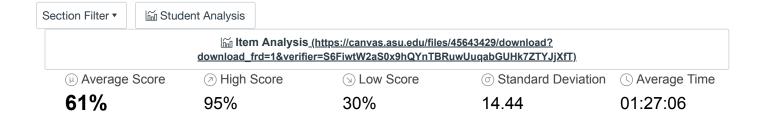
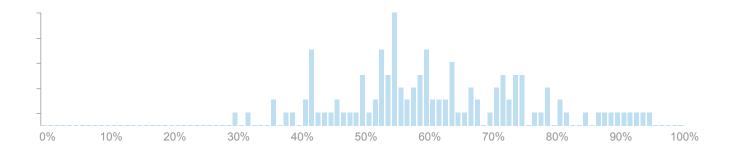
Quiz Summary





Question Breakdown

Attempts: 40 out of 40

Given the following preference lists and the matching M indicated by the asterisks, in the space below, list an unstable pair with respect to M, if one exists, or determine that no unstable pair exists. If you determine no unstable pair exists, write "N/A", otherwise, give the pair.

Men	1st	2nd	3rd
А	Y	*Z	×
В	Z	Y	*X
С	Х	*Y	Z

Women	1st	2nd	3rd
-------	-----	-----	-----

X	А	*B	С
Y	А	*C	В
Z	В	*A	С

N/A		0 %	57%
AX	5 respondents	13 %	answered
BY	4 respondents	10 %	correctly
CX	10 respondents	25 %	
BZ	36 respondents	90 %	✓
AY	32 respondents	80 %	~
CZ	4 respondents	10 %	

Attempts: 36 out of 48

Consider the following turn-based propose-and-reject variant where we are given n men and n women and both men and women may initiate proposals. Let an unstable pair remain defined exactly as given in lecture.

Algorithm 1 EGALITARIAN PROPOSE-AND-REJECT

- 1: Initialize each person to be free
- 2: Turn ← "men"
- 3: while Some man is free or some woman is free do
- 4: if Turn is "men" and some man is free then
- 5: Choose an unengaged man m
- 6: Let w be the first woman on m's preference list to whom m has not yet proposed
- 7: if w is free then
- 8: Assign m and w to be engaged
- 9: else if w prefers m to her fiance m_0 then
- 10: Assign m and w to be engaged and set m_0 to be free
- 11: else
- 12: w rejects m
- 13: if Turn is "women" and some woman is free then
- 14: Choose an unengaged woman w
- 15: Let m be the first man on w's preference list to whom w has not yet proposed
- 16: if m is free then
- 17: Assign m and w to be engaged
- 18: else if m prefers w to his fiance w_0 then

```
19: Assign m and w to be engaged and set w<sub>0</sub> to be free
20: else
21: m rejects w
22: if Turn is "men" then
23: Turn ← "women"
24: else if Turn is "women" then
25: Turn ← "men"
```

The following assertion is made about the egalitarian propose-and-reject algorithm.

ASSERTION: This algorithm will never find a stable matching.

For the above assertion, either **prove** that it will never find a stable matching, or **disprove** it by providing a *counterexample*.

Briefly justify all statements.

```
Answers which scored in the top 27% 28 respondents 58 %

Answers which scored in the middle 46% 7 respondents 15 %

Answers which scored in the bottom 27% 13 respondents 27 %
```

<u>Download All Files</u> (https://canvas.asu.edu/courses/95943/quizzes/73546 <u>zip=1)</u>

Attempts: 60 out of 60

The following statements all concern greedy algorithms. Select all statements below that are true.

```
22 respondents 37 % 3% answered correctly 43 respondents 72 % 58 respondents 58 %
```

Attempts: 103 out of 103

Assume that we have n jobs to schedule and that we are given the total processing time t_j and a target release time r_j , for each job j. We consider the problem of scheduling the jobs to be processed by a single resource such that only one job is processed at any point in time, and where the processor can never remain idle until it has completed all of the n jobs starting from time 0. The earliness e_j of job j measures how much earlier than the target release time we start processing the job and is equal to $\max(0, r_j - s_j)$, where s_j is the actual scheduled start time of job j. We would like to find a schedule that minimizes the maximum earliness of a job, i.e., to find a schedule that minimizes $\max_j e_j$.

