Generating Images with Waves

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1 Introduction

This report presents a method for generating images by combining different waves. Each image is a combination of waves with varying wavelengths, frequencies, and amplitudes.

2 Concept

The process of generating images using waves involves the following steps:

- 1. Get the Grayscale Image: Convert the original image to grayscale.
- 2. Fourier Transform: Find the Fourier Transform of the image to analyze its frequency components. The Fourier Transform F(k, l) of a 2D image

$$F(k,l) = \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} f(m,n) \cdot e^{-j2\pi \left(\frac{km}{M} + \frac{ln}{N}\right)}$$

3. Wave Partitioning: Partition the Fourier-transformed waves into n portions and visualize the result by computing the Inverse Fourier Transform of the waves in that portion. The Inverse Fourier Transform f(x, y) is given by:

$$f(m,n) = \frac{1}{MN} \sum_{k=0}^{M-1} \sum_{l=0}^{N-1} F(k,l) \cdot e^{j2\pi \left(\frac{km}{M} + \frac{ln}{N}\right)}$$

3 Code

```
6 % 2. APPLYING FOURIER TRANSFORM TO CONVERT THE SPACE DOMAIN
     TO FREQUENCY DOMAIN
ft = fft2(double(grayImage));
9 % 3. Shift the zero frequency component to the center
10 ft_shifted = fftshift(ft);
12 %%
13 % 4. Initialize a reconstructed image
14 [rows, cols] = size(ft_shifted); % Size of image same as
      previous
reconstruction = zeros(rows, cols); % Empty reconstruction
     image
17
18 %%
19 % 5. Loop to add frequency components
20
21 % num_portions: # steps to divide the process into
22
23 num_portion = 20; % the ft_shifted will be converted to
     num_portion portions for reconstruction
24
25 for step = 1:num_portion
      % For step value, add a portion of waves from the
          shifted fourier transform to the final image
      no_coeffecients = round(step * (rows * cols) /
27
         num_portion); % #coeffeints to add to reconstructed
          image
      reconstruction(1:no_coeffecients) = ft_shifted(1:
         no_coeffecients); % Add portion of image on top of
         the reconstructed image
29
      % Inverse Fourier Transform to reconstruct image
30
      reconstructed_image = abs(ifft2(ifftshift(reconstruction
31
         )));
      % Saving step wise image to device
      filename = sprintf('E:/codes/image-through-waves/images3
34
         /reconstructed_step_%d.png', step);
      imwrite(uint8(reconstructed_image), filename);
36
  end
37
38
39 % Display the final reconstructed image
41 imshow(reconstructed_image, []), title('Final Reconstructed
      Image');
```

4 Result

The result is a sequence of images generated by the addition of waves.

5 Reconstructed Images

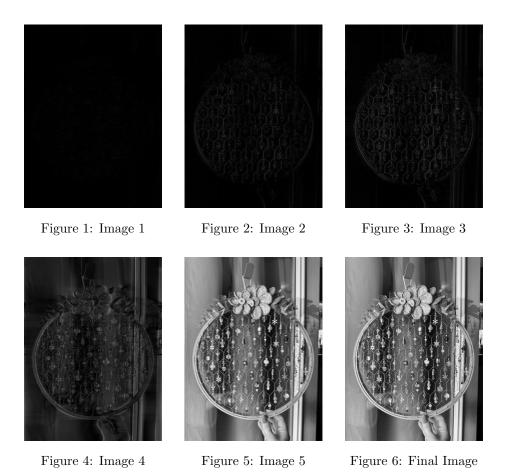


Figure 7: Series of Reconstructed Images by gradually increasing the number of waves