EDA & REGRESSION COURSEWORK 2024

The dataset for this coursework assignment, *MavenRail.csv*, is a synthetic dataset created by Maven Analytics for an online data analytics challenge. Participants were tasked with building an exploratory dashboard based on fictional traveler behavior and operational performance on the UK National Rail network.

According to Spiegelhalter's 'star rating' system, the dataset would earn a "4*" rating—if it were factual—indicating high confidence as "numbers we can believe" (Muldoon, 2024).

The dataset contains 31,645 rows of individual traveler journeys, described across 13 columns:

1	Payment Method	Contactless, Credit Card, Debit Card				
2	Railcard Type	Adult, Disabled, Senior, None				
3	Ticket Class	First Class, Standard				
4	Ticket Type	Advance, Anytime, Off-Peak				
5	Price	GBP				
6	Departure Station	Various UK National Rail Stations				
7	Arrival Station	Various UK National Rail Stations				
8	Departure Time	YYYY/mm/dd HH:MM				
9	Scheduled Arrival	YYYY/mm/dd HH:MM				
10	Actual Arrival					
11	Journey Status	On Time, Delayed, Cancelled				
12	Reason for Delay	Signal Failure, Technical Issue, Weather,				
		Staffing, Staff, Traffic				
13	Refund Request	Yes/No				

These details suggest the dataset was designed to study how journey delays and cancellations impact refund requests, a critical performance metric for service providers like National Rail.

Data Preparation

To begin, I examined the dataset structure. Most values were categorical, including Departure, Scheduled Arrival, and Actual Arrival, with some missing values in key columns: Railcard (67%), Actual Arrival (5.9%), and Reason for Delay (86.8%).

- Railcard: Null values were replaced with "None," a valid category alongside "Adult," "Disabled," and "Senior."
- Reason for Delay: Null values were similarly replaced with "None."

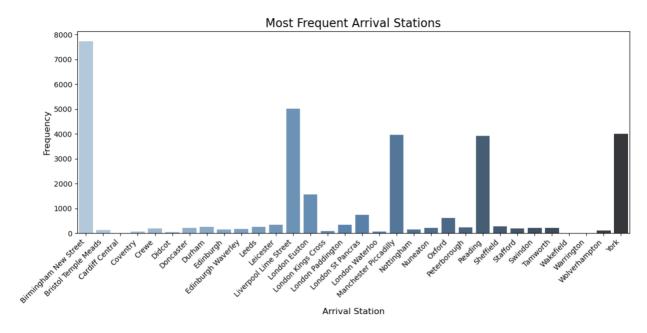
- Scheduled Arrival and Departure: Null values were removed due to their low frequency.
- Actual Arrival: Null values were replaced with "NA," indicating no delay.

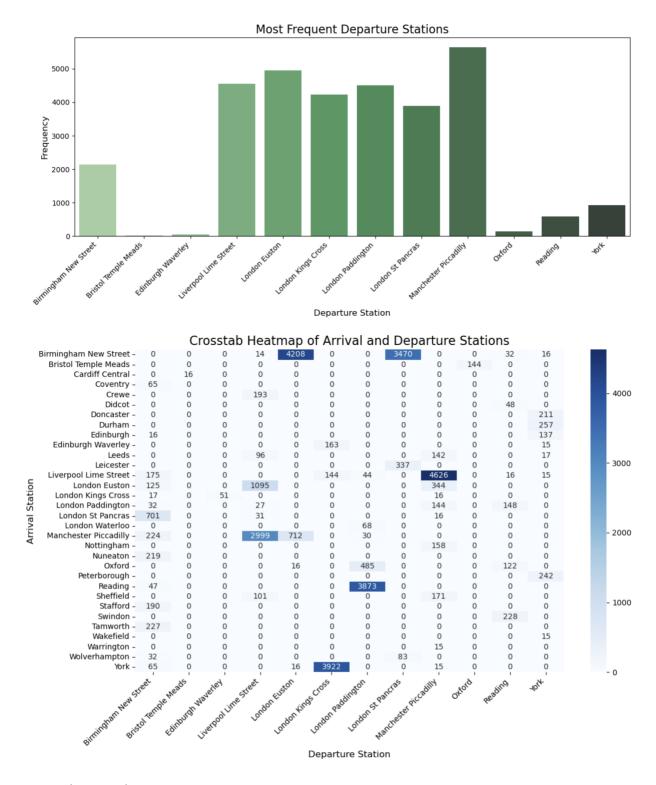
For analysis, departure and arrival times were converted to datetime64. Null values in Actual Arrival were marked as "Not a Time" to avoid exceptions during conversion.

Exploratory Data Analysis

Departure and Arrival Patterns

Using cross-tabulations, I found that Manchester Piccadilly was the most frequent departure station, and Liverpool Lime Street the most common arrival station. The most frequent journey was from Manchester Piccadilly to Liverpool Lime Street.