Select **all** options that correctly complete the following sentence: The same algorithm used for the problem of minimizing the maximum lateness as seen in lecture would work here if instead of ordering and scheduling the jobs in increasing order of their deadlines, we would order and schedule the jobs in...

decreasing order of their target release times.	23 respondents	22 [%]
no order, since there is no ordering of the jobs that will make the algorithm guaranteed to work in this case.	19 respondents	18 %
increasing order of their processing times.	18 respondents	17 %
increasing order of their target release times.	51 respondents	50 [%]
No Answer	17 respondents	17 %
45%		
answered		
correctly		

Attempts: 70 out of 70

Suppose you are given an undirected graph G(V,E) with associated edge costs c_e , which are all positive and distinct and let T be a minimum spanning tree of G. Now replace all edge costs c_e by a new cost c_e' , thereby creating a new instance of the problem with the same graph with set of nodes V and set of edges E but with the modified edge costs. Circle all options below where T would still be guaranteed to be a minimum spanning tree of G in this new instance of the graph (with modified edge costs c_e'):

Attempts: 49 out of 49

Consider the offline caching problem. Suppose we have a cache C of size 2 (i.e., C can hold **two** items at a time). Let *a*, *b*, *e*, *b*, *b*, *c*, *d*, *f*, *e*, *g*, *b*, *f*, *a*, *b*, *c*, *d*, *f*, *e*, *a*, *b*, *c*, *c* be the sequence of item requests. Use the Farthest-in-Future algorithm and assume that you start from an empty cache. The configuration of the cache C after the first request for item g (in the tenth position of the sequence) is satisfied, is as follows:

+0.2 Discrimination Index (?) fg 4 respondents 78% answered 12 % eg 6 respondents correctly 0 % cg **78** % gf 38 respondents 2 % gd 1 respondent

dg

0 %

Attempts: 56 out of 56

Identify which of the following items are true regarding a splay-tree with n nodes and splay-tree operations. Select all that apply.

```
17 respondents 30 % 20%
32 respondents 57 % answered correctly
40 respondents 71 %

10 respondents 18 %
```

Attempts: 49 out of 69

Let $\alpha \in \mathbb{Z}_{\geq 2}$ be an arbitrary integer of value greater than or equal to 2. Suppose we are performing operations on a data structure D where the cost of the k^{th} operation o_k is defined by

 $cost(o_k) = \{k \text{ if } k \text{ is a power of } \alpha, \text{ and } 1 \text{ otherwise } \}$

Use the **accounting method** to show that the amortized cost of an operation o_k is O(1). Justify all statements briefly and show all steps.

Note that you will need to derive a dollar amount analytically for full points.



<u>Download All Files</u> (<u>https://canvas.asu.edu/courses/95943/quizzes/73546</u> <u>zip=1)</u>

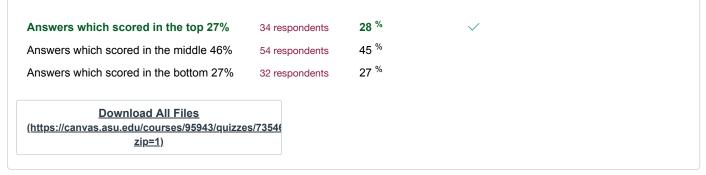
Attempts: 54 out of 54

Suppose we are given a splay-tree T of n nodes and we present an operation called ELEMENT-CHECK(T, e) that returns true if element e is the key of some node in splay-tree T and false otherwise. The algorithm works as follows: Beginning at the root of T, we walk down a branch of T searching for e making use of the binary search tree property (i.e. if the key of the currently visited node is less than e, we take the left branch, and if the key of the currently visited node is greater than e, we take the right branch). If a node with key e is found, we splay that node to the root of T and return true. If we reach a leaf node without finding a node with key e, we splay the leaf node and halt. Can we use the proof of amortized bounds for splay operations seen in lecture to conclude that the amortized cost of ELEMENT-CHECK is $O(\log n)$? Select all that apply.

