| | | | | | =\$M\$27+ (B3*\$M\$28)+ (C3*\$M\$29)+ (D | | | | |
|-------|-------|-------|-------|--------------|--|-------|------------|-------------|-------------|
| carat | depth | table | price | x | у | z | predict | error | error^2 |
| 0.23 | 61.5 | 55 | 326 | 3.95 | 3.98 | 2.43 | 0.11539047 | -0.11460953 | 0.013135343 |
| 0.21 | 59.8 | 61 | 326 | 3.89 | 3.84 | 2.31 | 0.09135677 | -0.11864323 | 0.014076217 |
| 0.23 | 56.9 | 65 | 327 | 4.05 | 4.07 | 2.31 | 0.10542332 | -0.12457668 | 0.015519349 |
| 0.29 | 62.4 | 58 | 334 | 4.2 | 4.23 | 2.63 | 0.22270237 | -0.06729763 | 0.00452897 |
| 0.31 | 63.3 | 58 | 335 | 4.34 | 4.35 | 2.75 | 0.28245805 | -0.02754195 | 0.000758559 |
| 0.24 | 62.8 | 57 | 336 | 3.94 | 3.96 | 2.48 | 0.1453311 | -0.0946689 | 0.008962201 |
| 0.24 | 62.3 | 57 | 336 | 3.95 | 3.98 | 2.47 | 0.13927245 | -0.10072755 | 0.01014604 |
| 0.26 | 61.9 | 55 | 337 | 4.07 | 4.11 | 2.53 | 0.16028295 | -0.09971705 | 0.009943491 |
| 0.22 | 65.1 | 61 | 337 | 3.87 | 3.78 | 2.49 | 0.18296363 | -0.03703637 | 0.001371693 |
| 0.23 | 59.4 | 61 | 338 | 4 | 4.05 | 2.39 | 0.11904332 | -0.11095668 | 0.012311384 |
| 0.3 | 64 | 55 | 339 | 4.25 | 4.28 | 2.73 | 0.25463188 | -0.04536812 | 0.002058266 |
| 0.23 | 62.8 | 56 | 340 | 3.93 | 3.9 | 2.46 | 0.13763304 | -0.09236696 | 0.008531656 |
| 0.22 | 60.4 | 61 | 342 | 3.88 | 3.84 | 2.33 | 0.09991491 | -0.12008509 | 0.014420429 |
| 0.31 | 62.2 | 54 | 344 | 4.35 | 4.37 | 2.71 | 0.24803011 | -0.06196989 | 0.003840268 |
| 0.2 | 60.2 | 62 | 345 | 3.79 | 3.75 | 2.27 | 0.07291754 | -0.12708246 | 0.016149951 |
| 0.32 | 60.9 | 58 | 345 | 4.38 | 4.42 | 2.68 | 0.25108528 | -0.06891472 | 0.004749238 |
| 0.3 | 62 | 54 | 348 | 4.31 | 4.34 | 2.68 | 0.23218015 | -0.06781985 | 0.004599532 |
| 0.3 | 63.4 | 54 | 351 | 4.23 | 4.29 | 2.7 | 0.23358237 | -0.06641763 | 0.004411301 |
| 0.3 | 63.8 | 56 | 351 | 4.23 | 4.26 | 2.71 | 0.24955107 | -0.05044893 | 0.002545095 |
| 0.3 | 62.7 | 59 | 351 | 4.21 | 4.27 | 2.66 | 0.23648226 | -0.06351774 | 0.004034503 |
| 0.3 | 63.3 | 56 | 351 | 4.26 | 4.3 | 2.71 | 0.24966846 | -0.05033154 | 0.002533263 |
| 0.23 | 63.8 | 55 | 352 | 3.85 | 3.92 | 2.48 | 0.1280261 | -0.1019739 | 0.010398677 |
| 0.23 | 61 | 57 | 353 | 3.94 | 3.96 | 2.41 | 0.11269857 | -0.11730143 | 0.013759627 |
| 0.31 | 59.4 | 62 | 353 | 4.39 | 4.43 | 2.62 | 0.24435653 | -0.06564347 | 0.004309065 |
| 0.31 | 58.1 | 62 | 353 | 4.44 | 4.47 | 2.59 | 0.23575967 | -0.07424033 | 0.004505005 |
| 0.23 | 60.4 | 58 | 354 | 3.97 | 4.01 | 2.41 | 0.11547199 | -0.11452801 | 0.013116664 |
| 0.24 | 62.5 | 57 | 355 | 3.97 | 3.94 | 2.47 | 0.14934078 | -0.09065922 | 0.008219093 |
| 0.24 | 62.2 | 57 | 357 | 4.28 | 4.3 | 2.67 | 0.24001807 | -0.05998193 | 0.003597832 |
| 0.23 | 60.5 | 61 | 357 | 3.96 | 3.97 | 2.4 | 0.12731067 | -0.10268933 | 0.010545098 |
| 0.23 | 60.9 | 57 | 357 | 3.96 | 3.99 | 2.42 | 0.12731007 | -0.11276919 | 0.010343038 |
| 0.23 | 60 | 57 | 402 | 4 | 4.03 | 2.41 | 0.11445856 | -0.11554144 | 0.013349824 |
| 0.23 | 59.8 | 57 | 402 | 4.04 | 4.06 | 2.42 | 0.1230564 | -0.1069436 | 0.011436933 |
| 0.23 | 60.7 | 59 | 402 | 3.97 | 4.01 | 2.42 | 0.12695298 | -0.10304702 | 0.011430333 |
| 0.23 | 59.5 | 58 | 402 | 4.01 | 4.06 | 2.4 | 0.12033230 | -0.10304702 | 0.013721693 |
| 0.23 | 61.9 | 58 | 402 | 3.92 | 3.96 | 2.44 | 0.12923534 | -0.10076466 | 0.010153518 |
| 0.23 | 58.2 | 59 | 402 | 4.06 | 4.08 | 2.37 | 0.10853387 | -0.12146613 | 0.010133318 |
| 0.23 | 64.1 | 59 | 402 | 3.83 | 3.85 | 2.46 | 0.14623594 | -0.08376406 | 0.007016418 |
| 0.31 | 64 | 54 | 402 | 4.29 | 4.31 | 2.75 | 0.26456596 | -0.04543404 | 0.007010418 |
| 0.26 | 60.8 | 59 | 403 | 4.13 | 4.16 | 2.52 | 0.17820168 | -0.08179832 | 0.006690964 |
| 0.33 | 61.8 | 55 | 403 | 4.49 | 4.51 | 2.78 | 0.29022492 | -0.03173632 | 0.00055554 |
| 0.33 | 61.2 | 56 | 403 | 4.49 | 4.5 | 2.75 | 0.28348597 | -0.03577308 | 0.001362637 |
| 0.33 | 61.1 | 56 | 403 | 4.49 | 4.55 | 2.76 | 0.28348397 | -0.04831403 | 0.002163333 |
| 0.26 | 65.2 | 56 | 403 | 3.99 | 4.02 | 2.76 | 0.20196314 | -0.04801686 | 0.002303619 |
| 0.26 | 58.4 | 63 | 403 | 4.19 | 4.24 | 2.46 | 0.20207437 | -0.03712343 | 0.003263313 |
| 0.26 | 63.1 | 56 | 403 | 4.19 | 4.24 | 2.75 | 0.17020379 | -0.08979421 | 0.008063 |
| 0.32 | 62.4 | 58 | 403 | | 4.26 | 2.75 | 0.27232143 | -0.04767857 | 0.002273246 |
| 0.29 | 61.8 | 55 | 403 | 4.24 4.35 | 4.42 | 2.03 | 0.23722607 | -0.05277193 | 0.002784877 |
| 0.52 | 01.0 | 33 | 403 | 4.33 | 4.42 | ۷.1 ا | 0.24730939 | -0.07269061 | 0.005283925 |