Ticket Prices

Univariate analysis of ticket prices revealed:

Mean: £23.43

Standard deviation: £29.98

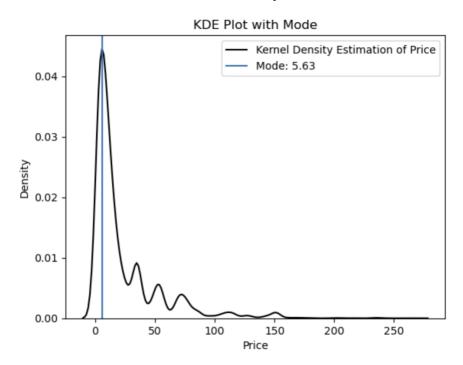
• Minimum: £1

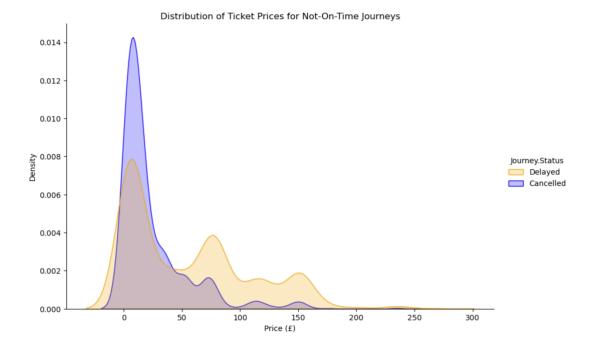
Maximum: £267

Median: £11

Mode: £3

A Kernel Density Estimation (KDE) plot showed a KDE mode of £5.63, differing from the raw data mode likely due to the influence of outliers (e.g., tickets above £250). Price analysis by journey status showed that delayed trips were costlier, while cancelled trips had a higher density at lower prices. This might indicate that cheaper, more frequent routes are cancelled more often, while costlier routes are delayed to avoid cancellations.





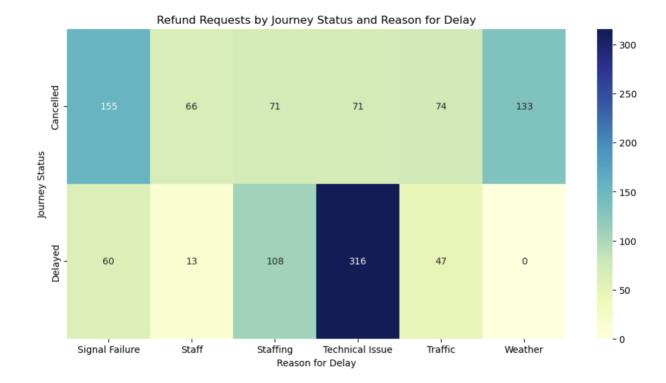
Analysis of Refund Requests

To examine refund requests, I filtered the dataset to include only delayed or cancelled journeys and cross-tabulated them with Reason for Delay. Results showed that:

- **Delayed Journeys:** Refund requests were most frequent when delays were due to technical issues.
- Cancelled Journeys: Signal failure was the leading cause, drawing the most refund requests.

When analyzing the relationship between Reason for Delay and Minutes Delayed:

- Travelers on delayed trains waited most often due to weather.
- For cancelled trains, the longest delays were caused by signal failure



Data Transformation

To prepare for modeling, I calculated the delay in minutes by subtracting Scheduled Arrival from Actual Arrival, with no-delay values marked as 0.0 and then replaced with "NA." A new column, *MediumPrice*, was created to indicate whether ticket prices fell between £10 and £30, mapped as binary values ("Yes" or "No").

Outliers in ticket prices were removed using a Z-score threshold, reducing the maximum price to £113 and the mean to £20.43 across 30,881 values. I converted categorical columns to numerical or categorical types as needed, with DelayInMinutes set to numeric, replacing "NA" values with 0.

Price	Departure.Station	Arrival.Station	Departure	Scheduled.Arrival	Actual.Arrival	Journey.Status	Reason.for.Delay	Refund.Request	DelayInMinutes
43	London Paddington	Liverpool Lime Street	2024-01- 01 11:00:00	2024-01-01 13:30:00	2024-01-01 13:30:00	On Time	NA	No	NA
23	London Kings Cross	York	2024-01- 01 09:45:00	2024-01-01 11:35:00	2024-01-01 11:40:00	Delayed	Signal Failure	No	5.0
3	Liverpool Lime Street	Manchester Piccadilly	2024-01- 02 18:15:00	2024-01-02 18:45:00	2024-01-02 18:45:00	On Time	NA	No	NA
13	London Paddington	Reading	2024-01- 01 21:30:00	2024-01-01 22:30:00	2024-01-01 22:30:00	On Time	NA	No	NA
76	Liverpool Lime Street	London Euston	2024-01- 01 16:45:00	2024-01-01 19:00:00	2024-01-01 19:00:00	On Time	NA	No	NA

