

# **Using Cowichan Problems to Investigate Programmability of X10 Programming System**

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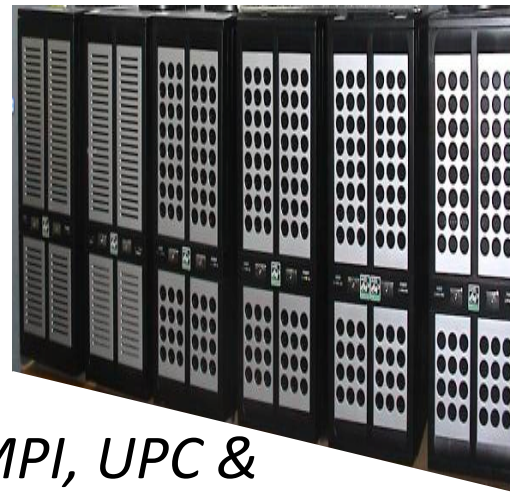
# X10: Design Goals



## Programmer Productivity

*An experiment to evaluate the programmability of three programming systems.*

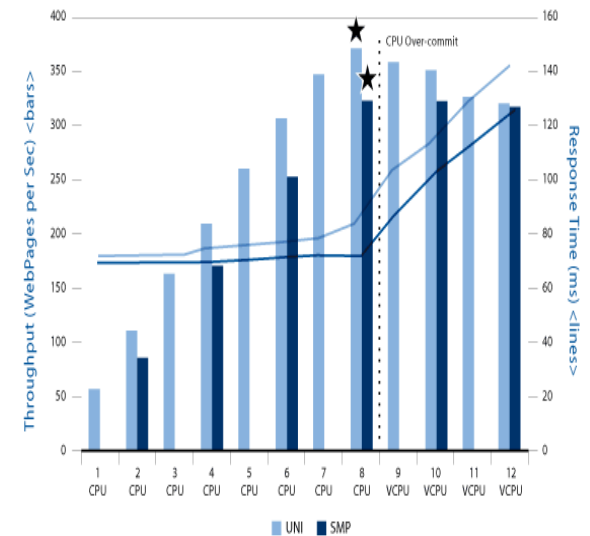
(Sarkar et al., Workshop on Productivity & Performance in High-End Computing 2006)



## Code Performance

*Performance evaluation of MPI, UPC & OpenMP on multicore architectures.*

(Mallon et al., EuroPVM/MPI 2009)



# Contributions

Performance assessment of X10

Implementation of a suite of parallel programs

# Cowichan Suite



Gregory Wilson

Salishan -- Cowichan



# Cowichan Suite

Designed to assess the programmability of a programming system  
for  
writing efficient parallel programs

# Cowichan Problems

## Communication & Dynamic Load Balancing



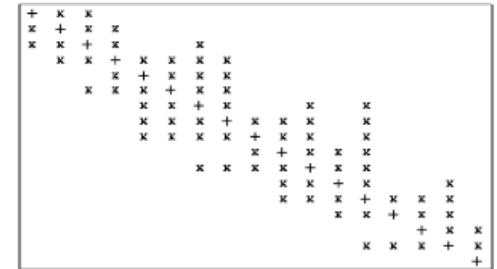
1. Turing Ring Problem

## Input/Output & Intense Communication



5. Image Thinning Problem

## Data Replication & Coherence



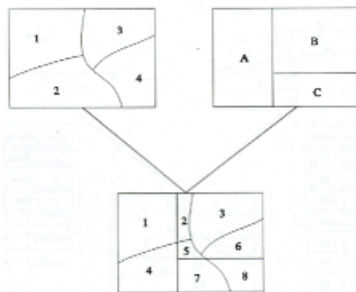
2. Skyline Matrix Problem

## Data Distribution & Coherence

$$((AB)C)D = (AB)(CD) = A(B(CD)) = A(BC)D$$

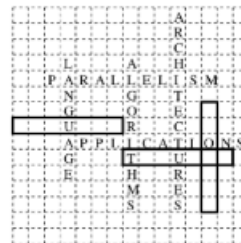
7. Matrix Chain Problem

## Concurrent Input/Output



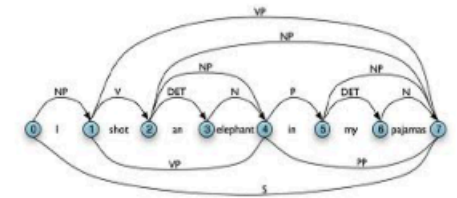
4. Polygon Overlay Problem

## Task & Data Parallelism



6. Kece Problem

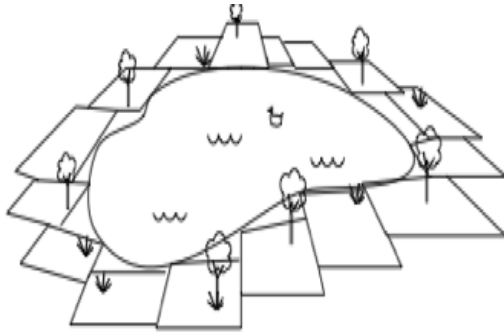
## Intense Communication



3. Active Chart Parsing Problem

# Example Implementations

## Turing Ring



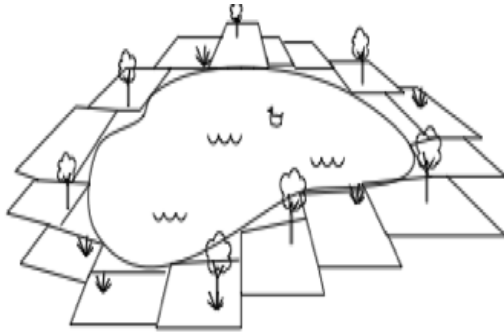
$$\frac{dX_i}{dt} = X_i(r_x + c_{xx}X_i + c_{xy}Y_i) + \mu_x(X_{i+1} + X_{i-1} - 2X_i)$$

$$\frac{dY_i}{dt} = Y_i(r_y + c_{yx}X_i + c_{yy}Y_i) + \mu_y(Y_{i+1} + Y_{i-1} - 2Y_i)$$

$r_{x,y}$ : birth rates       $c_{x,y}$ : death rates       $\mu_{x,y}$ : migration rates

# Example Implementations

## Turing Ring



$$\frac{dX_i}{dt} = X_i(r_x + c_{xx}X_i + c_{xy}Y_i) + \mu_x(X_{i+1} + X_{i-1} - 2X_i)$$

$$\frac{dY_i}{dt} = Y_i(r_y + c_{yx}X_i + c_{yy}Y_i) + \mu_y(Y_{i+1} + Y_{i-1} - 2Y_i)$$

$r_{x,y}$ : birth rates       $c_{x,y}$ : death rates       $\mu_{x,y}$ : migration rates

Pred (X) 

--	--	--	--	--	--	--	--	--	--	--	--

Prey (Y) 

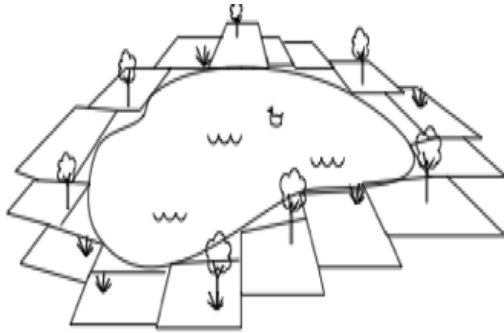
--	--	--	--	--	--	--	--	--	--	--	--

Sequential Implementation of Turing Ring Problem



# Example Implementations

## Turing Ring



$$\frac{dX_i}{dt} = X_i(r_x + c_{xx}X_i + c_{xy}Y_i) + \mu_x(X_{i+1} + X_{i-1} - 2X_i)$$

$$\frac{dY_i}{dt} = Y_i(r_y + c_{yx}X_i + c_{yy}Y_i) + \mu_y(Y_{i+1} + Y_{i-1} - 2Y_i)$$

$r_{x,y}$ : birth rates       $c_{x,y}$ : death rates       $\mu_{x,y}$ : migration rates

- Receive migration information
- Update local population using birth and death rates
- Update local population using migration values
- Send migration information to adjacent locations

Pred (X) 

--	--	--	--	--	--	--	--	--	--	--

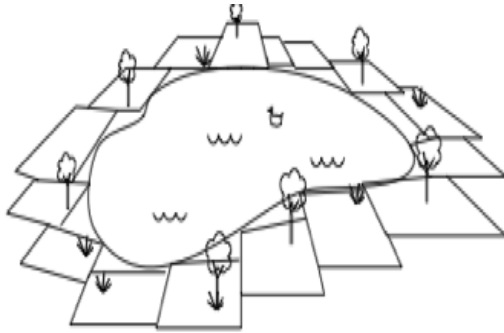
Prey (Y) 

--	--	--	--	--	--	--	--	--	--	--

Sequential Implementation of Turing Ring Problem

# Example Implementations

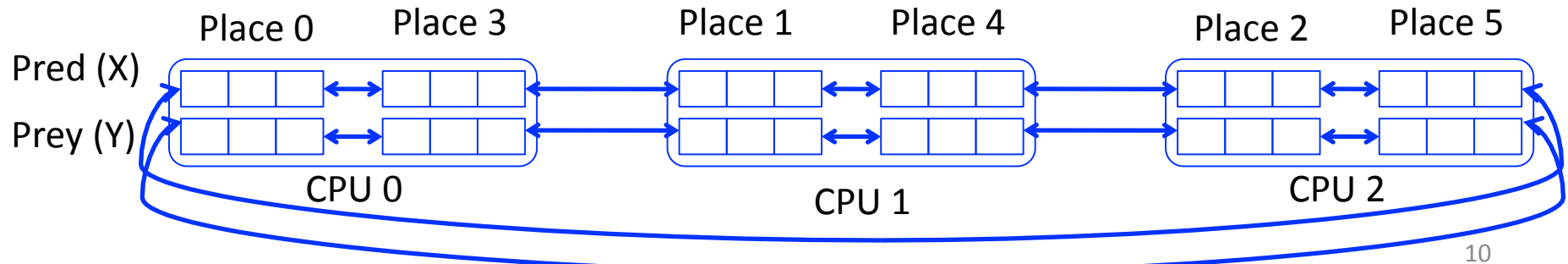
## Turing Ring



$$\frac{dX_i}{dt} = X_i(r_x + c_{xx}X_i + c_{xy}Y_i) + \mu_x(X_{i+1} + X_{i-1} - 2X_i)$$

$$\frac{dY_i}{dt} = Y_i(r_y + c_{yx}X_i + c_{yy}Y_i) + \mu_y(Y_{i+1} + Y_{i-1} - 2Y_i)$$

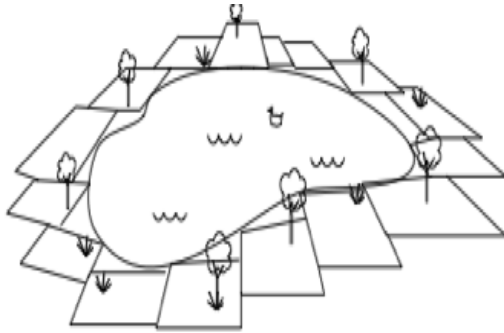
$r_{x,y}$ : birth rates       $c_{x,y}$ : death rates       $\mu_{x,y}$ : migration rates



