

```
import numpy as np
from tensorflow import keras
print (keras.__version__)
from keras.datasets import mnist
(x_train, y_train), (x_test, y_test) = mnist.load_data()
x_train_new, y_train_new = x_train[(y_train==0) | (y_train==1)], y_train[(y_train==0) | (y_train==1)]
x_train_final = x_train_new.reshape((-1, 784))
x_test_new, y_test_new = x_test[(y_test==0) | (y_test==1)], y_test[(y_test==0) | (y_test==1)]
x_test_final = x_test_new.reshape((-1, 784))
x_train_final = x_train_final / 255
x_test_final = x_test_final / 255
```

```
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, Activation, Dropout
from tensorflow.keras.utils import to_categorical, plot_model
from tensorflow.keras.datasets import mnist
```

```
from tensorflow import keras
```

```
model = Sequential()
```

```
model.add(Dense(1, input_shape=(784,)))
model.add(Activation('sigmoid'))
# this is the output for one-hot vector
#model.add(Activation('softmax'))
model.summary()
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)
```

```
model.compile(optimizer='sgd', loss='binary_crossentropy', metrics=['binary_accuracy'])
model.fit(
    x=x_train_final,
    y=y_train_new,
```

```

x = x_train_new,
shuffle=True,
epochs=5,
batch_size=16
)
eval = model.evaluate(x=x_test_final, y=y_test_new)

```

2.4.0

Model: "sequential_3"

| Layer (type) | Output Shape | Param # |
|---------------------------|--------------|---------|
| dense_8 (Dense) | (None, 1) | 785 |
| activation_1 (Activation) | (None, 1) | 0 |

Total params: 785

Trainable params: 785

Non-trainable params: 0

Epoch 1/5

792/792 [=====] - 2s 2ms/step - loss: 0.0786 - binary_accuracy: 0.9897

Epoch 2/5

792/792 [=====] - 2s 2ms/step - loss: 0.0207 - binary_accuracy: 0.9976

Epoch 3/5

792/792 [=====] - 2s 2ms/step - loss: 0.0150 - binary_accuracy: 0.9976

Epoch 4/5

792/792 [=====] - 2s 2ms/step - loss: 0.0124 - binary_accuracy: 0.9977

Epoch 5/5

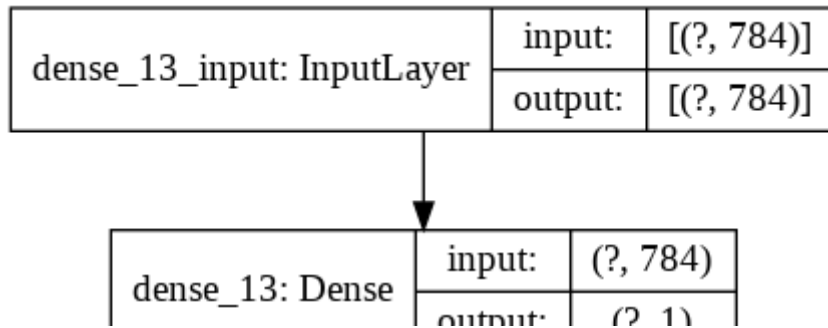
792/792 [=====] - 2s 2ms/step - loss: 0.0108 - binary_accuracy: 0.9979

67/67 [=====] - 0s 2ms/step - loss: 0.0066 - binary_accuracy: 0.9995

```

plot_model(model, to_file='mlp-mnist.png', show_shapes=True)

```



```
import numpy as np
from tensorflow.keras.datasets import mnist
import matplotlib.pyplot as plt
```

```
model = Sequential([
    InputLayer(input_shape=(784,)),
    Dense(784),
    Dense(10)
])
```

```
# load dataset
(x_train, y_train), (x_test, y_test) = mnist.load_data()
```

```
# count the number of unique train labels
unique, counts = np.unique(y_train, return_counts=True)
print("Train labels: ", dict(zip(unique, counts)))
```

```
Train labels:  {0: 5923, 1: 6742, 2: 5958, 3: 6131, 4: 5842, 5: 5421, 6: 5918, 7: 6265, 8: 5851, 9: 5949}
```

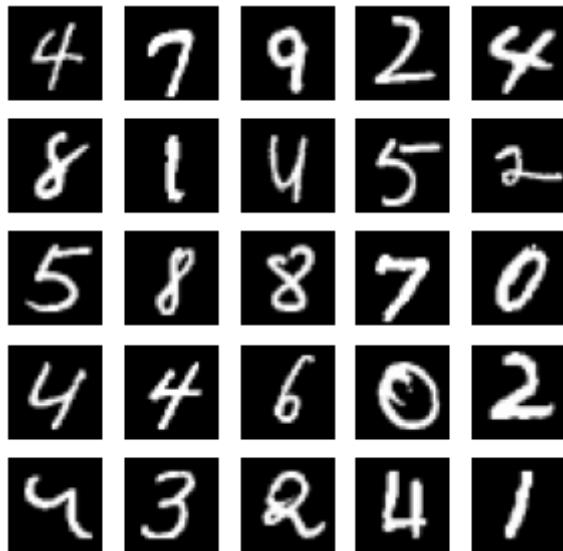
```
# count the number of unique test labels
unique, counts = np.unique(y_test, return_counts=True)
print("Test labels: ", dict(zip(unique, counts)))
```

```
Test labels:  {0: 980, 1: 1135, 2: 1032, 3: 1010, 4: 982, 5: 892, 6: 958, 7: 1028, 8: 974, 9: 1009}
```

```
# sample 25 mnist digits from train dataset
indexes = np.random.randint(0, x_train.shape[0], size=25)
images = x_train[indexes]
```

```
labels = y_train[indexes]
```

```
# plot the 25 mnist digits
plt.figure(figsize=(5,5))
for i in range(len(indexes)):
    plt.subplot(5, 5, i + 1)
    image = images[i]
    plt.imshow(image, cmap='gray')
    plt.axis('off')
```



```
plt.savefig("mnist-samples.png")
plt.show()
plt.close('all')
```