Logistic Regression Models

Single-Predictor Model

```
#fit small model with one predictor
X_1 = journey_final['MediumPrice'].values.reshape(-1, 1)
X_1 = sm.add_constant(X_1)
 #set response variable
y = journey_final.loc[:, journey_final.columns == 'Refund.Request_Yes']
logit_model=sm.Logit(y,X_1)
result1=logit_model.fit()
print(result1.summary2())
Optimization terminated successfully.

Current function value: 0.578797
                 Iterations 5
                                                 Results: Logit

        Model:
        Logit
        Method:
        MLE

        Dependent Variable:
        Refund.Request_Yes
        Pseudo R-squared:
        0.003

        Date:
        2024-11-21
        00:14
        AIC:
        4825.3797

No. Observations:
Df Model:
Df Residuals:
Converged:
No. Iterations:
                                                                                                             4838.0487
                                      4165
                                                                          BIC:
                                                                          Log-Likelihood:
LL-Null:
                                      4163
                                                                                                                        0.9751
                       Coef.
                                        Std.Err.
                                                                                  P>|z|
                                                                                                     [0.025
                     -1.0753
0.3540
                                           0.0393
0.0872
                                                             -27.3720
4.0583
                                                                                 0.0000
0.0000
                                                                                                    -1.1523
0.1830
                                                                                                                       -0.9983
0.5250
```

Using *MediumPrice* as the sole predictor, I developed a logistic regression model to predict refund requests. In this model:

- Travelers paying less than £10 or more than £30 had lower refund probabilities.
- For a £5 ticket, the refund probability was 25%.

$$p = \frac{1}{1 + e^{-\theta}} = \frac{1}{1 + e^{-(-1.0753 + 0.3540 \times 0)}} = \frac{1}{1 + e^{-(-1.0753)}} = \frac{1}{3.93} = 0.25 \times 100 = 25\%$$

For a £25 ticket, the refund probability was 33%.

$$p = \frac{1}{1 + e^{-\theta}} = \frac{1}{1 + e^{-(-1.0753 + 0.3540 \times 0)}} = \frac{1}{1 + e^{-(-0.7213)}} = \frac{1}{3.057} = 0.33 \times 100 = 33\%$$

However, this model performed poorly, with a Pseudo R-squared value of 0.003, indicating minimal explanatory power.

```
# Predict refund request using test data from to_predict

X_1 = predict_journey_final['MediumPrice'].values.reshape(-1, 1)

X_1 = sm.add_constant(X_1)

yhat = result1.predict(X_1)
prediction = list(map(round, yhat))

print("Predicted probabilities:", yhat)
print("Binary predictions (0 or 1):", prediction)
```

Predicted probabilities: [0.2543911 0.2543911 0.2543911 0.2543911 0.2543911 0.3271028] Binary predictions (0 or 1): [0, 0, 0, 0, 0, 0]

Multiple Logistic Regression

To improve predictions, I used the following predictors: *MediumPrice*, *Price*, *DelayInMinutes*, *Journey Status Delayed*, *Reason for Delay (Staffing)*, and *Reason for Delay (Technical Issue)*. This model achieved a better Pseudo R-squared value of 0.179. Key results:

Optimization terminated successfully. Current function value: 0.476949 Iterations 7 Results: Logit Logit Model: MLF Method: Refund.Request_Yes 0.179 Dependent Variable: Pseudo R-squared: Date: 2024-11-22 00:08 AIC: 3986.9828 No. Observations: 4165 BIC: 4031.3241 Log-Likelihood: Df Model: -1986.5 Df Residuals: 4158 LL-Null: -2418.7 1.0000 LLR p-value: 1.8257e-183 Converged: No. Iterations: 1.0000 Scale: Coef. Std.Err. P>|z| [0.025 0.975] -1.0594 0.0696 -15.2188 0.0000 -1.1958 -0.9230 const MediumPrice -0.0408 $0.0985 - 0.4141 \ 0.6788 - 0.2338$ 0.1523 Price -0.0048 0.0010 -4.5999 0.0000 -0.0068 -0.0028 DelayInMinutes -0.0593 0.0038 -15.5963 0.0000 -0.0667 -0.0518 Journey.Status_Delayed 1.4501 0.1293 11.2189 0.0000 1.1968 1.7035 1.2280 Reason.for.Delay_Staffing 0.9982 0.1172 8.5144 0.0000 0.7684 Reason.for.Delay_Technical Issue 1.4509 0.0965 15.0341 0.0000 1.2617 1.6400

- Journey Status Delayed (coefficient: 1.45): Strongly associated with refund requests.
- Reason for Delay Technical Issue (coefficient: 1.45): Significant contributor.
- MediumPrice (coefficient: -0.0408): Not a meaningful predictor compared to other variables.

