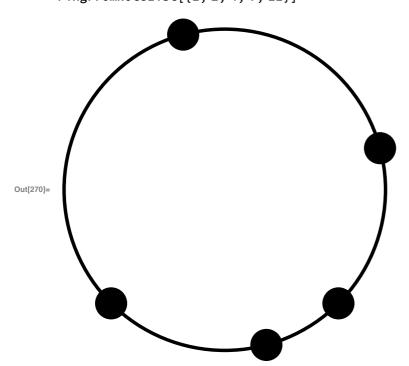
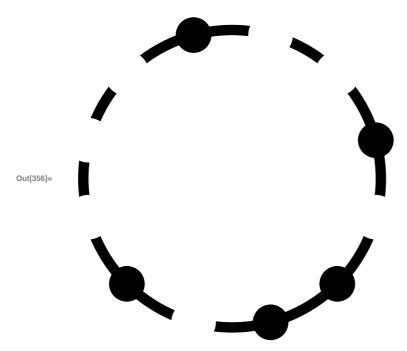


```
In[268]:= circle0[centre_: {0, 0}, radius_: 1] :=
      {Thickness -> 0.01, Circle[centre, radius]}
     ringFromNoteList[l_] :=
      Graphics[{Disk[#, 0.1] & /@ CirclePoints[12][[1]], circle0[]}]
     ringFromNoteList[{1, 2, 4, 7, 11}]
```



```
In[353]:= circle0[centre_: {0, 0}, radius_: 1] :=
      {Thickness -> 0.03, Circle[centre, radius]}
     complementaryNoteList[l_] := Complement[Range[12], l]
     ringFromNoteList[l_] :=
      Graphics[{{Black, Disk[#, 0.12] & /@ CirclePoints[12][[l]]}}, circle0[],
         {White, Disk[#, 0.15] & /@ CirclePoints[12][[complementaryNoteList[l]]]}}]
     ringFromNoteList[{1, 2, 4, 7, 11}]
```



```
In[406]:= whiteDotLineThickness = 0.01;
blackDotRadius = 0.15;
whiteDotRadius = blackDotRadius - whiteDotLineThickness;
ringFromNoteList[l_] :=
Graphics[{{Black, Disk[#, blackDotRadius] & /@ CirclePoints[12][[l]]},
{White, EdgeForm[Thickness[whiteDotLineThickness]],
Disk[#, whiteDotRadius] & /@ CirclePoints[12][[complementaryNoteList[l]]]]}]
ringFromNoteList[{1, 2, 4, 7, 11}]
Out[410]=
Out[410]=
```

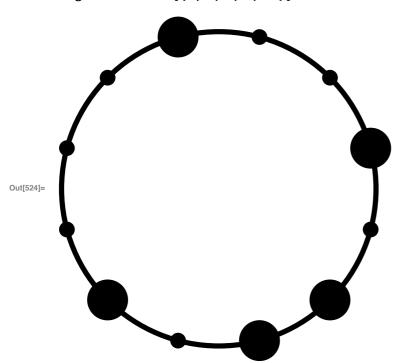
```
In[411]:= whiteDotLineThickness = 0.005;
      blackDotRadius = 0.15;
     whiteDotRadius = blackDotRadius - whiteDotLineThickness;
      ringFromNoteList[l_] :=
       Graphics[{{Black, Disk[#, blackDotRadius] & /@ CirclePoints[12][[1]]}},
         {White, EdgeForm[Thickness[whiteDotLineThickness]],
          Disk[#, whiteDotRadius] & /@ CirclePoints[12][[complementaryNoteList[l]]]}}]
      ringFromNoteList[{1, 2, 4, 7, 11}]
Out[415]=
```

```
In[416]:= whiteDotLineThickness = 0.01;
      blackDotRadius = 0.15;
     whiteDotRadius = 0.065;
      ringFromNoteList[l_] :=
       Graphics[{{Black, Disk[#, blackDotRadius] & /@ CirclePoints[12][[l]]}},
         {White, EdgeForm[Thickness[whiteDotLineThickness]],
          Disk[#, whiteDotRadius] & /@ CirclePoints[12][[complementaryNoteList[l]]]}}]
      ringFromNoteList[{1, 2, 4, 7, 11}]
Out[420]=
```