<Figure size 432x288 with 0 Axes>

```
# load mnist dataset
(x_train, y_train), (x_test, y_test) = mnist.load_data()
```

```
#print(f'{x_train}\n')
```

```
#print(1 {x_train} )
```

```
X_train = x_train  
Y_train = y_train  
X_test = x_test  
Y_test = y_test
```

```
import numpy as np
```

```
train_filter = np.where((y_train == 0 ) | (y_train == 4))  
test_filter = np.where((y_test == 0) | (y_test == 4))  
x_train, y_train = x_train[train_filter], y_train[train_filter]  
x_test, y_test = x_test[test_filter], y_test[test_filter]
```

```
#print(f'{x_train[0]}')
```

```
print('{train_filter}')
```

```
{train_filter}
```

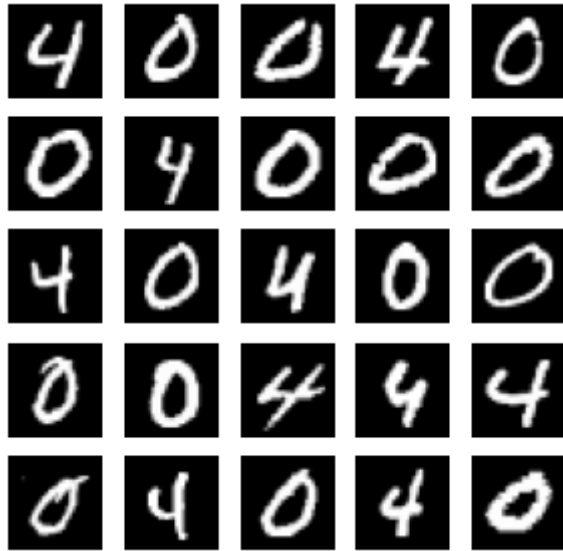
```
# sample 25 mnist digits from train dataset  
indexes = np.random.randint(0, x_train.shape[0], size=25)  
images = x_train[indexes]  
labels = y_train[indexes]
```

```
# plot the 25 mnist digits  
plt.figure(figsize=(5,5))  
for i in range(len(indexes)):  
    plt.subplot(5, 5, i + 1)  
    image = images[i]
```

```

image = images[i]
plt.imshow(image, cmap='gray')
plt.axis('off')

```



▼ minst mlp processing

```

import numpy as np
from tensorflow import keras
print (keras.__version__)
from keras.datasets import mnist
(x_train, y_train), (x_test, y_test) = mnist.load_data()
x_train_new, y_train_new = x_train[(y_train==0) | (y_train==1)], y_train[(y_train==0) | (y_train==1)]
x_train_final = x_train_new.reshape((-1, 784))
x_test_new, y_test_new = x_test[(y_test==0) | (y_test==1)], y_test[(y_test==0) | (y_test==1)]
x_test_final = x_test_new.reshape((-1, 784))
x_train_final = x_train_final / 255
x_test_final = x_test_final / 255

```

```

from tensorflow.keras.models import Sequential

```

```
from tensorflow.keras.layers import Dense, Activation, Dropout
from tensorflow.keras.utils import to_categorical, plot_model
from tensorflow.keras.datasets import mnist
```

```
from tensorflow import keras
```

```
model = Sequential()
model.add(Dense(12, input_shape=(784,), activation='relu'))
model.add(Dense(8, activation='relu'))
model.add(Dense(1, activation='sigmoid'))
```

```
model.summary()
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)
```

```
model.compile(optimizer='sgd', loss='binary_crossentropy', metrics=['binary_accuracy'])
model.fit(
    x=x_train_final,
    y=y_train_new,
    shuffle=True,
    epochs=5,
    batch_size=16
)
eval = model.evaluate(x=x_test_final, y=y_test_new)
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)
```

2.4.0

Model: "sequential_4"

| Layer (type) | Output Shape | Param # |
|------------------|--------------|---------|
| dense_9 (Dense) | (None, 12) | 9420 |
| dense_10 (Dense) | (None, 8) | 104 |
| dense_11 (Dense) | (None, 1) | 9 |

Total params: 9,533

Trainable params: 9,533

Non-trainable params: 0

Epoch 1/5

792/792 [=====] - 2s 2ms/step - loss: 0.1036 - binary_accuracy: 0.9840

Epoch 2/5

792/792 [=====] - 2s 2ms/step - loss: 0.0096 - binary_accuracy: 0.9979

Epoch 3/5

792/792 [=====] - 2s 2ms/step - loss: 0.0065 - binary_accuracy: 0.9984

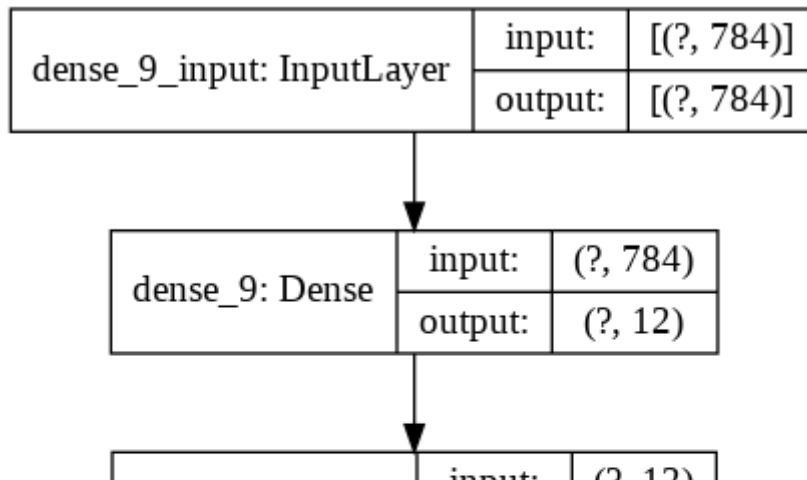
Epoch 4/5

792/792 [=====] - 2s 2ms/step - loss: 0.0053 - binary_accuracy: 0.9987

Epoch 5/5

792/792 [=====] - 2s 2ms/step - loss: 0.0046 - binary_accuracy: 0.9986

67/67 [=====] - 0s 2ms/step - loss: 0.0023 - binary_accuracy: 0.9995



validate the model on test dataset to determine generalization


```
_, acc = model.evaluate(x_test_final,
                        y_test_new,
                        batch_size=128,
                        verbose=0)
print("\nTest accuracy: %.1f%%" % (100.0 * acc))
```