Predictions on Test Data

Using the multiple logistic model, I predicted refund probabilities for the *To_Predict* dataset:

- Journey 2: 1%
- Journey 3: 14.8%
- Journey 4: 55.7%
- Journey 5: 45.4%
- Journey 6: 0.1%
- Journey 7: 12.3%

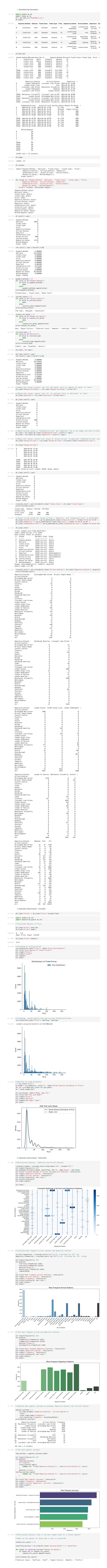
These probabilities reflect that journey delays, especially those caused by technical issues, significantly increase refund requests, far more than ticket price or whether the price falls within a specific range.

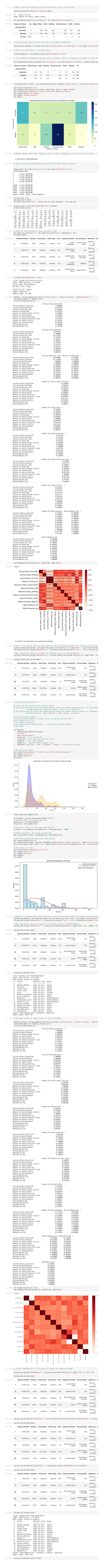
Conclusion

Delays and cancellations are critical drivers of refund requests, with technical issues and staffing delays being the most problematic causes. While pricing influences refund probabilities to a small extent, operational performance, particularly avoiding delays, has a more substantial impact. National Rail should focus on addressing the root causes of delays, especially technical issues, to improve customer satisfaction and reduce operational costs.

REFERENCES

- Agresti, A. (2018). 'Multiple Logistic Regression', *Statistical Methods for the Social Sciences*. Fifth edn: Pearson, pp. 477-479.
- Maven Rail Challenge (2024). Maven Analytics. Available at: https://bit.ly/MavenRailChallenge (Accessed: 25/11/2024).
- Muldoon, M. (2024). 'Lecture 2A: Univariate Exploratory Data Analysis', *Statistics and Machine Learning, Week 2*, 2024(15/11/2024) Available at: https://online.manchester.ac.uk/ultra/courses/_83866_1/cl/outline.





