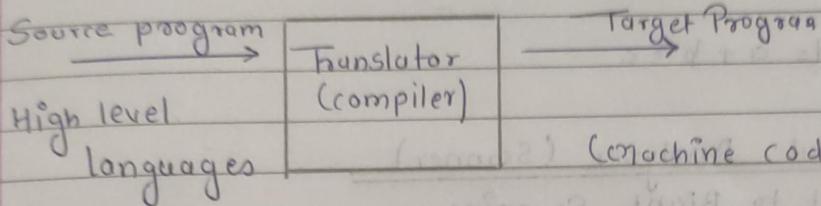


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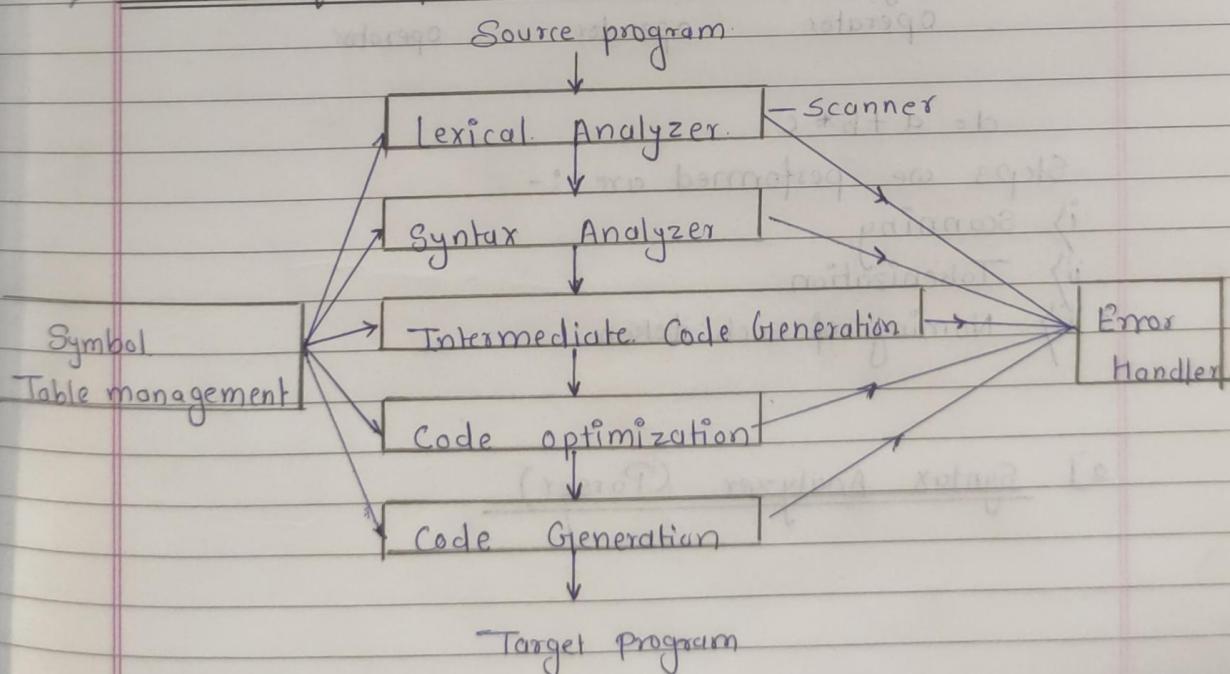
Compiler



Example of Translator

- ① Interpreter
② Assembler
- ADD 1,2
MOV A,B

* Phase of compiler (13 Marks Question)



For(i = 0 ; i <= 10 ; i++)
↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓
Keyword id constant id conditional operator punctuation mark incremental operator
Open parenthesis assignment operator punctuation mark constant punctuating mark close parenthesis