Parallelization of Turing Ring Problem

# Example Implementations

## Turing Ring

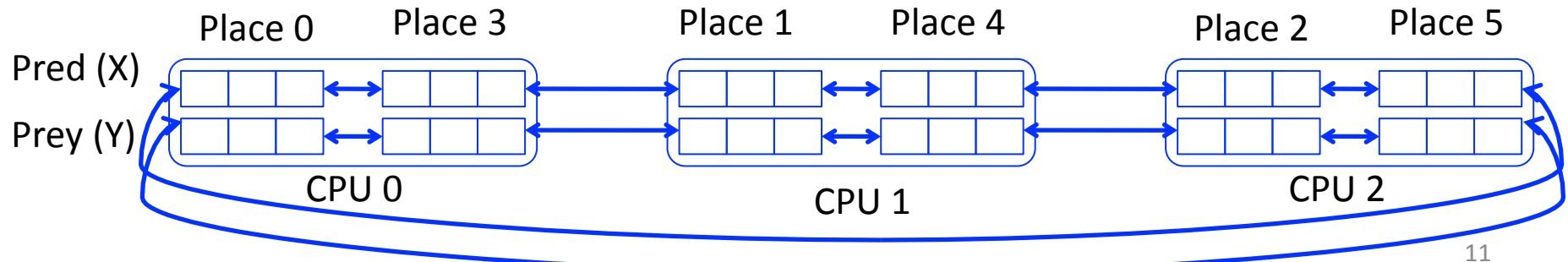


$$\frac{dX_i}{dt} = X_i(r_x + c_{xx}X_i + c_{xy}Y_i) + \mu_x(X_{i+1} + X_{i-1} - 2X_i)$$

$$\frac{dY_i}{dt} = Y_i(r_y + c_{yx}X_i + c_{yy}Y_i) + \mu_y(Y_{i+1} + Y_{i-1} - 2Y_i)$$

$r_{x,y}$ : birth rates       $c_{x,y}$ : death rates       $\mu_{x,y}$ : migration rates

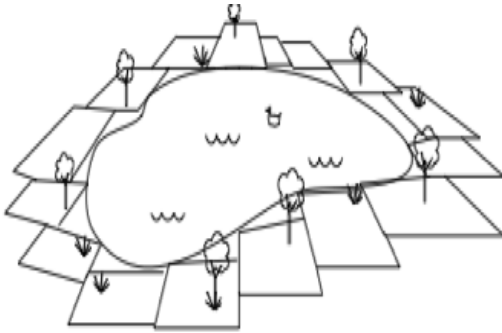
- Receive migration information
- Update local population using birth and death rates
- Update local population using migration values
- Send migration information to adjacent node
- Wait for other process to finish this iteration



Parallelization of Turing Ring Problem

# Example Implementations

## Turing Ring

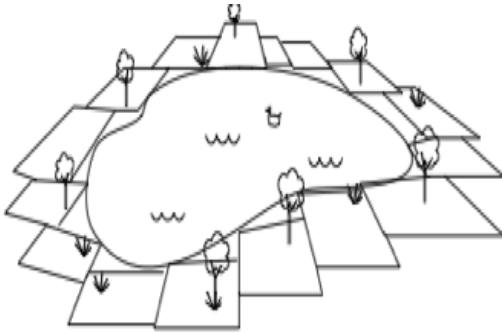


- Receive migration information
- Update local population using birth and death rates
- Update local population using migration values
- Send migration information to adjacent node
- Wait for other process to finish this iteration

```
for (i in per_place_region)
  clocked async {
    yk1(i) = step * eval(1,x,y,i);
    yt1(i) = y(i) + 0.5 * yk1(i);
    xk1(i) = step * eval(2, x, y, i);
    xt1(i) = x(i) + 0.5 * xk1(i);
    ...
  }
```

# Example Implementations

## Turing Ring



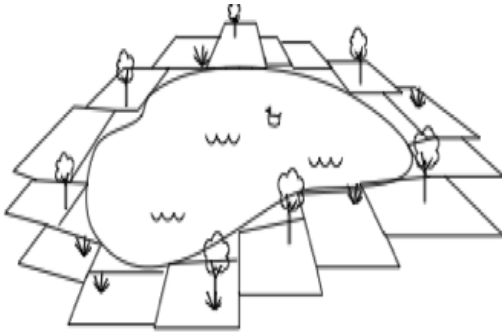
- Receive migration information
- Update local population using birth and death rates
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- Send migration information to adjacent node
- Wait for other process to finish this iteration

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for (i in per_place_region)
  clocked async {
    yk1(i) = step * eval(1,x,y,i);
    yt1(i) = y(i) + 0.5 * yk1(i);
    xk1(i) = step * eval(2, x, y, i);
    xt1(i) = x(i) + 0.5 * xk1(i);
    ...
  }

for (i in per_place_region)
  clocked async {
    yk2(i) = step * eval(1,xt1,yt1,i);
    yt2(i) = y(i) + 0.5 * yk2(i);
    xk2(i) = step * eval(2, xt1, yt1, i);
    xt2(i) = x(i) + 0.5 * xk2(i);
    ...
  }
```

# Example Implementations

## Turing Ring



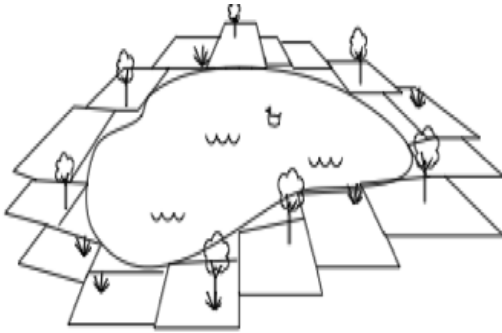
- Receive migration information
- Update local population using birth and death rates
- Update local population using migration values
- Send migration information to adjacent node
- Wait for other process to finish this iteration

```
for (z in base_dist)
  clocked async at (base_dist(z)) {
    ...
    for (i in per_place_region)
      clocked async {
        yk1(i) = step * eval(1,x,y,i);
        yt1(i) = y(i) + 0.5 * yk1(i);
        xk1(i) = step * eval(2, x, y, i);
        xt1(i) = x(i) + 0.5 * xk1(i);
        ...
      }

    for (i in per_place_region)
      clocked async {
        yk2(i) = step * eval(1,xt1,yt1,i);
        yt2(i) = y(i) + 0.5 * yk2(i);
        xk2(i) = step * eval(2, xt1, yt1, i);
        xt2(i) = x(i) + 0.5 * xk2(i);
        ...
      }
  }
}
```

# Example Implementations

## Turing Ring

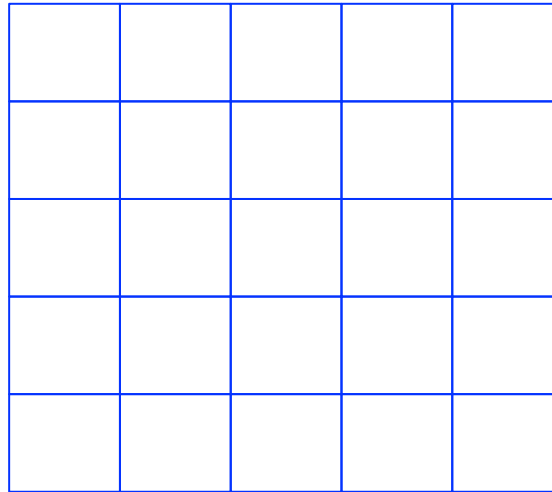


- Receive migration information
- Update local population using birth and death rates
- Update local population using migration values
- Send migration information to adjacent node
- Wait for other process to finish this iteration