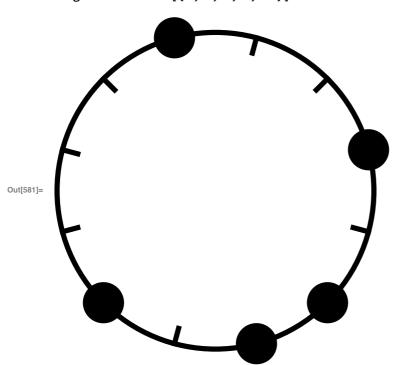
```
In[426]:= whiteDotLineThickness = 0.01;
      blackDotRadius = 0.15;
     whiteDotRadius = 0.05;
      ringFromNoteList[l_] :=
       Graphics[{{Black, Disk[#, blackDotRadius] & /@ CirclePoints[12][[l]]}, {Black,
          Disk[#, whiteDotRadius] & /@ CirclePoints[12][[complementaryNoteList[l]]]}}]
      ringFromNoteList[{1, 2, 4, 7, 11}]
Out[430]=
```

```
In[461]:= whiteDotLineThickness = 0.01;
      blackDotRadius = 0.13;
     whiteDotRadius = 0.035;
      ringFromNoteList[l_] :=
       Graphics[{{Black, Disk[#, blackDotRadius] & /@ CirclePoints[12][[l]]}, {Black,
          Disk[#, whiteDotRadius] & /@ CirclePoints[12][[complementaryNoteList[l]]]}}]
      ringFromNoteList[{1, 2, 4, 7, 11}]
Out[465]=
```

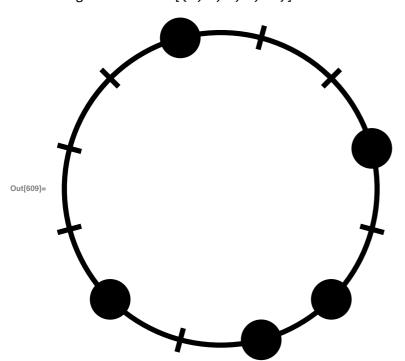
```
In[519]:= whiteDotLineThickness = 0.01;
     blackDotRadius = 0.13;
     whiteDotRadius = 0.05;
     circle1[centre_: {0, 0}, radius_: 1] :=
      {Thickness -> 0.015, Circle[centre, radius]}
     ringFromNoteList[l_] :=
      Graphics[{{Black, Disk[#, blackDotRadius] & /@ CirclePoints[12][[1]]}},
         {Black, Disk[#, whiteDotRadius] & /@
           CirclePoints[12][[complementaryNoteList[l]]]}, circle1[]}]
     ringFromNoteList[{1, 2, 4, 7, 11}]
```



```
In[575]:= radialLine[p_, innerRadius_] := {Line[{p, Normalize[p] * innerRadius}]}
     whiteDotLineThickness = 0.01;
     blackDotRadius = 0.13;
     lineThickness = 0.015;
     circle1[centre_: {0, 0}, radius_: 1] :=
      {Thickness -> lineThickness, Circle[centre, radius]}
     ringFromNoteList[l_] :=
      Graphics[{{Black, Disk[#, blackDotRadius] & /@ CirclePoints[12][[1]]}},
         {{Thickness \rightarrow lineThickness, radialLine[#, 0.9]} &/@
           CirclePoints[12][[complementaryNoteList[l]]]}, circle1[]}]
     ringFromNoteList[{1, 2, 4, 7, 11}]
```