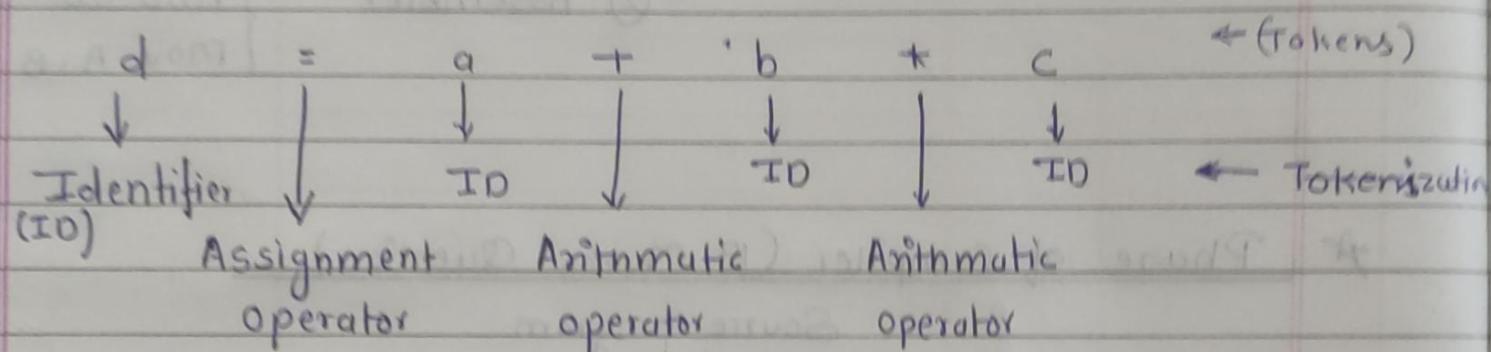
If we have an expression

$$d = a + b * c$$

1] Lexical Analyzer (Scanner)

i) Left to Right Scanning

ii) Then separation of continuous expression into single element which we will call it 'Token'



$$d = a + b * c$$

Steps we performed are :-

- i) Scanning
- ii) Tokenization
- iii) Naming of each token

2] Syntax Analyzer (Parser)

* Cross Compiler:

Cross compiler is a compiler that runs on one machine & produces the object code on another machine.

The cross compiler is used to implement the compiler which is characterized by 3 languages.

- 1) The source language
- 2) The Object language
- 3) The language in which it is written

* Bootstrap Compiler:

The compiler which is written in its own language is called bootstrap compiler.

Unit II Syntax Analysis (Parser)

* Grammar

Set of 4 tuples.

$$G_1 = \{T, N, P, S\}$$

$T \rightarrow$ Terminal Symbol

$N \rightarrow$ Non-terminal symbol

$P \rightarrow$ Production.

$S \rightarrow$ Start symbol.

$$S \rightarrow + a A;$$

$$A \rightarrow b$$

- * Terminal Symbol

Small \Rightarrow alphabet, digit 0-9 and special symbol
 $\therefore T \rightarrow \{+, a, b, ;\}$

- * Non-terminal Symbol

Capital alphabet and which is produced production.

$$\therefore N \rightarrow \{A, S\}$$

- * Production

$$S \rightarrow + a A; \quad \& \quad A \rightarrow b \text{ after a production}$$

- * Start Symbol

The S is a start symbol in $S \rightarrow + a A b$ because A is replaced by b according to $A \rightarrow b$.

* Type of Grammar

1) Context Free Grammar

$$X \rightarrow Y$$

Where, X is always Non-terminal and Y is a combination of terminal & non-terminal or only terminal.

eg

$$A \rightarrow b$$

— only Terminal

$$A \rightarrow bB$$

— Combination of terminal & non-terminal

2) Context Sensitive Grammar

$$X \rightarrow Y$$

where X and Y be the combination of terminal and non-terminal and $X \rightarrow Y$ is the non-terminal only.

eg

$$aA \rightarrow b$$

— X be combination of terminal & non-terminal
 Y be the terminal.

$$aA \rightarrow bB$$

— X and Y both are combination

3) Right Linear Grammar

$$A \rightarrow wB$$

$$B \rightarrow \underline{w}$$

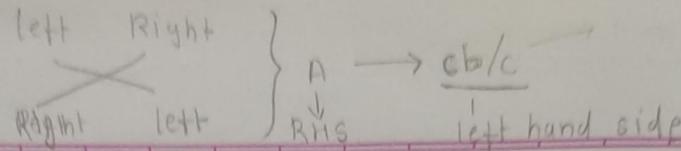
Where, w is always string of terminal symbol

eg

$$A \rightarrow aB$$

$$B \rightarrow a$$

in a is a string of terminal symbol and production of another.