Test accuracy: 100.0%

```
import numpy as np
from tensorflow import keras
print (keras.__version__)
from keras.datasets import mnist
(x_train, y_train), (x_test, y_test) = mnist.load_data()
x_train_new, y_train_new = x_train[(y_train==0) | (y_train==1)], y_train[(y_train==0) | (y_train==1)]
x_train_final = x_train_new.reshape((-1, 784))
x_test_new, y_test_new = x_test[(y_test==0) | (y_test==1)], y_test[(y_test==0) | (y_test==1)]
x_test_final = x_test_new.reshape((-1, 784))
x_train_final = x_train_final / 255
x_test_final = x_test_final / 255
```

```
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, Activation, Dropout
from tensorflow.keras.utils import to_categorical, plot_model
from tensorflow.keras.datasets import mnist
```

```
from tensorflow import keras
```

```
model = Sequential()
model.add(Dense(12, input_shape=(784,), activation='relu'))
model.add(Dense(8, activation='relu'))
model.add(Dense(4, activation='relu'))
model.add(Dense(1, activation='sigmoid'))
```

```
model.summary()
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)
```

```
model.compile(optimizer='sgd', loss='binary_crossentropy', metrics=['binary_accuracy'])
model.fit(
    x=x_train_final,
    y=y_train_new,
    shuffle=True,
    epochs=5,
    batch_size=16
)
eval = model.evaluate(x=x_test_final, y=y_test_new)
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)
```

2.4.0

Model: "sequential_5"

| Layer (type) | Output Shape | Param # |
|------------------|--------------|---------|
| dense_12 (Dense) | (None, 12) | 9420 |
| dense_13 (Dense) | (None, 8) | 104 |
| dense_14 (Dense) | (None, 4) | 36 |
| dense_15 (Dense) | (None, 1) | 5 |

Total params: 9,565

Trainable params: 9,565

Non-trainable params: 0

Epoch 1/5

792/792 [=====] - 2s 2ms/step - loss: 0.1052 - binary_accuracy: 0.9853

Epoch 2/5

792/792 [=====] - 2s 2ms/step - loss: 0.0081 - binary_accuracy: 0.9979

Epoch 3/5

792/792 [=====] - 2s 2ms/step - loss: 0.0053 - binary_accuracy: 0.9985

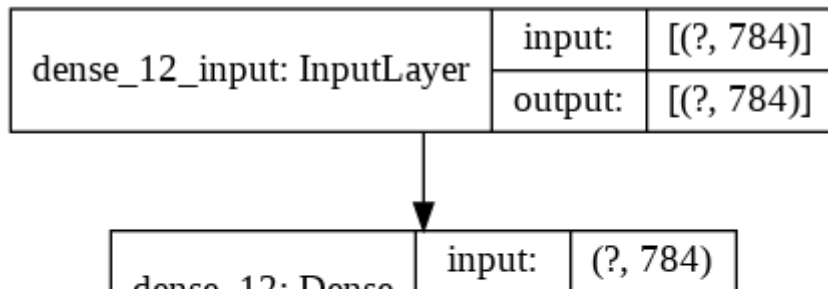
Epoch 4/5

792/792 [=====] - 2s 2ms/step - loss: 0.0042 - binary_accuracy: 0.9989

Epoch 5/5

792/792 [=====] - 2s 2ms/step - loss: 0.0036 - binary_accuracy: 0.9991

67/67 [=====] - 0s 2ms/step - loss: 0.0020 - binary_accuracy: 0.9995



Double-click (or enter) to edit

|

validate the model on test dataset to determine generalization

model.evaluate(test_data_loader)

```
_, acc = model.evaluate(x_test_final,
                        y_test_new,
                        batch_size=128,
                        verbose=0)
print("\nTest accuracy: %.1f%%" % (100.0 * acc))
```

Test accuracy: 100.0%

|

| dense_15: Dense | 128 | 0.45 |

Double-click (or enter) to edit

1. Task 1: Here you need to use MLP for classification. (a) Use the pair of classes, of MNIST data used by you in assignment 5, with around 6000 training patterns per class. So, you will have 12000 training patterns totally. Train an MLP each with 1, 2, 3 and 4 hidden layers using Backpropagation. (b) Take 2000 test patterns (1000 per class) and classify using the networks trained in (a). Compute the classification accuracy on the test patterns. (c) Pick the best MLP based on (a) and (b) and vary the following:
 - i. Number of nodes in the hidden layers.
 - ii. Tanh, Relu, and Logistic activation functions
 - iii. Hyperparameters: Momentum term, Early stopping, and Learning Rate
 (d) Report the classification accuracies obtained and analyse.

```
import numpy
from sklearn.model_selection import GridSearchCV
from keras.models import Sequential
from keras.layers import Dense
from keras.wrappers.scikit_learn import KerasClassifier
# Function to create model, required for KerasClassifier
def create_model():
```

```

model = Sequential()
model.add(Dense(12, input_shape=(784,), activation='relu'))
model.add(Dense(8, activation='relu'))
model.add(Dense(4, activation='relu'))
model.add(Dense(1, activation='sigmoid'))
model.compile(loss='binary_crossentropy', optimizer='adam', metrics=['accuracy'])
return model

model = KerasClassifier(build_fn=create_model, verbose=0)
# define the grid search parameters
batch_size = [10,20]
epochs = [10, 50]
#optimizer = ['SGD', 'RMSprop', 'Adagrad', 'Adadelta', 'Adam', 'Adamax', 'Nadam']
learn_rate = [0.001, 0.01, 0.1, 0.2, 0.3]
momentum = [0.0, 0.2, 0.4, 0.6, 0.8, 0.9]

param_grid = dict(batch_size=batch_size, epochs=epochs)
#grid = GridSearchCV(estimator=model, param_grid=param_grid, n_jobs=-1, cv=3)
#param_grid = dict(optimizer=optimizer)

from sklearn.model_selection import RandomizedSearchCV
parameters = {'batch_size':[5,10],
              'nb_epoch':[10,20,50],
              #'optimizer':['adam','rmsprop','SGD'],
              #'kernel_initializer':['random_uniform'],
              #'units':[4,8,13]
              }
#random_search= RandomizedSearchCV(estimator=model, param_distributions=parameters,n_iter=20,n_jobs=-1,cv=5)

grid = GridSearchCV(estimator=model, param_grid=parameters, n_jobs=-1, cv=3)
X = x_train_final
Y=y_train_new
grid_result = grid.fit(X, Y)
# summarize results
print("Best: %f using %s" % (grid_result.best_score_, grid_result.best_params_))
means = grid_result.cv_results_['mean_test_score']

