

## Question 3

**Solve the following small size problem manually to understand the working of the algorithm. Consider four training patterns, one from each region, as follows.**

- From Region1,  $X = (0, -0.5)t \in \text{NLClass1}$ . So,  $X_a = (0, -0.5, 0, 0.25)t$ .
- From Region3,  $X = (-1, -0.5)t \in \text{NLClass1}$ ;  $X_a = (-1, -0.5, 1, 0.25)t$ .
- From Region4,  $X = (-0.5, 0)t \in \text{NLClass2}$ ;  $X_a = (-0.5, 0, 0.25, 0)t$ .
- From Region2,  $X = (-0.5, -1)t \in \text{NLClass2}$ ;  $X_a = (-0.5, -1, 0.25, 1)t$ .
- Start with  $W_0 = (0,0,0,0)t$  and use the perceptron algorithm on the normalized augmented data given by  $0, -0.5, 0, 0.25$   $-1, -0.5, 1, 0.25$   $0.5, 0, -0.25, 0$   $0.5, 1, -0.25, -1$
- After some updates you will get  $W = (0.5, -0.5, 0.75, -0.75)t$ . So, the function is  $0.5x_1 - 0.5x_2 + 0.75x_3 - 0.75x_4$ .

```
In [1]: import pandas as pd
import numpy as np
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D # noqa: F401 unused import
from matplotlib import cm
import seaborn as sns
from sklearn.model_selection import train_test_split
import pdb

w = 4
h = 4
d = 70
```

```

In [3]: import pdb
cluster_list_pattern={}
Error_Threshold_List=[]

PATTERNS = 1000
FEATURES = 100

PATTERNS= 9
FEATURES = 3

cluster_leader_list= []

def perceptron_fit_x(x):

    print(x)

    #row_count = len(DataFrame.index)

    # initialize W0
    W0 = [[0,0,0,0]]
    #print('WWWWW', W0)
    WT = pd.DataFrame(W0)
    print(WT.info(), '\n')
    row_count = len(x.index)

    epoch = 0
    i = 0
    while (True):
        #print( f"\n Weight { WT[0][0]} {WT[1][0]} {WT[2][0]} {WT[3][0]}")
        dot_prod = WT.iloc[0].dot(x.iloc[i])
        print( f"\n Weight { WT[0][0]} {WT[1][0]} {WT[2][0]} {WT[3][0]} Feature Index {i} {x[0][i]}
{x[1][i]} {x[2][i]} {x[3][i]} \n dotprod {dot_prod} \n ")
        if dot_prod <= 0:
            W0 = [WT.iloc[0].add(x.iloc[i])]
            WT = pd.DataFrame(W0)
            epoch = 0
        else:
            epoch = epoch + 1

        i = i + 1
        if i >= 4 :
            i = 0

```

```

        print("-----")
    if epoch > row_count:
        break;
return

def perceptron_fit(x_data):
    # initialize W0
    W0 = [[0,0,0,0]]

    WT = pd.DataFrame(W0)
    print(WT.info(), '\n')
    row_count = len(x_data.index)

    #x = x_data.drop(['C1', 'C2', 'C3', 'C4', 'R13', 'R14', 'R24', 'R23', 'NC1', 'NC2'], axis=1)

    print( f'\n---ooooo-----print-----\n')
    x = x.reset_index(drop=True)
    print(x)
    print( f'\n---ooooo-----print----- {test_data} \n')


    #x = x.rename(columns = {'X1': '0', 'value': 'Income'}, inplace = False)

    epoch = 0
    i = 0

    feature = []
    while (True):
        nWT =WT.to_numpy()
        #print( "x----->\n", x.iloc[i])
        #print("\n WT----->\n",WT)


        nx = x.iloc[[i]].to_numpy()

        nxf = nx.flatten()
        nWTf = nWT.flatten()

        dot_prod = np.dot(nWTf,nxf)

```

```

        #print( f"\n W [ { WT[0][0]} {WT[1][0]} {WT[2][0]} {WT[3][0]} ] X Index {i} [{x[0][i]} {x[1]
[i]} {x[2][i]} {x[3][i]} ] ==> dp {dot_prod} \n ")

        # X1    X2    X1Square    X2Square
        #print( f"\n W [ { WT[0][0]} {WT[1][0]} {WT[2][0]} {WT[3][0]} ] X Index {i} [{x['X1'][i]} {x
['X2'][i]} {x['X1Square'][i]} {x['X2Square'][i]} ] ==> dp {dot_prod} \n ")

        #print(f'\n WT = {WT}')
        if dot_prod <= 0:
            W0 = np.add(nWTf,nxf)
            WT = pd.DataFrame(W0)
            epcoh = 0
        else:
            epcoh = epcoh + 1
            #return

        i = i + 1
        #if i >= 100 :
        if i >= row_count :

            i = 0
            #print("-----")
        if epcoh > row_count:
            break;

print(f' Weight Vector ==> {WT}')
```