4) Left Linear Grammar

$$A \rightarrow Bw$$

$$B \rightarrow w$$

Where w is a string of terminal symbol

eg $A \rightarrow Ba$

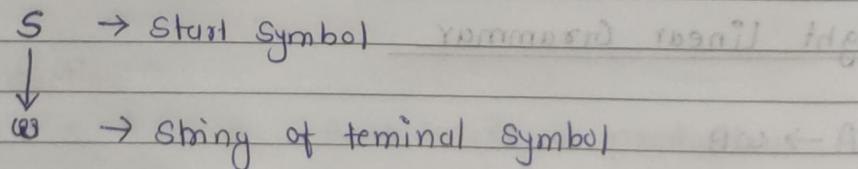
$B \rightarrow a$

* Syntax Analyzer (Parser)

Two types of parser.

- 1) Top-down parser.
- 2) Bottom-up parser.

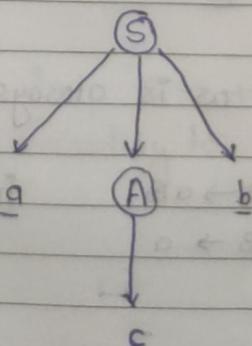
2) Top-down Parser



$$S \rightarrow ab$$

$$A \rightarrow cd/c \quad \left\{ \begin{array}{l} A \rightarrow cd \\ A \rightarrow c \end{array} \right.$$

$$w \rightarrow abc \quad \left\{ \begin{array}{l} \text{- Required string} \\ \text{of terminal symbols} \end{array} \right.$$



8/02/23

Backtracking is possible in top-down parser?

- * Why top-down parser is left most derivative in parser?

* Predictive Top-Down Parser

- 1) FIRST() function. — For finding the set of terminal symbol.

- How to calculate FIRST().

Rules \rightarrow $\text{FIRST}(\alpha) \rightarrow$ Set of these terminals with which the strings derivable from α start.

If $\alpha = XYZ$, then $\text{FIRST}(\alpha)$ is computed as follows

1) $\text{FIRST}(\alpha) = \text{FIRST}(XYZ) = \{x\}$ if x is terminal.

2) $\text{FIRST}(\alpha) = \text{FIRST}(XYZ) = \text{FIRST}(X)$ if X does not derive to an empty string. $\text{FIRST}(X)$ does not contain ϵ .

3) If $\text{FIRST}(X)$ contains ϵ , then $\text{FIRST}(\alpha) = \text{FIRST}(XYZ) = \text{FIRST}(X) - \{\epsilon\} \cup \text{FIRST}(YZ)$

Rule. 1) $S \rightarrow aC B$.
 $B \rightarrow b$.

$$\begin{aligned}\text{FIRST}(S) &\rightarrow \text{FIRST}(aB) \\ &\rightarrow \{a\}\end{aligned}$$

$$\begin{aligned}\text{FIRST}(B) &\rightarrow \text{FIRST}(b) \\ &\rightarrow \{b\}\end{aligned}$$

• Consider the grammar $S \rightarrow ACB / CbB / Ba$

$A \rightarrow da / B\epsilon$

$B \rightarrow g / \epsilon$

$C \rightarrow abh / \epsilon$

Calculate FIRST for each production.

