

Swap_Pricing

January 22, 2018

1 Get discount factor for JPY

- input: MoneyMarket (short term interest rate), Swap rate.
- output: discount factors for each tenor listed by MoneyMarket and Swap rate.

1.1 Pricing

1.1.1 Swap pricing formula

The value of the exchange between a float and a fixed side is given by

$$V = \sum_{i=1}^N L(t_{i-1}, t_i) \times DF(t_i) \times \delta_i - \sum_{i=1}^N SwapRate \times DF(t_i) \times \delta_i,$$

where $L(t_{i-1}, t_i)$ is the float interest rate between t_{i-1} and t_i , $DF(t_i)$ is a discount factor, δ_i is a day-count-fraction and $SwapRate$ is a Swap rate which means a par rate for a swap trade.

1.1.2 Bootstrap method for getting discount factors

Discount factors as of today can be estimated from a par swap trade which corresponds to $V = 0$ under swap pricing formula. For example, let us consider a swap trade with maturity of 1.5 year. The discount factor for 1.5 year $DF(t_{1.5Y})$ is calculated by solving the following equation:

$$\sum_{i=1}^3 L(t_{i-1}, t_i) \times DF(t_i) \times \delta = \sum_{i=1}^3 SwapRate(1.5Y) \times DF(t_i) \times \delta$$

where a quoted swap rate is used for $SwapRate(1.5Y)$, the day-count-fraction δ is assumed 6 month and the float side interest rate is assumed that a following model expressed as

$$L(t_{i-1}, t_i) = \frac{1}{\delta} \left(\frac{DF(t_{i-1})}{DF(t_i)} - 1 \right).$$

The above equation can be solved by using $DF(t_{0.5Y})$, $DF(t_{1.0Y})$ and the float interest rate which is defined as above equation. As a result, the discount factor $DF(t_{1.5Y})$ is given by

$$DF(t_{1.5Y}) = \frac{1}{(1 + \delta \times SwapRate(1.5Y))} \left(DF(t_0) - SwapRate(1.5Y) \times \delta \times (DF(t_{0.5Y}) + DF(t_{1.0Y})) \right),$$

where $DF(t_{0.5Y})$ and $DF(t_{1.0Y})$ is calculated by using a quoted LIBOR (the rate of Money Market). The short rate of Money Market means spot rate, where the cashflows is expressed as only two terms. For example, $DF(t_{0.5Y})$ is given by

$$DF(t_{0.5Y}) = \frac{1}{(1 + \delta \times L(0.0Y, 0.5Y))},$$

where $L(0.0Y, 0.5Y)$ is the LIBOR rate between today and 6 month later. Discount factors after $t_{1.5Y}$ can be calculated by the same way as the derivation of $DF(t_{1.5Y})$. This method of getting discount factors gradually is called Bootstrap method.

```
In [1]: ''' import matplotlib.pyplot as plt
import numpy as np
import datetime

class getDF_moneymarket:
    def __init__(self, libor_rate, start_day, end_day):
        self.libor_rate = libor_rate
        self.start_day = start_day
        self.end_day = end_day
        self.datetime_obj_start = datetime.datetime.strptime(start_day, '%Y/%m/%d')
        self.datetime_obj_end = datetime.datetime.strptime(end_day, '%Y/%m/%d')
        self.daycount = (self.datetime_obj_end - self.datetime_obj_start).days / 360
        self.discount_factor = 0

    def __init__(self, today, array_ccy):
        self._start_day = today

    def getDF(self, seq_moneymarket):
'''

File "<ipython-input-1-180ce8381581>", line 14
'''

~
IndentationError: expected an indented block
```

```
In [175]: '''DF = getDF_moneymarket(0.2, '2017/12/18', '2019/12/30')
print(DF.discount_factor)
print(DF.getDF())
print(DF.discount_factor)
'''
```

```
Out[175]: "DF = getDF_moneymarket(0.2, '2017/12/18', '2019/12/30')\nprint(DF.discount_factor)\nnp
```

```
In [174]: '''DF1 = getDF_moneymarket(0.3, '2017/12/18', '2018/3/20')
DF1.getDF()
'''
```

```
Out[174]: "DF1 = getDF_moneymarket(0.3, '2017/12/18', '2018/3/20')\nDF1.getDF()\n"
```

```
In [3]: import csv
```

```
with open('sample_moneymarket.csv', 'r') as csvfile:
    reader_obj = csv.reader(csvfile)
    # rewritten header_obj by using next method(???)
    header_obj = next(reader_obj)
    mm_list = []
    for row in reader_obj:
        mm_list.append(row)
```

```
mm_list
```

```
Out[3]: [['O/N', '2017/12/23', '2017/12/24', '0.014348'],
         ['T/N', '2017/12/24', '2017/12/25', '0.014348'],
         ['1W', '2017/12/25', '2018/1/1', '0.014876'],
         ['2W', '2017/12/25', '2018/1/8', '0.015'],
         ['1M', '2017/12/25', '2018/1/24', '0.01563'],
         ['2M', '2017/12/25', '2018/2/23', '0.01616'],
         ['3M', '2017/12/25', '2018/3/25', '0.01685'],
         ['6M', '2017/12/25', '2018/6/23', '0.01833'],
         ['1Y', '2017/12/25', '2018/12/20', '0.021']]
```

```
In [1]: import csv
```

```
with open('sample_swaprate.csv', 'r') as csvfile:
    reader_obj = csv.reader(csvfile)
    # rewritten header_obj by using next method(???)
    header_obj = next(reader_obj)
    swap_rate_list = []
    for row in reader_obj:
        swap_rate_list.append(row)
    temp_num = [[] for i in range(len(swap_rate_list))] # comprehension expression for m
    ### proceccing the expression for the type of 1Y to 1.0Y.
    for i in range(len(swap_rate_list)):
        if (len(swap_rate_list[i][0]) == 2):
            temp_num[i] = "{:.1f}".format(int(swap_rate_list[i][0][0])) + swap_rate_list
            swap_rate_list[i][0] = temp_num[i]
        elif (len(swap_rate_list[i][0]) == 3):
            temp_num[i] = "{:.1f}".format(int(swap_rate_list[i][0][0:2])) + swap_rate_li
            swap_rate_list[i][0] = temp_num[i]
        else:
            break
```

```
swap_rate_list
```

NameError

Traceback (most recent call last)

```
<ipython-input-1-598ae1a76b85> in <module>()
    1 with open('sample_swaprate.csv', 'r') as csvfile:
----> 2     reader_obj = csv.reader(csvfile)
    3     # rewritten header_obj by using next method(???)
    4     header_obj = next(reader_obj)
    5     swap_rate_list = []
```

NameError: name 'csv' is not defined

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- money market の DF のリストの形式を変更
 - [tenor, DF] から [tenor, start, end, labor_rate, DF] の形式に変更

```
In [9]: %matplotlib inline
import numpy as np
import csv
import time
import datetime
import matplotlib.pyplot as plt

with open('sample_moneymarket.csv', 'r') as csvfile:
    reader_obj = csv.reader(csvfile)
    # rewritten header_obj by using next method(???)
    header_obj = next(reader_obj)
    mm_list = []
    for row in reader_obj:
        mm_list.append(row)

def get_DF_MM(money_market_list):
    list_len = len(money_market_list)
    # discount_factor = np.zeros(list_len*2).reshape(list_len, 2)
    discount_factor_list = [["", "", "", 0.0, 0.0] for i in range(list_len)]
    # discount_factor = [["", 0.0] for i in range(list_len)]
    day_count_fraction = np.zeros(list_len)
    # substitution the kinf of trade
    for i in range(0, list_len):
        discount_factor_list[i][0] = money_market_list[i][0]
        discount_factor_list[i][1] = money_market_list[i][1]
        discount_factor_list[i][2] = money_market_list[i][2]
        discount_factor_list[i][3] = float(money_market_list[i][3])
    # calc daycount-fraction
```

```

convention = 360.0
for i in range(0, len(day_count_fraction)):
    day_count_fraction[i] = calc_daycount(money_market_list[i][1], money_market_list[i][2], convention)
    # calculate DF of 0/N
    discount_factor_list[0][4] = 1.0 / (1.0 + day_count_fraction[0] * float(discount_factor_list[0][3]))
    # calculate DF of T/N
    discount_factor_list[1][4] = discount_factor_list[0][4] / (1.0 + day_count_fraction[1] * float(discount_factor_list[0][3]))
    # calculate DF after 1W
for i in range(2, list_len):
    discount_factor_list[i][4] = discount_factor_list[1][4] / (1.0 + day_count_fraction[i] * float(discount_factor_list[0][3]))
return discount_factor_list

def calc_daycount(start_day, end_day, convention):
    datetime_obj_start = datetime.datetime.strptime(start_day, '%Y/%m/%d')
    datetime_obj_end = datetime.datetime.strptime(end_day, '%Y/%m/%d')
    daycount = (datetime_obj_end - datetime_obj_start).days / convention
    return daycount

def calc_days(start_day, end_day):
    datetime_obj_start = datetime.datetime.strptime(start_day, '%Y/%m/%d')
    datetime_obj_end = datetime.datetime.strptime(end_day, '%Y/%m/%d')
    return (datetime_obj_end - datetime_obj_start).days

def draw_DF(seq_discount_factor):
    list_len = len(seq_discount_factor)
    seq_DF = np.zeros(list_len)
    for i in range(0, list_len):
        seq_DF[i] = seq_discount_factor[i][4]
    plt.plot(seq_DF)
    plt.ylim([0,1.0])

list_discountfactor = get_DF_MM(mm_list)
list_discountfactor
# draw_DF(list_discountfactor)

```

```

Out[9]: [['0/N', '2017/12/23', '2017/12/24', 0.014348, 0.99996014603284633],
['T/N', '2017/12/24', '2017/12/25', 0.014348, 0.99992029365403134],
['1W', '2017/12/25', '2018/1/1', 0.014876, 0.99963114479189386],
['2W', '2017/12/25', '2018/1/8', 0.015, 0.99933734686835807],
['1M', '2017/12/25', '2018/1/24', 0.01563, 0.99861959163592562],
['2M', '2017/12/25', '2018/2/23', 0.01616, 0.9972344089791807],
['3M', '2017/12/25', '2018/3/25', 0.01685, 0.99572579872689437],
['6M', '2017/12/25', '2018/6/23', 0.01833, 0.99083925191027356],
['1Y', '2017/12/25', '2018/12/20', 0.021, 0.97935386254067724]]

```

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- データの加工
 - 小数点表記 (" {:.1f}".format())
 - 文字列の結合 (+でできる)
- 空のリスト作成
 - 内包表記 -> [5 for i in range(10)] -> 5 が 10 個のリスト

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- エクセルの Vlookup 風の作業
 - 半年置きで、空の swap rate のリストを作成
 - 外部データとして存在する、加工済みの (1Y->1.0Y) データとマッチする行はそのまま置き換え
 - マッチしない行は据え置きでデフォルトの 0 を代入したままのリストを作成

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- get_end_day() 関数の作成
 - 祝日、土日勘案はせず。(ってかどうやるの?)

```
In [10]: def get_end_day(maturity, start_day):
    datetime_obj_start = datetime.datetime.strptime(start_day, '%Y/%m/%d')
    effective_days = float(maturity[0:len(maturity)-1])*365
    end_day = datetime_obj_start + datetime.timedelta(days=effective_days)
    return end_day.strftime('%Y/%m/%d')

def calc_end_day(future_days, start_day):
    datetime_obj_start = datetime.datetime.strptime(start_day, '%Y/%m/%d')
    end_day = datetime_obj_start + datetime.timedelta(days=future_days)
    return end_day.strftime('%Y/%m/%d')

from scipy.interpolate import interp1d
def interpolation_swap_rate(swap_rate_list):
    xaxis_date = []
    yaxis_swap_rate = []
    for i in range(len(swap_rate_list)):
        xaxis_date.append(float(swap_rate_list[i][0][0:len(swap_rate_list[i][0])-1]))
        yaxis_swap_rate.append(float(swap_rate_list[i][3]))
    f_interpolated_swap_rate = interp1d(xaxis_date, yaxis_swap_rate)
    return f_interpolated_swap_rate

from scipy.interpolate import interp1d
def interpolation_extract_list(original_list, index_xaxis, index_yaxis):
```

```

xaxis = []
yaxis = []
for i in range(len(original_list)):
    xaxis.append(float(original_list[i][index_xaxis]))
    yaxis.append(float(original_list[i][index_yaxis]))
f_interpolation = interp1d(xaxis, yaxis)
return f_interpolation

def get_interpolated_swap_rate_list(swap_rate_list, tenor):
    max_maturity = float(swap_rate_list[-1][0][0:len(swap_rate_list[-1][0])-1])
    seq_len_of_swap_rate = int(max_maturity/tenor - 1)
    array_swap_rate = [("", 0, 0, 0) for i in range(seq_len_of_swap_rate)]
    for i in range(2, seq_len_of_swap_rate + 2):
        array_swap_rate[i-2][0] = "{}Y".format(i*tenor)
    func_interpolated_swap_rate = interpolation_swap_rate(swap_rate_list)
    ## for sentence is nested...
    ## I wanna reviese code, but I have not an idea. Please tell me better coding if you
    for i in range(len(array_swap_rate)):
        array_swap_rate[i][1] = swap_rate_list[0][1]
        array_swap_rate[i][2] = get_end_day(array_swap_rate[i][0], array_swap_rate[i][1])
        interpolated_date = float(array_swap_rate[i][0][0:len(array_swap_rate[i][0])-1])
        array_swap_rate[i][3] = float(func_interpolated_swap_rate(interpolated_date))
        for j in range(len(swap_rate_list)):
            if (array_swap_rate[i][0] in swap_rate_list[j][0]):
                array_swap_rate[i] = swap_rate_list[j]
                break

    return array_swap_rate

def get_DF(money_market_list, swap_rate_list, tenor):
    interpolated_swap_rate_list_temp = get_interpolated_swap_rate_list(swap_rate_list,
    interpolated_swap_rate_list = interpolated_swap_rate_list_temp[1:len(interpolated_s
    interpolated_DF_swap_rate_list = [("", "", "", 0.0, 0.0) for i in range(len(interpo
    ## interpolated_swa_rate_list[i].append(0) では, swap_rate_listが上書きされていく...
    for i in range(len(interpolated_swap_rate_list)):
        interpolated_DF_swap_rate_list[i][0] = interpolated_swap_rate_list[i][0]
        interpolated_DF_swap_rate_list[i][1] = interpolated_swap_rate_list[i][1]
        interpolated_DF_swap_rate_list[i][2] = interpolated_swap_rate_list[i][2]
        interpolated_DF_swap_rate_list[i][3] = float(interpolated_swap_rate_list[i][3])
    discount_factor_len = len(money_market_list) + len(interpolated_swap_rate_list)
    discount_factor_list = [("", "", "", 0.0, 0.0) for i in range(discount_factor_len)]
    DF_money_market_list = get_DF_MM(money_market_list)
    # listの結合 llist_new = listA + listB でいける
    discount_factor_list = DF_money_market_list + interpolated_DF_swap_rate_list

    return discount_factor_list

def bootstrapping_DF_swap_rate(discount_factor_list, tenor_name):

```

```

extract_date_list = extract_1d_list(discount_factor_list, 0)
index_roll_tenor = extract_date_list.index(tenor_name)
# day_count_fraction
convention = 360
day_count_fraction = calc_daycount(discount_factor_list[index_roll_tenor][1], discount_factor_list[index_start_tenor])
index_start_tenor = extract_date_list.index('1.5Y')
index_end_tenor = len(discount_factor_list)
discount_factor = np.zeros(len(discount_factor_list))
# for i in range(0, index_start_tenor):
#     discount_factor[i] = discount_factor_list[i][4]
for i in range(index_start_tenor, index_end_tenor):
    annuity = calc_annuity(discount_factor_list, discount_factor_list[i][0], tenor_list[index_start_tenor])
    discount_factor[i] = 1.0 / (1.0 + day_count_fraction * discount_factor_list[i][4])
    discount_factor_list[i][4] = discount_factor[i]
return discount_factor_list

def extract_1d_list(discount_factor_list, index):
    extracted_list = []
    for i in range(len(discount_factor_list)):
        extracted_list.append(discount_factor_list[i][index])
    return extracted_list

'''def calc_annuity(discount_factor_list, target_tenor, roll_tenor):
    extract_date_list = extract_1d_list(discount_factor_list, 0)
    index_target_tenor = extract_date_list.index(target_tenor)
    num_of_roll_tenor_in_unit_year = float(transform_tenor_to_unit_in_year(roll_tenor))
    num_of_target_tenor_in_unit_year = float(transform_tenor_to_unit_in_year(target_tenor))
    num_of_roll = num_of_target_tenor_in_unit_year / num_of_roll_tenor_in_unit_year
    tenor_list_for_sum = ['{}Y'.format(i * num_of_roll_tenor_in_unit_year) for i in range(1, num_of_target_tenor_in_unit_year + 1)]
    for i in range(len(tenor_list_for_sum)):
        if (tenor_list_for_sum[i][0:len(tenor_list_for_sum[i])-1] < 1.0):
            tenor_list_for_sum[i] = tenor_list_for_sum[i][0:len(tenor_list_for_sum[i])-1] + 'M'
    # change expression #M to #Y
'''

def calc_annuity(discount_factor_list, target_tenor, roll_tenor):
    extract_date_list = extract_1d_list(discount_factor_list, 0)
    index_target_tenor = extract_date_list.index(target_tenor)
    index_roll_tenor = extract_date_list.index(roll_tenor)
    annuity = 0
    convention = 360
    day_count_fraction = calc_daycount(discount_factor_list[index_roll_tenor][1], discount_factor_list[index_target_tenor])
    for i in range(index_roll_tenor, index_target_tenor):
        annuity += discount_factor_list[i][4] * day_count_fraction
    return annuity

def transform_tenor_to_unit_in_year(tenor_string):
    tenor = 0

```



```

tenor_unit = tenor_string[-1]
if (tenor_unit == 'Y'):
    tenor = float(tenor_string[0:len(tenor_string)-1])
elif (tenor_unit == 'M'):
    tenor = float(tenor_string[0:len(tenor_string)-1]) / 12
return tenor

def interpolation_DF(discount_factor_list):
    # make list including days between start_day and end_day in fourth column.
    len_discount_factor_list = len(discount_factor_list)
    interpolated_discount_factor_list = [["", "", "", 0.0, 0.0, 0.0] for i in range(len_discount_factor_list)]
    for i in range(len_discount_factor_list):
        interpolated_discount_factor_list[i][0] = discount_factor_list[i][0]
        interpolated_discount_factor_list[i][1] = discount_factor_list[i][1]
        interpolated_discount_factor_list[i][2] = discount_factor_list[i][2]
        interpolated_discount_factor_list[i][4] = discount_factor_list[i][3]
        interpolated_discount_factor_list[i][5] = discount_factor_list[i][4]
    for i in range(len_discount_factor_list):
        if (discount_factor_list[i][0] == 'O/N'):
            interpolated_discount_factor_list[i][3] = calc_days(discount_factor_list[i][1], discount_factor_list[i][2])
            # TODO going to revise 1 and 2 day-count. have to consider Sat., Sun. and H
        elif (discount_factor_list[i][0] == 'T/N'):
            interpolated_discount_factor_list[i][3] = calc_days(discount_factor_list[i][1], discount_factor_list[i][2])
        else:
            interpolated_discount_factor_list[i][3] = calc_days(discount_factor_list[i][1], discount_factor_list[i][2])
    # interpolate DF
    index_days = 3
    index_DF = 5
    func_interpolation_DF = interpolation_extract_list(interpolated_discount_factor_list)
    return func_interpolation_DF

def get_interpolated_DF(discount_factor_list):
    max_maturity = float(discount_factor_list[-1][0][0:len(discount_factor_list[-1][0])])
    len_interpolated_DF_list = int(max_maturity * 365)
    contract_day = discount_factor_list[0][1]
    interpolated_DF_list = [[i, contract_day, "", 0.0] for i in range(0, len_interpolated_DF_list)]
    interpolated_DF_list[0][2] = contract_day
    interpolated_DF_list[0][3] = 1.0
    func_interpolation_DF = interpolation_DF(discount_factor_list)
    for i in range(1, len_interpolated_DF_list):
        interpolated_DF_list[i][2] = calc_end_day(i, contract_day)
        interpolated_DF_list[i][3] = float(func_interpolation_DF(i))
    return interpolated_DF_list

