once.

arr

$\{2: 1, 8: 1, 5: 1, 6: 1, 3: 1\}$

Prefix sum

2	6	-3	1	-3	2	5
---	---	----	---	----	---	---

↓ Prefix sum

$(i-1)$

$i$

$j$

2	8	5	6	3	5	10
---	---	---	---	---	---	----

just check if there are 2 indices with same values or not.

key-value

freq

$$\text{Sum}(i, j) = \text{prefix sum}(j) - \text{prefix sum}(i-1)$$

↪ we are looking for Sum 0:

$$0 = \text{prefix sum}(j) - \text{prefix sum}(i-1)$$

$$\Rightarrow \text{prefix sum}(i-1) = \text{prefix sum}(j)$$

$a \rightarrow$

2	5	-7	3	2
---	---	----	---	---

)

prefix sum

2	7	0	3	5
---	---	---	---	---

$$O(n+n+n)$$

$$\text{Time} = O(n)$$

$$\text{Space} = \underline{\underline{O(n)}}$$

$$\text{prefixsum}(x) = 0 \leftarrow \text{sum}(0, x)$$

↓  
subarray starting from 0 endy at x

final approach  $\rightarrow$  either 2 elements are same or one element  
is all out 0.

$i \neq x \neq y$

$a_{\infty} \rightarrow$

0	1	2	3	4
1	2	3	-5	6

prefixsum  $\rightarrow$

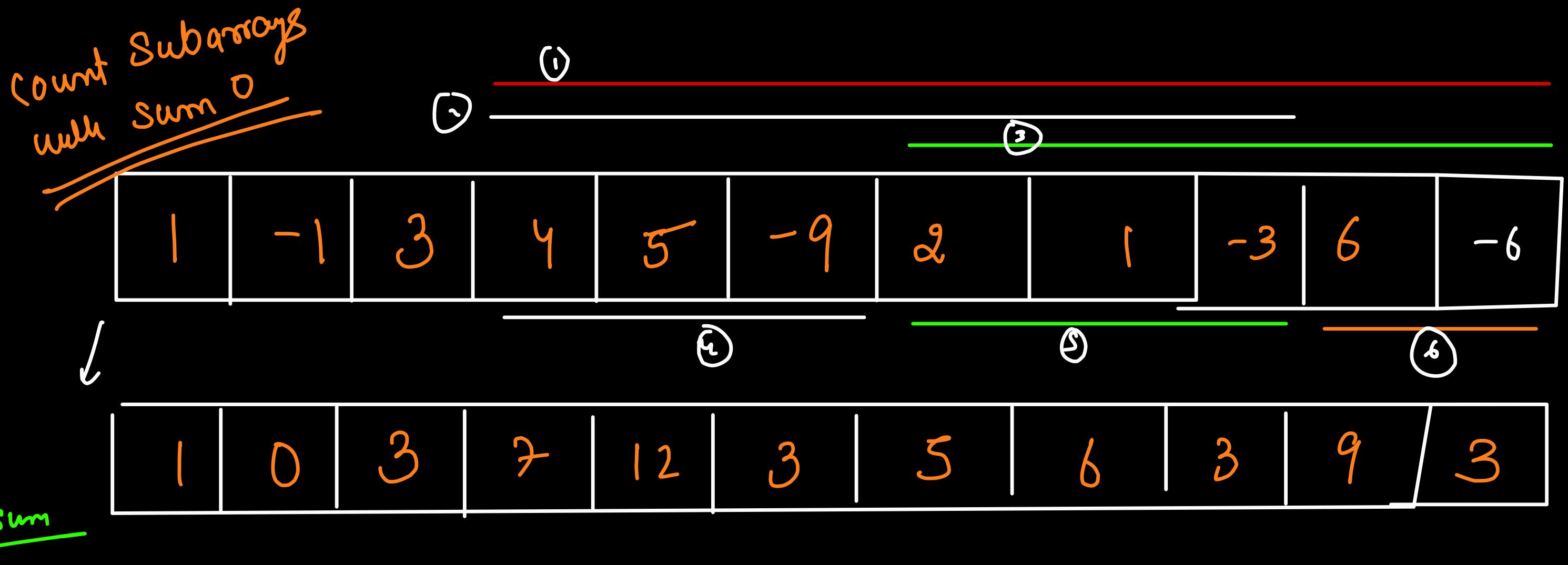
1	3	6	1	7
---	---	---	---	---

prefixsum [0] =  $a_{\infty}[0]$ ;

for ( $i=1$ ;  $i < n$ ;  $i++$ )