$$\Rightarrow \text{FIRST}(S) \rightarrow \text{FIRST}(ACB) \cup \text{FIRST}(CbB) \cup \text{FIRST}(Ba) \quad \text{--- (1)}$$

$$\text{FIRST}(A) \rightarrow \text{FIRST}(da) \cup \text{FIRST}(B\epsilon)$$

$$\text{FIRST}(B) \rightarrow \text{FIRST}(g) \cup \text{FIRST}(\epsilon)$$

$$\rightarrow \{g, \epsilon\}$$

$$\text{FIRST}(C) \rightarrow \text{FIRST}(ab) \cup \text{FIRST}(\epsilon)$$

$$\rightarrow \{ab, \epsilon\}$$

$$\begin{aligned}
 ② \Rightarrow \text{FIRST}(A) &\rightarrow \text{FIRST}(da) \cup \text{FIRST}(bc) \\
 &\rightarrow \{d\} \cup \text{FIRST}(bc) - ③ \\
 &\rightarrow \{d\} \cup \{g, h, e\} \\
 &\rightarrow \{d, g, h, e\}
 \end{aligned}$$

$$\begin{aligned}
 ③ \Rightarrow \text{FIRST}(bc) &\rightarrow \text{FIRST}(b) \cup \text{FIRST}(c) \\
 &\rightarrow \{g, e\} - \{g\} \cup \{h, e\} \\
 &\rightarrow \{g, h, e\} \quad (\dots \text{put in eq } ③)
 \end{aligned}$$

$$\begin{aligned}
 ① \Rightarrow \text{First}(ba) &\rightarrow \text{FIRST}(b) - \{e\} \cup \text{FIRST}(a) \\
 &\rightarrow \{g, e\} - \{g\} \cup \{a\} \\
 &\rightarrow \{a, e\} \leftarrow
 \end{aligned}$$

$$\begin{aligned}
 ① \Rightarrow \text{FIRST}(cb) &\rightarrow \text{FIRST}(c) - \{e\} \cup \text{FIRST}(b) \\
 &\rightarrow \{h, e\} - \{e\} \cup \{b\} \\
 &\rightarrow \{h, b\} \leftarrow
 \end{aligned}$$

$$\begin{aligned}
 ① \Rightarrow \text{FIRST}(acb) &\rightarrow \text{FIRST}(a) - \{e\} \cup \text{FIRST}(cb) - ④ \\
 &\rightarrow \{d, g, h, e\} - \{e\} \cup \{h, g, e\} \\
 &\rightarrow \{d, g, h, e\} \leftarrow
 \end{aligned}$$

$$\begin{aligned}
 ④ \Rightarrow \text{FIRST}(cb) &\rightarrow \text{FIRST}(c) - \{e\} \cup \text{FIRST}(b) \\
 &\rightarrow \{h, e\} - \{e\} \cup \{g, e\} \\
 &\rightarrow \{h, g, e\} \leftarrow
 \end{aligned}$$

$$\begin{aligned}
 ① \Rightarrow \text{FIRST}(a(b) \cup \text{FIRST}(cb) \cup \text{FIRST}(ba) \\
 &\rightarrow \{d, g, h, e\} \cup \{h, b\} \cup \{g, a\} \\
 &\rightarrow \{a, b, d, g, h, e\} \leftarrow
 \end{aligned}$$

13/02/23

- Consider the following grammar calculate the FIRST for every production.

$$S \rightarrow ABC$$

$$A \rightarrow a / \epsilon$$

$$B \rightarrow r / \epsilon$$

$$C \rightarrow b / \epsilon$$

$$\text{FIRST}(S) \rightarrow \text{FIRST}(ABC) \quad -\textcircled{1}$$

$$\text{FIRST}(A) \rightarrow \text{FIRST}(a) \cup \text{FIRST}(\epsilon)$$

$$\rightarrow \{a, \epsilon\}$$

$$\text{FIRST}(B) \rightarrow \text{FIRST}(r) \cup \text{FIRST}(\epsilon)$$

$$\rightarrow \{r, \epsilon\}$$

$$\text{FIRST}(C) \rightarrow \text{FIRST}(b) \cup \text{FIRST}(\epsilon)$$

$$\rightarrow \{b, \epsilon\}$$

$$\textcircled{1} = \text{FIRST}(S) \rightarrow \text{FIRST}(ABC)$$

$$\rightarrow \text{FIRST}(A) - \{\epsilon\} \cup \text{FIRST}(BC) \quad -\textcircled{2}$$

$$\rightarrow \{r, b\} - \{\epsilon\} \cup \{r, b, \epsilon\}$$

$$\rightarrow \underline{\{a, r, b, \epsilon\}}$$

$$\textcircled{2} = \text{FIRST}(BC) \rightarrow \text{FIRST}(B) - \{\epsilon\} \cup \text{FIRST}(C)$$

$$\rightarrow \{r, b\} - \{\epsilon\} \cup \text{FIRST}\{b, \epsilon\}$$

$$\rightarrow \underline{\{r, b, \epsilon\}}$$

$$\textcircled{1} = \text{FIRST}(S) \rightarrow \{a, r, b, \epsilon\}$$

- Consider the following grammar. find FIRST for every production

$$F \rightarrow XYZa$$

$$X \rightarrow x/\epsilon$$

$$Y \rightarrow y/G$$

$$Z \rightarrow z/G$$

$$\Rightarrow \text{FIRST}(F) \rightarrow \text{FIRST}(XYZa)$$

$$\text{FIRST}(X) \rightarrow \text{FIRST}(X) \cup \text{FIRST}(\epsilon)$$

$$\rightarrow \{x, \epsilon\}$$

$$\text{FIRST}(Y) \rightarrow \text{FIRST}(y) \cup \text{FIRST}(\epsilon)$$

$$\rightarrow \{y, \epsilon\}$$

$$\text{FIRST}(Z) \rightarrow \text{FIRST}(z) \cup \text{FIRST}(\epsilon)$$

$$\rightarrow \{z, \epsilon\}$$

$$\textcircled{1} \Rightarrow \text{FIRST}(F) \rightarrow \text{FIRST}(X) - \{\epsilon\} \cup \text{FIRST}(YZa) \quad - \textcircled{2}$$

$$\textcircled{2} \Rightarrow \text{FIRST}(X) - \{\epsilon\} \cup \text{FIRST}(Za) \quad - \textcircled{3}$$

$$\textcircled{3} \Rightarrow \text{FIRST}(Za) \rightarrow \text{FIRST}(Z) - \{G\} \cup \text{FIRST}(a)$$

$$\rightarrow \{z, G\} - \{\epsilon\} \cup \{a\}$$

$$\rightarrow \{z, a\}$$

$$\textcircled{2} \Rightarrow \text{FIRST}(YZa) \rightarrow \text{FIRST}(Y) - \{\epsilon\} \cup \text{FIRST}(Za)$$

$$\rightarrow \{y, G\} - \{\epsilon\} \cup \{z, a\}$$

$$\rightarrow \{y, z, a\}$$

$$\textcircled{1} \Rightarrow \text{FIRST}(F) \rightarrow \text{FIRST}(X) - \{\epsilon\} \cup \text{FIRST}(YZa)$$

$$\rightarrow \{x, G\} - \{\epsilon\} \cup \{y, z, a\}$$

$$\rightarrow \{x, y, z, a\}$$

* Predictive Table Driver Parser

Consider the following grammar

$$S \rightarrow aAb$$

$$A \rightarrow cd / ef / \epsilon$$

calculate $\text{first}(A)$

$$\text{FIRST}(S) \rightarrow \text{FIRST}(aAb) \rightarrow \{a\} \rightarrow \{S, a\}$$

$$\text{FIRST}(A) \rightarrow \text{FIRST}(cd) \cup \text{FIRST}(ef) \rightarrow A \rightarrow cd = \{A, c\}$$

$$\rightarrow \{c, e\}$$

$$A \rightarrow ef = \{A, e\}$$

Table

	a	b	c	d	e	f	\$	ϵ
S	$S \rightarrow aAb$							
A			$A \rightarrow cd$		$A \rightarrow ef$			

We use $\text{follow}(A)$ function for finding the epsilon table if any production contain epsilon (ϵ).