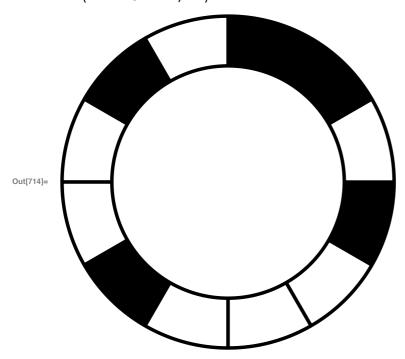


```
In[603]:= radialLine[p_, innerRadius_] :=
      {Line[{Normalize[p] / innerRadius, Normalize[p] * innerRadius}]}
     whiteDotLineThickness = 0.01;
     blackDotRadius = 0.13;
     lineThickness = 0.015;
     circle1[centre_: {0, 0}, radius_: 1] :=
      {Thickness -> lineThickness, Circle[centre, radius]}
     ringFromNoteList[l_] :=
      Graphics[{{Black, Disk[#, blackDotRadius] & /@ CirclePoints[12][[l]]}},
         {\{\{Thickness \rightarrow lineThickness, radialLine[\#, 0.94]\} \& / @}
           CirclePoints[12][[complementaryNoteList[l]]]}, circle1[]}]
     ringFromNoteList[{1, 2, 4, 7, 11}]
```

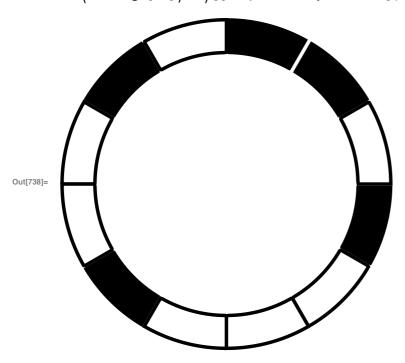


```
In[659]:= radialLine[p_, innerRadius_] :=
       {Line[{Normalize[p] / innerRadius, Normalize[p] * innerRadius}]}
      whiteDotLineThickness = 0.01;
      blackDotRadius = 0.13;
      lineThickness = 0.013;
      circle1[centre_: {0, 0}, radius_: 1] :=
       {Thickness -> lineThickness, Circle[centre, radius]}
      ringFromNoteList[l_] :=
       Graphics[{White, EdgeForm[Thickness[whiteDotLineThickness]],
         Disk[#, blackDotRadius] & /@ CirclePoints[12][[1]],
         {{Black, Thickness → lineThickness, radialLine[#, 0.96]} &/@
           CirclePoints[12][[complementaryNoteList[l]]]}}]
      ringFromNoteList[{1, 2, 4, 7, 11}]
Out[665]=
```

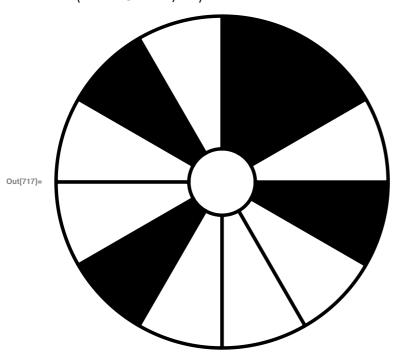
```
\label{eq:local_local_local} $$ \inf[714] = Graphics[\{\{EdgeForm[Thickness[0.01]], Black, Annulus[\{0,0\}, \{0.7,1\}, (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1), (0.7,1),
                                                                                                                 \{ \pm, \pm + 2\pi/12 \} ]  & /@ (2\pi Range[12]/12)[[\{1, 2, 4, 7, 11\}]] \},
                                                                 \big\{ \texttt{EdgeForm}[\mathsf{Thickness} \texttt{[0.01]]} \,,\, \mathsf{White},\, \mathsf{Annulus} \big[ \, \{ \mathtt{0} \,,\, \mathtt{0} \} \,,\,
                                                                                                        \{0.7, 1\}, \{\#, \#+2\pi/12\}]\} \&/@
                                                                            (2 \pi Range[12]/12)[[complementaryNoteList[{1, 2, 4, 7, 11}]]]
```



