

21BCE7371

RADHA KRISHNA GARG

AI LAB ASSIGNMENT-4

1. DEPTH FIRST SEARCH [DFS]

In the depth-first search (DFS), we go as far down as possible into search tree/graph before backing up and trying alternatives. It works by always generating a descendent of the most recently expanded node until some depth cut off is reached and then backtracks to next most recently expanded node and generates one of its

descendants. DFS is memory efficient, as it only stores a single path from the root to leaf node along with the remaining unexpanded siblings for each node on the path.

We can implement DFS by using two lists called OPEN and CLOSED. The OPEN list contains those states that are to be expanded, and CLOSED list keeps track of states already expanded. Here OPEN and CLOSED lists are maintained as stacks. If we discover that first element of OPEN is the goal state then search terminates successfully. We can get track of the path through state space as we traversed, but in those situations where many nodes after expansion are in the closed list, we fail to keep track of our path. This information can be obtained by modifying CLOSED list by putting pointer back to its parent in the search tree.

Algorithm

Input: START and GOAL states.

Local variables: OPEN, CLOSED, STATE-X, SUCCs, FOUND;

Output: yes or NO

RECORD-X

Method:

- initialize OPEN list with START^{nil} and CLOSED = \emptyset ;
- FOUND = false;
- While (OPEN $\neq \emptyset$ and FOUND = false) do
 - {
record (initially (START, nil))
 - remove the first state from OPEN and call it
STATE-X;
RECORD-X

- put ^{RECORD-X}STATE-X in the front of CLOSED list {maintained as stack};
- If STATE-X_i = GOAL then FOUND = true else
if RECORD-X
 - perform EXPAND operation on STATE-X, producing a list of states; records called SUCCs;
 - remove from successors those states, if any, that are in the CLOSED lists:
 - ^{insert}append SUCCs ⁱⁿat the ^{end}of the OPEN list:
front
- }
- }/ * End While */
- if FOUND = true then return ^{the path by tracing}yes else ~~return NO~~
- Stop. ^{through the pointers to the parents on}the CLOSED list else return NO.

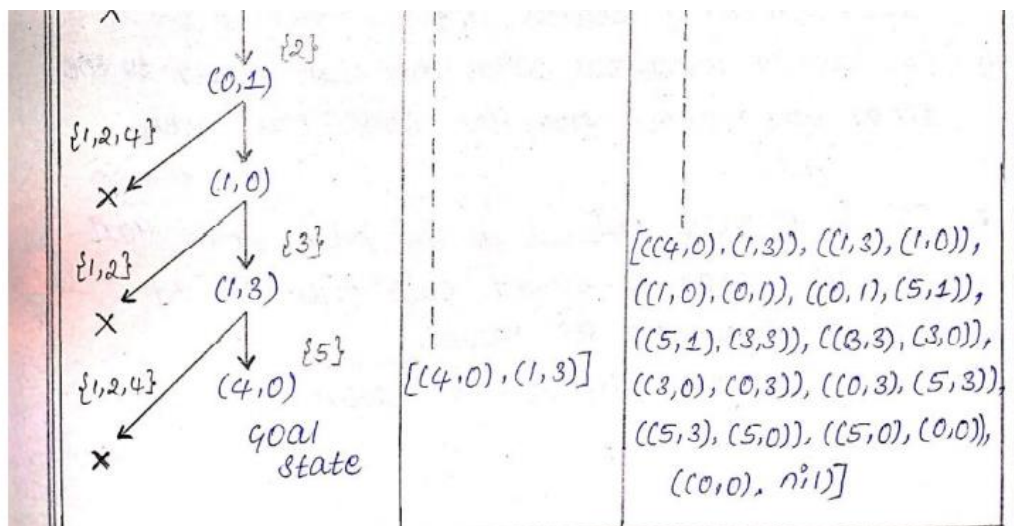
Let us see the search tree generation from start state of the water jug problem using DFS algorithm. At each state, we apply first applicable

rule. if it generates previously generated state then cross it and try another rule in the sequence to avoid the looping. If new state is generated then cross it and try another rule in sequence to avoid the looping. If new state is generated then expand this state in breadth first problem/ fashion.