=\$M\$27+ (B3*\$M\$28)+ (C3*\$M\$29)+ (D3*\$M\$30)+ (E3*\$M\$31)+ (F3*\$M\$32)+ (G3*\$M\$33)

Multiple Linear Regression

carat = f(depth, table, price, x, y, z)

carat = b0 + b1*(depth) + b2*(table) + b3*(price) + b4*(x) + b5*(y) + b6*(z)

Sum error 366.651 =SUM(J3:J53942) < the best minimize

RMSE 0.082 =SQRT(AVERAGE(J3:J53942))

SUMMARY OUTPUT

| Regression Statistics | | | | | |
|-----------------------|-------------|--|--|--|--|
| Multiple R | 0.984757181 | | | | |
| R Square | 0.969746706 | | | | |
| Adjusted R Square | 0.969743341 | | | | |
| Standard Error | 0.082451608 | | | | |
| Observations | 53940 | | | | |

ANOVA

| | df | SS | MS | F | Significance F |
|------------|-------|-------------|-------------|-------------|----------------|
| Regression | 6 | 11752.72277 | 1958.787128 | 288130.3304 | 0.00000 |
| Residual | 53933 | 366.6509738 | 0.006798268 | | |
| Total | 53939 | 12119 37374 | | | |

| | Coefficients | Standard Error | t Stat | P-value | Lower 95% | Upper 95% |
|-----------|--------------|----------------|---------------|---------|--------------|--------------|
| Intercept | -2.487423398 | 0.02274703 | -109.3515679 | 0.00000 | -2.532007758 | -2.442839038 |
| depth | 0.018368491 | 0.000296597 | 61.93078929 | 0.00000 | 0.017787159 | 0.018949824 |
| table | 0.004397095 | 0.000170558 | 25.78061245 | 0.00000 | 0.0040628 | 0.004731391 |
| price | 0.000032420 | 0.00000192 | 169.085010066 | 0.00000 | 0.000032044 | 0.000032795 |
| x | 0.301606222 | 0.002009598 | 150.0828924 | 0.00000 | 0.297667395 | 0.305545049 |
| у | 0.006336437 | 0.00140562 | 4.507929514 | 0.00001 | 0.00358141 | 0.009091464 |
| Z | 0.00171975 | 0.002440289 | 0.704732025 | 0.48098 | -0.003063236 | 0.006502735 |