```

```
stds = grid_result.cv_results_['std_test_score']
params = grid_result.cv_results_['params']
for mean, stdev, param in zip(means, stds, params):
    print("%f (%f) with: %r" % (mean, stdev, param))
```

```
Best: 0.998816 using {'batch_size': 10, 'nb_epoch': 10}
0.998026 (0.000487) with: {'batch_size': 5, 'nb_epoch': 10}
0.997552 (0.000487) with: {'batch_size': 5, 'nb_epoch': 20}
0.998737 (0.000805) with: {'batch_size': 5, 'nb_epoch': 50}
0.998816 (0.000670) with: {'batch_size': 10, 'nb_epoch': 10}
0.997947 (0.001116) with: {'batch_size': 10, 'nb_epoch': 20}
0.998421 (0.000487) with: {'batch_size': 10, 'nb_epoch': 50}
```

```
# i. Number of nodes in the hidden layers.
```

```
/usr/local/lib/python3.6/dist-packages/sklearn/model_selection/_search.py:281: UserWarning: The total space o
 % (grid_size, self.n_iter, grid_size), UserWarning)
Best score obtained: -0.20594636561788607
Parameters:
```

```
# i. Number of nodes in the hidden layers.
```

```
node_list = [ 12,24,36,48,60]
for node in node_list :
```

```
import numpy as np
from tensorflow import keras
print (keras.__version__)
from keras.datasets import mnist
(x_train, y_train), (x_test, y_test) = mnist.load_data()
x_train_new, y_train_new = x_train[(y_train==0) | (y_train==1)], y_train[(y_train==0) | (y_train==1)]
x_train_final = x_train_new.reshape((-1, 784))
x_test_new, y_test_new = x_test[(y_test==0) | (y_test==1)], y_test[(y_test==0) | (y_test==1)]
x_test_final = x_test_new.reshape((-1, 784))
```

```
x_train_final = x_train_final / 255
x_test_final = x_test_final / 255
```

```
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, Activation, Dropout
from tensorflow.keras.utils import to_categorical, plot_model
from tensorflow.keras.datasets import mnist
```

```
from tensorflow import keras
```

```
print(f" Processing - Node changes { node}")
model = Sequential()
model.add(Dense(node , input_shape=(784,), activation='relu'))
model.add(Dense(node -4, activation='relu'))
model.add(Dense(node - 8, activation='relu'))
model.add(Dense( 1, activation='sigmoid'))
```

```
model.summary()
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)
```

```
model.compile(optimizer='sgd', loss='binary_crossentropy', metrics=['binary_accuracy'])
model.fit(
    x=x_train_final,
    y=y_train_new,
    shuffle=True,
    epochs=5,
    batch_size=16
)
eval = model.evaluate(x=x_test_final, y=y_test_new)
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)
```

2.4.0

Processing - Node changes 12

Model: "sequential_1"

| Layer (type) | Output Shape | Param # |
|-----------------|--------------|---------|
| dense_4 (Dense) | (None, 12) | 9420 |
| dense_5 (Dense) | (None, 8) | 104 |
| dense_6 (Dense) | (None, 4) | 36 |
| dense_7 (Dense) | (None, 1) | 5 |

Total params: 9,565

Trainable params: 9,565

Non-trainable params: 0

Epoch 1/5

792/792 [=====] - 2s 2ms/step - loss: 0.1548 - binary_accuracy: 0.9641

Epoch 2/5

792/792 [=====] - 2s 2ms/step - loss: 0.0086 - binary_accuracy: 0.9979

Epoch 3/5

792/792 [=====] - 2s 2ms/step - loss: 0.0055 - binary_accuracy: 0.9985

Epoch 4/5

792/792 [=====] - 2s 2ms/step - loss: 0.0044 - binary_accuracy: 0.9987

Epoch 5/5

792/792 [=====] - 2s 2ms/step - loss: 0.0038 - binary_accuracy: 0.9989

67/67 [=====] - 0s 2ms/step - loss: 0.0017 - binary_accuracy: 0.9995

2.4.0

Processing - Node changes 24

Model: "sequential_2"

| Layer (type) | Output Shape | Param # |
|------------------|--------------|---------|
| dense_8 (Dense) | (None, 24) | 18840 |
| dense_9 (Dense) | (None, 20) | 500 |
| dense_10 (Dense) | (None, 16) | 336 |
| dense_11 (Dense) | (None, 1) | 17 |