Out[140... Payment.Method Railcard 0 Ticket.Class 0 0 Ticket.Type Price 0 Departure.Station 0 Arrival.Station 0 Departure 0 Scheduled.Arrival 0 Actual.Arrival 0 Journey.Status 0 Reason.for.Delay 0 0 Refund.Request DelayInMinutes 0 MediumPrice 0 dtype: int64 In [142... journey_not_ontime.head() Out [142... Payment.Method Railcard Ticket.Class Ticket.Type Price Departure.Station Arrival.Station Departure So 2024-01-**London Kings** 1 Credit Card Adult Standard Advance 23.0 York Cross 09:45:00 2024-01-8 Credit Card Standard None Advance 37.0 **London Euston** York 01 00:00:00 2024-01-Birmingham New Manchester 20 Debit Card Adult Standard 7.0 Advance 01 Piccadilly Street 11:15:00 2024-01-**Bristol Temple** 26 Credit Card First Class 34.0 Oxford Senior Advance 01 Meads 14:15:00 2024-01-Birmingham **London Euston** 39 Credit Card None Standard Advance 7.0 02 **New Street** 02:15:00 In [144... # # Logistic regression model using sklearn # from sklearn.model_selection import train_test_split # from sklearn.linear_model import LogisticRegression # from sklearn.metrics import classification_report, accuracy_score # X = journey_not_ontime[['MediumPrice']] # y = journey_not_ontime['Refund.Request'] # X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3, random_state=0) # # Fit the logistic regression model # log_model = LogisticRegression() # log_model.fit(X_train, y_train) # # Make predictions # y_pred = log_model.predict(X_test) # # Evaluate the model # print("Accuracy:", accuracy_score(y_test, y_pred)) # print(classification_report(y_test, y_pred, zero_division=0)) 4. Logistic Regression Model with Single Predictor "MediumPrice" In [147... # Logistic regression model using statsmodels import statsmodels.api as sm In [149... # Convert object types to categorical journey_not_ontime = journey_not_ontime.apply(lambda col: col.astype('category') if col.dtypes == In [151... print(journey_not_ontime.dtypes) Payment.Method category Railcard category category Ticket.Class Ticket.Type category float64 Price Departure Station category Arrival.Station category datetime64[ns] Departure Scheduled.Arrival datetime64[ns] Actual.Arrival datetime64[ns] Journey.Status category Reason.for.Delay category Refund.Request category DelayInMinutes float64 MediumPrice int64 dtype: object In [153... # Concatenate category values to dataset cat_vars = journey_not_ontime.select_dtypes(include=['category']).columns for var in cat_vars: cat_list = pd.get_dummies(journey_not_ontime[var], prefix=var, drop_first=True) journey_not_ontime = pd.concat([journey_not_ontime, cat_list], axis=1) In [155... | data_vars=journey_not_ontime.columns.values.tolist() to_keep=[i for i in data_vars if i not in cat_vars] In [157... # Final dataset for logistic regression model journey_final=journey_not_ontime[to_keep] journey_final.columns.values Out[157... array(['Price', 'Departure', 'Scheduled.Arrival', 'Actual.Arrival', 'DelayInMinutes', 'MediumPrice', 'Payment.Method_Credit Card', 'Payment.Method_Debit Card', 'Railcard_Disabled', 'Railcard_None', 'Railcard_Senior', 'Ticket.Class_Standard', 'Ticket.Type_Anytime', 'Ticket.Type_Off-Peak', 'Departure.Station_Edinburgh Waverley', 'Departure.Station_Liverpool Lime Street', 'Departure.Station_London Euston', 'Departure.Station_London Kings Cross', 'Departure.Station_London Paddington', 'Departure.Station_London St Pancras', 'Departure.Station_Manchester Piccadilly', 'Departure.Station_Oxford', 'Departure.Station_Reading', 'Departure.Station_York', 'Arrival.Station_Bristol Temple Meads', 'Arrival.Station_Coventry', 'Arrival.Station_Crewe', 'Arrival.Station_Didcot', 'Arrival.Station_Doncaster', 'Arrival.Station_Durham', 'Arrival.Station_Edinburgh', 'Arrival.Station_Edinburgh Waverley', 'Arrival.Station_Leeds', 'Arrival.Station_Leicester', 'Arrival.Station_Liverpool Lime Street', 'Arrival.Station_London Euston', 'Arrival.Station_London Kings Cross', 'Arrival.Station_London Paddington', 'Arrival.Station_London St Pancras', 'Arrival.Station_London Waterloo', 'Arrival.Station_Manchester Piccadilly', 'Arrival.Station_Nottingham', 'Arrival.Station_Nuneaton', 'Arrival.Station_Oxford', 'Arrival.Station_Peterborough', 'Arrival.Station_Reading', 'Arrival.Station_Sheffield', 'Arrival.Station_Stafford', 'Arrival.Station_Swindon', 'Arrival.Station_Tamworth', 'Arrival.Station_Wakefield' 'Arrival.Station_Wolverhampton', 'Arrival.Station_York', 'Journey.Status_Delayed', 'Reason.for.Delay_Staff', 'Reason.for.Delay_Staffing', 'Reason.for.Delay_Technical Issue', 'Reason.for.Delay_Traffic', 'Reason.for.Delay_Weather', 'Refund.Request_Yes'], dtype=object) journey_final.head() In [159... Out [159... Payment.Method_Credit | | Price Departure Scheduled.Arrival Actual.Arrival DelayInMinutes MediumPrice Card 2024-01-2024-01-01 2024-01-01 1 23.0 01 5.0 1 True 11:35:00 11:40:00 