The rules applied and enclosed for water jug problem are:

Let us see the search tree generation from start state of the water jug problem using DFS algorithm.

| Water jug problem | | |
|---|------------------|--|
| Search tree generation using DFS | OPEN list | CLOSED list |
| Start State (0,0) | $[(0,0), nil]$ | |
| $\downarrow \{1\}$ (5,0) | $[(5,0), (0,0)]$ | $[(0,0), nil]$ |
| $\swarrow \{2\}$ X $\downarrow \{3\}$ (5,3) | $[(5,3), (5,0)]$ | $[(5,0), (0,0)], [(0,0), nil]$ |
| $\downarrow \{2\}$ (0,3) | $[(0,3), (5,3)]$ | $[(5,3), (5,0)], [(5,0), (0,0)], [(0,0), nil]$ |
| $\swarrow \{1,4\}$ X $\downarrow \{5\}$ (3,0) | $[(3,0), (0,3)]$ | $[(0,3), (5,3)], [(5,3), (5,0)], [(5,0), (0,0)], [(0,0), nil]$ |
| $\downarrow \{3\}$ (3,3) | $[(3,3), (3,0)]$ | $[(3,3), (3,0)], [(0,3), (5,3)], [(5,3), (5,0)], [(5,0), (0,0)], [(0,0), nil]$ |
| $\swarrow \{1,2,4\}$ X $\downarrow \{7\}$ (5,1) | | |
| $\downarrow \{2\}$ (0,1) | | |
| $\swarrow \{1,2,4\}$ | | |



The path is obtained from the list stored in CLOSED. The solution path is

$(0,0) \rightarrow (5,0) \rightarrow (5,3) \rightarrow (0,3) \rightarrow (3,0) \rightarrow (3,3) \rightarrow (5,1) \rightarrow (0,1) \rightarrow (1,0) \rightarrow (1,3) \rightarrow (4,0)$

- ⊙ BFS is effective when the search tree has a low branching factor.
- ⊙ BFS can work even in trees that are infinitely deep.
- ⊙ BFS requires a lot of memory as number of nodes in level of the tree increases exponentially.
- ⊙ BFS is superior when the GOAL exists in the upper right portion of a search tree.
- ⊙ BFS gives optimal solution.
- ⊙ DFS is effective when there are few sub trees in the search tree that have only one connection point to the rest of states.
- ⊙ DFS is best when the GOAL exists in the lower left portion of search tree.
- ⊙ DFS can be dangerous when the path closer to the START and farther from the GOAL has been chosen.
- ⊙ DFS is memory efficient as the path from start to current node is stored. Each node should contain state and its parent.
- ⊙ DFS may not give optimal solution.

Algorithm:

Input: START and GOAL states

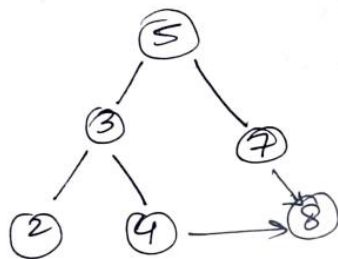
Local variables: OPEN, CLOSED, STATE-X, SUCCESS, FOUND;

Output: yes or NO

Method:

- initialize OPEN list with START and CLOSED = \emptyset
- FOUND = false;

SFS



If we implement using ~~SFS~~ DFS we travel to depth first and then to other nodes so it should be

Output:-

5 3 2 4 8 7

```
main.py
1 graph = {
2     '5' : ['3','7'],
3     '3' : ['2', '4'],
4     '7' : ['8'],
5     '2' : [],
6     '4' : ['8'],
7     '8' : []
8 }
9
10 visited = set() # Set to keep track of visited nodes of graph.
11
12 def dfs(visited, graph, node): #function for dfs
13     if node not in visited:
14         print (node)
15         visited.add(node)
16         for neighbour in graph[node]:
17             dfs(visited, graph, neighbour)
18
19 # Driver Code
20 print("Following is the Depth-First Search")
21 dfs(visited, graph, '5')
```