```
clocked finish {  
  val base_dist = y.dist;  
  val per_place_reg = y.region;  
  for (z in base_dist)  
    clocked async at (base_dist(z)) {  
    ...  
    for (i in per_place_region)  
      clocked async {  
        yk1(i) = step * eval(1,x,y,i);  
        yt1(i) = y(i) + 0.5 * yk1(i);  
        xk1(i) = step * eval(2, x, y, i);  
        xt1(i) = x(i) + 0.5 * xk1(i);  
        ...  
      }  
    next;  
    ...  
    for (i in per_place_region)  
      clocked async {  
        yk2(i) = step * eval(1,xt1,yt1,i);  
        yt2(i) = y(i) + 0.5 * yk2(i);  
        xk2(i) = step * eval(2, xt1, yt1, i);  
        xt2(i) = x(i) + 0.5 * xk2(i);  
        ...  
      }  
    next;  
    ...  
  }  
}
```

# Example Implementations

## Skyline Matrix



$N \times N$



# Example Implementations

## Skyline Matrix

29	1			
	12	2	5	
	2	8	10	
		16	11	
	22	7	3	25

$N \times N$

# Example Implementations

## Skyline Matrix

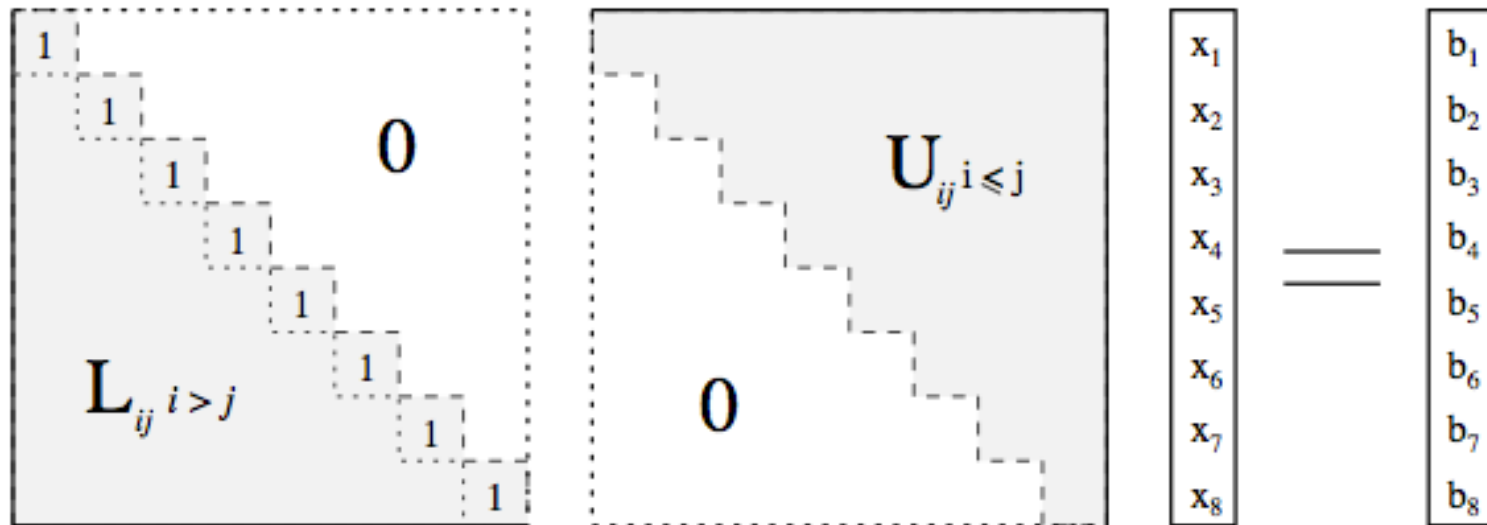
$$Ax = b$$

29	1	0	0	0
0	12	2	5	0
0	2	8	10	0
0	0	16	11	0
0	22	7	3	25

N X N

# Example Implementations Skyline Matrix

$$Ax = b$$



LU Decomposition

# Example Implementations

## Skyline Matrix

29	1	0	0	0
0	12	2	5	0
0	2	8	10	0
0	0	16	11	0
0	22	7	3	25

A



The diagram illustrates a sequence of 16 numbers arranged in a staircase pattern. The numbers are: 1, 0, 0, 0, 29, 2, 5, 0, 12, 10, 0, 0, 8, 11, 0, 0, 16, 25, 0, 22, 7, 3.

### Sub-diagonal Rows

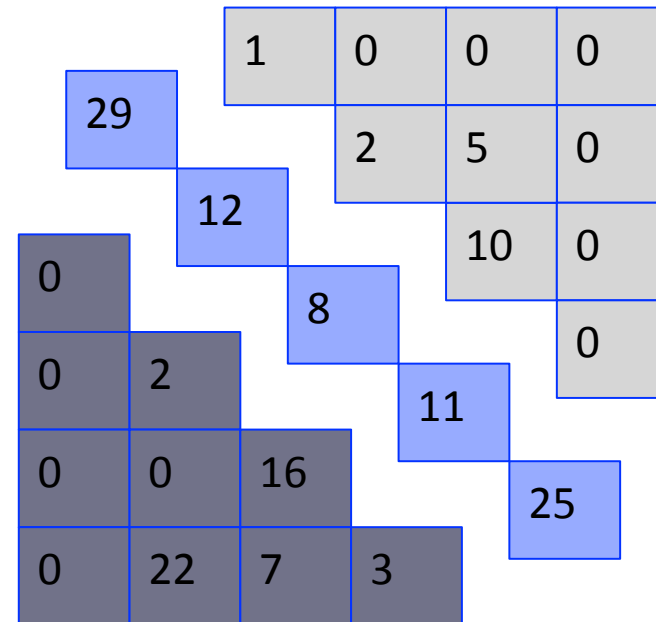
## Supra-diagonal Columns

# Example Implementations

## Skyline Matrix

29	1	0	0	0
0	12	2	5	0
0	2	8	10	0
0	0	16	11	0
0	22	7	3	25

A



Sub-diagonal Rows

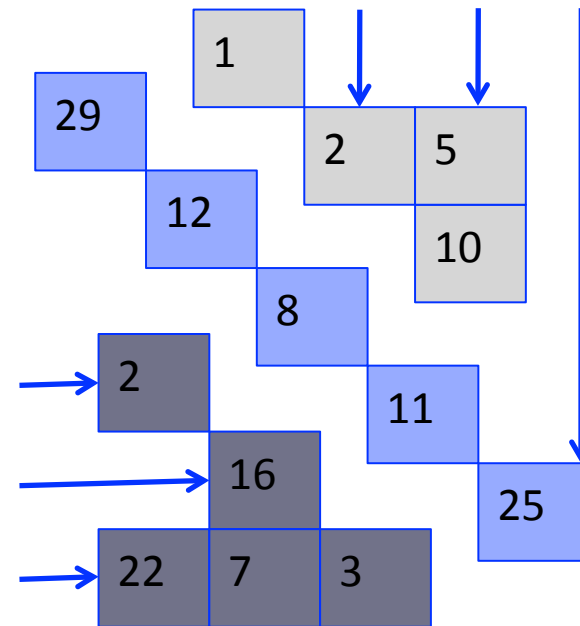
Supra-diagonal Columns

# Example Implementations

## Skyline Matrix

29	1	0	0	0
0	12	2	5	0
0	2	8	10	0
0	0	16	11	0
0	22	7	3	25

A



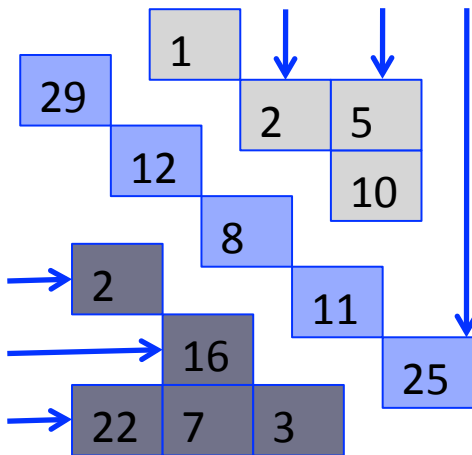
Sub-diagonal Rows

Supra-diagonal Columns

# Example Implementations

## Skyline Matrix

29	1	0	0	0
0	12	2	5	0
0	2	8	10	0
0	0	16	11	0
0	22	7	3	25

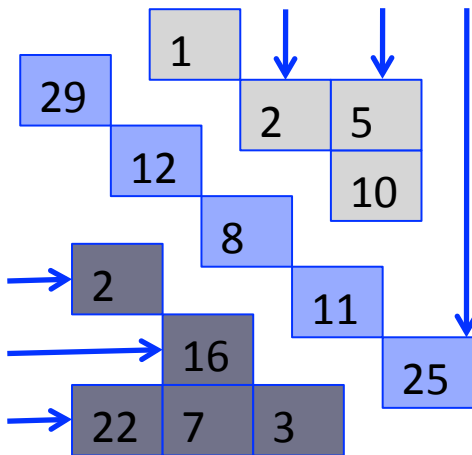


# Example Implementations

## Skyline Matrix

29	1	0	0	0
0	12	2	5	0
0	2	8	10	0
0	0	16	11	0
0	22	7	3	25

*/\* Row indices where zero-prefix ends \*/*  
`lower(1..N) = {0, 2, 2, 3, 2}`





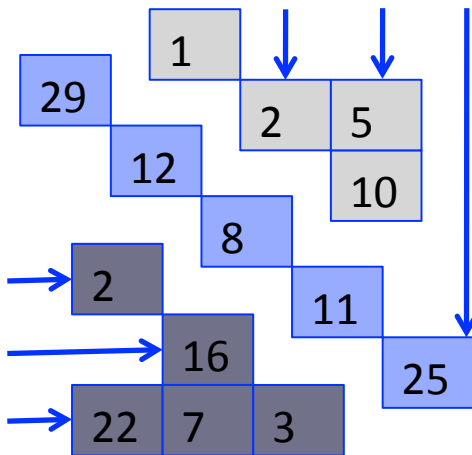
# Example Implementations

## Skyline Matrix

29	1	0	0	0
0	12	2	5	0
0	2	8	10	0
0	0	16	11	0
0	22	7	3	25

*/\* Row indices where zero-prefix ends \*/*  
`lower(1..N) = {0, 2, 2, 3, 2}`

*/\* Column indices where zero-prefix ends \*/*  
`upper(1..N) = {1, 1, 2, 2, 5}`



# Example Implementations

## Skyline Matrix

29	1	0	0	0
0	12	2	5	0
0	2	8	10	0
0	0	16	11	0
0	22	7	3	25

*/\* Row indices where zero-prefix ends \*/*

`lower(1..N) = {0, 2, 2, 3, 2}`

*/\* Column indices where zero-prefix ends \*/*

`upper(1..N) = {1, 1, 2, 2, 5}`

*/\* Array Region for sub-diagonals rows \*/*

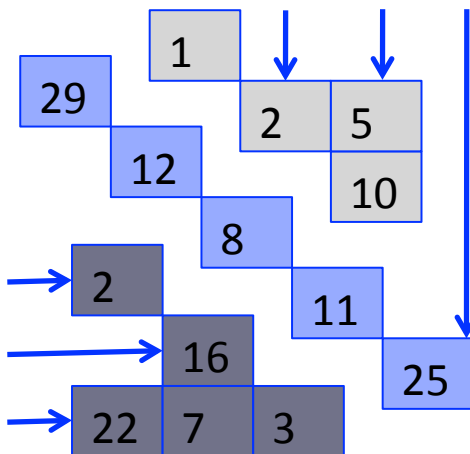
`for i in 1..N`

`var region_row_i <: Region = lower[i] .. (lower[i]==0)? 0: i-1`

*/\* Array Region for supra-diagonal columns \*/*

`for i in 1 .. N`

`var region_column_i <: Region = upper[i] .. i`



# Example Implementations

## Skyline Matrix

29	1	0	0	0
0	12	2	5	0
0	2	8	10	0
0	0	16	11	0
0	22	7	3	25

```
/* Row indices where zero-prefix ends */
```

```
lower(1..N) = {0, 2, 2, 3, 2}
```

```
/* Column indices where zero-prefix ends */
```

```
upper(1..N) = {1, 1, 2, 2, 5}
```

```
/* Array Region for sub-diagonals rows */
```

```
for i in 1..N
```

```
var region_row_i <: Region = lower[i] .. (lower[i]==0)? 0: i-1
```

```
/* Array Region for supra-diagonal columns */
```

```
for i in 1 .. N
```

```
var region_column_i <: Region = upper[i] .. i
```

```
/* Define separate arrays to store each sub-diagonal row elements */
```

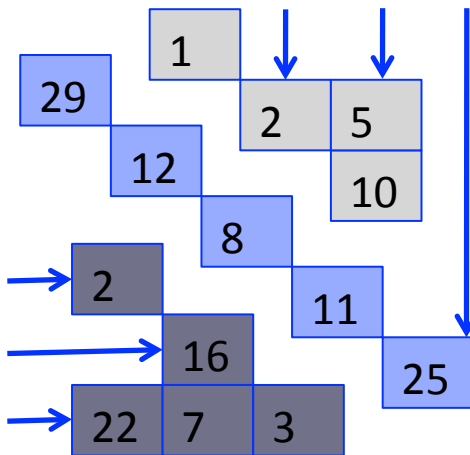
```
for i in 1 .. N
```

```
SubRowArray[i] (region_row_i)
```

```
/* Define separate arrays to store each supra-diagonal column elements */
```

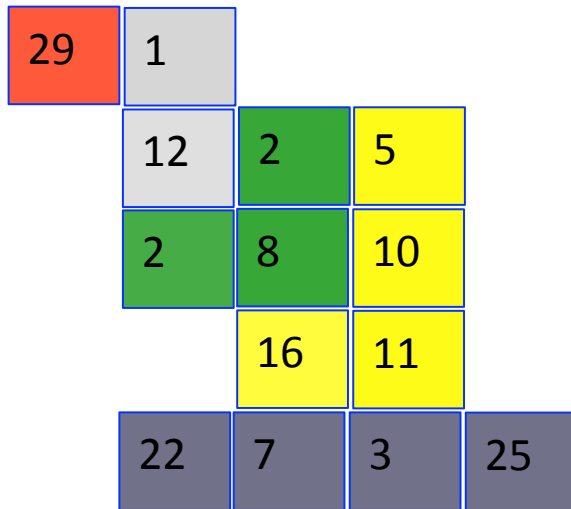
```
for i in 1 .. N
```