  

```

nWT =WT.transpose().to_numpy()
nWTf = nWT.flatten()

print(f' Weight Vector ==> {nWTf[0]} , {nWTf[1]}, {nWTf[2]} , {nWTf[3]}')
```

  

```

# Test the pattern
```

  

```

a = nWTf[0]
b = nWTf[1]
c = nWTf[2]
```

```

d = nWTf[3]

for i in test_data.index:
    # Equivalently  $X \in NC1$  if  $ax1+bx2+cx21+dx2 > 0$  and  $X \in NC2$  if  $ax1+bx2+cx21+dx2 < 0$ .
    # 'X1', 'X2', 'X1Square', 'X2Square'
    val = test_data.iloc[i]['X1'] * a + test_data.iloc[i]['X2'] * b + test_data.iloc[i]['X1Square'] * c + test_data.iloc[i]['X2Square'] * d

    #val = test_data.iloc[0]['X1']
    print( f"Predict Val = {val}")

    if (val > 0):
        print("NC1 YES")
    else :
        print("NC2 NO")

    print (f'{test_data.iloc[i]}')

return WT.transpose().to_string(index=False, header=False)

data = [[1,1],[3,3],[2,2],[3,4]]
data = [[2,2],[1,1],[3,3],[3,4]]
data = [[1, 2, 2],[2, 1, 3],[3, 3, 1],[6, 1, 1],[6, 2, 3],[6, 3, 2],[6, 6, 6],[6, 6, 7],[6, 6, 8]]

data = [ [0,-0.5,0, 0.25],
[-1,-0.5, 1, 0.25],
[0.5, 0, -0.25, 0 ],
[0.5, 1, -0.25, -1] ]

DM = pd.DataFrame(data)

print('DM Matrix for Data Points ')
print(f"{DM.to_string(header=None,index=False)}")
print('\n')
Threshold = 3
perceptron_fit_x(DM)

```

DM Matrix for Data Points

```
0.0 -0.5 0.00 0.25
-1.0 -0.5 1.00 0.25
0.5 0.0 -0.25 0.00
0.5 1.0 -0.25 -1.00
```

```
      0      1      2      3
0  0.0 -0.5 0.00 0.25
1 -1.0 -0.5 1.00 0.25
2  0.5 0.0 -0.25 0.00
3  0.5 1.0 -0.25 -1.00
```

<class 'pandas.core.frame.DataFrame'>

RangeIndex: 1 entries, 0 to 0

Data columns (total 4 columns):

#	Column	Non-Null Count	Dtype
0	0	1 non-null	int64
1	1	1 non-null	int64
2	2	1 non-null	int64
3	3	1 non-null	int64

dtypes: int64(4)

memory usage: 160.0 bytes

None

Weight 0 0 0 0 Feature Index 0 0.0 -0.5 0.0 0.25  
dotprod 0.0

Weight 0.0 -0.5 0.0 0.25 Feature Index 1 -1.0 -0.5 1.0 0.25  
dotprod 0.3125

Weight 0.0 -0.5 0.0 0.25 Feature Index 2 0.5 0.0 -0.25 0.0  
dotprod 0.0

Weight 0.5 -0.5 -0.25 0.25 Feature Index 3 0.5 1.0 -0.25 -1.0  
dotprod -0.4375

-----

Weight 1.0 0.5 -0.5 -0.75 Feature Index 0 0.0 -0.5 0.0 0.25  
dotprod -0.4375

Weight 1.0 0.0 -0.5 -0.5 Feature Index 1 -1.0 -0.5 1.0 0.25  
dotprod -1.625

Weight 0.0 -0.5 0.5 -0.25 Feature Index 2 0.5 0.0 -0.25 0.0  
dotprod -0.125

Weight 0.5 -0.5 0.25 -0.25 Feature Index 3 0.5 1.0 -0.25 -1.0  
dotprod -0.0625

-----  
Weight 1.0 0.5 0.0 -1.25 Feature Index 0 0.0 -0.5 0.0 0.25  
dotprod -0.5625

Weight 1.0 0.0 0.0 -1.0 Feature Index 1 -1.0 -0.5 1.0 0.25  
dotprod -1.25

Weight 0.0 -0.5 1.0 -0.75 Feature Index 2 0.5 0.0 -0.25 0.0  
dotprod -0.25

Weight 0.5 -0.5 0.75 -0.75 Feature Index 3 0.5 1.0 -0.25 -1.0  
dotprod 0.3125

-----  
Weight 0.5 -0.5 0.75 -0.75 Feature Index 0 0.0 -0.5 0.0 0.25  
dotprod 0.0625

Weight 0.5 -0.5 0.75 -0.75 Feature Index 1 -1.0 -0.5 1.0 0.25  
dotprod 0.3125

Weight 0.5 -0.5 0.75 -0.75 Feature Index 2 0.5 0.0 -0.25 0.0

dotprod 0.0625

Weight 0.5 -0.5 0.75 -0.75 Feature Index 3 0.5 1.0 -0.25 -1.0  
dotprod 0.3125

-----

In [ ]:

In [ ]:

In [ ]:

In [ ]:

In [ ]:

In [ ]: