

First - order Logic (FOL)?

* First - order Logic (FOL) also called predicate Logic (∞) First order predicate Logic (FopL) is an extension of propositional Logic.

which only deals with simple true / false statements.

components

1) constants

Represent specific objects in a domain.

Ex: John, Apple, 2, Earth.

2) variables

Represent arbitrary objects

Ex, x, y, z.

3) Predicates (Relations)

Describe properties of object (or)
relationships b/w them

$\text{Human}(\text{John}) \rightarrow \text{John is a human}$

4) Functions.

A function takes inputs and
produces one output.

Ex: $\text{Father}(\text{John}) = \text{David}$
(David is John's father).

5) Logical connectives.

AND (\wedge)

OR (\vee)

Not (\neg)

implies (\rightarrow)

If and only if (\leftrightarrow).

6) Quantifiers

Quantifiers allow us to make general (or) existential statements.

1. Universal Quantifier (\forall) ("For all")

$$\forall x \text{ human}(x) \rightarrow \text{mortal}(x)$$

For all x , if x is a human, then x is mortal.

2. Existential Quantifier (\exists) ("There exists").

$$\exists x \text{ Loves}(x, \text{mary})$$

There exists at least one x who loves mary.

Difference b/w propositional Logic and First order Logic

Feature	Propositional Logic	First-order Logic (FOL).
objects	no objects	uses objects (constant, variables)
Relations	cannot express relations	can find relationships (predicates)
Functions	Not possible	Functions are allowed
Quantifiers	Not available	uses \forall (For all) and \exists (exists)
Ex:	$p \vee q$ (Either p or q)	$\forall x (\text{Human}(x) \rightarrow \text{Mortal}(x))$