```
SupraColumnArray[i] (region_column_i)
```



# Example Implementations

## Skyline Matrix

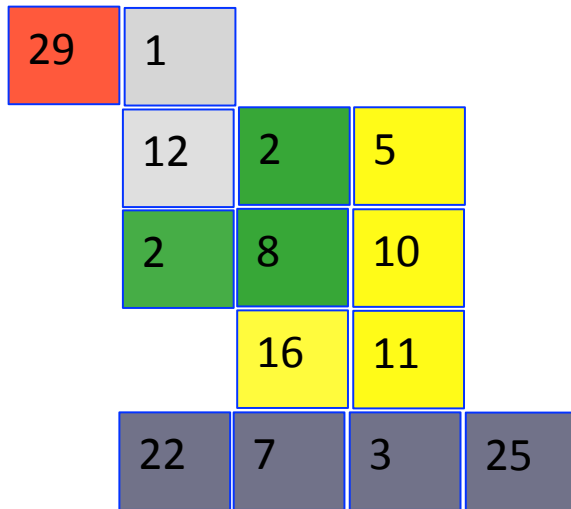


A

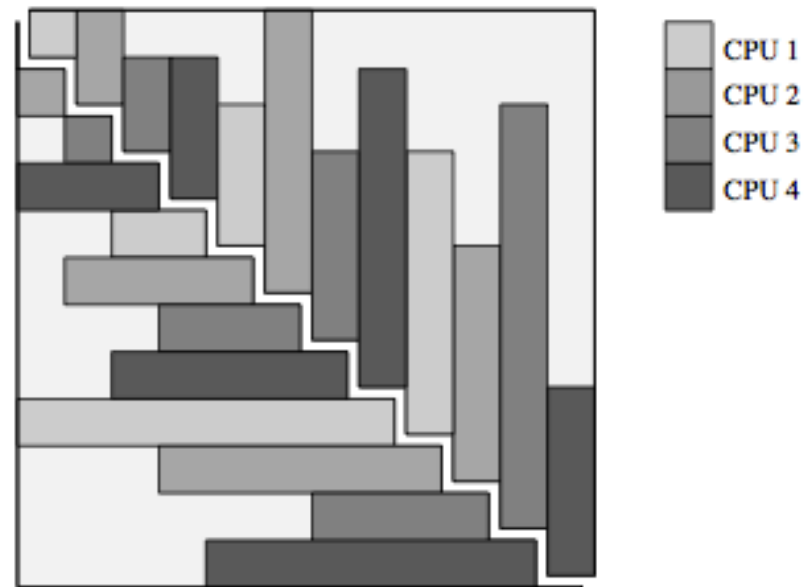
Data Distribution for Parallel Solution

# Example Implementations

## Skyline Matrix



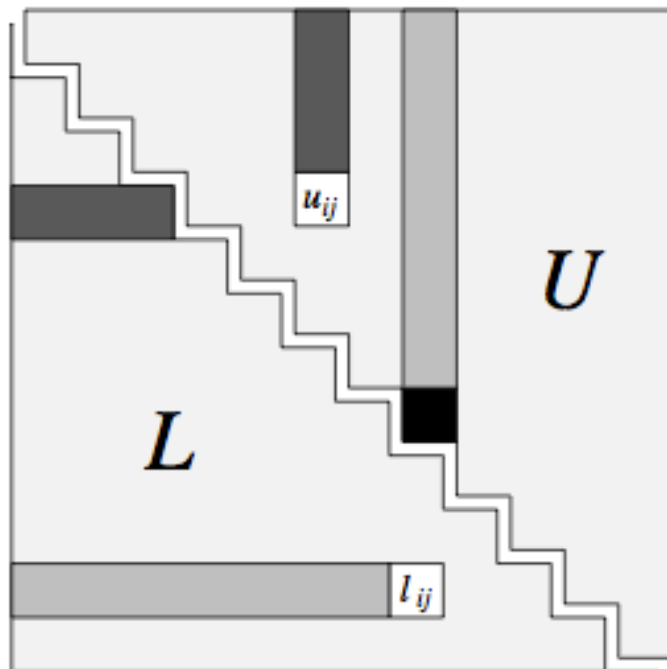
A



Data Distribution for Parallel Solution

# Example Implementations Skyline Matrix

Need for Data Replication



$$(i \leq j): \quad u_{ij} = a_{ij} - \text{[diagonal band]} \cdot \text{[diagonal band]}$$

$$(i > j): \quad l_{ij} = \left( a_{ij} - \text{[diagonal band]} \cdot \text{[diagonal band]} \right) / \text{[diagonal band]}$$

asyncCopy(...) and copy(...)

# Experimental Setup

Platform



Server with 16 nodes, each featuring two Quad-Core AMD Opteron processors

Compiler

X10c++ backend