OUTPUT

```
Shell
Following is the Depth-First Search
5
3
2
4
8
7
> |
```


2. BREADTH FIRST SEARCH [BFS]

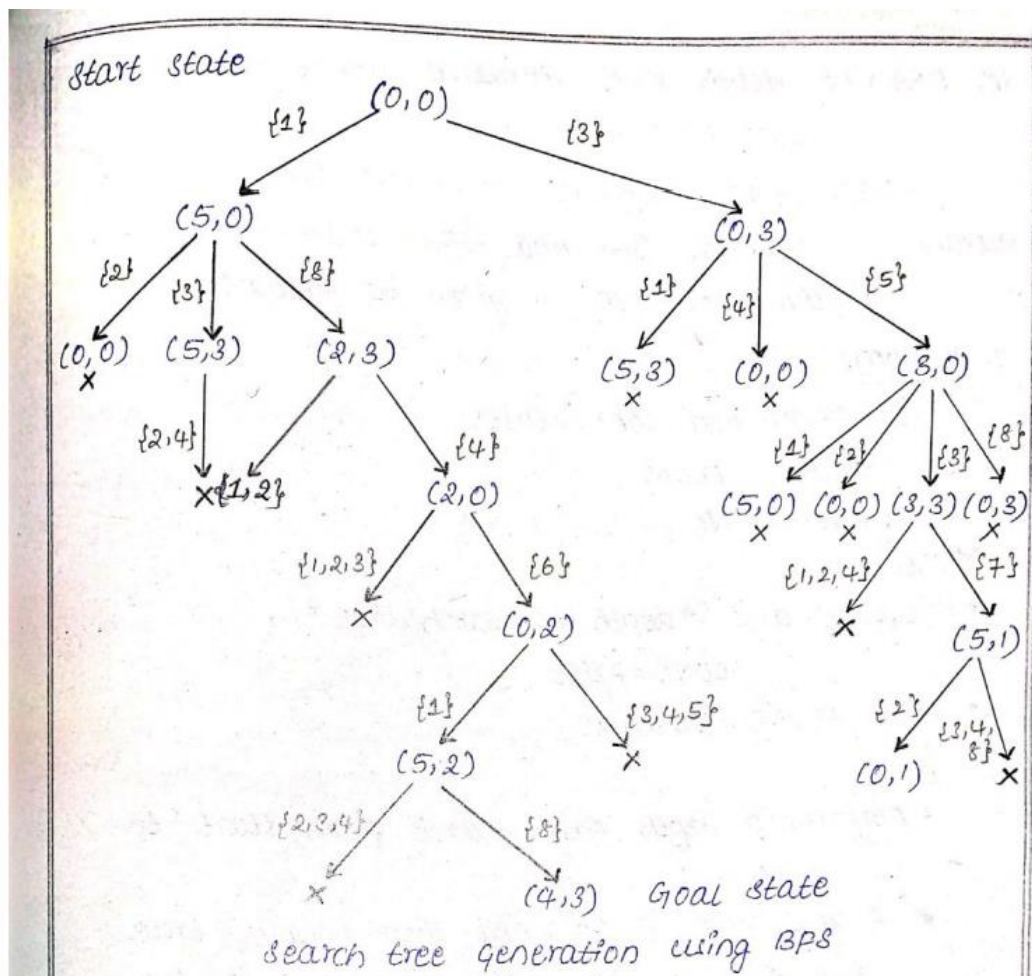
Breadth first search:

The breadth first search expands all the states one step away from the start state and then expands all states two steps from start, then three steps, etc., until a goal state is reached. All successor states are examined at the same depth before going deeper. The BFS always gives an optimal path or solution.

This search is implemented using two lists called open and closed. The open list contains those states that are to be expanded and closed list keeps track of states already expanded. Here open list is maintained as a queue and closed list as a stack. For the sake of simplicity, we are writing BFS algorithm for checking whether a goal node exists or not. Further, this algorithm can be modified to get a path from start to goal nodes by maintaining closed list with pointer back to its parent in the search tree.

- While ($OPEN \neq \emptyset$ and $FOUND = \text{false}$) do
 - {
 - perform EXPAND operation remove the first state from OPEN and call it STATE-X;
 - put STATE-X in the front of CLOSED list;
 - if STATE-X = GOAL then $FOUND = \text{true}$ else
 - {
 - perform EXPAND operation on STATE-X, producing a list of SUCCS;
 - remove from successors those states, if any, that are in the CLOSED list;
 - append SUCCS at the end of OPEN list;
 - }
 - }
- } /* end while */
- if $FOUND = \text{true}$ then return yes else return no
- stop

Let us see the search tree generation from start state of the water jug problem using BFS algorithm. At each state, we apply first applicable rule. If it generates previously generated state then cross it and try another rule in the sequence to avoid the looping. If new state is generated then expand this state in breadth first fashion.



Search tree is developed level wise. This is not memory efficient as partially developed tree is to be kept in the memory but it finds optimal solution or path. We can easily see the path from start to goal by tracing the tree from goal state to start state through parent link. This path is optimal and we cannot get a path shorter than this.