Total params: 19,693
Trainable params: 19,693
Non-trainable params: 0

```
Epoch 1/5
792/792 [=====] - 2s 2ms/step - loss: 0.0605 - binary_accuracy: 0.9957
Epoch 2/5
792/792 [=====] - 2s 2ms/step - loss: 0.0070 - binary_accuracy: 0.9984
Epoch 3/5
792/792 [=====] - 2s 2ms/step - loss: 0.0050 - binary_accuracy: 0.9985
Epoch 4/5
792/792 [=====] - 2s 2ms/step - loss: 0.0041 - binary_accuracy: 0.9987
Epoch 5/5
792/792 [=====] - 2s 2ms/step - loss: 0.0035 - binary_accuracy: 0.9990
67/67 [=====] - 0s 2ms/step - loss: 0.0019 - binary_accuracy: 0.9995
```

▼ New Section

Tanh, Relu, and Logistic activation functions.

```
fn_list = [ "tanh", "relu","sigmoid"]
for fn in fn_list :

    import numpy as np
    from tensorflow import keras
    print (keras.__version__)
    from keras.datasets import mnist
    (x_train, y_train), (x_test, y_test) = mnist.load_data()
    x_train_new, y_train_new = x_train[(y_train==0) | (y_train==1)], y_train[(y_train==0) | (y_train==1)]
    x_train_final = x_train_new.reshape((-1, 784))
    x_test_new, y_test_new = x_test[(y_test==0) | (y_test==1)], y_test[(y_test==0) | (y_test==1)]
    x_test_final = x_test_new.reshape((-1, 784))
    x_train_final = x_train_final / 255
    x_test_final = x_test_final / 255
```

```
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, Activation, Dropout
from tensorflow.keras.utils import to_categorical, plot_model
from tensorflow.keras.datasets import mnist
```

```
from tensorflow import keras
```

```
print(f" Processing - activation function  changes { fn }")
model = Sequential()
node = 16 # No. of nodes - fixed
model.add(Dense(node , input_shape=(784,), activation=fn))
model.add(Dense(node -4, activation=fn))
model.add(Dense(node - 8, activation=fn))
model.add(Dense( 1, activation=fn))
```

```
model.summary()
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)
```

```
model.compile(optimizer='sgd', loss='binary_crossentropy', metrics=['binary_accuracy'])
model.fit(
    x=x_train_final,
    y=y_train_new,
    shuffle=True,
    epochs=5,
    batch_size=16
)
eval = model.evaluate(x=x_test_final, y=y_test_new)
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)
```

2.4.0

Processing - activation function changes tanh

Model: "sequential_6"

| Layer (type) | Output Shape | Param # |
|------------------|--------------|---------|
| dense_24 (Dense) | (None, 16) | 12560 |
| dense_25 (Dense) | (None, 12) | 204 |
| dense_26 (Dense) | (None, 8) | 104 |
| dense_27 (Dense) | (None, 1) | 9 |

Total params: 12,877

Trainable params: 12,877

Non-trainable params: 0

Epoch 1/5

792/792 [=====] - 2s 2ms/step - loss: 0.0238 - binary_accuracy: 0.9962

Epoch 2/5

792/792 [=====] - 2s 2ms/step - loss: 0.0102 - binary_accuracy: 0.9990

Epoch 3/5

792/792 [=====] - 2s 2ms/step - loss: 0.0094 - binary_accuracy: 0.9987

Epoch 4/5

792/792 [=====] - 2s 2ms/step - loss: 0.0088 - binary_accuracy: 0.9990

Epoch 5/5

792/792 [=====] - 2s 2ms/step - loss: 0.0079 - binary_accuracy: 0.9992

67/67 [=====] - 0s 2ms/step - loss: 0.0103 - binary_accuracy: 0.9981

2.4.0

Processing - activation function changes relu

Model: "sequential_7"

| Layer (type) | Output Shape | Param # |
|------------------|--------------|---------|
| dense_28 (Dense) | (None, 16) | 12560 |
| dense_29 (Dense) | (None, 12) | 204 |
| dense_30 (Dense) | (None, 8) | 104 |
| dense_31 (Dense) | (None, 1) | 9 |

Total params: 12,877

Trainable params: 12,877

Non-trainable params: 0

```
Epoch 1/5
792/792 [=====] - 2s 2ms/step - loss: 0.0297 - binary_accuracy: 0.9931
Epoch 2/5
792/792 [=====] - 2s 2ms/step - loss: 0.0116 - binary_accuracy: 0.9987
Epoch 3/5
792/792 [=====] - 2s 2ms/step - loss: 0.0060 - binary_accuracy: 0.9984
Epoch 4/5
792/792 [=====] - 2s 2ms/step - loss: 0.0056 - binary_accuracy: 0.9991
Epoch 5/5
792/792 [=====] - 2s 2ms/step - loss: 0.0047 - binary_accuracy: 0.9988
67/67 [=====] - 0s 2ms/step - loss: 0.0100 - binary_accuracy: 0.9991
```

#Hyperparameters: Momentum term, Early stopping, and Learning Rate

```
from keras import backend as K
```

```
learning_rate_list = [ 0.001, 0.010, 0.1, 1]
```

```
for l_r in learning_rate_list:
```

```
    import numpy as np
    from tensorflow import keras
    print (keras.__version__)
    from keras.datasets import mnist
    (x_train, y_train), (x_test, y_test) = mnist.load_data()
    x_train_new, y_train_new = x_train[(y_train==0) | (y_train==1)], y_train[(y_train==0) | (y_train==1)]
    x_train_final = x_train_new.reshape((-1, 784))
    x_test_new, y_test_new = x_test[(y_test==0) | (y_test==1)], y_test[(y_test==0) | (y_test==1)]
    x_test_final = x_test_new.reshape((-1, 784))
    x_train_final = x_train_final / 255
    x_test_final = x_test_final / 255
```

```

from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, Activation, Dropout
from tensorflow.keras.utils import to_categorical, plot_model
from tensorflow.keras.datasets import mnist

from tensorflow import keras

print(f" Processing - learning rate  changes { l_r }")
model = Sequential()
node = 16 # No. of nodes - fixed

model.add(Dense(node , input_shape=(784,), activation=fn))
model.add(Dense(node -4, activation=fn))
model.add(Dense(node - 8, activation=fn))
model.add(Dense( 1, activation=fn))


model.summary()
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)


print (f'model {model}')

keras.optimizers.Adam(lr=l_r)

#K.set_value(model.optimizer.learning_rate, l_r)


model.compile(optimizer='adam', loss='binary_crossentropy', metrics=['binary_accuracy'])
model.fit(
    x=x_train_final,
    y=y_train_new,
    shuffle=True,
    epochs=5