* How to Calculate

The derivation by $A \rightarrow \epsilon$ is a right choice when the parser is on worse of the non-terminal A and the next input symbols happens to be a terminal which can occur immediately following

A in any string occurring on the right side of production. It will lead to the expansion of $A \rightarrow \epsilon$ and the next lead in the parse tree will be considered which is labeled by the symbol immediate following A and therefore may match next input symbol. Therefore we conclude that $A \rightarrow \epsilon$ is to be added in the table at $[A, b]$ for every small b immediately follows A in any of the production is a right hand string. To compute the set of such terminals we make the use of function $\text{FOLLOW}(A)$ where, A is a non-terminal and as defined below

* Rules -

$\text{FOLLOW}(A) \rightarrow$ Set of Terminal that immediately follow A in any string occurring on the right side of production of grammar.

If $A \rightarrow \alpha B \beta$ is a production, then $\text{follow}(B)$ will be computed as

Rule 1) $\text{FOLLOW}(B) = \text{FOLLOW}(\beta)$ if $\text{first}(\beta)$ does not contain ϵ

Rule 2) $\text{FOLLOW}(B) = \text{FOLLOW}(\beta) - \{\epsilon\} \cup \text{FOLLOW}(A)$ if $\text{first}(\beta)$ contains ϵ

17/02/23

$\text{FOLLOW}(S) \rightarrow \{\$\}$

When S is not getting the RHS of production rule

eg1) $S \rightarrow aAb$
 $A \rightarrow c$

$\text{FOLLOW}(A) \rightarrow \text{FIRST}(b)$
 $\rightarrow \{b\}$

$S \rightarrow aAbc$

$A \rightarrow c$

$\text{FOLLOW}(A) \rightarrow \text{FIRST}(bc)$
 $\rightarrow \{b\}$

eg2) $S \rightarrow aAB$
 $A \rightarrow d$
 $B \rightarrow c/e$

$\text{FOLLOW}(S) \rightarrow \{\$\}$

$\text{FOLLOW}(A) \rightarrow \text{FIRST}(B) - \{\epsilon\} \cup \text{FOLLOW}(S)$

$\text{FIRST}(B) \rightarrow \{c, \epsilon\}$

$\text{FOLLOW}(A) \rightarrow \{c, d\} - \{\epsilon\} \cup \{\$\}$
 $\rightarrow \{c, \$\}$

- Consider the following grammar & generate the predictive parsing table

$S \rightarrow aABBb$

$A \rightarrow c/e$

$B \rightarrow d/\epsilon$

$\text{FIRST}(S) \rightarrow \text{FIRST}(aABBb) \rightarrow \{a\}$ (S, 4)

$\text{FIRST}(A) \rightarrow \text{FIRST}(c) \cup \text{FIRST}(\epsilon)$
 $\rightarrow \{c, \epsilon\}$

$\text{FIRST}(B) \rightarrow \text{FIRST}(d) \cup \text{FIRST}(\epsilon)$
 $\rightarrow \{d, \epsilon\}$

$S \rightarrow aABb$

$\text{FOLLOW}(A) \rightarrow \text{FIRST}(Bb) \quad \rightarrow \textcircled{1}$

$\text{FIRST}(Bb) \rightarrow \text{FIRST}(B) \cup \text{FIRST}(b)$

$\rightarrow \text{FIRST}(B) - \{\epsilon\} \cup \text{FIRST}(b)$

$\rightarrow \{d, g\} - \{\epsilon\} \cup \{b\}$

$\rightarrow \{d, b\}$

$\Rightarrow \text{FOLLOW}(A) \rightarrow \{d, b\}$

$\text{FOLLOW}(B) \rightarrow \text{FIRST}(b)$

$\rightarrow \{b\}$

Predictive parsing Table.

	a	b	c	d	\$
$S \rightarrow aABb$					
A		$A \rightarrow e$	$A \rightarrow c$	$A \rightarrow g$	
B		$B \rightarrow e$		$B \rightarrow d$	

