

1 Concrete Semantics of Scheme CESK*

Syntax:

$$\begin{aligned}
 e \in \mathbf{Exp} &::= \mathfrak{x} \\
 &\quad | (\mathbf{if} \ e \ e \ e) \\
 &\quad | (\mathbf{let} \ (x \ e) \ e) \\
 &\quad | (\mathbf{prim} \ op \ e \ e \dots) \\
 &\quad | (e \ e \dots) \\
 \mathfrak{x} \in \mathbf{AExp} &::= lam \mid \mathbb{Z} \mid \#\mathbf{t} \mid \#\mathbf{f} \\
 lam \in \mathbf{Lam} &::= (\lambda \ (x \dots) \ e) \\
 x \in \mathbf{Var} &\quad \text{A set of identifiers}
 \end{aligned}$$

Semantics:

$$\begin{aligned}
 \varsigma \in \Sigma &\triangleq \mathbf{Exp} \times \mathbf{Env} \times \mathbf{Kont} \\
 \rho \in \mathbf{Env} &\triangleq \mathbf{Var} \rightarrow \mathbf{Addr} \\
 \sigma \in \mathbf{Store} &\triangleq \mathbf{Addr} \rightarrow \mathbf{Val} \\
 v \in \mathbf{Val} &\triangleq \mathbf{Clo} + \mathbb{Z} + \{\#\mathbf{t}, \#\mathbf{f}\} \\
 clo \in \mathbf{Clo} &\triangleq \mathbf{Lam} \times \mathbf{Env} \\
 \kappa \in \mathbf{Kont} &\triangleq \mathbf{mt} \mid \mathbf{appk}(done, todo, \rho, a) \\
 &\quad \mid \mathbf{ifk}(e, e, \rho, a) \\
 &\quad \mid \mathbf{letk}(x, e, \rho, a) \\
 a, b, c \in \mathbf{Addr} &\quad \text{A set of addresses} \\
 done &\triangleq \mathbf{Val}^* \quad todo \triangleq \mathbf{Exp}^*
 \end{aligned}$$

Atomic Evaluation Function:

$$\begin{aligned}
 \mathcal{A}(x, \rho, \sigma) &\triangleq \sigma(\rho(x)) \\
 \mathcal{A}(lam, \rho, \sigma) &\triangleq (lam, \rho) \\
 \mathcal{A}(\mathfrak{x}, \rho, \sigma) &\triangleq \mathfrak{x}
 \end{aligned}$$

Transition Function:

$$(\Sigma \times \mathbf{Store}) \rightsquigarrow (\Sigma \times \mathbf{Store})$$

$(\varsigma \times \sigma) \rightsquigarrow (\varsigma' \times \sigma)$, where $\kappa = \sigma(a)$, $b = \text{alloc}(\varsigma)$
 proceed by matching on ς

$\langle (\text{if } e_c \ e_t \ e_f), \rho, a \rangle$	$\langle e_c, \rho, b \rangle$ $\sigma[b \mapsto \text{ifk}(e_t, e_f, \rho, a)]$
$\langle (\text{let } (x \ e_x) \ e_b), \rho, a \rangle$	$\langle e_x, \rho, b \rangle$ $\sigma[b \mapsto \text{letk}(x, e_b, \rho, a)]$
$\langle (\text{prim } op \ e_0 \ es...), \rho, a \rangle$	$\langle e_0, \rho, b \rangle$ $\sigma[b \mapsto \text{appk}([op], es, \rho, a)]$
$\langle (e_f \ es...), \rho, a \rangle$	$\langle e_f, \rho, b \rangle$ $\sigma[b \mapsto \text{appk}([], es, \rho, a)]$
$\langle \mathfrak{x}, \rho, a \rangle$ let $v = \mathcal{A}(\mathfrak{x}, \rho, \sigma)$ match on κ below	
mt	ς
ifk (e_t, e_f, ρ', c) when $v = \#f$	$\langle e_f, \rho', c \rangle$
ifk (e_t, e_f, ρ', c) when $v \neq \#f$	$\langle e_t, \rho', c \rangle$
letk (x, e_b, ρ', c)	$\langle e_b, \rho'[x \mapsto b], c \rangle$ $\sigma[b \mapsto v]$
appk $(done, e_h :: e_t, \rho', c)$	$\langle e_h, \rho', b \rangle$ $\sigma[b \mapsto \text{appk}(done \# [v], e_t, \rho', c)]$
appk $(op :: v_s, [], \rho', c)$	$\langle v', \rho', c \rangle$ $v' = op$ applied to $(v_s \# [v])$
appk $(clo :: v_s, [], \rho', c)$ where $clo = ((\lambda (x_s...) \ e_b), \rho_\lambda)$	$\langle e_b, \rho_\lambda[x_{s0} \mapsto b_0 \dots x_{si} \mapsto b_i], c \rangle$ $v'_s = v_s \# [v]$ $\sigma[b_0 \mapsto v'_{s0} \dots b_i \mapsto v'_{si}]$

2 Abstract Semantics of Scheme CESK*