Attempts: 75 out of 120

Given a connected graph G=(V,E) with distinct edge costs $c(e):e\in E$, a maximum bottleneck tree of G is a spanning tree T(V,E') of G where the largest weight of any edge in E' is as large as possible. Give a polynomial time algorithm that is guaranteed to find some maximum bottleneck tree of G. Prove that your algorithm is correct and justify its polynomial running time.

The description of your algorithm need only be a high-level description as opposed to a detailed pseudocode description. Note that you may directly cite material from lectures, graded quizzes and graded assignments without reproducing it. For example, if you wish to cite the proof of correctness for interval scheduling, simply refer to "the proof of correctness for interval scheduling as seen in lecture..."





Attempts: 31 out of 41

Consider the following turn-based propose-and-reject variant where we are given n men and n women and both men and women may initiate proposals. Let an unstable pair remain defined exactly as given in lecture.

1: Initialize each person to be free 2: Turn ← "men" 3: while Some man is free or some woman is free do if Turn is "men" and some man is free then 5: Choose an unengaged man m 6: Let w be the first woman on m's preference list to whom m has not yet proposed 7: if w is free then 8: Assign m and w to be engaged 9: else if w prefers m to her fiance m₀ then Assign m and w to be engaged and set m₀ to be free 10: 11: else 12: w rejects m 13: if Turn is "women" and some woman is free then 14: Choose an unengaged woman w 15: Let m be the first man on w's preference list to whom w has not yet proposed 16: if m is free then 17: Assign m and w to be engaged else if m prefers w to his fiance w₀ then 18: 19: Assign m and w to be engaged and set w₀ to be free 20: else 21: m rejects w 22: if Turn is "men" then 23: Turn ← "women" 24: else if Turn is "women" then 25: Turn ← "men"

The following assertion is made about the egalitarian propose-and-reject algorithm.

ASSERTION: This algorithm is guaranteed to find a stable matching.

For the above assertion, either **prove** that the algorithm will always produce a stable matching, or **disprove** it by providing a *counterexample*.

Briefly justify all statements.

Answers which scored in the top 27% 11 respondents 27 %

Answers which scored in the middle 46% 23 respondents 56 %

Answers which scored in the bottom 27% 7 respondents 17 %

<u>Download All Files</u>
(https://canvas.asu.edu/courses/95943/quizzes/73546
zip=1)

Attempts: 59 out of 59

The following statements all concern greedy algorithms. Select all statements below that are true. 10 % 6 respondents 47 % 28 respondents 52 respondents 88 % Regarding the interval partitioning problem, there may not exist a schedule 27 % 16 respondents where the number of classrooms is equal to the depth of the interval set. 42 respondents 71 % 2 % No Answer 1 respondent 19% answered correctly

Attempts: 49 out of 49

Suppose you are given an undirected graph G(V,E) with associated edge costs c_e , which are all positive and distinct and let P be a shortest-path from node s to node t in t. Now replace all edge costs t by a new cost t , thereby creating a new instance of the problem with the same graph with set of nodes t and set of edges t but with the modified edge costs. Circle all options below where t would still be guaranteed to be a shortest path from t to t in this new instance of the graph (with modified edge costs t):

49 respondents

100 %

10 respondents

20 %

answered correctly

15 respondents

45 %

1 respondent

2 %

Attempts: 32 out of 51

No Answer

Let $\alpha \in \mathbb{Z}_{\geq 2}$ be an arbitrary integer of value greater than or equal to 2. Suppose we are performing operations on a data structure D where the cost of the k^{th} operation o_k is defined by

 $cost(o_k) = \{k \text{ if } k \text{ is a power of } \alpha, \text{ and } 1 \text{ otherwise } \}$

Use the **potential method** to show that the amortized cost of an operation o_k is O(1). Justify all statements briefly and show all steps.