More mature and better optimizations

Runtime

pgas\_sockets

Supports multiple places

Processors

pbs\_resources

To control number of cores, and processors used

# Experimental Methodology

*Timing*

Unix time and system wall time

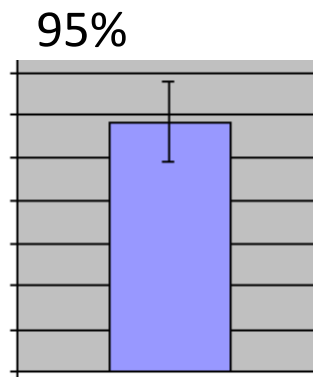
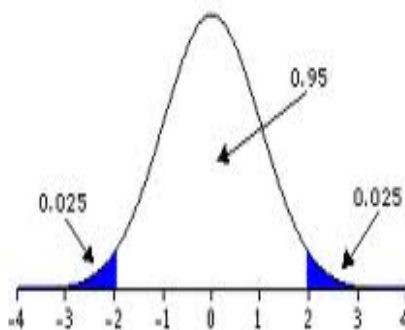
report real time

*Repetitions*

150

account for variances

*Confidence Interval*



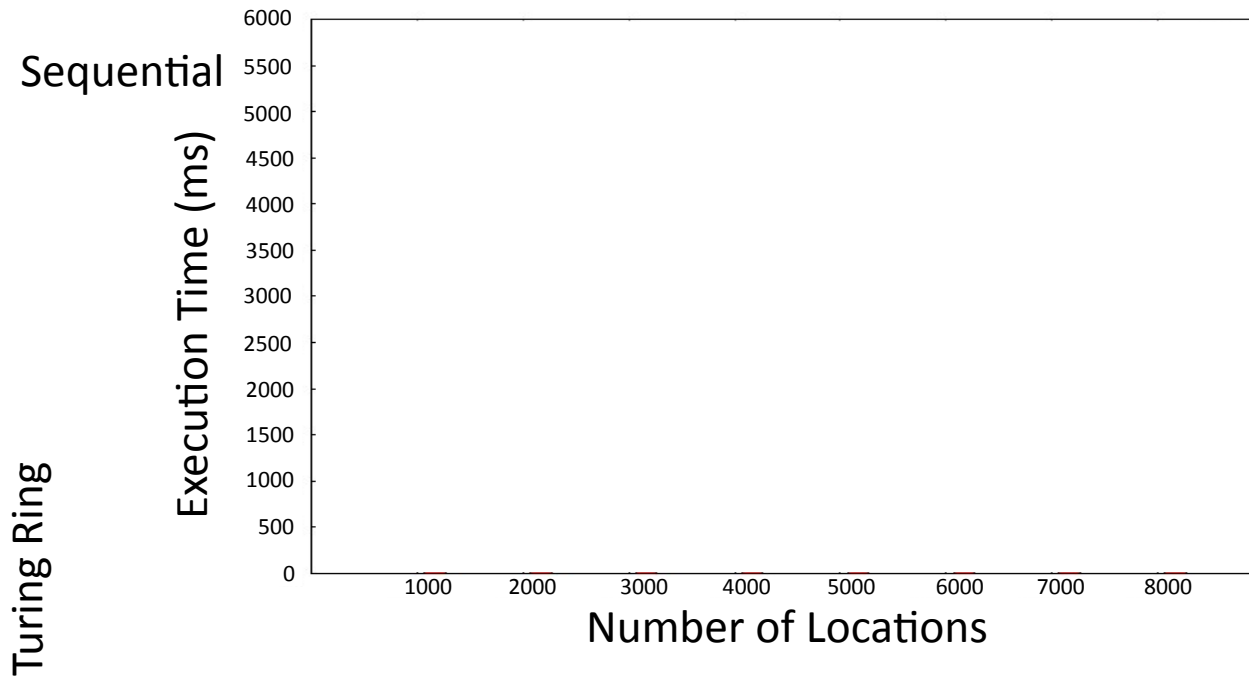
range of values that is likely to include differences from variable factors



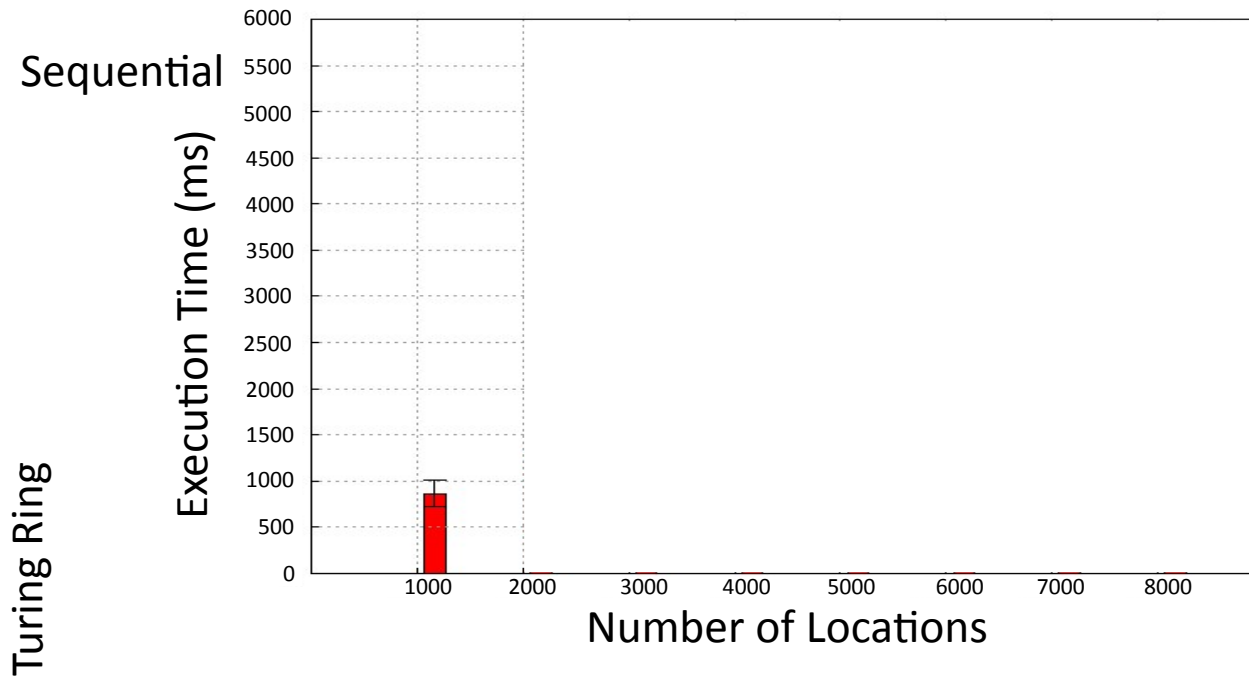
# Performance Reports

Turing Ring

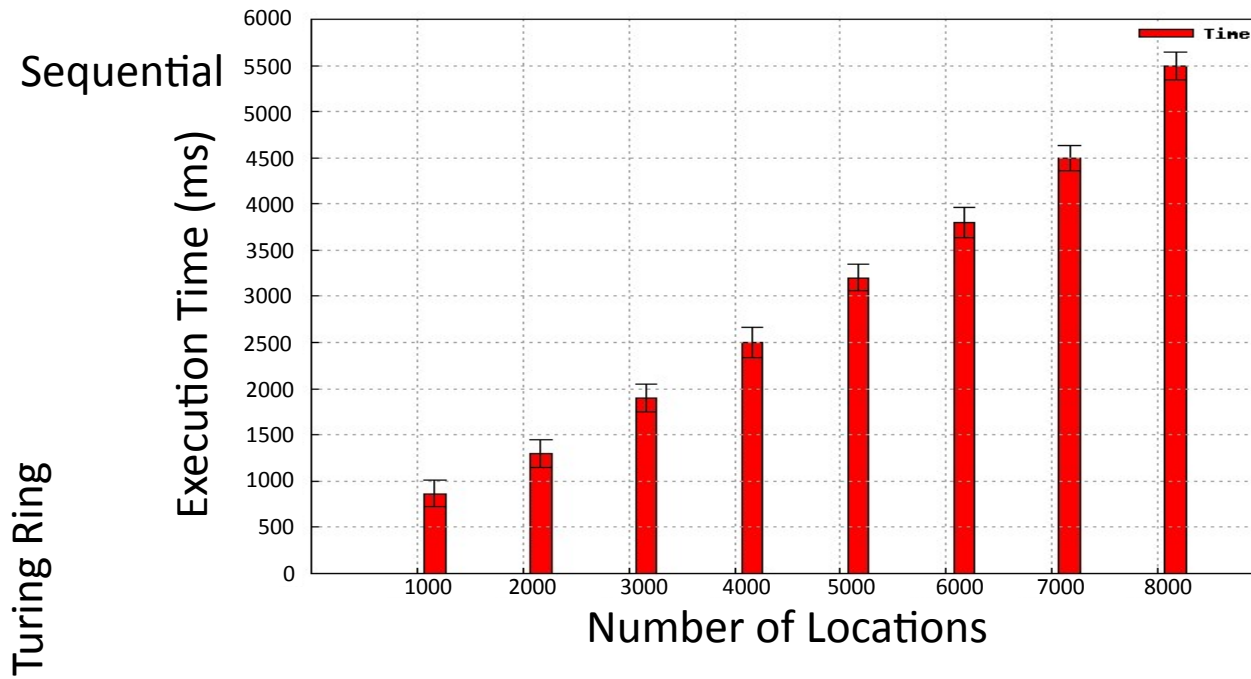
# Performance Reports



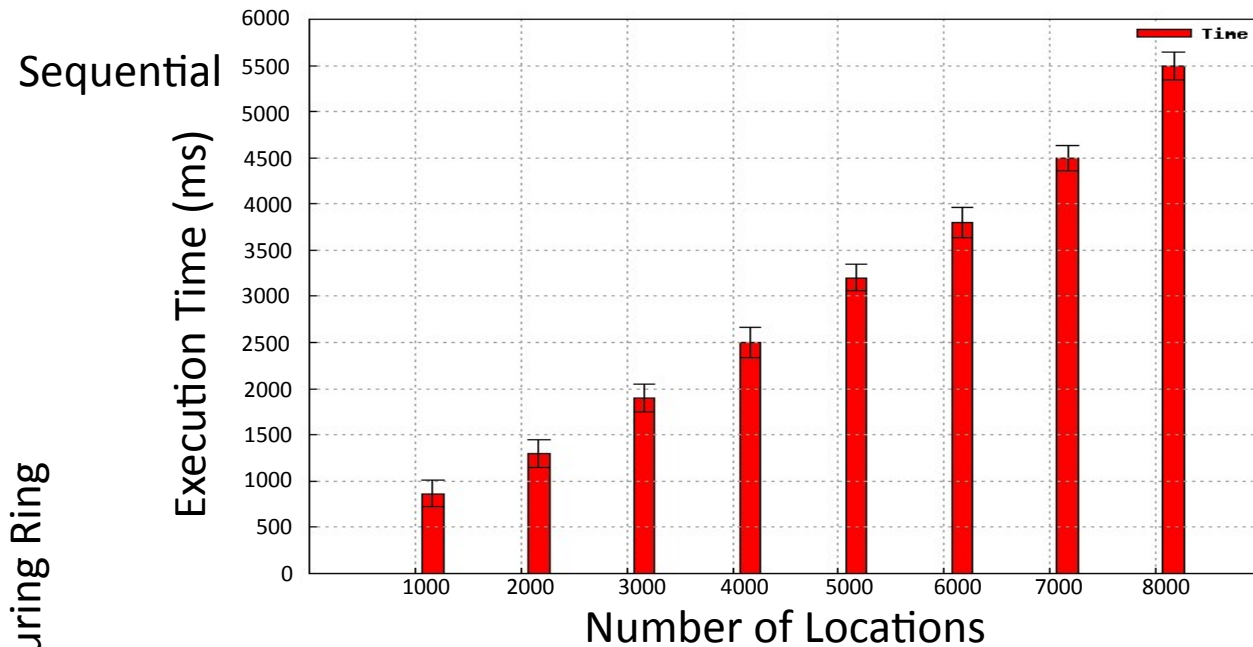
# Performance Reports



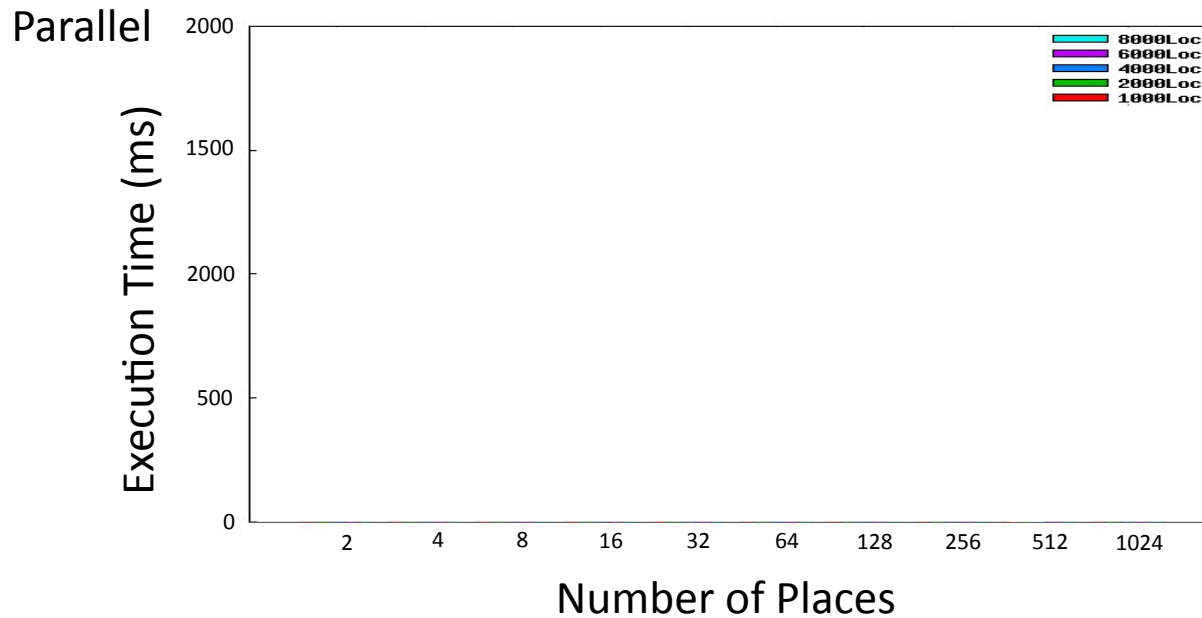
# Performance Reports



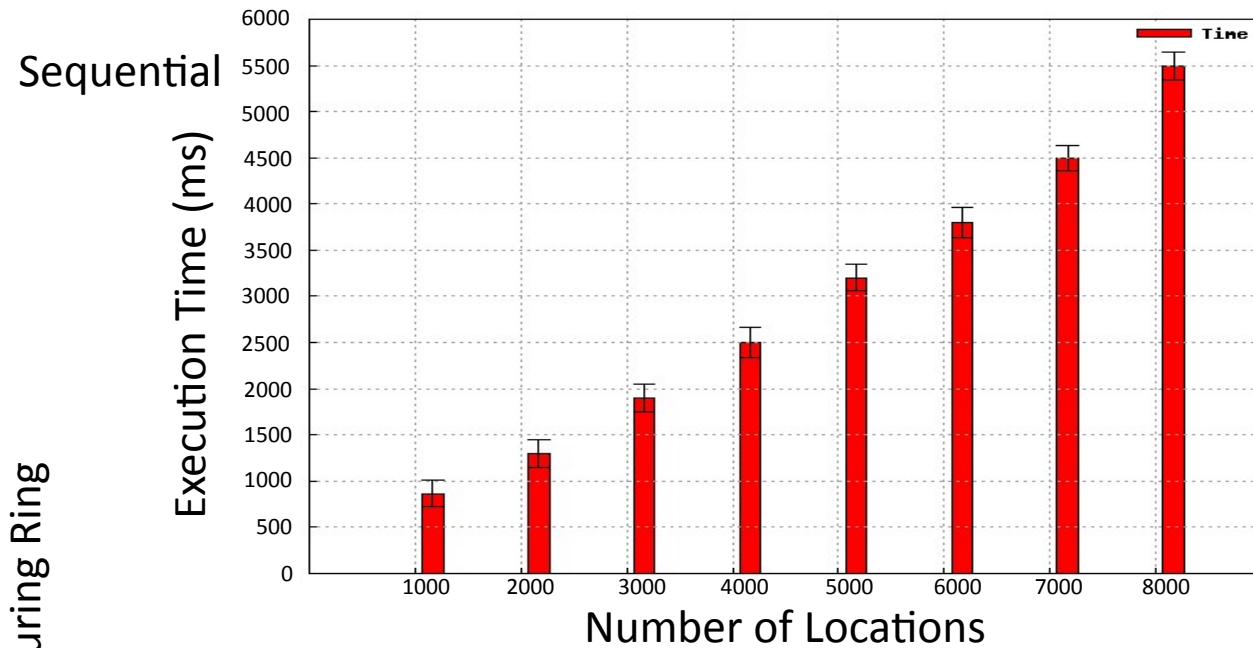