20/02/23
Lecture 10

Consider the grammar

$F \rightarrow XYZa$

$X \rightarrow x/\epsilon$

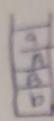
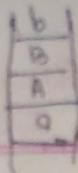
$Y \rightarrow y/\epsilon$

$Z \rightarrow z/\epsilon$

1) Find the FIRST() & FOLLOW()

2) Generate the parsing table

\Rightarrow as per the schedule of 13/02/23. for calculating of FIRST



$$F \rightarrow XYZa$$

$$\text{FOLLOW}(X) \rightarrow \text{FIRST}(YZa)$$

$$\rightarrow \{Y, Z, a\}$$

$$\text{FOLLOW}(Y) \rightarrow \text{FIRST}(Za)$$

$$\rightarrow \{Z, a\}$$

$$\text{FOLLOW}(Z) \rightarrow \text{FIRST}(a)$$

$$\rightarrow \{a\}$$

Predictive parsing Table

	x	y	z	a	s
F	$F \rightarrow XYZa$	$F \rightarrow XYZa$	$F \rightarrow XYZa$	$F \rightarrow XYZa$	
X	$X \rightarrow x$	$X \rightarrow \epsilon$	$X \rightarrow \epsilon$	$X \rightarrow \epsilon$	
Y		$Y \rightarrow y$	$Y \rightarrow \epsilon$	$Y \rightarrow \epsilon$	
Z			$Z \rightarrow z$	$Z \rightarrow \epsilon$	

20/02/23
2nd class

- consider the grammar

$$S \rightarrow aABb$$

$$A \rightarrow c/\epsilon$$

$$B \rightarrow d/\epsilon$$

1) string $w \rightarrow acdb$

The string is parseable or not by stacking method/
Stack in top-down parser with stack?

2)

1) $w \rightarrow acdb$

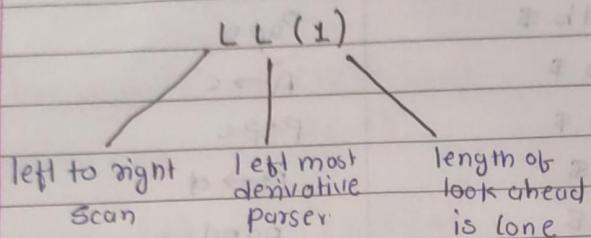
Stack	Unspent I/p	Moves
\$ S	acdb \$	$S \rightarrow aABb$
\$ bBAg	acdb \$	(Pop a $A' \rightarrow c$)
\$ bBA	cdb \$	Pop c
\$ bBc	cdb \$	$B \rightarrow d$
\$ bB	db \$	pop d
\$ b	db \$	pop b
\$	\$	String is parse

2) $w \rightarrow ab$

Stack	Unspent I/p	Moves
\$ S	ab \$	$S \rightarrow aAb$
\$ aAb	ab \$	(Pop a)
\$ bBA	b \$	$A \rightarrow \epsilon$
\$ bBc	c \$	Pop c
\$ bB	b \$	$B \rightarrow \epsilon$
\$ b	b \$	Pop b
\$	\$	String is parse

★ LL(1) - parser.

LL(1) is top-down parser.



If the predictive table contain only single production in single cell.

→ Algorithm

For every pair of production.
 $A \rightarrow \alpha / \beta$

$\text{FIRST}(\alpha) \cap \text{FIRST}(\beta) = \emptyset$

{
 grammar is LL(1)

→ Test whether the grammar is LL(1) or not and construct a predictive parsing table for it.