$\rightarrow O(n)$

prefixsum [i] = prefixsum [:i-1] +  $a_{\infty}[i]$ ;



1 : 1	5 : 1
0 : 1	6 : 1
3 : 4	9 : 1
7 : 1	
12 : 1	

① Total no. of 0's in the map tells about  
Count of prefix subarray with sum 0.

Among these 4 occ of 3 we can choose  
any 2, to form a  $[i-1, j]$  pair  
 $\rightarrow 4 \binom{2}{2} \rightarrow \frac{4!}{2!2!} \rightarrow \frac{4 \times 3}{2} \rightarrow \underline{\underline{6}}$

y

JOIN THE DASH SIDE

$\alpha \infty$

$\alpha C_2 \rightarrow$

$$\frac{\alpha \times (\alpha - 1)}{2}$$

3		1		-1		2		3		-3		7		-9		2		-1		1
---	--	---	--	----	--	---	--	---	--	----	--	---	--	----	--	---	--	----	--	---

prefix  
sum

4 3 4 3 5 8 5 12 3 5 4 5

4 3 5 8 5 12 3 5 4 5

$$\{ 3 : 3 \checkmark$$

$$5 : 9$$

$$9 : 2$$

$$8 : 1$$

$$12 : 1$$

$$3C_2 + 4C_2 + 2C_2 \rightarrow \frac{3 \times 2}{2} + \frac{4 \times 3}{2} + \frac{2 \times 1}{2}$$

$$3 + 6 + 1 = 10$$

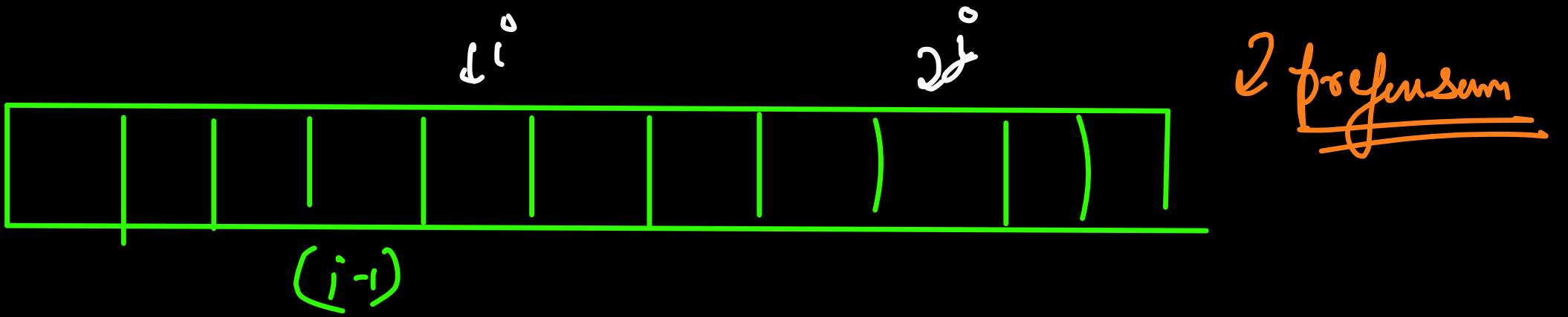
]

Sum  $\leftarrow \frac{v \times (v-1)}{2}$

$$\sum_{v \in V} \frac{v \times (v-1)}{2} \neq v \in C_{K,V} \rightarrow \boxed{v > 1}$$