09:45:00 2024-01-2024-01-01 2024-01-01 0 37.0 17.0 8 01 True 01:50:00 02:07:00 00:00:00 2024-01-2024-01-01 2024-01-01 0 20 7.0 31.0 False 01 12:35:00 13:06:00 11:15:00 2024-01-2024-01-01 2024-01-01 0 26 34.0 01 24.0 True 15:30:00 15:54:00 14:15:00 2024-01-2024-01-02 2024-01-02 0.0 0 39 7.0 02 True 03:35:00 03:35:00 02:15:00 5 rows × 60 columns In [161... | #fit small model with one predictor X_1 = journey_final['MediumPrice'].values.reshape(-1, 1) $X_1 = sm.add_constant(X_1)$ #set response variable y = journey_final.loc[:, journey_final.columns == 'Refund.Request_Yes'] In [163... | logit_model=sm.Logit(y,X_1) result1=logit_model.fit() print(result1.summary2()) Optimization terminated successfully. Current function value: 0.578797 Iterations 5 Results: Logit Logit Method: Dependent Variable: Refund.Request_Yes Pseudo R-squared: 0.003 2024-11-22 00:08 AIC: Date: 4825.3797 No. Observations: 4165 BIC: 4838.0487 Df Model: 1 Log-Likelihood: -2410.7Df Residuals: 4163 LL-Null: -2418.7Converged: 1.0000 LLR p-value: 6.1887e-05 No. Iterations: 5.0000 1.0000 Scale: P>|z| 0.975] Coef. Std.Err. [0.025 Z -1.07530.0393 -27.3720 0.0000 -1.1523 -0.9983 const x1 0.3540 0.0872 4.0583 0.0000 0.1830 0.5250 In [165... print(result1.params) const -1.075328x1 0.354010 dtype: float64 In [167... # Plot model results # import numpy as np # import matplotlib.pyplot as plt # Model coefficients intercept = -1.0753 $coef_x1 = 0.3540$ # Define the logistic function def logistic_function(x): return 1 / $(1 + np.exp(-(intercept + coef_x1 * x)))$ # Generate a range of values for the predictor (e.g., ticket prices) x1_values = np.linspace(0, 50, 100) # You can change the range based on your data # Calculate the predicted probabilities for these x1 values predicted_probabilities = logistic_function(x1_values) # Create the plot plt.figure(figsize=(8, 6)) plt.plot(x1_values, predicted_probabilities, label='Probability of Refund Request', color='blue') plt.title('Logistic Regression: Probability of Refund Request vs. Predictor (MediumPrice)') plt.xlabel('Predictor (e.g., Ticket Price)') plt.ylabel('Probability of Refund Request') plt.grid(True) plt.legend() plt.show() Logistic Regression: Probability of Refund Request vs. Predictor (MediumPrice) 1.0 0.9 Probability of Refund Request 0.8 0.7 0.6 0.5 0.4 0.3 Probability of Refund Request 10 40 0 20 30 50 Predictor (e.g., Ticket Price) 5. Fit Regression Models to To_Predict using MavenRail Predictors In [170... | # Clean and format To_Predict data to conform with MavenRail data In [172... | to_predict = pd.read_csv('ToPredict.csv') to_predict.head() Out [172... Payment.Method Railcard Ticket.Class Ticket.Type Price Departure.Station Arrival.Station Departure Scl Birmingham 2024-01-0 **Debit Card** NaN First Class Advance London St Pancras 20 **New Street** 04 17:45 Birmingham 2024-01-London Euston 1 Credit Card NaN Standard Advance 7 20 New Street 05 08:15 Liverpool Lime 2024-01-2 Debit Card NaN Standard Off-Peak 113 **London Euston** 20 Street 09 15:30 Liverpool Lime Manchester 2024-01-3 Contactless Adult Standard Off-Peak 20 Piccadilly 31 05:45 Street Manchester Liverpool Lime 2024-02-4 Credit Card 4 20 NaN Standard Off-Peak Piccadilly Street 10 16:00 # Remove null values. Convert 'nan' for 'No reason' entry in 'Reason for delay' to 'none'. to_predict['Reason.for.Delay'] = to_predict['Reason.for.Delay'].fillna('NA') In [176... | # Remove null values. Convert 'nan' for 'no railcard' entry in 'Railcards' to 'none'. to_predict['Railcard'] = to_predict['Railcard'].fillna('None') to_predict['Actual.Arrival'] = to_predict['Actual.Arrival'].fillna(to_predict['Scheduled.Arrival']) In [180... to_predict.isnull().sum() Out[180... Payment.Method Railcard 0 Ticket.Class 0 Ticket.Type 0 Price 0 Departure.Station 0 0 Arrival.Station Departure Scheduled.Arrival 0 Actual.Arrival 0 0 Journey.Status Reason.for.Delay 0 dtype: int64 In [182… # Convert string values for 'Actual Arrival', 'Departure', and 'Scheduled Arrival' to datetime64 to_predict['Actual.Arrival'] = pd.to_datetime(to_predict['Actual.Arrival'], format='%Y-%m-%d %H:%M' to_predict['Departure'] = pd.to_datetime(to_predict['Departure'], format='%Y-%m-%d %H:%M') to_predict['Scheduled.Arrival'] = pd.to_datetime(to_predict['Scheduled.Arrival'], format='%Y-%m-%d In [184... | to_predict.info() <class 'pandas.core.frame.DataFrame'> RangeIndex: 8 entries, 0 to 7 Data columns (total 12 columns): # Column Non-Null Count Dtype object 0 Payment.Method 8 non-null 1 Railcard 8 non-null object 2 8 non-null Ticket.Class object object 3 Ticket.Type 8 non-null 4 Price 8 non-null int64 5 Departure.Station 8 non-null object 6 8 non-null Arrival.Station object 7 Departure 8 non-null datetime64[ns] datetime64[ns] 8 Scheduled.Arrival 8 non-null 9 8 non-null datetime64[ns] Actual.Arrival 8 non-null 10 