```

```

epochs=5,
batch_size=16
)
eval = model.evaluate(x=x_test_final, y=y_test_new)
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)

```

2.4.0

Processing - learning rate changes 0.1
Model: "sequential_21"

| Layer (type) | Output Shape | Param # |
|------------------|--------------|---------|
| dense_84 (Dense) | (None, 16) | 12560 |
| dense_85 (Dense) | (None, 12) | 204 |
| dense_86 (Dense) | (None, 8) | 104 |
| dense_87 (Dense) | (None, 1) | 9 |

Total params: 12,877
Trainable params: 12,877
Non-trainable params: 0

model <tensorflow.python.keras.engine.sequential.Sequential object at 0x7f0851a3dac8>
Epoch 1/5

792/792 [=====] - 2s 2ms/step - loss: 0.2745 - binary_accuracy: 0.9721
Epoch 2/5
792/792 [=====] - 2s 2ms/step - loss: 0.0388 - binary_accuracy: 0.9988
Epoch 3/5
792/792 [=====] - 2s 2ms/step - loss: 0.0166 - binary_accuracy: 0.9992
Epoch 4/5
792/792 [=====] - 2s 2ms/step - loss: 0.0096 - binary_accuracy: 0.9994
Epoch 5/5
792/792 [=====] - 2s 2ms/step - loss: 0.0070 - binary_accuracy: 0.9993
67/67 [=====] - 0s 2ms/step - loss: 0.0070 - binary_accuracy: 0.9991

2.4.0

Processing - learning rate changes 1
Model: "sequential_22"

| Layer (type) | Output Shape | Param # |
|------------------|--------------|---------|
| dense_88 (Dense) | (None, 16) | 12560 |

| | | |
|------------------|------------|-----|
| dense_89 (Dense) | (None, 12) | 204 |
| dense_90 (Dense) | (None, 8) | 104 |
| dense_91 (Dense) | (None, 1) | 9 |

=====
Total params: 12,877
Trainable params: 12,877
Non-trainable params: 0

```
model <tensorflow.python.keras.engine.sequential.Sequential object at 0x7f0852b86d30>
Epoch 1/5
792/792 [=====] - 2s 2ms/step - loss: 0.2457 - binary_accuracy: 0.9464
Epoch 2/5
792/792 [=====] - 2s 2ms/step - loss: 0.0348 - binary_accuracy: 0.9987
Epoch 3/5
792/792 [=====] - 2s 2ms/step - loss: 0.0152 - binary_accuracy: 0.9991
Epoch 4/5
792/792 [=====] - 2s 2ms/step - loss: 0.0088 - binary_accuracy: 0.9995
Epoch 5/5
792/792 [=====] - 2s 2ms/step - loss: 0.0068 - binary_accuracy: 0.9993
```

```
from keras import backend as K

learning_rate_list = [ 0.001, 0.010, 0.1, 1]

for l_r in learning_rate_list:

    import numpy as np
    from tensorflow import keras
    print (keras.__version__)
    from keras.datasets import mnist
    (x_train, y_train), (x_test, y_test) = mnist.load_data()
    x_train_new, y_train_new = x_train[(y_train==0) | (y_train==1)], y_train[(y_train==0) | (y_train==1)]
    x_train_final = x_train_new.reshape((-1, 784))
    x_test_new, y_test_new = x_test[(y_test==0) | (y_test==1)], y_test[(y_test==0) | (y_test==1)]
    x_test_final = x_test_new.reshape((-1, 784))
    x_train_final = x_train_final / 255
    x_test_final = x_test_final / 255
```

```

from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, Activation, Dropout
from tensorflow.keras.utils import to_categorical, plot_model
from tensorflow.keras.datasets import mnist

from tensorflow import keras

print(f" Processing - learning rate  changes { l_r }")
model = Sequential()
node = 16 # No. of nodes - fixed

model.add(Dense(node , input_shape=(784,), activation=fn))
model.add(Dense(node -4, activation=fn))
model.add(Dense(node - 8, activation=fn))
model.add(Dense( 1, activation=fn))


model.summary()
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)


print (f'model {model}')


opt = keras.optimizers.Adam(lr=l_r)

#K.set_value(model.optimizer.learning_rate, l_r)


model.compile(optimizer=opt, loss='binary_crossentropy', metrics=['binary_accuracy'])
model.fit(
    x=x_train_final,
    y=y_train_new,
    #callbacks=callbacks

```



```

    snurle=True,
    epochs=5,
    batch_size=16
)
eval = model.evaluate(x=x_test_final, y=y_test_new)
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)

```

2.4.0

Processing - learning rate changes 0.001

Model: "sequential_29"

| Layer (type) | Output Shape | Param # |
|-------------------|--------------|---------|
| dense_116 (Dense) | (None, 16) | 12560 |
| dense_117 (Dense) | (None, 12) | 204 |
| dense_118 (Dense) | (None, 8) | 104 |
| dense_119 (Dense) | (None, 1) | 9 |

Total params: 12,877

Trainable params: 12,877

Non-trainable params: 0

model <tensorflow.python.keras.engine.sequential.Sequential object at 0x7f08529e1cc0>