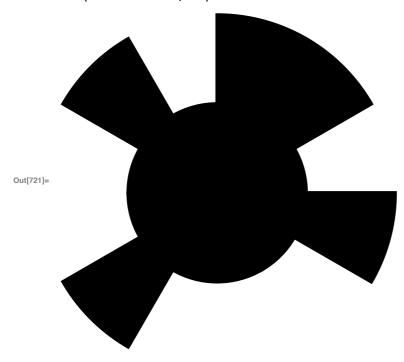
```
In[738]:= Graphics[
                                                          \big\{ \big\{ \big\{ EdgeForm[\{White, Thickness[0.01]\}], \, Black, \, Annulus\big[\{0,\,0\}, \, \{0.78,\, 1.02\}, \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02), \, (0.78,\, 1.02),
                                                                                                                     \{ \pm, \pm + 2\pi/12 \} ]  & /@ (2\pi Range[12]/12)[[\{1, 2, 4, 7, 11\}]] \},
                                                                   \big\{ {\sf EdgeForm[Thickness[0.01]], White, Annulus[\{0,\,0\},}
                                                                                                           \{0.8, 1\}, \{\#, \#+2\pi/12\}]\} \&/@
                                                                              (2 \pi Range[12] / 12) [[complementaryNoteList[{1, 2, 4, 7, 11}]]]}]
```



```
In[717]:= Graphics [\{\{EdgeForm[Thickness[0.01]], Black, Annulus[\{0,0\},\{0.2,1\},
               \{ \#, \# + 2\pi/12 \} ]  & /@ (2\pi Range[12]/12)[[\{1, 2, 4, 7, 11\}]] \},
         \{ EdgeForm[Thickness[0.01]], White, Annulus[{0, 0},
              \{0.2, 1\}, \{\#, \#+2\pi/12\}\} & /@
          (2 \pi \text{Range}[12] / 12) [[complementaryNoteList[{1, 2, 4, 7, 11}]]]}
```



 $\label{eq:local_limit} $$ \ln[721] = $ Graphics \left[\left\{ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{0,\,0\},\,1,\,\left\{ \#,\,\#+2\,\pi \right/12 \right\} \right] \right\} \& /@ 1. $$ $ \left\{ \left\{ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{0,\,0\},\,1,\,\left\{ \#,\,\#+2\,\pi \right/12 \right\} \right] \right\} \& /@ 1. $$ $ \left\{ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{0,\,0\},\,1,\,\left\{ \#,\,\#+2\,\pi \right/12 \right\} \right] \right\} \& /@ 1. $$ $ \left\{ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{0,\,0\},\,1,\,\left\{ \#,\,\#+2\,\pi \right/12 \right\} \right] \right\} \& /@ 1. $$ $ $ \left\{ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{0,\,0\},\,1,\,\left\{ \#,\,\#+2\,\pi \right/12 \right\} \right] \right\} \& /@ 1. $$ $ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{0,\,0\},\,1,\,\left\{ \#,\,\#+2\,\pi \right/12 \right\} \right] \right\} \& /@ 1. $$ $ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{0,\,0\},\,1,\,\left\{ \#,\,\#+2\,\pi \right/12 \right\} \right] \right\} \& /@ 1. $$ $ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{0,\,0\},\,1,\,\left\{ \#,\,\#+2\,\pi \right/12 \right\} \right] \right\} \& /@ 1. $$ $ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{0,\,0\},\,1,\,\left\{ \#,\,\#+2\,\pi \right/12 \right\} \right] \right\} \& /@ 1. $$ $ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{0,\,0\},\,1,\,\left\{ \#,\,\#+2\,\pi \right/12 \right\} \right\} \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{0,\,0\},\,1,\,\left\{ \#,\,\#+2\,\pi \right/12 \right\} \right\} \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \& /@ 1. $$ $ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \& /@ 1. $$ $ \left\{ EdgeForm[Thickness[0.01]], Black, Disk \left[\{1,\,\#+2\,\pi \right/12 \right\} \& /@ 1.$ $(2 \pi Range[12] / 12) [[{1, 2, 4, 7, 11}]],$ {EdgeForm[Thickness[0.01]], Black, Disk[$\{0, 0\}, 0.5, \{\#, \#+2\pi/12\}$]} & /@ $(2 \pi Range[12]/12)[[complementaryNoteList[{1, 2, 4, 7, 11}]]]$



 $(2\pi Range[12]/12)[[{1, 2, 4, 7, 11}]]$, $\left\{ \text{Thickness[0.03], Black, Circle} \left[\{ 0\,,\,0 \}\,,\,0.7,\,\left\{ \sharp\,,\,\sharp\,+\,2\,\pi\,\middle/\,19 \right\} \right] \right\}\,\&\,/@$ $(2 \pi Range[12] / 12)[[complementaryNoteList[{1, 2, 4, 7, 11}]]]$