Journey.Status object 11 Reason.for.Delay 8 non-null object dtypes: datetime64[ns](3), int64(1), object(8) memory usage: 900.0+ bytes In [186... | to_predict.head() Out [186... Payment.Method Railcard Ticket.Class Ticket.Type Price Departure.Station Arrival.Station Departure Scl 2024-01-Birmingham London St Pancras 0 **Debit Card** None First Class 04 Advance **New Street** 17:45:00 2024-01-Birmingham 1 Credit Card None Standard Advance 7 **London Euston** 05 **New Street** 08:15:00 2024-01-Liverpool Lime 2 **Debit Card** None Standard Off-Peak 113 London Euston 09 Street 15:30:00 2024-01-Liverpool Lime Manchester 3 Adult Off-Peak 3 Contactless Standard 31 Street Piccadilly 05:45:00 2024-02-Manchester Liverpool Lime 4 Credit Card None Standard Off-Peak 4 10 Piccadilly 16:00:00 In [188... # Add a new column, DelayInMinutes, and calculate delay times in minutes delay_time = to_predict['Actual.Arrival']-to_predict['Scheduled.Arrival'] $secs_per_min = 60$ secs_per_hour= 60*60 to_predict['DelayInMinutes'] = delay_time.dt.total_seconds() / secs_per_min In [190... | to_predict.info() <class 'pandas.core.frame.DataFrame'> RangeIndex: 8 entries, 0 to 7 Data columns (total 13 columns): # Column Non-Null Count Dtype 0 Payment.Method 8 non-null object 1 Railcard 8 non-null object 2 Ticket.Class 8 non-null object 3 Ticket.Type 8 non-null object 8 non-null int64 Departure.Station 8 non-null 5 object 6 8 non-null Arrival.Station object 7 Departure 8 non-null datetime64[ns] 8 Scheduled.Arrival 8 non-null datetime64[ns] 9 datetime64[ns] Actual.Arrival 8 non-null 10 Journey.Status 8 non-null object 11 Reason.for.Delay 8 non-null object 12 DelayInMinutes 8 non-null float64 dtypes: datetime64[ns](3), float64(1), int64(1), object(8) memory usage: 964.0+ bytes In [192... | # Restrict to journeys that did not arrive on time and determine whether the ticket price was great predict_journey_not_ontime = to_predict[(to_predict['Journey.Status']=='Cancelled') | (to_predict[' predict_journey_not_ontime['MediumPrice'] = (predict_journey_not_ontime['Price'] > 10) & (predict_j # Map 'True/False' values to 'Yes/No' to replicate values in 'Refund Request' predict_journey_not_ontime['MediumPrice'] = predict_journey_not_ontime['MediumPrice'].map({True: 'Y In [194... predict_journey_not_ontime.head() Out [194... Payment.Method Railcard Ticket.Class Ticket.Type Price Departure.Station Arrival.Station Departure 2024-01-Liverpool Lime 2 **Debit Card** None Standard Off-Peak 113 London Euston 09 Street 15:30:00 2024-01-Liverpool Lime Manchester 3 Contactless Adult Standard Off-Peak 3 31 Piccadilly Street 05:45:00 2024-02-Liverpool Lime Manchester 4 Credit Card Off-Peak None Standard 10 Piccadilly 16:00:00 2024-02-Manchester Liverpool Lime 5 Contactless None Standard Advance 3 Piccadilly Street 15:45:00 2024-03-Manchester 6 **Debit Card** Standard Off-Peak 126 None London Euston 20 Piccadilly 15:30:00 In [196... | predict_journey_not_ontime.info() <class 'pandas.core.frame.DataFrame'> Index: 6 entries, 2 to 7 Data columns (total 14 columns): Column Non-Null Count Dtype 0 Payment.Method 6 non-null object 1 Railcard 6 non-null object 2 Ticket.Class 6 non-null object 3 Ticket.Type 6 non-null object Price 6 non-null int64 5 Departure.Station 6 non-null object 6 Arrival.Station object 6 non-null 7 Departure 6 non-null datetime64[ns] 8 Scheduled.Arrival 6 non-null datetime64[ns] 9 datetime64[ns] Actual.Arrival 6 non-null 10 Journey.Status 6 non-null object 11 Reason.for.Delay 6 non-null object float64 12 DelayInMinutes 6 non-null object 13 MediumPrice 6 non-null dtypes: datetime64[ns](3), float64(1), int64(1), object(9) memory usage: 720.0+ bytes In [198... # Convert 'MediumPrice' to 1/0 values to prepare for regression model predict_journey_not_ontime['MediumPrice'] = predict_journey_not_ontime['MediumPrice'].map({'Yes': 1 predict_journey_not_ontime.head() Out [198... Payment.Method Railcard Ticket.Class Ticket.Type Price Departure.Station Arrival.Station Departure Scl 2024-01-Liverpool Lime 2 **Debit Card** None Standard Off-Peak 113 London Euston 09 Street 15:30:00 2024-01-Liverpool Lime Manchester 3 Contactless Adult Off-Peak 3 Standard Street Piccadilly 05:45:00 2024-02-Manchester Liverpool Lime 4 Credit Card None Standard Off-Peak 4 Piccadilly Street 16:00:00 2024-02-Manchester Liverpool Lime 5 Contactless None Standard Advance 3 25 Piccadilly Street 15:45:00 2024-03-Manchester 6 **Debit Card** None Standard Off-Peak 126 London Euston 20 Piccadilly 15:30:00 In [200... # Convert object types to categorical predict_journey_not_ontime = predict_journey_not_ontime.apply(lambda col: col.astype('category') if In [202... | print(predict_journey_not_ontime.dtypes) Payment.Method category Railcard category Ticket.Class category Ticket.Type category Price int64 Departure.Station Departure.scal.