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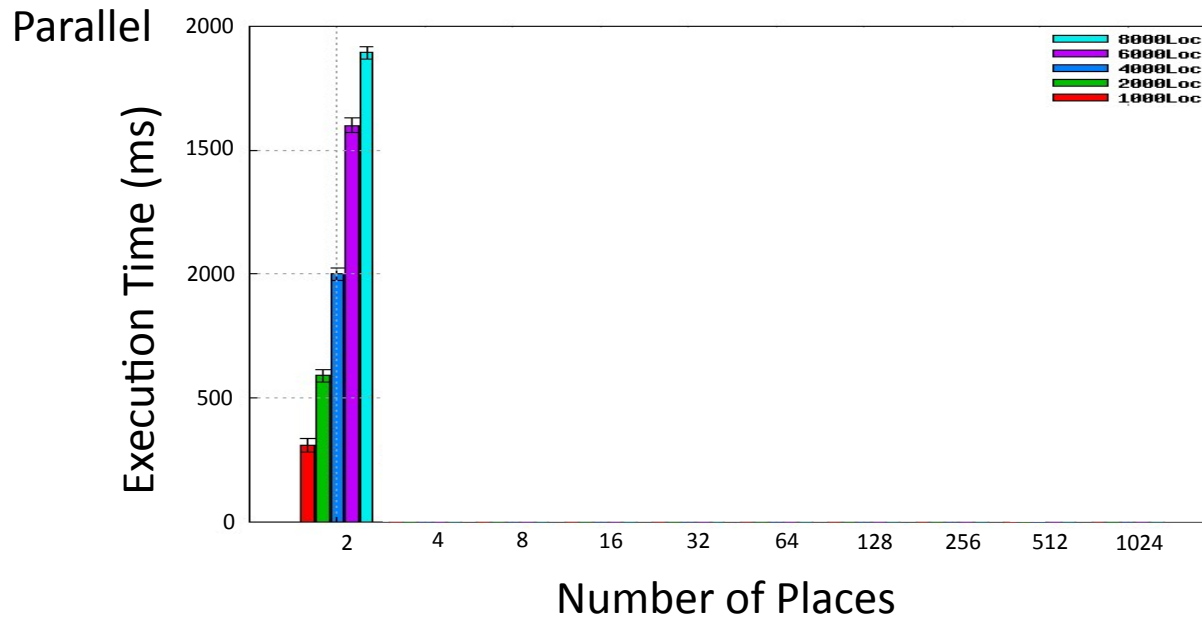
Turing Ring



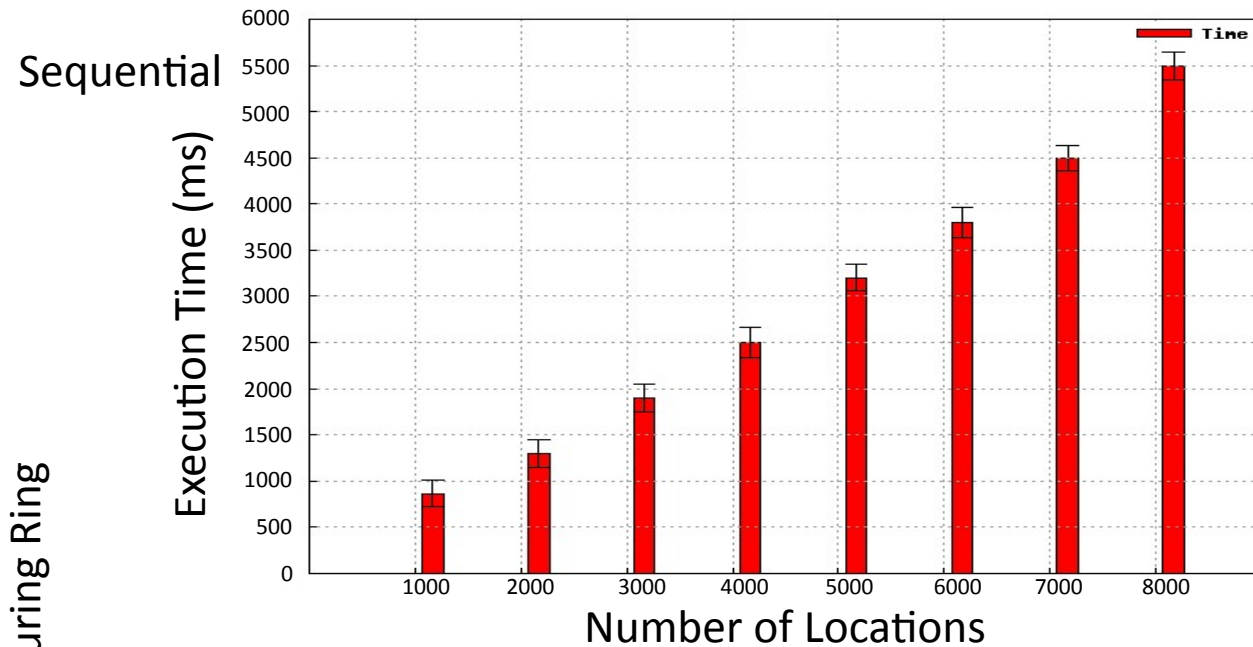
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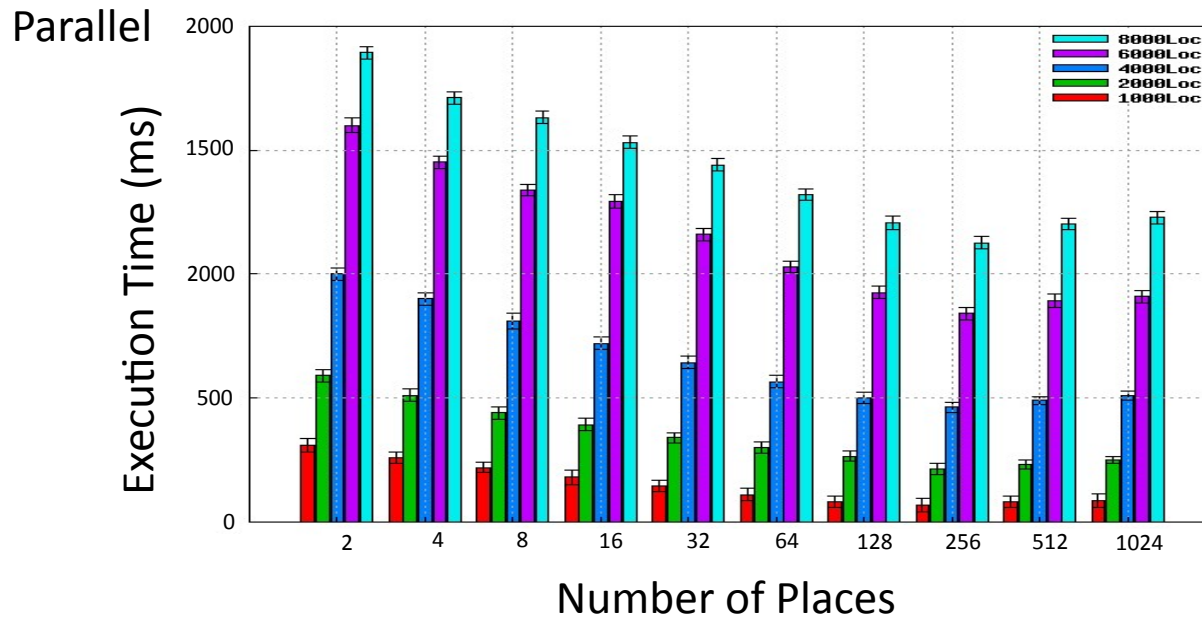
Turing Ring



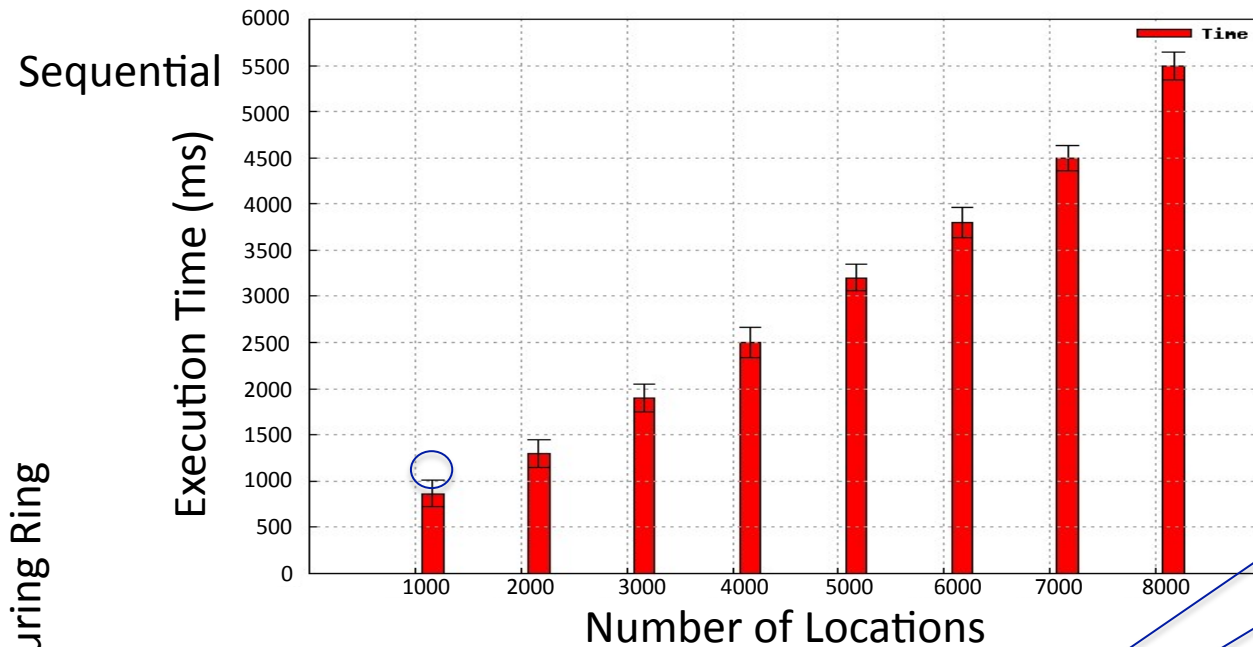
# Performance Reports



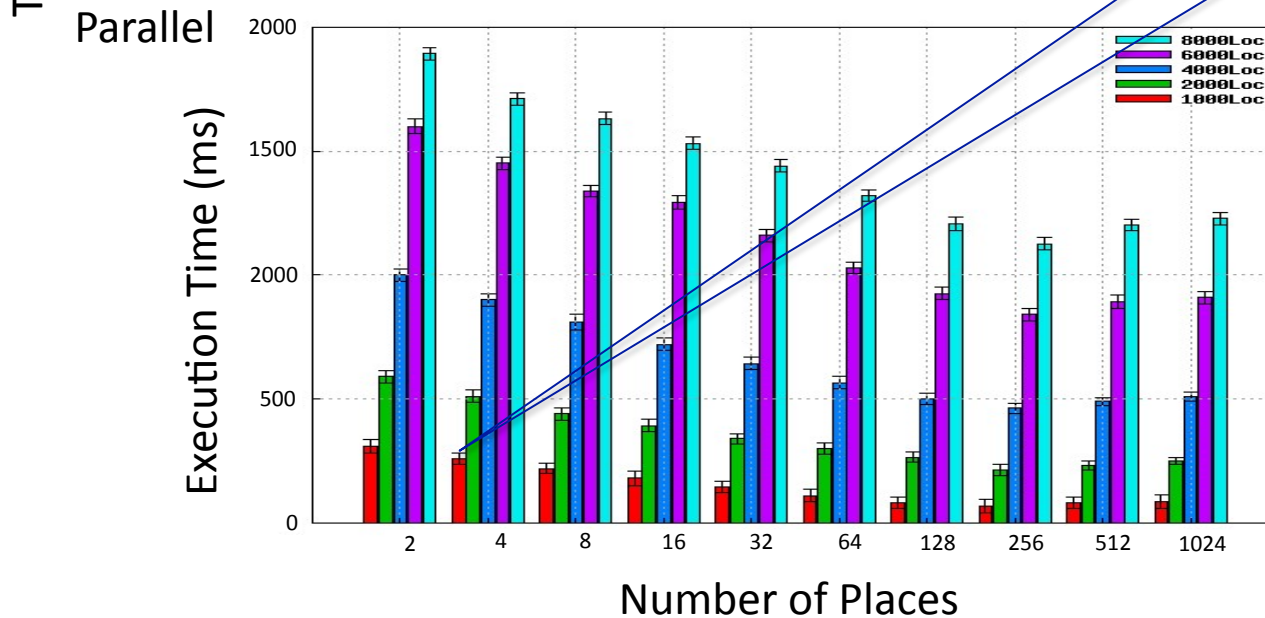
Turing Ring



# Performance Reports

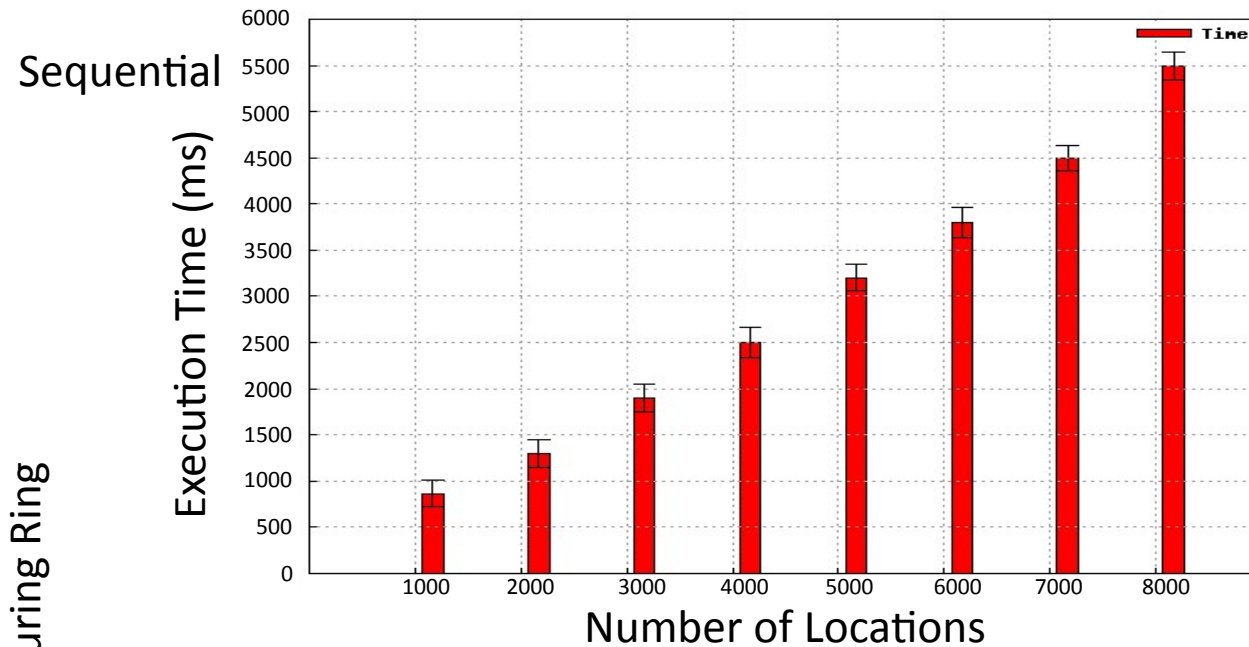


For 1000 locations & 4 places  
speedup = 3.6

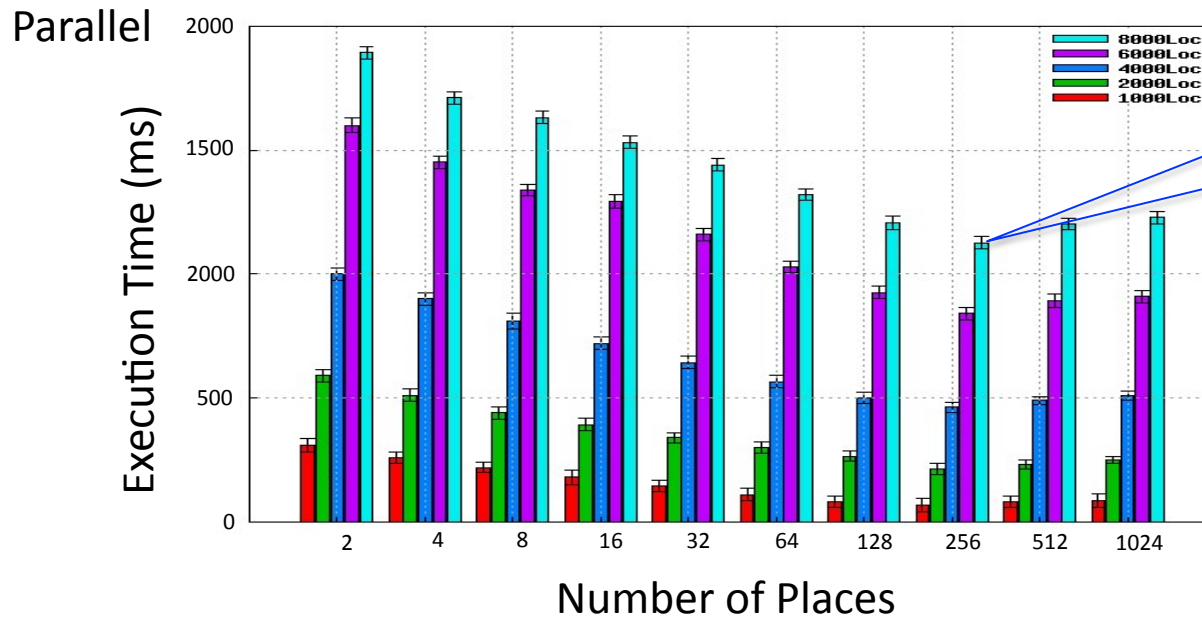




# Performance Reports

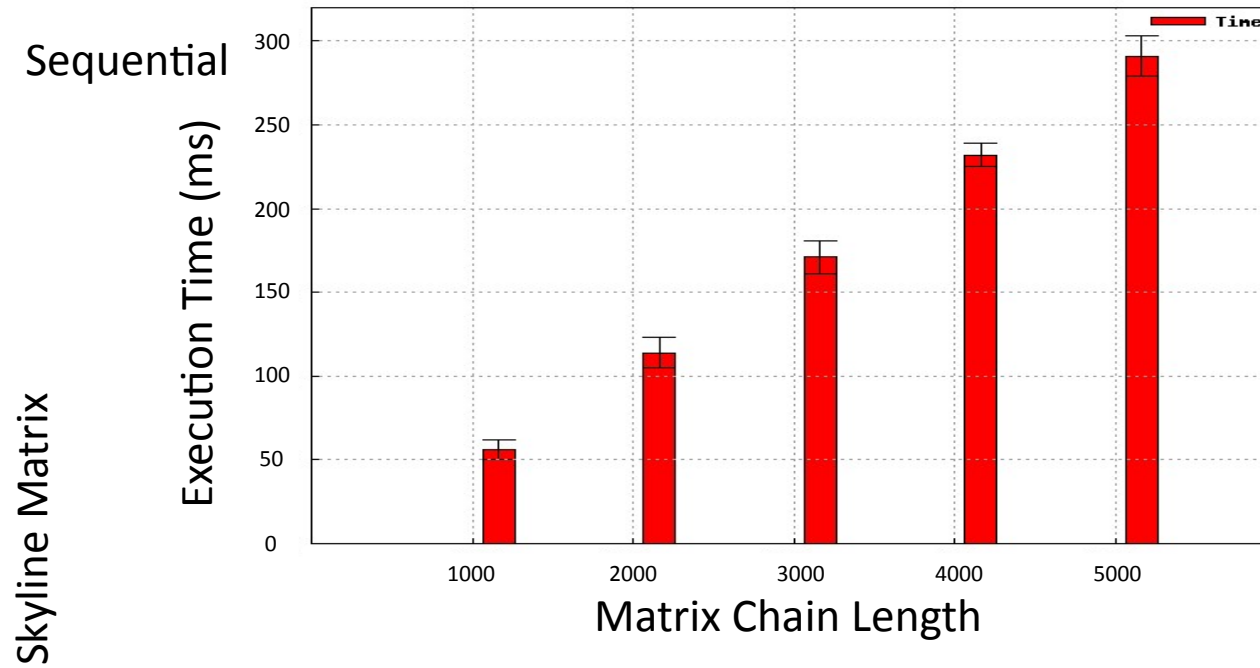


Turing Ring

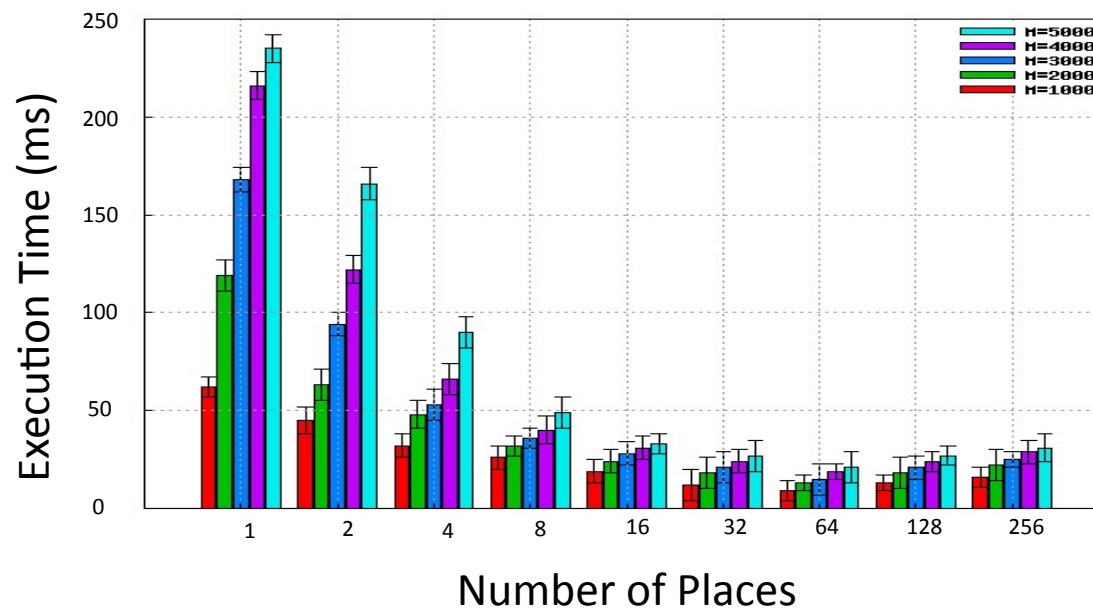
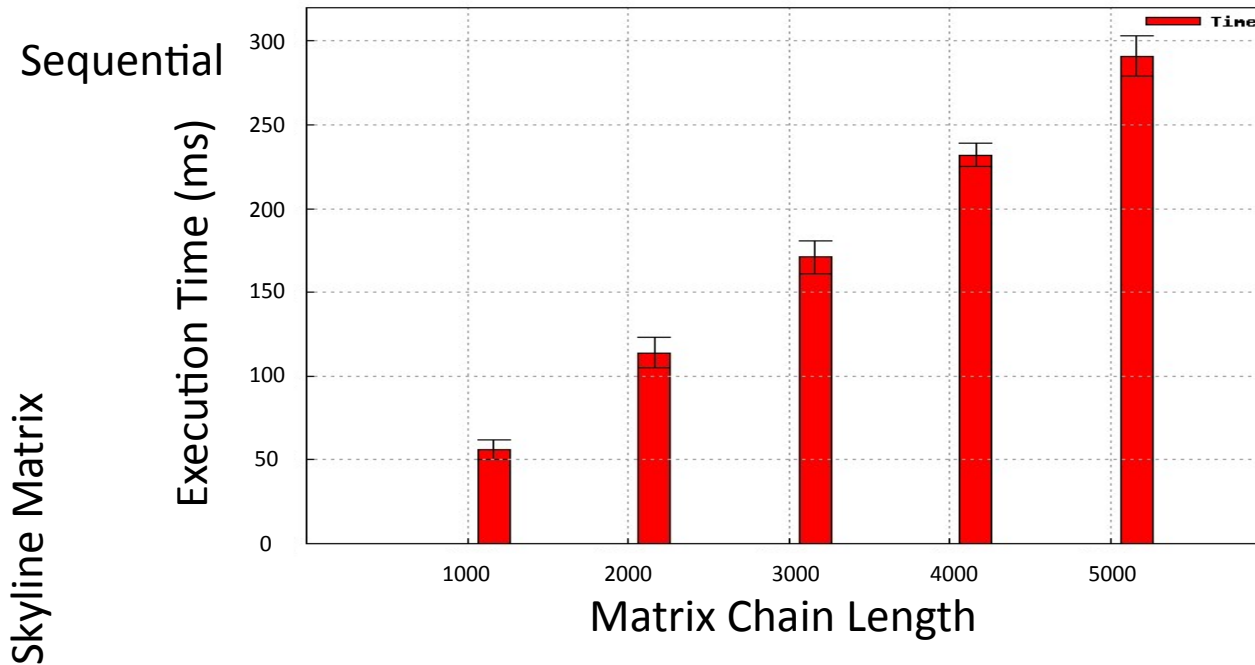


Optimal number of places  $\geq 256$  &  $< 512$