Epoch 1/5

792/792 [=====] - 2s 2ms/step - loss: 0.2486 - binary_accuracy: 0.9589

Epoch 2/5

792/792 [=====] - 2s 2ms/step - loss: 0.0343 - binary_accuracy: 0.9990

Epoch 3/5

792/792 [=====] - 2s 2ms/step - loss: 0.0144 - binary_accuracy: 0.9994

Epoch 4/5

792/792 [=====] - 2s 2ms/step - loss: 0.0093 - binary_accuracy: 0.9991

Epoch 5/5

792/792 [=====] - 2s 2ms/step - loss: 0.0062 - binary_accuracy: 0.9994

67/67 [=====] - 0s 2ms/step - loss: 0.0052 - binary_accuracy: 0.9995

2.4.0

Processing - learning rate changes 0.01

Model: "sequential_30"

| Layer (type) | Output Shape | Param # |
|--------------|--------------|---------|
| ===== | ===== | ===== |

| | | |
|-------------------|------------|-------|
| dense_120 (Dense) | (None, 16) | 12560 |
| dense_121 (Dense) | (None, 12) | 204 |
| dense_122 (Dense) | (None, 8) | 104 |
| dense_123 (Dense) | (None, 1) | 9 |
| ===== | | |

Total params: 12,877
Trainable params: 12,877
Non-trainable params: 0

```
model <tensorflow.python.keras.engine.sequential.Sequential object at 0x7f085e4f3208>
Epoch 1/5
792/792 [=====] - 2s 2ms/step - loss: 0.0495 - binary_accuracy: 0.9952
Epoch 2/5
792/792 [=====] - 2s 2ms/step - loss: 0.0072 - binary_accuracy: 0.9987
Epoch 3/5
792/792 [=====] - 2s 3ms/step - loss: 0.0055 - binary_accuracy: 0.9985
Epoch 4/5
792/792 [=====] - 2s 2ms/step - loss: 0.0050 - binary_accuracy: 0.9987
Epoch 5/5
792/792 [=====] - 2s 2ms/step - loss: 0.0021 - binary_accuracy: 0.9993
```

```
from keras import backend as K
```

```
momentum_list = [ 0.0, 0.2, 0.4, 0.9]
```

```
for momentum in momentum_list:
```

```
import numpy as np
from tensorflow import keras
print (keras.__version__)
from keras.datasets import mnist
(x_train, y_train), (x_test, y_test) = mnist.load_data()
x_train_new, y_train_new = x_train[(y_train==0) | (y_train==1)], y_train[(y_train==0) | (y_train==1)]
x_train_final = x_train_new.reshape((-1, 784))
x_test_new, y_test_new = x_test[(y_test==0) | (y_test==1)], y_test[(y_test==0) | (y_test==1)]
x_test_final = x_test_new.reshape((-1, 784))
x_train_final = x_train_final / 255
```

```
x_test_final = x_test_final / 255
```

```
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, Activation, Dropout
from tensorflow.keras.utils import to_categorical, plot_model
from tensorflow.keras.datasets import mnist
```

```
from tensorflow import keras
```

```
print(f" Processing - momemtum  changes { momentum }")
```

```
model = Sequential()
```

```
node = 16 # No. of nodes - fixed
```

```
model.add(Dense(node , input_shape=(784,), activation=fn))
```

```
model.add(Dense(node -4, activation=fn))
```

```
model.add(Dense(node - 8, activation=fn))
```

```
model.add(Dense( 1, activation=fn))
```

```
model.summary()
```

```
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)
```

```
print (f'model {model}')
```

```
l_r = 1
```

```
opt=keras.optimizers.SGD(lr=l_r, momentum=momentum)
```

```
#optimizer.momentum.set_value(0.04)
```

```
#K.set_value(model.optimizer.learning_rate, l_r)
```

```
#opt = keras.optimizers.Adam(momentum=0.9)
```

```
#model.compile(..., optimizer=opt)
```

```

model.compile(optimizer=opt, loss='binary_crossentropy', metrics=['binary_accuracy'])
model.fit(
    x=x_train_final,
    y=y_train_new,
    shuffle=True,
    epochs=5,
    batch_size=16
)
eval = model.evaluate(x=x_test_final, y=y_test_new)
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)

```

2.4.0

Processing - momentum changes 0.4

Model: "sequential_44"

| Layer (type) | Output Shape | Param # |
|-------------------|--------------|---------|
| dense_176 (Dense) | (None, 16) | 12560 |
| dense_177 (Dense) | (None, 12) | 204 |
| dense_178 (Dense) | (None, 8) | 104 |
| dense_179 (Dense) | (None, 1) | 9 |

=====
Total params: 12,877

Trainable params: 12,877

Non-trainable params: 0

=====
model <tensorflow.python.keras.engine.sequential.Sequential object at 0x7f08fdda52b0>

Epoch 1/5

792/792 [=====] - 2s 2ms/step - loss: 0.0465 - binary_accuracy: 0.9758

Epoch 2/5

792/792 [=====] - 2s 2ms/step - loss: 0.0068 - binary_accuracy: 0.9983

Epoch 3/5

792/792 [=====] - 2s 2ms/step - loss: 0.0024 - binary_accuracy: 0.9994

Epoch 4/5

792/792 [=====] - 2s 2ms/step - loss: 0.0027 - binary_accuracy: 0.9993

Epoch 5/5

792/792 [=====] - 2s 2ms/step - loss: 0.0037 - binary_accuracy: 0.9989

67/67 [=====] - 0s 2ms/step - loss: 0.0054 - binary_accuracy: 0.9981

2 4 0

2.4.0

Processing - momentum changes 0.9

Model: "sequential_45"

| Layer (type) | Output Shape | Param # |
|-------------------|--------------|---------|
| dense_180 (Dense) | (None, 16) | 12560 |
| dense_181 (Dense) | (None, 12) | 204 |
| dense_182 (Dense) | (None, 8) | 104 |
| dense_183 (Dense) | (None, 1) | 9 |

Total params: 12,877

Trainable params: 12,877

Non-trainable params: 0

model <tensorflow.python.keras.engine.sequential.Sequential object at 0x7f0852c22d68>