Arrival.Station

datetime64[ns] Scheduled.Arrival datetime64[ns] Actual.Arrival datetime64[ns]
Journey.Status category Reason for Delay category DelayInMinutes float64 MediumPrice int64 dtype: object In [204... predict_cat_vars = predict_journey_not_ontime.select_dtypes(include=['category']).columns for var in predict_cat_vars: cat list = pd.get dummies(predict journey not ontime[var], prefix=var, drop first=True) predict_journey_not_ontime = pd.concat([predict_journey_not_ontime, cat_list], axis=1) In [206... | predict_data_vars=predict_journey_not_ontime.columns.values.tolist() predict_to_keep=[i for i in predict_data_vars if i not in predict_cat_vars] In [208... predict_journey_final=predict_journey_not_ontime[predict_to_keep] predict_journey_final.columns.values Out[208... array(['Price', 'Departure', 'Scheduled.Arrival', 'Actual.Arrival', 'DelayInMinutes', 'MediumPrice', 'Payment.Method_Credit Card', 'Payment.Method_Debit Card', 'Railcard_None', 'Ticket.Type_Off-Peak', 'Departure.Station_Liverpool Lime Street', 'Departure.Station_Manchester Piccadilly', 'Arrival.Station_London Euston', 'Arrival.Station_London St Pancras', 'Arrival.Station_Manchester Piccadilly', 'Journey.Status_Delayed', 'Reason.for.Delay_Staffing', 'Reason.for.Delay_Technical Issue'], dtype=object) Predictions for To_Predict using single predictor logit model In [211... # Predict refund request using test data from to predict X_1 = predict_journey_final['MediumPrice'].values.reshape(-1, 1) $X_1 = sm.add_constant(X_1)$ yhat = result1.predict(X_1) prediction = list(map(round, yhat)) print("Predicted probabilities:", yhat) print("Binary predictions (0 or 1):", prediction) Predicted probabilities: [0.2543911 0.2543911 0.2543911 0.2543911 0.2543911 0.3271028] Binary predictions (0 or 1): [0, 0, 0, 0, 0, 0] Multiple Predictor Logistic Model Trained on MavenRail In [214... # Fit multiple predictors logistic regression model In [216... # Select numerical predictors numerical_predictors = journey_final[['MediumPrice', 'Price', 'DelayInMinutes']] # Select categorical predictors (assuming they are already dummy—encoded) categorical_predictors = journey_final[['Journey.Status_Delayed', 'Reason.for.Delay_Staffing', 'Reason.for.Delay_Technical Issue']] # Combine numerical and categorical predictors X = pd.concat([numerical_predictors, categorical_predictors], axis=1) # X = journey_final[['Price', 'DelayInMinutes', 'Journey.Status_Delayed','Reason.for.Delay_Staff',' # 'Reason.for.Delay_Technical Issue', 'Reason.for.Delay_Traffic', 'Reason.for.Delay_Weather']] # Add a constant for the intercept X = sm.add_constant(X) # Set response variable y = journey_final['Refund.Request_Yes'].astype(int) # Build the logistic regression model logit_model = sm.Logit(y, X.astype(float)) result = logit_model.fit() # Print the model summary print(result.summary2()) Optimization terminated successfully. Current function value: 0.476949 Iterations 7 Results: Logit Model: Logit Method: MLE Dependent Variable: 3986.9828 Date: No. Observations: 4165 BIC: 4031.3241 6 -1986.5 Df Model: Log-Likelihood: Df Residuals: 4158 1.0000 LL-Null: -2418.7 LLR p-value: Scale: Converged: 1.8257e-183 No. Iterations: 7.0000 1.0000 Coef. Std.Err. z P>|z| [0.025 0.975] const -1.0594 0.0696 -15.2188 0.0000 -1.1958 -0.9230 -0.0408 0.0985 -0.4141 0.6788 -0.2338 0.1523 MediumPrice

 Price
 -0.0048
 0.0010
 -4.5999
 0.0000
 -0.0068
 -0.0028

 DelayInMinutes
 -0.0593
 0.0038
 -15.5963
 0.0000
 -0.0667
 -0.0518

 Journey.Status_Delayed
 1.4501
 0.1293
 11.2189
 0.0000
 1.1968
 1.7035

 Reason.for.Delay_Staffing
 0.9982
 0.1172
 8.5144
 0.0000
 0.7684
 1.2280

 Reason.for.Delay_Technical Issue 1.4509 0.0965 15.0341 0.0000 1.2617 1.6400 Test Multiple Predictor Logistic Model on To_Predict In [219... # Predict refund request using test data from to_predict X_new = predict_journey_final[['Price', 'MediumPrice', 'DelayInMinutes', 'Journey.Status_Delayed', 'Reason.for.Delay_Technical Issue']] X_new = sm.add_constant(X_new) $X_{new} = X_{new.astype}(float)$ predictions = result.predict(X_new) print("Predicted probabilities:", predictions) # print("Binary predictions (0 or 1):", prediction) Predicted probabilities: 2 0.010726 3 0.148387 4 0.556840 5 0.454240 0.009024 6 7 0.123304 dtype: float64