Time  $\rightarrow O(n)$   
Space  $\rightarrow O(n)$

6



2 prefsum

$$\text{Sum}(i, j) = \text{prefsum}[j] - \text{prefsum}[i-1]$$

Sum of subarray from  $i$  to  $j$

if we can find two index  $(i-1)$  and  $j$  that follows this eq<sup>n</sup>  
then we can say  $\text{sum}(i, j) == k$

$$\text{sum}(i, j) = k$$

$$\text{prefsum}[j] - \text{prefsum}[i-1] = k$$

$$\text{prefsum}[i-1] = \text{prefsum}[j] - k$$

$$K=3 \quad \text{ans} \rightarrow [1, 6, 2, -5, 4, 3, -7, 7, -4] \xrightarrow{\substack{\text{ans} - 3 \\ +2}} [1, 7, 9, 4, 8, 11, 4, 11, 7]$$

~~freq map~~ - prefix  $\rightarrow [1, 7, 9, 4, 8, 11, 4, 11, 7]$

~~freq sum~~  $\rightarrow \cancel{0} \cancel{7} 9$   
 $(i-1) \leftrightarrow (j)$

$$\text{prefix}(i-1) = \text{prefix}(j) - K$$

$mp \rightarrow \{$   
 $1:1$   
 $7:1$   
 $9:1$   
 $O(n)$   
 $O(n)$   
 $\dots$   
 $\dots$

$(i-1) < j$

if ( $mp[\text{ans}[j] - K]$ )  $\leftarrow$   
 $\text{ans} \leftarrow mp[\text{ans}[j] - K];$

$\}$

[ 1, 1, 1 ]

$k=2$

[ 1, 2, 3 ]

profusion =  $\infty$

- ↳ there might be some players who never loose i.e  
always win.
- ↳ there might be some players who never player
- ↳ there might be some players who loose multiple times

State of the players

unplayed

always winning

who lost  
once

who loose  
more than  
once

$\{ [1, 6] \{ 3, 5] \}$

$\{$

$\{ x, y \}$

$\{ 2, 3 \}$

0 1 2 3 4 5 6 7 8 9 10  
 $\boxed{-1 | -1 | 2 | 1 | 0 | 1 | 0 | -1 | -1 | -1 | -1}$

win lost

$\{ 4, 5 \}$

$O(n)$   $O(\max(\text{win}, \text{lost})) < \underline{\underline{O(n)}}$

$\{ 4, 2 \}$

$\{ 6, 2 \}$

$a[i] == -1$  no match played by player  $i$ .

$a[i] == 0$  player  $i$  is winning always up till now.

$a[i] == 1$  player  $i$  lost atmost one match

$a[i] > 1$  player  $i$  lost more than one match.

if (  $a[x] == -1$  or  $a[x] == 0$  )

$a[x] = 0$

if ( $a[y] == -1$ )

$a[y] = 0;$

(else if ( $a[y] >= 0$ )