Epoch 1/5

792/792 [=====] - 2s 2ms/step - loss: 0.0374 - binary_accuracy: 0.9848

Epoch 2/5

792/792 [=====] - 2s 2ms/step - loss: 0.0120 - binary_accuracy: 0.9968

Epoch 3/5

792/792 [=====] - 2s 2ms/step - loss: 0.0110 - binary_accuracy: 0.9969

Epoch 4/5

792/792 [=====] - 2s 2ms/step - loss: 0.0054 - binary_accuracy: 0.9981

Epoch 5/5

792/792 [=====] - 2s 2ms/step - loss: 0.0042 - binary_accuracy: 0.9986

```
early_stopping_list = [ 'min', 'max', 'auto' ]
```

```
for e_s in early_stopping_list:
```

```
import numpy as np
```

```
from tensorflow import keras
```

```
print (keras.__version__)
```

```
from keras.datasets import mnist
```

```
(x_train, y_train), (x_test, y_test) = mnist.load_data()
```

```
x_train_new, y_train_new = x_train[(y_train==0) | (y_train==1)], y_train[(y_train==0) | (y_train==1)]
```

```
x_train_final = x_train_new.reshape((-1, 784))
```

```
x_test_new, y_test_new = x_test[(y_test==0) | (y_test==1)], y_test[(y_test==0) | (y_test==1)]
x_test_final = x_test_new.reshape((-1, 784))
x_train_final = x_train_final / 255
x_test_final = x_test_final / 255
```

```
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, Activation, Dropout
from tensorflow.keras.utils import to_categorical, plot_model
from tensorflow.keras.datasets import mnist
```

```
from tensorflow import keras as k
```

```
print(f" Processing - early stopping  changes { e_s }")
model = Sequential()
node = 16 # No. of nodes - fixed
fn = 'sigmoid'
```

```
model.add(Dense(node , input_shape=(784,)), activation=fn))
model.add(Dense(node -4, activation=fn))
model.add(Dense(node - 8, activation=fn))
model.add(Dense( 1, activation=fn))
```

```
model.summary()
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)
```

```
print (f'model {model}')
```

```
callback = k.callbacks.EarlyStopping(
#monitor='binary_accuracy', min_delta=0.0001,
monitor='accuracy', min_delta=0.0001,

patience=1)
```

```

l_r = 1
momentum=0.9
opt=keras.optimizers.SGD(lr=l_r, momentum=momentum)
#optimizer.momentum.set_value(0.04)

#K.set_value(model.optimizer.learning_rate, l_r)

#opt = keras.optimizers.Adam(momentum=0.9)
#model.compile(..., optimizer=opt)

#model.compile(optimizer=opt, loss='binary_crossentropy', metrics=['binary_accuracy'])

model.compile(optimizer=opt, loss='binary_crossentropy', metrics=['accuracy'])

...
history = model.fit(
    x=x_train_final,
    y=y_train_new,
    shuffle=True,
    epochs=10, batch_size=1, callbacks=[callback], verbose=0)
...

#from keras.callbacks import EarlyStopping
#early_stopping_monitor = EarlyStopping(patience=2)
history = model.fit(x=x_train_final, y=y_train_new, validation_split=0.3, epochs=100, callbacks=[callback])

l = len(history.history['loss'])
print(f' No of epochs ran {l}') # Only 4 epochs are run.

eval = model.evaluate(x=x_test_final, y=y_test_new)
plot_model(model, to_file='mlp-mnist.png', show_shapes=True)

```

2.4.0

Processing - early stopping changes max

Model: "sequential_9"

| Layer (type) | Output Shape | Param # |
|------------------|--------------|---------|
| dense_36 (Dense) | (None, 16) | 12560 |
| dense_37 (Dense) | (None, 12) | 204 |
| dense_38 (Dense) | (None, 8) | 104 |
| dense_39 (Dense) | (None, 1) | 9 |

Total params: 12,877
 Trainable params: 12,877
 Non-trainable params: 0

model <tensorflow.python.keras.engine.sequential.Sequential object at 0x7f284e0d60b8>

Epoch 1/100

278/278 [=====] - 1s 3ms/step - loss: 0.0568 - accuracy: 0.9748 - val_loss: 0.0048 -

Epoch 2/100

278/278 [=====] - 1s 3ms/step - loss: 0.0074 - accuracy: 0.9984 - val_loss: 0.0045 -

Epoch 3/100

278/278 [=====] - 1s 3ms/step - loss: 0.0044 - accuracy: 0.9990 - val_loss: 0.0029 -

Epoch 4/100

278/278 [=====] - 1s 3ms/step - loss: 0.0066 - accuracy: 0.9984 - val_loss: 0.0029 -

No of epochs ran 4

67/67 [=====] - 0s 2ms/step - loss: 0.0025 - accuracy: 0.9991

2.4.0

Processing - early stopping changes auto

Model: "sequential_10"

| Layer (type) | Output Shape | Param # |
|------------------|--------------|---------|
| dense_40 (Dense) | (None, 16) | 12560 |
| dense_41 (Dense) | (None, 12) | 204 |
| dense_42 (Dense) | (None, 8) | 104 |
| dense_43 (Dense) | (None, 1) | 9 |

Total params: 12,877
 Trainable params: 12,877
 Non-trainable params: 0

model <tensorflow.python.keras.engine.sequential.Sequential object at 0x7f2842742e10>

Epoch 1/100

278/278 [=====] - 1s 3ms/step - loss: 0.0683 - accuracy: 0.9649 - val_loss: 0.0044 -

Epoch 2/100

278/278 [=====] - 1s 3ms/step - loss: 0.0113 - accuracy: 0.9966 - val_loss: 0.0040 -

Epoch 3/100

278/278 [=====] - 1s 3ms/step - loss: 0.0052 - accuracy: 0.9984 - val_loss: 0.0025 -

Epoch 4/100

278/278 [=====] - 1s 3ms/step - loss: 0.0047 - accuracy: 0.9992 - val_loss: 0.0035 -

Epoch 5/100

278/278 [=====] - 1s 3ms/step - loss: 0.0044 - accuracy: 0.9985 - val_loss: 0.0028 -