Note that you will need to carefully define a potential function and show that it is valid for full points.

Answers which scored in the top 27% 20 respondents 39 %

Answers which scored in the middle 46% 18 respondents 35 %

Answers which scored in the bottom 27% 13 respondents 25 %

<u>Download All Files</u> (https://canvas.asu.edu/courses/95943/quizzes/73546 <u>zip=1)</u>

Attempts: 37 out of 37

Given the following preference lists and the matching M indicated by the asterisks, in the space below, list an unstable pair with respect to M, if one exists, or determine that no unstable pair exists. If you determine no unstable pair exists, write "N/A", otherwise, give the pair.

Men	1st	2nd	3rd
А	×	*Z	Y
В	Y	*X	Z
С	X	*Y	Z

Women	1st	2nd	3rd
X	А	*B	С
Y	А	*C	В
Z	В	*A	С

BY	1 respondent	3 %	59%
N/A	1 respondent	3 %	answered
CX	6 respondents	16 %	correctly
AY	8 respondents	22 %	
CZ	2 respondents	5 %	
BZ	11 respondents	30 %	
AX	29 respondents	78 %	✓

Attempts: 22 out of 31

Consider the following turn-based propose-and-reject variant where we are given n men and n women and both men and women may initiate proposals. Let an unstable pair remain defined exactly as given in lecture.

Algorithm 1 EGALITARIAN PROPOSE-AND-REJECT

- 1: Initialize each person to be free
- 2: Turn ← "men"
- 3: while Some man is free or some woman is free do
- 4: if Turn is "men" and some man is free then
- 5: Choose an unengaged man m
- 6: Let w be the first woman on m's preference list to whom m has not yet proposed
- 7: if w is free then
- 8: Assign m and w to be engaged
- 9: else if w prefers m to her fiance m_0 then
- 10: Assign m and w to be engaged and set m_0 to be free
- 11: else
- 12: w rejects m
- 13: if Turn is "women" and some woman is free then
- 14: Choose an unengaged woman w
- 15: Let m be the first man on w's preference list to whom w has not yet proposed
- 16: if m is free then
- 17: Assign m and w to be engaged
- 18: else if m prefers w to his fiance w_0 then
- 19: Assign m and w to be engaged and set w_0 to be free
- 20: else
- 21: m rejects w
- 22: if Turn is "men" then
- 23: Turn ← "women"
- 24: else if Turn is "women" then
- 25: Turn ← "men"

The following assertion is made about the egalitarian propose-and-reject algorithm.

ASSERTION: This algorithm will guarantee a stable matching that is neither female optimal nor male optimal.

For the above assertion, either **prove** that it will always find a stable matching that is neither male nor female optimal, or **disprove** it by providing a *counterexample*.

Briefly justify all statements.

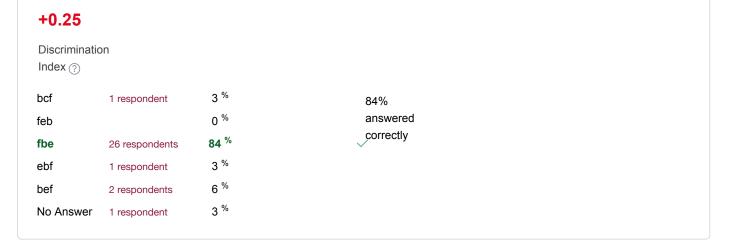
Answers which scored in the top 27% 8 respondents 26 %