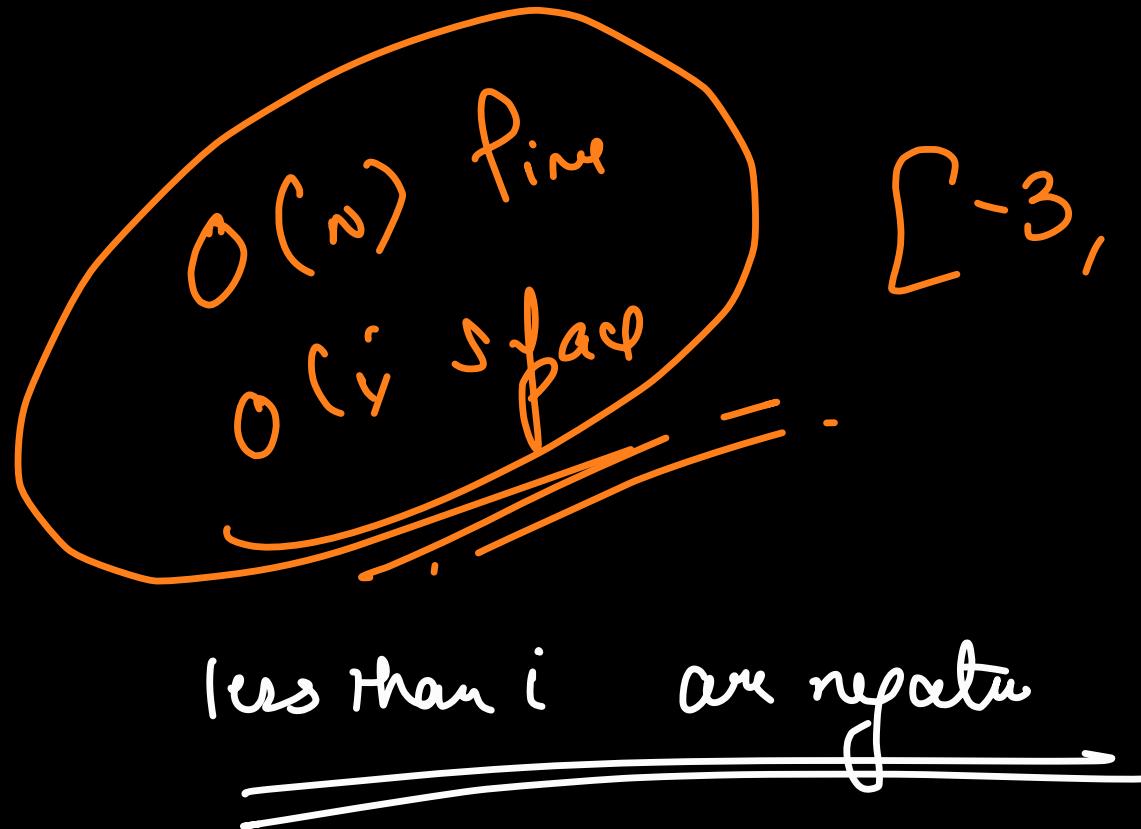
$a[y]++;$

$i$

$\left[ 1, -3, 7, \underline{-5}, \underline{7}, 8, 9 \right]$

$\underline{\underline{O(n)}}$

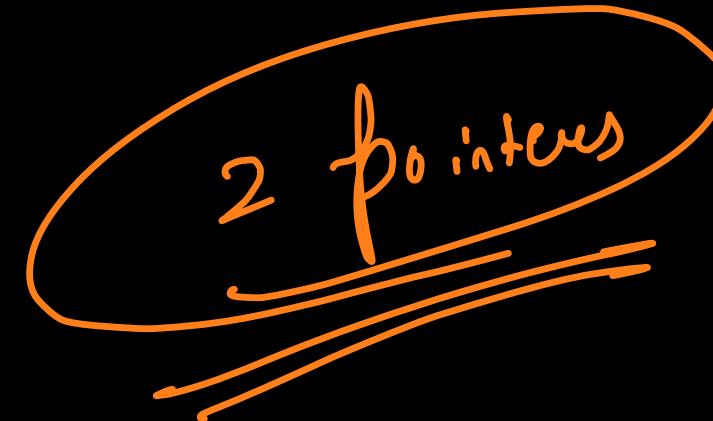
$x_{count} \Rightarrow [-3, -6, 1, 4]$

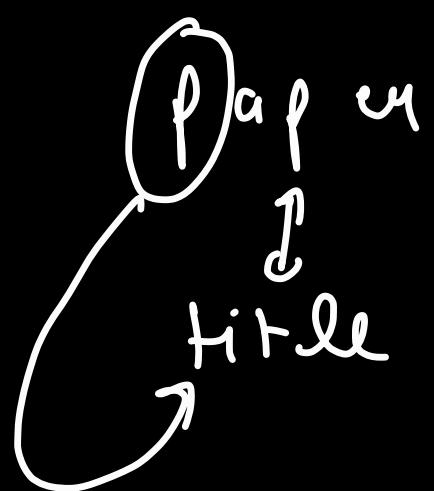
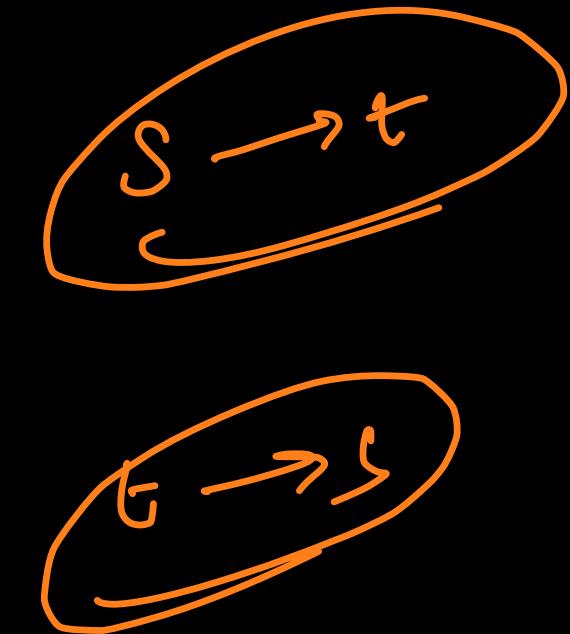