Solution path : $(0,0) \rightarrow (5,0) \rightarrow (2,3) \rightarrow (2,0) \rightarrow (0,2) \rightarrow (5,2) \rightarrow (4,3)$

Q 2 Jugs A and B, Jug A can hold $\rightarrow 3L$

Jug B $\rightarrow 4L$, There's a requirement to obtain 2L of water from one of the Jugs somehow

Sol Steps we can perform

1. Empty a Jug

2. fill a Jug

3. Pour water from one jug to another until one of the Jugs is either empty or full.

USING BFS

States as (A, B)

A \rightarrow Amount of water in A

B \rightarrow Amount of water in B

$(0, 0) \rightarrow$ initial

$(0, 2), (2, 0) \rightarrow$ final

Steps using this approach

1. Fill Empty a Jug \rightarrow Transition could be $(A, B) \rightarrow (0, B)$
Let's assume we empty Jug A.

2. fill a Jug $\rightarrow (0, 0) \rightarrow (A, 0)$, Assume filling Jug A.

3. Pour water $\rightarrow (A, B) \rightarrow (A-d, B+d)$

Implementation in Code

IMPLEMENTATION IN CODE:

```
main.py
1 from collections import deque
2
3 def BFS(a, b, target):
4
5     # Map is used to store the states, every
6     # state is hashed to binary value to
7     # indicate either that state is visited
8     # before or not
9     m = {}
10    isSolvable = False
11    path = []
12
13    # Queue to maintain states
14    q = deque()
15
16    # Initialing with initial state
17    q.append((0, 0))
18
19    while (len(q) > 0):
20
21        # Current state
22        u = q.popleft()
23
24        # If this state is already visited
25        if ((u[0], u[1]) in m):
26            continue
27
28        # Doesn't met jug constraints
29        if ((u[0] > a or u[1] > b or
30             u[0] < 0 or u[1] < 0)):
31            continue
32
33        # Filling the vector for constructing
34        # the solution path
35        path.append([u[0], u[1]])
36
37        # Marking current state as visited
38        m[(u[0], u[1])] = 1
39
40        # If we reach solution state, put ans=1
41        if (u[0] == target or u[1] == target):
42            isSolvable = True
43
44            if (u[0] == target):
45                if (u[1] != 0):
46
47                    # Fill final state
48                    path.append([u[0], 0])
49            else:
50                if (u[1] != 0):
51
52                    # Fill final state
53                    path.append([0, u[1]])
54
55        # Print the solution path
56        sz = len(path)
57        for i in range(sz):
58            print("(", path[i][0], ",",
59                  path[i][1], ")")
60        break
61
62        # If we have not reached final state
63        # then, start developing intermediate
64        # states to reach solution state
65        q.append([u[0], b]) # Fill Jug B
66        q.append([a, u[1]]) # Fill Jug A
67
68        for ap in range(max(a, b) + 1):
69
70            # Pour amount ap from Jug B to Jug A
71            c = u[0] + ap
72            d = u[1] - ap
73
74            # Check if this state is possible or not
75            if (c == a or (d == 0 and d >= 0)):
76                q.append([c, d])
77
78            # Pour amount ap from Jug A to Jug B
79            c = u[0] - ap
80            d = u[1] + ap
81
82            # Check if this state is possible or not
83            if ((c == 0 and c >= 0) or d == b):
84                q.append([c, d])
85
86            # Empty Jug B
87            q.append([a, 0])
88
89            # Empty Jug A
90            q.append([0, b])
91
92        # No, solution exists if ans=0
93        if (not isSolvable):
94            print("No solution")
95
96    # Driver code
97    if __name__ == '__main__':
98
99        JugA, JugB, target = 3, 4, 2
100        print("Path from initial state "
101              "to solution state ::")
102
103        BFS(JugA, JugB, target)
```

OUTPUT

```
Path from initial state to solution state ::
( 0 , 0 )
( 0 , 4 )
( 3 , 0 )
( 3 , 4 )
( 3 , 1 )
( 0 , 3 )
( 3 , 3 )
( 2 , 4 )
( 2 , 0 )
```


#Path from initial state to solution state ::

(0 , 0)

(0 , 4)

(3 , 0)

(3 , 4)

(3 , 1)

(0 , 3)

(3 , 3)

(2 , 4)

(2 , 0)