```

```
In [85]: import csv
```

```

with open('interpolated_DF_list.csv', 'w') as f:
    writer = csv.writer(f, lineterminator='\n') # 改行コード (\n) を指定しておく

```

```

writer.writerow(get_interpolated_DF(bootstrapping_DF_swap_rate(DF_LIST, '6M'))) #

In [11]: DF_LIST = get_DF(mm_list, swap_rate_list, 1/2);
bootstrapping_DF_swap_rate(DF_LIST, '6M');
f = interpolation_DF(bootstrapping_DF_swap_rate(DF_LIST, '6M'))
f(10950)
get_interpolated_DF(bootstrapping_DF_swap_rate(DF_LIST, '6M'))

Out[11]: [[0, '2017/12/23', '2017/12/23', 1.0],
[1, '2017/12/23', '2017/12/24', 0.9999601460328463],
[2, '2017/12/23', '2017/12/25', 0.9999202936540313],
[3, '2017/12/23', '2017/12/26', 0.999878986673726],
[4, '2017/12/23', '2017/12/27', 0.9998376796934206],
[5, '2017/12/23', '2017/12/28', 0.9997963727131153],
[6, '2017/12/23', '2017/12/29', 0.9997550657328099],
[7, '2017/12/23', '2017/12/30', 0.9997137587525046],
[8, '2017/12/23', '2017/12/31', 0.9996724517721992],
[9, '2017/12/23', '2018/01/01', 0.9996311447918939],
[10, '2017/12/23', '2018/01/02', 0.9995891736599601],
[11, '2017/12/23', '2018/01/03', 0.9995472025280265],
[12, '2017/12/23', '2018/01/04', 0.9995052313960928],
[13, '2017/12/23', '2018/01/05', 0.9994632602641591],
[14, '2017/12/23', '2018/01/06', 0.9994212891322254],
[15, '2017/12/23', '2018/01/07', 0.9993793180002918],
[16, '2017/12/23', '2018/01/08', 0.9993373468683581],
[17, '2017/12/23', '2018/01/09', 0.999292487166331],
[18, '2017/12/23', '2018/01/10', 0.9992476274643041],
[19, '2017/12/23', '2018/01/11', 0.999202767762277],
[20, '2017/12/23', '2018/01/12', 0.99915790806025],
[21, '2017/12/23', '2018/01/13', 0.9991130483582229],
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```
...]
```

```
In [164]: x = np.arange(67)
          y = []
          for i in range(len(bootstrapping_DF_swap_rate(DF_LIST, '6M'))):
              y.append(bootstrapping_DF_swap_rate(DF_LIST, '6M')[i][4])
          plt.plot(x,y)
```

```
Out[164]: [<matplotlib.lines.Line2D at 0x18148c9128>]
```

```
In [63]: from scipy.interpolate import interp1d
          x = []
          y = []
          for i in range(len(swap_rate_list)):
              x.append(float(swap_rate_list[i][0][0:len(swap_rate_list[i][0])-1]))
              y.append(float(swap_rate_list[i][3]))
          print(x)
          print(y)
          f = interp1d(x,y)
          xnew = np.linspace(1, 30, num=60, endpoint=True)
          plt.plot(xnew, f(xnew), '-')
          f(1.5)
```

```
[1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0, 10.0, 15.0, 20.0, 30.0]
```

```
[0.01904, 0.02086, 0.02187, 0.02248, 0.02295, 0.02337, 0.02376, 0.02411, 0.02444, 0.02475, 0.025
```

```
Out[63]: array(0.019950000000000002)
```

5.0.1 エラーメッセージ

5.0.2 解決策

- 数値と文字列が混ざっているなのでどちらかに統一すべし