$j$

$\left[ -3, -6, -9, 1, 7, 8, 4 \right]$

$\uparrow_i^o$





{ p: t a:i, e:l, M:r }

{ t:p i:a, l:e, c:s }

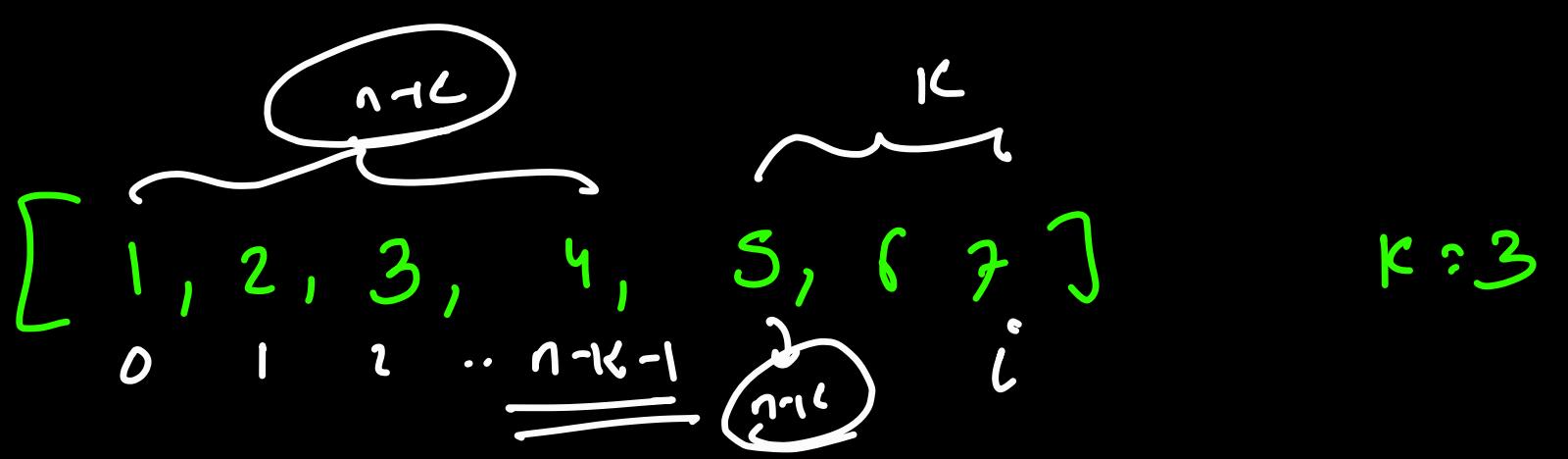
paper  
titles

$S \rightarrow$   $x \downarrow y \geq a$   $\{ x: x, y: y, \dots \}$

$L \rightarrow$   $x \downarrow y \quad x \downarrow y \quad \{ x: x, y: y, \dots \}$

$O(n)$

$O(1)$   
Space



Ans  $\Rightarrow [5, 6, 7, 1, 2, 3, 4]$

Approach 1  $\rightarrow$  Another array  $\rightarrow [?]$

$\left\{ \begin{array}{l} \text{for } (i=n-k; i < n; i+1) \\ \text{for } (i=0; i < n-k; i+1) \end{array} \right.$

$[5, 6, 7, 1, 2, 3, 4]_n$

Time  $\sim O(n)$

Space  $\sim O(1)$