Answers which scored in the middle 46% 15 respondents 48 %

Answers which scored in the bottom 27% 8 respondents 26 %

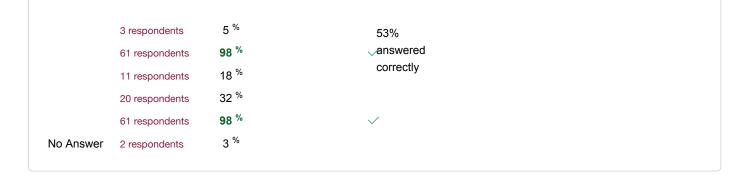
<u>Download All Files</u> (https://canvas.asu.edu/courses/95943/quizzes/73546 zip=1) Attempts: 30 out of 31

Consider the offline caching problem. Suppose we have a cache C of size 3 (i.e., C can hold **three** items at a time). Let *a*, *b*, *e*, *b*, *b*, *c*, *d*, *f*, *e*, *g*, *b*, *f*, *a*, *b*, *c*, *d*, *f*, *e*, *a*, *b*, *c*, *c* be the sequence of item requests. Use the Farthest-in-Future algorithm and assume that you start from an empty cache. The configuration of the cache C after the first request for item f (in the eighth position of the sequence) is satisfied, is as follows:



Attempts: 62 out of 62

Identify which of the following items are true regarding a splay-tree with n nodes and splay-tree operations. Select all that apply.



Attempts: 51 out of 51

Suppose we are given a splay-tree T of n nodes and we present an operation called ELEMENT-CHECK(T, e) that returns true if element e is the key of some node in splay-tree T and false otherwise. The algorithm works as follows: Beginning at the root of T, we walk down a branch of T searching for e making use of the binary search tree property (i.e. if the key of the currently visited node is less than e, we take the left branch, and if the key of the currently visited node is greater than e, we take the right branch). If a node with key e is found, we splay that node to the root of T and return true. If we reach a leaf node without finding a node with key e, we simply return false and halt. Can we use the proof of amortized bounds for splay operations seen in lecture to conclude that the amortized cost of ELEMENT-CHECK is $O(\log n)$? Select all that apply.

:	21 respondents 22 respondents 8 respondents	41 % 0 % 43 % 16 %	29% answered correctly
No Answer	8 respondents	16 ^	

Attempts: 39 out of 40

Consider the offline caching problem. Suppose we have a cache C of size 3 (i.e., C can hold **three** items at a time). Let *a*, *b*, *e*, *b*, *b*, *c*, *d*, *f*, *e*, *g*, *b*, *f*, *a*, *b*, *c*, *d*, *f*, *e*, *a*, *b*, *c*, *c* be the sequence of item requests. Use the Farthest-in-Future algorithm and assume that you start from an empty cache. The configuration of the cache C after the first request for item g (in the tenth position of the sequence) is satisfied, is as follows:

+0.02

Discrimination

Index ?

ebg gbf	2 respondents	5 % 0 %	80% answered
fbg	32 respondents	80 %	correctly
bfg	3 respondents	8 %	
dgf	2 respondents	5 %	
No Answer	1 respondent	3 %	

Attempts: 43 out of 43

Given the following preference lists and the matching M indicated by the asterisks, in the space below, list an unstable pair with respect to M, if one exists, or determine that no unstable pair exists. If you determine no unstable pair exists, write "N/A", otherwise, give the pair.

Men	1st	2nd	3rd
А	×	*Z	Y
В	Z	Y	*X
С	X	*Y	Z

Women	1st	2nd	3rd
x	Α	*B	С
Y	Α	*C	В

	Z	В	*A	С	
				•	
BY	5 respondent	ts 12 [%]		70%	
N/A	2 respondent	ts 5 %	answered		
AY	6 respondent	ts 14 %		correctly	
BZ	35 responder	nts 81 %		✓	
CX	5 respondent	ts 12 %			
AX	32 responder	nts 74 %		✓	
CZ	5 respondent	ts 12 [%]			