$$S \rightarrow AaAb / BbBq$$

$$A \rightarrow \epsilon$$

$$B \rightarrow \epsilon$$

$$\rightarrow S \rightarrow \frac{AaAb}{\alpha} / \frac{BbBq}{\beta}$$

$$\text{FIRST}(\alpha) \cap \text{FIRST}(\beta) = \emptyset \quad - \textcircled{1}$$

$$\begin{aligned} \text{FIRST}(AaAb) &\rightarrow \text{FIRST}(A) - \{\epsilon\} \cup \text{FIRST}(aAb) \\ &\rightarrow \{\epsilon\} - \{\epsilon\} \cup \{a\} \\ &\rightarrow \{a\} \end{aligned}$$

$$\begin{aligned}\text{FIRST}(BbBa) &\rightarrow \text{FIRST}(B) - \{\epsilon\} \cup \text{FIRST}(bBa) \\ &\rightarrow \{\epsilon\} \cup \{b\} \cup \{b\} \\ &\rightarrow \{b\}\end{aligned}$$

i) $\Rightarrow \{a\} \cap \{b\} \rightarrow \{\phi\} \rightarrow$ Hence, the grammar is LL(1)

ii) FOLLOW(S) $\rightarrow \{\$\}$ to obtain initial
 FOLLOW(A) $\rightarrow \text{FIRST}(aAb)$ $\because S \rightarrow \underline{AaAb}$
 $\rightarrow \{a\}$

iii) FOLLOW(A) $\rightarrow \text{FIRST}(b)$
 $\rightarrow \{b\}$

from i) and ii)
 $\text{FOLLOW}(A) = \{b, a\}$

i) FOLLOW(B) $\rightarrow \text{FIRST}(bBa)$ $\{\phi\} \leftarrow \because S \rightarrow \underline{BbBa}$
 $\rightarrow \{b\}$

ii) FOLLOW(B) $\rightarrow \text{FIRST}(a)$ $\because S \rightarrow \underline{BbBa}$
 $\rightarrow \{a\}$ Both are first at

from i) and ii)

$$\text{FOLLOW}(B) = \{b, a\}$$

$$\text{FIRST}(S) \rightarrow \text{FIRST}(AaAb) \cup \text{FIRST}(BbBa)$$

$$\begin{aligned}&\rightarrow \{a\} \cup \{b\} \\ &\rightarrow \{a, b\}\end{aligned}$$

$$\text{FIRST}(A) \rightarrow \epsilon$$

$$\text{FIRST}(B) \rightarrow \epsilon$$

	a	b	g	REDUCE IT
S	$S \rightarrow AaAb$	$S \rightarrow BbBb$	-	-
A	$A \rightarrow \epsilon$	$A \rightarrow \epsilon$	-	-
B	$B \rightarrow \epsilon$	$B \rightarrow \epsilon$	-	-

* Elimination of Left Recursion

$$S \rightarrow aIJh$$

$$I \rightarrow IbSe / c$$

$$J \rightarrow kLkx / \epsilon$$

$$k \rightarrow d / \epsilon$$

$$L \rightarrow p / \epsilon$$

$$\text{FIRST}(S) \rightarrow \text{FIRST}(aIJh)$$

$$\rightarrow \{a\}$$

$$\text{FIRST}(I) \rightarrow \text{FIRST}(IbSe) \cup \text{FIRST}(c)$$

In that we are getting the left Recursion

Consider the given

If a grammar contains pair of production of the form $A \rightarrow A\alpha / \beta$ then the grammar is called left recursive grammar.

Consider the grammar containing left recursion.
 $A \rightarrow A\alpha/B$ where B does not begin with A to
 eliminate the left recursion replace the pair of production
 with $A \rightarrow BA'$

$$A' \rightarrow \alpha A'/\epsilon$$

→ New production will be,

Hence,

$$\begin{array}{l} S \xrightarrow{\cdot} aIJh \\ \quad I \rightarrow \underset{\alpha}{I} \underset{B}{\underline{bSe}} / \epsilon \\ \quad \quad \downarrow \\ \quad 1) \quad I \rightarrow cI' \\ \quad 2) \quad I' \rightarrow bSeI'/\epsilon \end{array}$$

$$\times \text{ Now, } S \rightarrow aIJh$$

$$I \rightarrow cI'$$

$$I' \rightarrow bSeI'/\epsilon$$

$$J \rightarrow kLkr/\epsilon$$

$$k \rightarrow d/\epsilon$$

$$L \rightarrow p/\epsilon$$