

AI1103-Assignment 1

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Download all python codes from

https://github.com/siri003/AI1103-PROBABILITY-AND-RANDOM-VARIABLES/blob/main/Assignment_1.py

and latex codes from

<https://github.com/siri003/AI1103-PROBABILITY-AND-RANDOM-VARIABLES/blob/main/main.tex>

Problem Statement: The probability that a student is not a swimmer is $\frac{1}{5}$. Then the probability that out of five students, four are swimmers is

Solution: Let X be the number of students who can swim.

$n=5$ (total number of students)

$p=\frac{4}{5}$ (probability that a student can swim)

$q=\frac{1}{5}$ (probability that a student cannot swim)

From Bernoulli's distribution we know that,

$$P(X = r) = \binom{n}{r}(p)^r(q)^{n-r} \quad (0.0.1)$$

$$\begin{aligned} P(X = 4) &= \binom{5}{4}(p)^4(q)^1 \\ &= \binom{5}{4}\left(\frac{4}{5}\right)^4\left(\frac{1}{5}\right)^1 \\ &= \binom{5}{1}\left(\frac{4}{5}\right)^4\left(\frac{1}{5}\right) \end{aligned} \quad (0.0.2)$$

Therefore, the desired probability is $\binom{5}{1}\left(\frac{4}{5}\right)^4\left(\frac{1}{5}\right)=0.4096$.