# Performance Reports

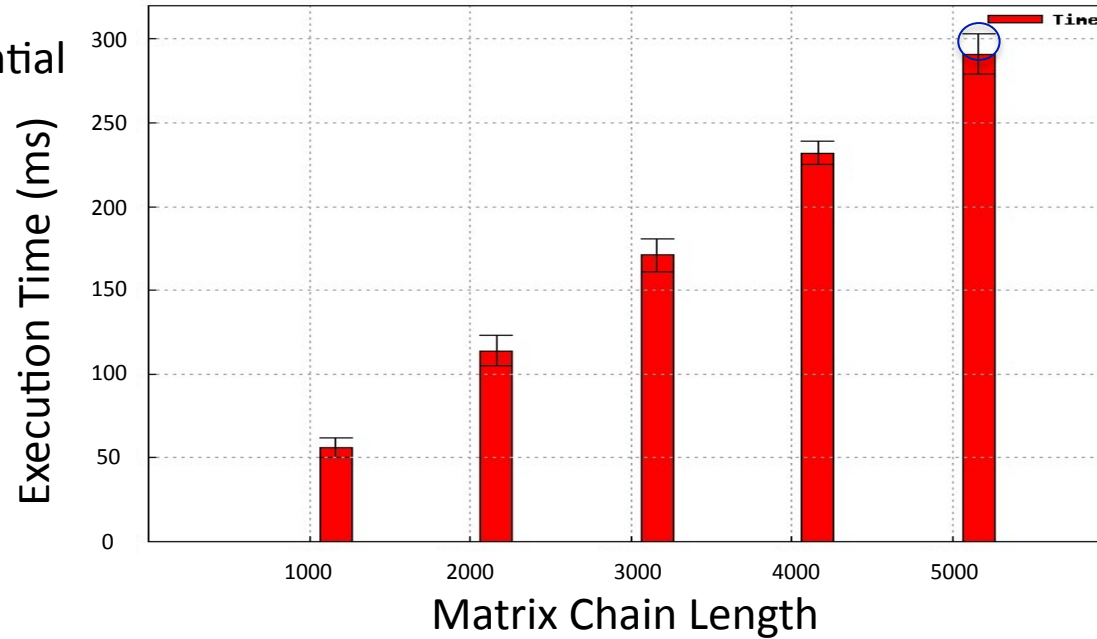


# Performance Reports



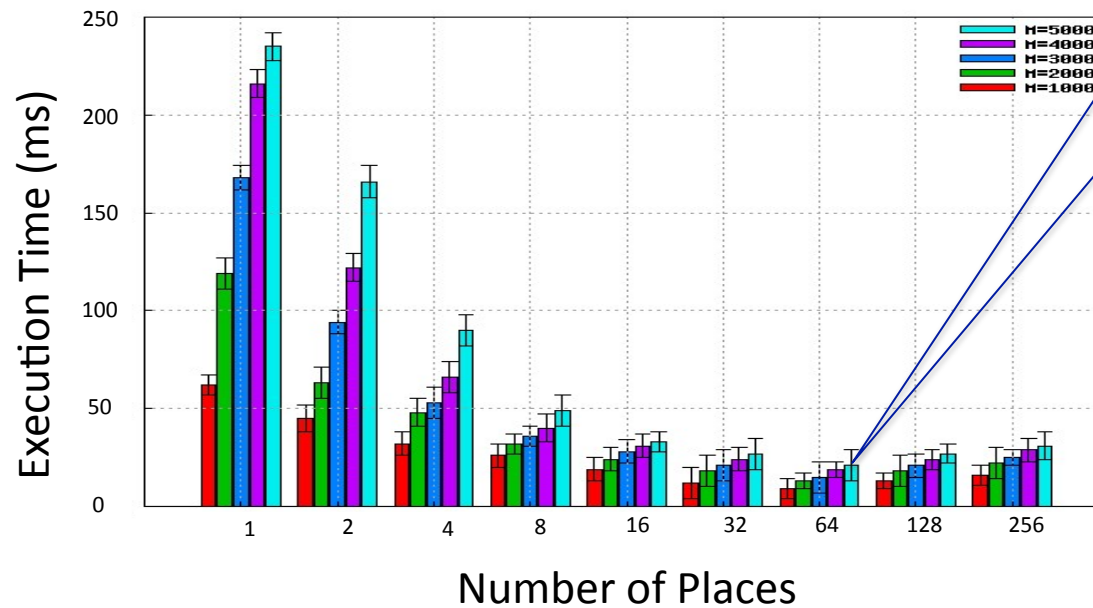
# Performance Reports

Sequential



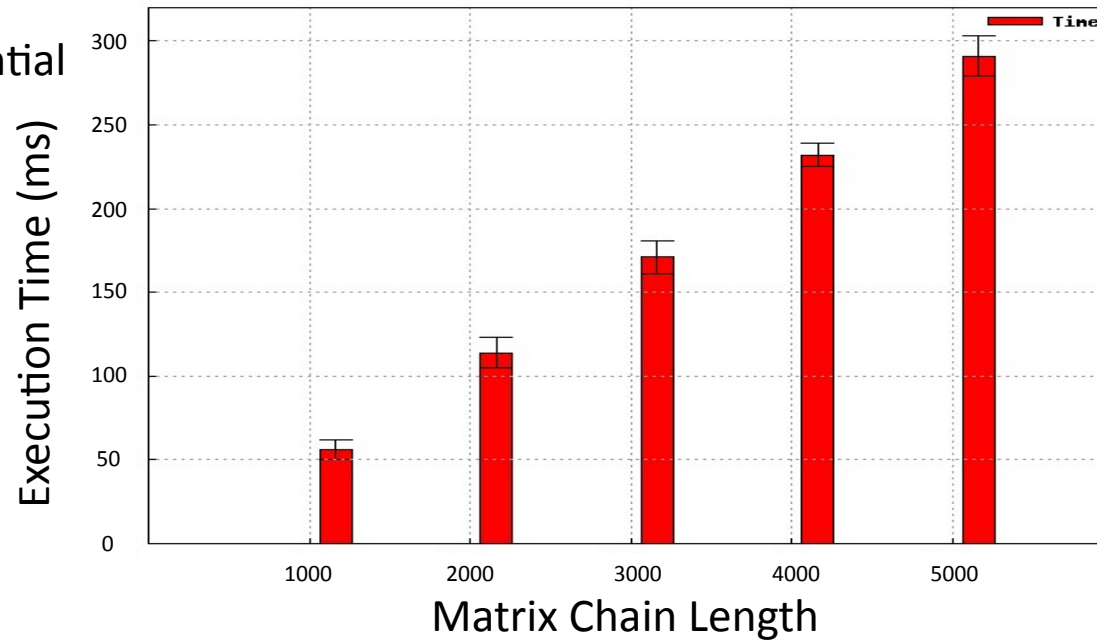
For chain length 5000 & 64 places, speedup = 11.2

Skyline Matrix

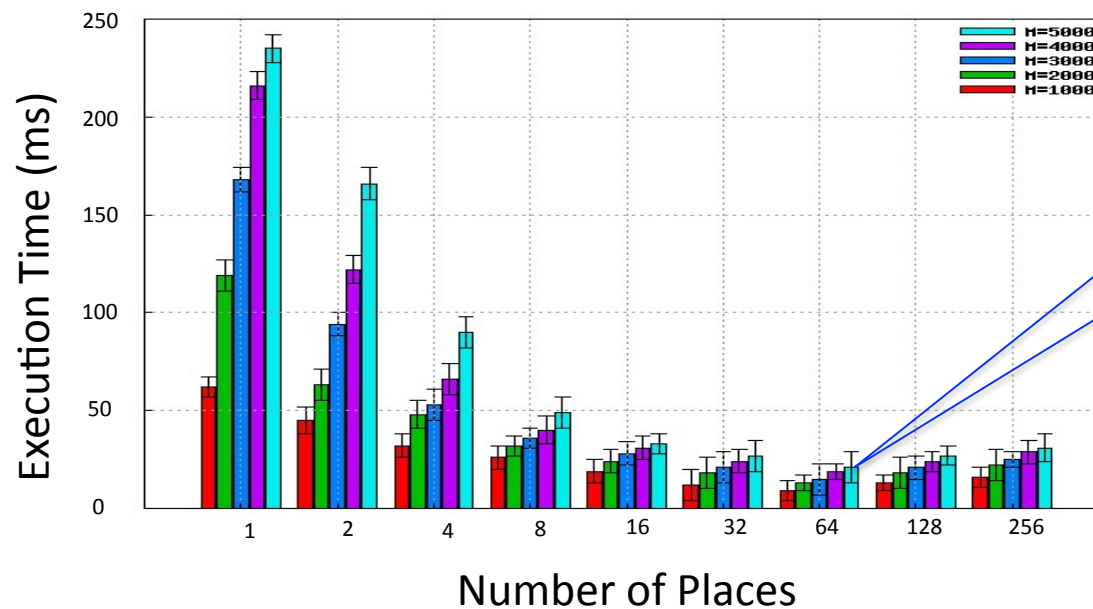


# Performance Reports

Sequential



Skyline Matrix



Optimal number of places  $\geq 64$  &  $< 128$

# Insights

## Expressiveness:

- Data representation & distribution

- Task and data parallelism

- Aggregate operations

## Language Deficiencies:

- Fine-grained async -- poor performance

- Concurrent Input/Output -- useful

- Error Messages -- cryptic

# Comparison with Other Languages

X10 and UPC:

- both exploit data layout in memory (PGAS)
- X10 richer through async activities (APGAS)
- expressive
  - data and task parallelism
  - stripped allocation of arrays
  - collective operations
- remote shared memory accesses
- compiler technology

# Comparison with Other Languages

X10 and OpenMP:

- OpenMP restricted to shared memory systems
- lacks efficient data locality support
- scalability issue



# Comparison with Other Languages

X10 and Orca:

Orca uses shared objects for communication  
shared objects encapsulated in abstract data types

X10 relies on APGAS model and uses messages  
only immutable values are shared

# Summary

As an emerging programming model, performance analyses necessary

Measured

- programmability of X10 language

- performance of X10 code

Better than UPC, OpenMP because of APGAS memory model

Runtime performance improvements needed

Additional language constructs useful

Questions?